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Tietze extension theorem

Canonical name	TietzeExtensionTheorem
Date of creation	2013-03-22 13:35:30
Last modified on	2013-03-22 13:35:30
Owner	matte (1858)
Last modified by	matte (1858)
Numerical id	5
Author	matte (1858)
Entry type	Theorem
Classification	msc 54D15
Related topic	ApplicationsOfUrysohnsLemmaToLocallyCompactHausdorffSpaces

Let X be a topological space. Then the following are equivalent:

1. X is normal.
2. If A is a closed subset in X , and $f: A \rightarrow [-1, 1]$ is a continuous function, then f has a continuous extension to all of X . (In other words, there is a continuous function $f^*: X \rightarrow [-1, 1]$ such that f and f^* coincide on A .)

Remark: If X and A are as above, and $f: A \rightarrow (-1, 1)$ is a continuous function, then f has a continuous extension to all of X .

The present result can be found in [?].

References

- [1] A. Mukherjea, K. Pothoven, *Real and Functional analysis*, Plenum press, 1978.