

*Proof.* Left to the reader.

□