

$$pLerp(t, p0, pM) := p0 \cdot (1 - t) + pM \cdot t$$

$$sqrLerp(t, p0, pM) := p0 \cdot (1 - \sqrt{t}) + pM \cdot \sqrt{t}$$

basic lerp formulas

$$ro(h) := Adens0 - \frac{h}{Ha} \cdot Adens0$$

density sampler

$$vpoint(s) := pLerp(s, Pv, Pve)$$

$$Lendp(s) := pLerp(s, endpPv, endpPve)$$

Light end point lerp between two light endpoints at view start and end

$$scanLightPt(t, s) := pLerp(t, vpoint(s), Lendp(s))$$

final sampling point in atmosphere.

$$RayAtmLen(s) := pLerp(s, endlPv, endlPve)$$

lerped length of atmosphere ray

$$H(s) := pLerp(s, 0, Ha) \rightarrow Ha \cdot s$$

interpolated point of ray atmospheric exit

distance to exit for light at t-point

$$Hr(t, s) := pLerp(t, H(s), Ha) \rightarrow Ha \cdot s \cdot (-t + 1) + Ha \cdot t$$

$$curVLen(p) := pLerp(p, 0, LmaxV)$$

Length to current view t-point on view ray

Sum density over line, defined by heights

Remaining power after travelling some distance at heights

sk is 0..1 where 0.9 means 10% of light gets scattered

remaining direct ray power, after travelling Len from Hs to He.

$$RemPower(Hs, He, Len, Pow0) := Pow0 \cdot ProdDensAvgP(Hs, He, Len)$$

$vpHitPow(pv) := RemPower(H(pv), Ha, RayAtmLen(pv), LPower)$ Total Ray power that hits point on view line
hf0- height at which it is 0, hfmax - height at which it is 1.

$$foc(hf) := \frac{hf + hf0}{hfmax}$$

Ray power that is reflected towards eye as scattered light. focusP is percent of sk

$$remTop := LPower \cdot (1 + sk \cdot (prk - 1))^{endlPve \cdot roTop}$$

$$remBot := LPower \cdot (1 + sk \cdot (prk - 1))^{endlPv \cdot roBot}$$

$$lerpHitPow(pv) := sqrLerp(pv, remBot, remTop)$$

$$reflectedBack(pr) := lerpHitPow(pr) \cdot focusP \cdot sk \cdot ro(H(pr)) \cdot ppxi$$

power that reaches eye form view t-point thorough atmos.

$$remToEye(TEpow, TElen, pr) := TEpow \cdot (1 + sk \cdot (prk - 1))^{TElen \cdot roEye}$$

$$indirectEye(pn) := remToEye(reflectedBack(pn), curVLen(pn), pn)$$

This seems to be the latest version of formula

$$TotalToEye := \int_0^1 reflectedBack(pp) \cdot LmaxV \, dpp \rightarrow \frac{Adens0 \cdot LPower \cdot LmaxV \cdot focusP \cdot ppxi \cdot sk \cdot \langle 8 \cdot ((prk - 1) \cdot sk + 1)^{endlPve \cdot roTop} + 7 \cdot ((prk - 1) \cdot sk + 1)^{endlPv \cdot roBot} \rangle}{30}$$

$$\frac{Adens0 \cdot LPower \cdot LmaxV \cdot focusP \cdot ppxi \cdot sk \cdot \langle 8 \cdot ((prk - 1) \cdot sk + 1)^{endlPve \cdot roTop} + 7 \cdot ((prk - 1) \cdot sk + 1)^{endlPv \cdot roBot} \rangle}{30}$$

**solution
to to above**

$$FadedToEye := \boxed{TotalToEye} \cdot (1 + sk \cdot (prk - 1))^{-\frac{LmaxV}{2} \cdot roEyeAvg}$$

$$\int_0^1 indirectEye(pp) \cdot LmaxV \, dpp \rightarrow -\left(Adens0 \cdot LPower \cdot focusP \cdot ppxi \cdot sk \cdot \left(\left(2 \cdot LmaxV \cdot roEye \cdot \sqrt{\pi} \cdot \ln((prk - 1) \cdot sk + 1) + 3 \cdot \sqrt{\pi} \right) \cdot ((prk - 1) \cdot sk + 1) \right) \right)$$

$$\frac{1}{Lmax} \cdot \int_0^{Lmax} ro \left(H \left(\frac{s}{Lmax} \right) \right) \, ds \rightarrow \frac{Adens0}{2}$$

$$sk := 0.3 \cdot \frac{m^3}{kg \cdot km} = (3 \cdot 10^{-4}) \frac{m^2}{kg}$$

$$\frac{kg}{m^3} \cdot km$$

how much light hits one m^2

$$powM2 := lx$$

$$\rho := \frac{kg}{m^3} \quad sk_{unit} := \frac{1}{kg}$$

$$sk := 3 \quad \begin{array}{l} \text{skm is how much light is} \\ \text{scattered by } 1m \cdot 1m \cdot 1km \cdot \\ \rho \end{array}$$

$$mass1 := \boxed{\rho_{AV}} \cdot \frac{kg}{m^3} \cdot dist \cdot 1000 \cdot m^3$$

$$sk^{mass1 \cdot sk_{unit}} \rightarrow 3^{1000 \cdot dist \cdot \rho_{AV}}$$

$$2 \cdot x = b \xrightarrow{\text{solve}, x} \frac{b}{2}$$

$$vol := \boxed{\rho_{Avg}} \cdot \left(\frac{kg}{m^3} \right) \cdot dist \cdot 1000 \cdot m$$

$$powM2 \cdot sk^{vol} \rightarrow lx \cdot 3^{\frac{1000 \cdot dist \cdot kg \cdot \rho_{Avg}}{m^2}}$$

$$x^{pow} = K Msk \xrightarrow{\text{solve}, x} e^{\frac{\ln(K Msk)}{pow}}$$

$$e^{\frac{\ln(0.05)}{1000}} = 0.997$$

$$x^{-1000} \rightarrow \frac{1}{x^{1000}}$$