

Event Calculus with duration

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Abstract

TODO

1 MAPF in event Calculus

Given a graph $G = \langle V, E \rangle$, a list of agent R , a starting point and a goal for each agent $O = \langle A, V, V \rangle$.

1.1 Fluents and Events

Event calculus is a sorted predicate calculus (with equality). There are the sorts:

- Timepoints : $\mathcal{T} = [0, 1, \dots, h]$.
- Fluents : $\forall r \in R, \forall v \in V, on(r, v) \in \mathcal{F}$.
- Event : $\forall r \in R, \forall \langle v_o, v_d \rangle \in E, move(r, v_o, v_d) \in \mathcal{E}$.

1.2 The four predicates

- $happens \subseteq \mathcal{E} * \mathcal{T}$
- $holds_at \subseteq \mathcal{F} * \mathcal{T}$
- $initiates \subseteq \mathcal{E} * \mathcal{F} * \mathcal{T}$
- $terminates \subseteq \mathcal{E} * \mathcal{F} * \mathcal{T}$

1.3 E : Domain independant axioms

1.3.1 Effect of events on fluents

If an event e happens, and this event has the effect of starting f , then f holds the moment after the event.

$$[happens(e, t-1) \wedge initiates(e, f, t-1)] \Rightarrow holds_at(f, t) \quad (E.1)$$

If an event e happens, and this event has the effect of ending f , then f don't holds the moment after the event.

$$[happens(e, t-1) \wedge terminates(e, f, t-1)] \Rightarrow \neg holds_at(f, t) \quad (E.2)$$

1.3.2 Inertia

If a fluent f holds and is not terminated, it continue to hold the next moment.

$$[holds_at(f, t-1) \wedge \neg \exists e(happens(e, t-1) \wedge terminates(e, f, t-1))] \Rightarrow holds_at(f, t) \quad (E.3)$$

If a fluent f don't holds and is not started, it continue to not hold the next moment.

$$[\neg holds_at(f, t-1) \wedge \neg \exists e(happens(e, t-1) \wedge initiates(e, f, t-1))] \Rightarrow \neg holds_at(f, t) \quad (E.4)$$

1.4 Σ : Effects

If an agent move, it goes to another vertice.

$$\forall move(r, v_o, v_d) \in \mathcal{E}, initiates(move(r, v_o, v_d), on(r, v_d), t) \quad (\Sigma.1)$$

If an agent move, he left his vertice.

$$\forall move(r, v_o, v_d) \in \mathcal{E}, terminates(move(r, v_o, v_d), on(r, v_o), t) \quad (\Sigma.2)$$

1.5 Γ : Observations

The agents have their starting vertices.

$$\forall \langle r, v_s, v_g \rangle \text{ in } O, holds_at(on(r, v_s), 0) \quad (\Gamma_i)$$

The agents have their goals.

$$\forall \langle r, v_s, v_g \rangle \text{ in } O, holds_at(on(r, v_g), h) \quad (\Gamma_f)$$

1.6 Ψ : Actions preconditions and State constraints

For an agent to move, he must be on the vertice.

$$happens(move(r, v_o, v_d), t) \Rightarrow holds_at(on(r, v_o), t) \quad (\Psi.1)$$

An agent is on one vertice max at each time.

$$[holds_at(on(r, v), t) \wedge v \neq v'] \Rightarrow \neg holds_at(on(r, v'), t) \quad (\Psi.2)$$

1.7 Ω : Unique names

List of the unique names. ¹

$$U[move, on] \quad (\Omega)$$

¹This is just to say that every on(something) is different to each move(something)

1.8 Domain description

$$CIRC[\Sigma; initiates, terminates] \wedge CIRC[\Delta; happens] \wedge \Omega \wedge \Psi \wedge \Gamma \wedge E \quad (\Phi)$$

- $\Sigma = \Sigma.1 \wedge \Sigma.2$
- Δ being the conjunction of all event occurrence formulas (aka the "happens facts")
- Ω
- $\Psi = \Psi.1 \wedge \Psi.2 \wedge \Psi.3 \wedge \Psi.4$
- Γ being the conjunction of all observations (aka the "holds_at facts") counting Γ_i and Γ_f
- $E = E.1 \wedge E.2 \wedge E.3 \wedge E.4$

1.9 Planning

A planning problem consist of taking Σ , Ω , Ψ , Γ (without Γ_f), Γ_f , and E as input, and producing as output zero or more Δ (our plan) such as Φ is consistant and $\Phi \models \Gamma_f$.

2 Approach

2.1 Without touching Event Calculus

2.2 With changes in Event Calculus

3 Discussion

Paper used :
mostly : [1].
potassco.org

References

- [1] Erik T Mueller. *Commonsense Reasoning*. Elsevier, 2010.