



Math for the people, by the people.

dense in-itself

Canonical name	DenseInitself
Date of creation	2013-03-22 14:38:29
Last modified on	2013-03-22 14:38:29
Owner	rspuzio (6075)
Last modified by	rspuzio (6075)
Numerical id	4
Author	rspuzio (6075)
Entry type	Definition
Classification	msc 54A99
Related topic	ScatteredSpace

A subset  $A$  of a topological space is said to be *dense-in-itself* if  $A$  contains no isolated points.

Note that if the subset  $A$  is also a closed set, then  $A$  will be a perfect set. Conversely, every perfect set is dense-in-itself.

A simple example of a set which is dense-in-itself but not closed (and hence not a perfect set) is the subset of irrational numbers. This set is dense-in-itself because every neighborhood of an irrational number  $x$  contains at least one other irrational number  $y \neq x$ . On the other hand, this set of irrationals is not closed because every rational number lies in its closure.

For similar reasons, the set of rational numbers is also dense-in-itself but not closed.