

1D Linear Advection - Sine Wave

Problem Specification

Use Case. Linear Advection

Spatial domain: $0 \leq x < 1$ meters, periodic boundary conditions

Governing equations: 1D Linear Advection Equation

$$\frac{\partial \phi}{\partial t} = -\mathbf{u} \cdot \nabla \phi$$

Initial conditions:

$$\phi(x) = \sin(2\pi x)$$

$$\mathbf{u} = 1 \text{ m/s}$$

The Saiph's code specification can be seen at: [Click to Saiph code](#)

Simulation details

$$\Delta x = 1 \text{ mm}$$

$$\Delta t = 1 \text{ ms}$$

$$nsteps = 1000$$

Forward in-time integration using Euler method: $\mathcal{O}(x)$

Spatial differentiation accuracy (default): $\mathcal{O}(x^4)$

Results

Output results at three time-steps are presented in Figure 1.

The L_2 norm has been computed over the ϕ variable taking the initial conditions as the analytic solution. The output simulation presents no truncation error $L_2 = 0$

The Saiph's simulation animation can be seen at: [Click to video](#)

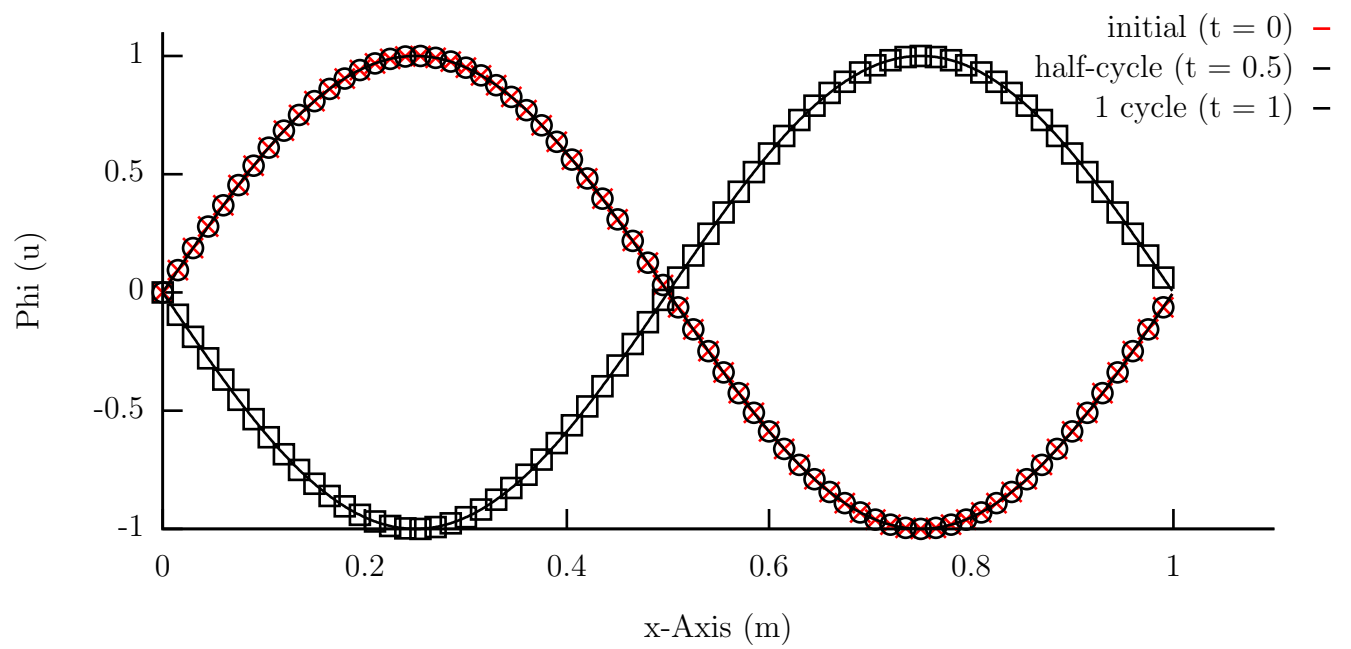


Figure 1: Phi profile at different time-steps.