



planetmath.org

Math for the people, by the people.

Schauder lemma

Canonical name	SchauderLemma
Date of creation	2013-03-22 19:09:44
Last modified on	2013-03-22 19:09:44
Owner	karstenb (16623)
Last modified by	karstenb (16623)
Numerical id	4
Author	karstenb (16623)
Entry type	Theorem
Classification	msc 54E50
Classification	msc 46A30
Related topic	OpenMappingTheorem
Defines	almost open set

The following theorem is in the functional analysis literature generally referred to as the *Schauder lemma*. It is a version of the open mapping theorem in Fréchet spaces and is often used to verify the open-ness of linear, continuous maps.

Theorem. Let E, F be Fréchet spaces. Denote by $\mathcal{U}_0(E), \mathcal{U}_0(F)$ the zero neighborhood filter of E and F respectively. Let $T: E \rightarrow F$ be a linear and continuous map which is *almost open*, i.e.

$$\forall U \in \mathcal{U}_0(E) \overline{T(U)}^F \in \mathcal{U}_0(F)$$

Then T is open.