

$$G(2,7) \quad p=11 \quad q=5 \quad x=?$$

$$K = A \cdot B \cdot G = 5 \cdot 11 \cdot G = 55G$$

$$2G = (12, 16)$$

$$4G = (1, 5)$$

$$5G = 4G + G = (1, 12)$$

$$10G = (2, 7)$$

$$20G = (12, 16)$$

$$40G = (1, 5)$$

$$50G = (1, 12)$$

$$55G = (2, 7)$$

$$DSA \quad d=4, \quad p=11, \quad q=5$$

$$a) (11, 5, 4, 2)$$

$$b) (11, 5, 5, 7)$$

$$c) (11, 5, 5, 9)$$

$$d) (11, 5, 7, 3)$$

$$e) (11, 5, 2, 4)$$

$$5^5 \equiv 1 \pmod{11} \quad \text{OK}$$

$$4^5 \equiv 1 \pmod{11} \quad \text{OK}$$

$$7^5 \not\equiv 1 \pmod{11} \quad \text{NO}$$

$$2^5 \not\equiv 1 \pmod{11} \quad \text{NO}$$

$$\beta = 4^h \pmod{11} = 3 \quad \text{NOW IN SOLVING.}$$

$$\beta = 5^h \pmod{11} = 9$$

$$516^{5192} + 35^{4317} + 907^{7892} + 103^{5537} \quad \text{unit digit?}$$

$$\begin{array}{cccc} 5192 & 4317 & 7892 & 5537 \\ \downarrow & \downarrow & \downarrow & \downarrow \\ 6 & 5 & 7 & 3 \end{array}$$

$$6 + 5 + 7 + 3 = 15 \rightarrow 5$$

$$\begin{array}{l} 6^0 = 1 \\ 6^1 = 6 \\ 6^2 = 36 \\ 6^3 = 216 \\ 6^4 = 1296 \end{array}$$

$$m=6$$

$$\begin{array}{l} 7^0 = 1 \\ 7^1 = 7 \\ 7^2 = 49 \\ 7^3 = 343 \\ 7^4 = 2401 \end{array}$$

$$\Rightarrow x = 7892 \pmod{4} = 0$$

$$m = 7^0 = 1$$

$$\begin{array}{l} 3^0 = 1 \\ 3^1 = 3 \\ 3^2 = 9 \\ 3^3 = 27 \\ 3^4 = 81 \end{array}$$

$$\Rightarrow x = 5537 \pmod{4} = 1$$

$$m = 3^1 = 3$$

$$\begin{array}{l} 5^0 = 1 \\ 5^1 = 5 \\ 5^2 = 25 \\ 5^3 = 125 \end{array}$$

$$m=5$$