Using the R Squared statistic

BAYESIAN REGRESSION MODELING WITH RSTANARM



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What is R squared?

Coefficient of determination

$$R^{2} = 1 - \frac{\sum_{i} (y_{i} - \hat{y}_{i})^{2}}{\sum_{i} (y_{i} - \bar{y})^{2}}$$

What is R squared?

Coefficient of determination

$$R^2 = 1 - \frac{\sum_{i}^{\text{Observed value}} (y_i - \hat{y}_i)^2}{\sum_{i} (y_i - \bar{y})^2}$$

What is R squared?

Coefficient of determination

$$R^{2} = 1 - \frac{\sum_{i}^{\text{Observed value}} (\bar{y}_{i})^{2}}{\sum_{i} (\bar{y}_{i})^{2}}$$

$$\frac{\sum_{i} (\bar{y}_{i})^{2}}{\sum_{i} (\bar{y}_{i})^{2}}$$
Observed value

Observed value

Mean value

Calculating R squared statistic

```
lm_model <- lm(kid_score ~ mom_iq, data = kidiq)
lm_summary <- summary(lm_model)
lm_summary$r.squared</pre>
```

0.2009512

```
ss_res <- var(residuals(lm_model))
ss_total <- var(residuals(lm_model)) + var(fitted(lm_model))
1 - (ss_res / ss_total)</pre>
```

0.2009512



The R squared statistic of a Bayesian Model

```
stan_model <- stan_glm(kid_score ~ mom_iq, data = kidiq)
ss_res <- var(residuals(stan_model))
ss_total <- var(fitted(stan_model)) + var(residuals(stan_model))
1 - (ss_res / ss_total)</pre>
```

0.2004996

lm_summary\$r.squared

0.2009512



Let's practice!

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Posterior predictive model checks

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Using posterior distributions

```
stan_model <- stan_glm(kid_score ~ mom_iq, data = kidiq)
spread_draws(stan_model, `(Intercept)`, mom_iq) %>%
  select(-.draw)
```

Posterior predictions

```
predictions <- posterior_linpred(stan_model)
predictions[1:10, 1:5]</pre>
```

```
iterations
      [1,] 100.18694 79.04791 96.40964 85.76310 81.30045
      [2,] 100.24843 82.00786 96.98905 87.80231 83.95155
      [3,] 100.85608 81.13109 97.33146 87.39709 83.23295
      [4,] 102.31392 80.81881 98.47300 87.64712 83.10930
      [5,] 97.25617 81.18278 94.38404 86.28879 82.89553
      [6,] 100.86263 79.89830 97.11655 86.55800 82.13223
      [7,] 99.36166 81.10329 96.09910 86.90339 83.04887
      [8,] 101.13487 80.97878 97.53321 87.38173 83.12658
      [9,] 98.72686 79.97596 95.37629 85.93252 81.97403
     [10,] 100.22835 81.04603 96.80069 87.13964 83.09007
```

```
predictions <- posterior_linpred(stan_model)</pre>
# First replication
iter1 <- predictions[1,]</pre>
# Second replication
iter2 <- predictions[2,]</pre>
# Data summaries
summary(kidiq$kid_score)
   Min. 1st Qu. Median
                           Mean 3rd Qu.
                                           Max.
   20.0
           74.0
                   90.0
                           86.8 102.0
                                          144.0
summary(iter1)
summary(iter2)
   Min. 1st Qu. Median
                           Mean 3rd Qu.
                                           Max.
  68.54 79.86
                  85.80
                          87.14 93.74 112.12
   Min. 1st Qu. Median
                        Mean 3rd Qu.
                                           Max.
                          86.71 92.62 109.08
  70.05
          80.19
                  85.51
```

Comparing single scores

```
predictions <- posterior_linpred(stan_model)
kidiq$kid_score[24]
summary(predictions[, 24])</pre>
```

```
87
Min. 1st Qu. Median Mean 3rd Qu. Max.
83.34 86.17 86.77 86.75 87.34 90.23
```

```
kidiq$kid_score[185]
summary(predictions[, 185])
```

```
111
Min. 1st Qu. Median Mean 3rd Qu. Max.
82.81 85.65 86.25 86.24 86.83 89.69
```



Let's practice

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Model fit with posterior predictive model checks

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R squared posterior distribution

```
stan_model <- stan_glm(kid_score ~ mom_iq, data = kidiq)
r2_posterior <- bayes_R2(stan_model)
summary(r2_posterior)</pre>
```

```
Min. 1st Qu. Median Mean 3rd Qu. Max.
0.09677 0.18034 0.20006 0.20042 0.22048 0.33414
```

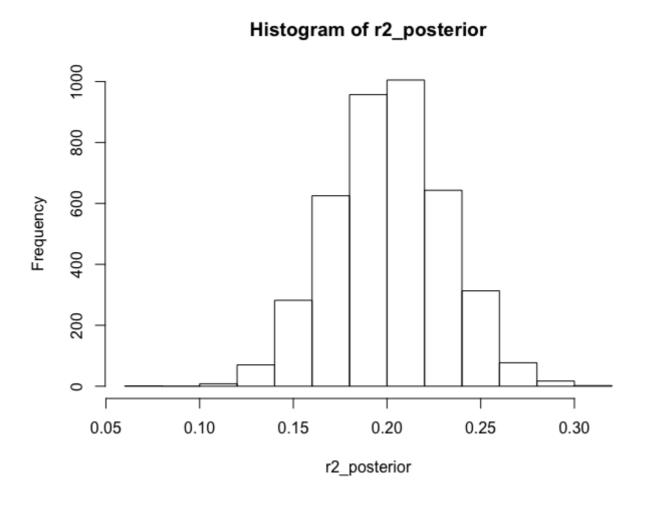
```
quantile(r2_posterior, probs = c(0.025, 0.975))
```

```
2.5% 97.5%0.1402846 0.2619605
```



R squared histogram

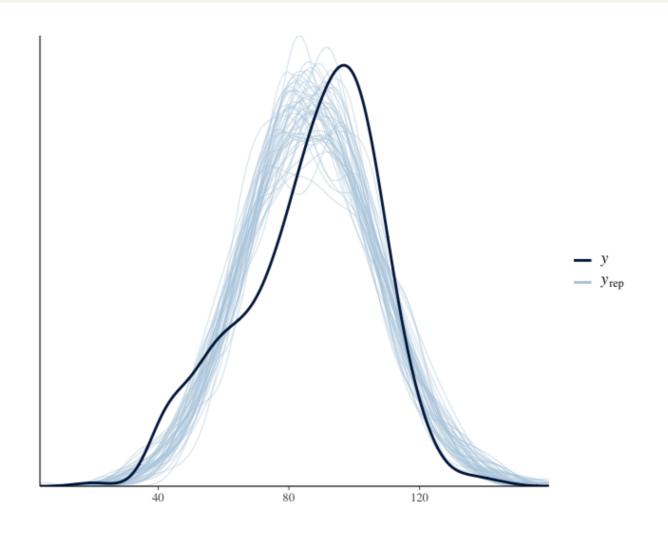
hist(r2_posterior)





Density overlay

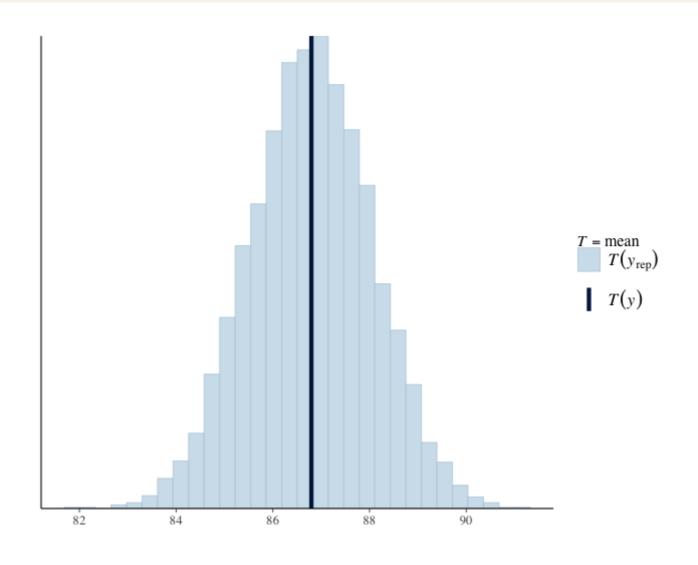
```
pp_check(stan_model, "dens_overlay")
```





Posterior predictive tests

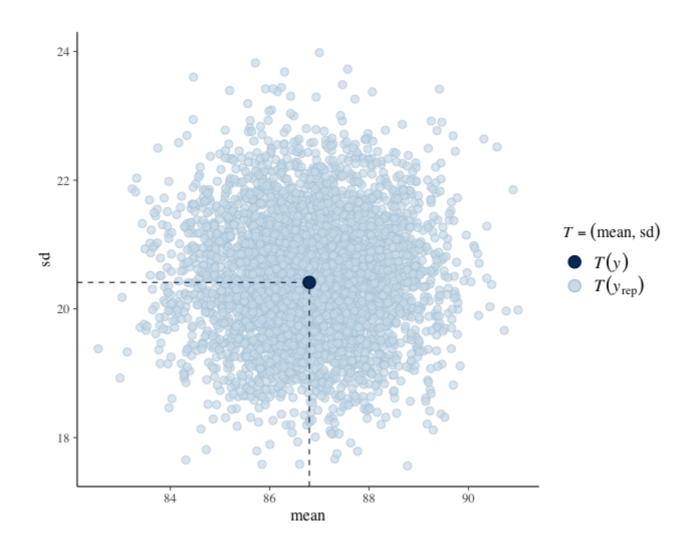
```
pp_check(stan_model, "stat")
```





Posterior predictive tests

```
pp_check(stan_model, "stat_2d")
```



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Bayesian model comparisons

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The loo package

- LOO = leave-one-out
 - Approximated cross validation
 - ?loo-package
 - Using loo for model comparisons

Using loo on a single model

```
library(rstanarm)
library(loo)
stan_model <- stan_glm(kid_score ~ mom_iq, data = kidiq)
loo(stan_model)</pre>
```

Model comparisons with loo

```
model_1pred <- stan_glm(kid_score ~ mom_iq, data = kidiq)
model_2pred <- stan_glm(kid_score ~ mom_iq * mom_hs, data = kidiq)

loo_1pred <- loo(model_1pred)
loo_2pred <- loo(model_2pred)

compare(loo_1pred, loo_2pred)</pre>
```

```
elpd_diff se
6.1 3.9
```

Model comparisons with loo

```
compare(loo_1pred, loo_2pred)
```

```
elpd_diff se
6.1 3.9
```

- Positive = prefer second model
- Negative = prefer first model
- Significant difference?
 - Absolute value of difference relative to standard error

Let's practice!

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