

# Full Presentation Title

## Optional Subtitle

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# Outline

Introduction

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# Slide Title

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# Simplified Foundation Model

$$y = f_n(f_{n-1}(\dots f_1(x)))$$

$$f_i = \sigma(W_i x + b_i)$$

Our input  $x$  is a 2d matrix, the  $W$ 's are linear transformations so they can be represented as matrices, and  $\sigma$  is a nonlinear function.

# Pipeline Parallelism

## Tensor Parallelism(Row)

We can split the weight matrix  $W_i$  into groups of rows depending on how many devices we have. Each entry of the  $k$ th result of  $W_i x$  is equal to the  $k$ th row of  $W_i$  times  $x$ , so we just have each device compute  $C_j x$ . Since each device is fully responsible for specific entries of the result, we can also give the corresponding entries of  $b_i$ , which we will label  $b_{L_j}$  to each device and apply our nonlinear function. We end up with each device computing  $\sigma(C_j x + b_{L_j})$ , and then gathering the various elements from each device into a single vector to be fed into the next function

$$W_i = \begin{bmatrix} C_1 \\ C_2 \\ \vdots \\ C_m \end{bmatrix}$$

## Tensor Parallelism(Column)

We can split the weight matrix  $W_i$  into smaller matrices depending on the number of devices we have. Each  $A_j$  is stored on a different device, and along with it we send the entries of  $x$  that correspond to the columns of  $W_i$  that are held within each  $A_j$  as a column vector,  $x_{L_j}$ .

$$W_i = [A_1 \quad A_2 \quad \dots \quad A_3]$$

Each device is then computing  $A_j x_{L_j}$  which we can think of as

$$A_j x_{L_j} = \begin{bmatrix} a_{11}(j) & a_{12}(j) & \dots & a_{1k}(j) \\ a_{21}(j) & a_{22}(j) & \dots & a_{2k}(j) \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1}(j) & a_{m2}(j) & \dots & a_{mk}(j) \end{bmatrix} \begin{bmatrix} x_p \\ x_p + 1 \\ \vdots \\ x_p + k - 1 \end{bmatrix}$$

# Tensor Parallelism(Column) pt 2

# Thank You

Questions?