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How are normal and T4 spaces defined in books?

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A recent discussion on PlanetMath has led me to consider how various sources define normal and T4 spaces. I limited myself to books, mostly textbooks. No articles were consulted. As will be seen from the table below, there is no agreement on the question of how to define it. I am not giving precise references at this time, and may choose to never do that. I think the abbreviated form may be sufficient for those that seek to check what I have done. If you want to add something to the table, file a correction. S refers to the condition that closed sets can be separated by open sets. The condition S is due to Tietze, according to Alexandroff and Hopf. Of course, $T1 + S$ is the same as $T2 + S$.

Source	Normal	T4	Page	Year
Alexandroff and Hopf	$T1+S$	$T1+S$	68	1935
Wilder	S	?	49	1949
Kelley	S	$T1+S$	112	1955
Hocking and Young	$T1+S$	$T1+S$	41	1961
Pervin	S	$T1+S$	88	1964
Gaal	$T1+S$	S	87	1964
Lipschutz	S	$T1+S$	141	1965
Husain	$T1+S$	S	7	1966
Dugundji	$T2+S$	$T2+S$	144	1966
Gemignani	$T1+S$	S	102	1967
Willard	S	$T1+S$	99	1970
Steen and Seebach	$T1+S$	S	12	1970
Maunder	S	-	15	1970
Munkres	$T1+S$	-	195	1975
Morris	S	$T2+S$	121	1988
Repovš	$T1+S$	S	6	1998
Stroppel	$T2+S$	S	6	2006