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characterization of connected compact metric spaces.

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Let  $(A, d)$  be a compact metric space. Then  $A$  is connected  $\iff \forall x, y \in A, \forall \varepsilon > 0 \exists n \in \mathbb{N}$ , and  $p_1, \dots, p_n \in A$ , such that  $p_1 = x, p_n = y$  and  $d(p_i, p_{i+1}) < \varepsilon$  ( $i = 1, \dots, n - 1$ )