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relatively prime integer topology

Canonical name	RelativelyPrimeIntegerTopology
Date of creation	2013-03-22 14:42:07
Last modified on	2013-03-22 14:42:07
Owner	mathcam (2727)
Last modified by	mathcam (2727)
Numerical id	7
Author	mathcam (2727)
Entry type	Definition
Classification	msc 54E30
Defines	prime integer topology

Let X be the set of strictly positive integers. The *relatively prime integer topology* on X is the topology determined by a basis consisting of the sets

$$U(a, b) = \{ax + b \mid x \in X\}$$

for any a and b are relatively prime integers. That this does indeed form a basis is found in <http://planetmath.org/HausdorffSpaceNotCompletelyHausdorff> this entry.

Equipped with this topology, X is <http://planetmath.org/T0SpaceT0>, <http://planetmath.org/T1SpaceT1>, and <http://planetmath.org/T2SpaceT2>, but satisfies none of the higher separation axioms (and hence meet very few compactness criteria).

We can define a coarser topology on X by considering the subbasis of the above basis consisting of all $U(a, b)$ with a being a prime. This is called the *prime integer topology* on \mathbb{Z}^+ .

References

- [1] L.A. Steen, J.A. Seebach, Jr., *Counterexamples in topology*, Holt, Rinehart and Winston, Inc., 1970.