# ReSCORE: Label-free Iterative Retriever Training for Multi-hop Question Answering with Relevance-Consistency Supervision

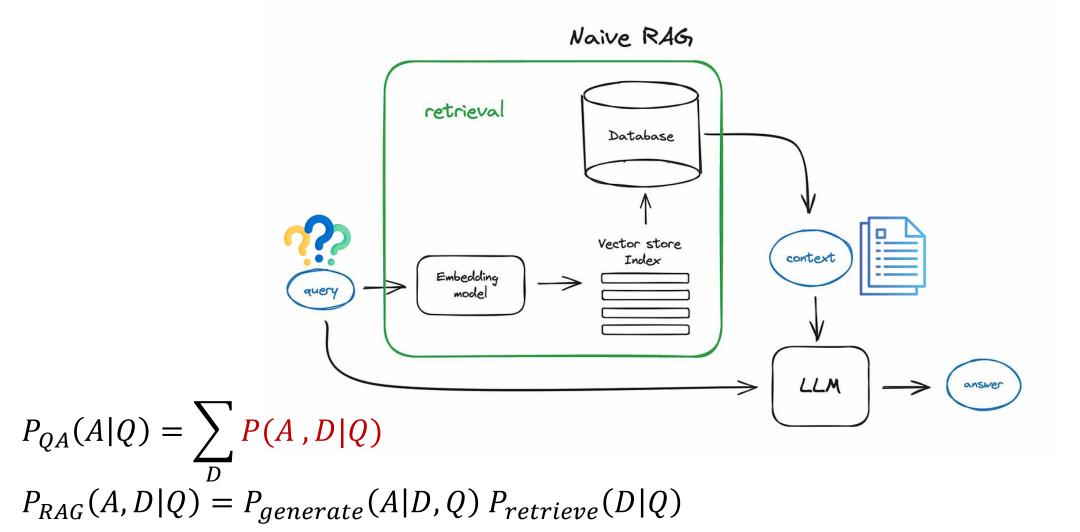
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#### Retrieval Augmented Generation

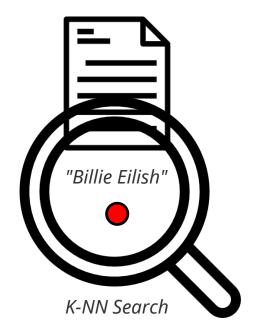




### Multi-hop Question Answering & Challenges

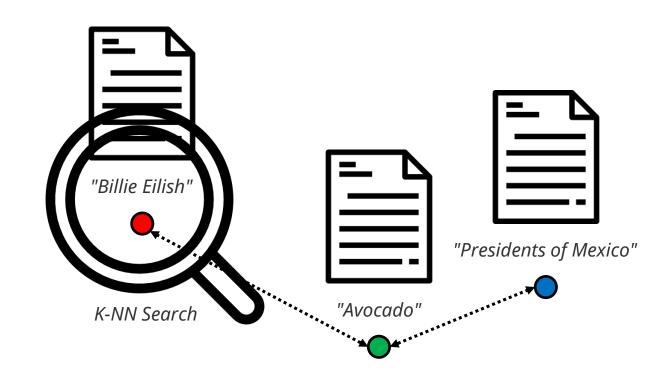
#### Single-hop





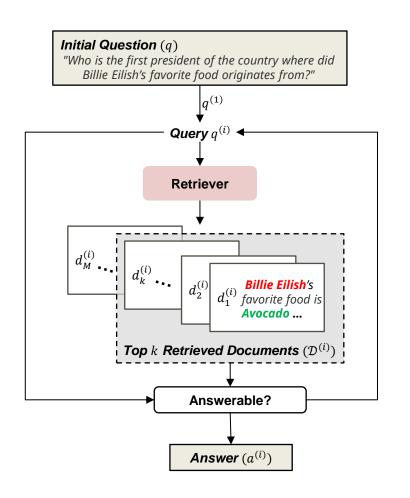
#### Multi-hop

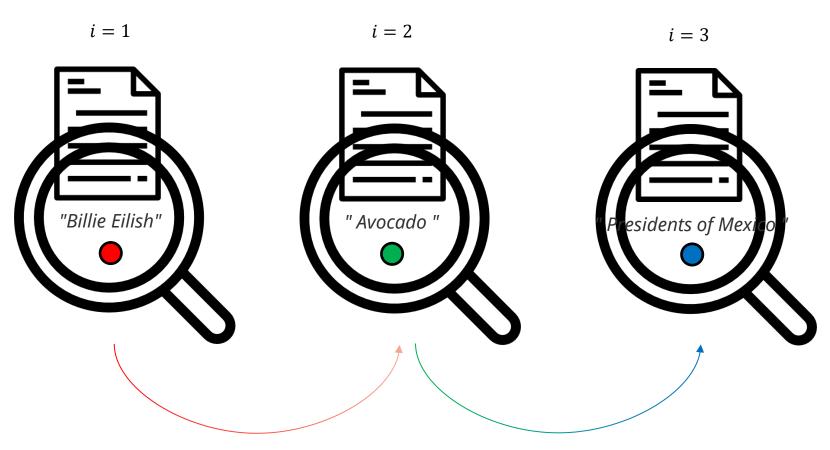
"Who is the first president of the country where did Billie Eilish's favorite food originates from?"





#### Iterative RAG Inference Framework





"Billie Eilish's favorite food is Avocado" "Avocado originated from Mexico"



## Challenges of Labeling MHQA & Label-free Training



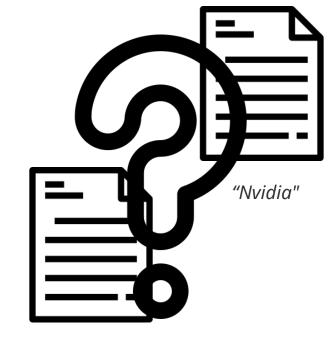
"Who is the first president of the country where did Billie Eilish's favorite food originates from?"



"Billie Eilish"



"Elon Musk"



"South Korea"



" Presidents of Mexico "



" Avocado"



"Paris"

#### Relevance-Consistency Supervision

$$P_{QA}(A|Q) = \sum_{D} P(A, D|Q)$$

 $P_{RAG}(A, D|Q) = P_{generate}(A|D, Q) P_{retrieve}(D|Q)$ 

 $P_{Retriever}(D|Q) \propto P_{LLM}(A,Q|D)$ 

 $P_{LLM}(A, Q|D) = P_{Consistency}(A|D, Q) P_{Relevance}(Q|D)$ 



"Who is the first president of the country where did Billie Eilish's favorite food originates from?"



"Presidents of Mexico"

 $P_{Consistency}(A|D,Q)$ 

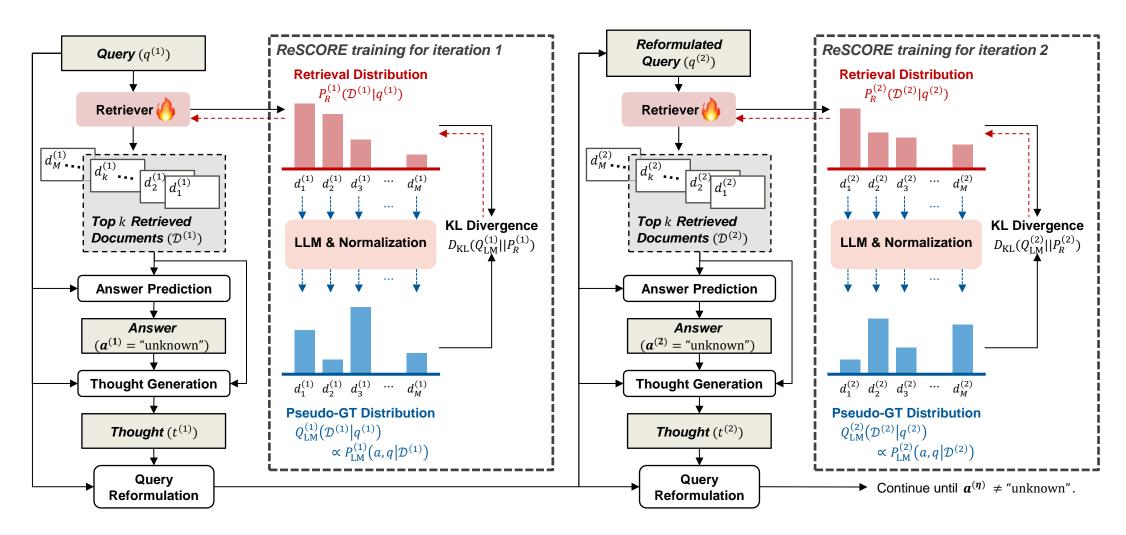


"Billie Eilish"

 $P_{Relevance}(Q|D)$ 



### ReSCORE Training





## Comparison to SOTA MHQA Baselines

| Model  | MuS<br>EM   | iQue<br>F1 | Hotpo<br>EM | otQA<br>F1 | 2Wiki<br>EM | iMHQA<br>F1 | Model                     | EM          | PA<br>F1     | i =      |
|--|-------------|------------|-------------|------------|-------------|-------------|---------------------------|-------------|--------------|----------|
| ReAcT (GPT-3.5+BM25)†                              | 10.2        | 19.7       | 36.0        | 46.9       | 28.0        | 37.3        |                           |             | MuSiQ        | ue       |
| FLARE (GPT-3.5+BM25)†                              | 11.2        | 18.7       | 36.4        | 47.8       | 31.8        | 42.8        | Self-RAG*                 | 1.2         | 8.2          | 25       |
| Self-RAG (GPT-3.5+BM25)†                           | 10.6        | 19.2       | 33.8        | 44.4       | 24.4        | 30.8        | +ReSCORE                  | 2.8         | 10.8         | 24       |
| Adaptive-Note (GPT-3.5+BM25)†                      | 13.2        | 24.2       | 45.6        | 58.4       | 43.2        | 54.2        | FLARE                     | 7.3         | 13.3         | 31       |
| IRCoT (Flan-T5-XL+BM25)‡                           | 22.0        | 31.8       | 44.42       | 56.2       | 49.7        | <u>54.9</u> | +ReSCORE                  | 8.2         | 15.3         | 30       |
| Adaptive-RAG (Flan-T5-XL+BM25)‡‡                   | 23.6        | 31.8       | 42.0        | 53.8       | 40.6        | 49.8        | Adaptive-Note<br>+ReSCORE | 9.6<br>11.2 | 17.7<br>20.5 | 44<br>45 |
| Our Baseline (Llama-3.1-8B+BM25)                   | 15.2        | 23.6       | 42.2        | 55.7       | 44.6        | 52.2        | Our Baseline              | 15.2        | 23.8         | 44       |
| Our Baseline (Llama-3.1-8B+Contriever)             | 15.2        | 23.8       | 39.4        | 52.3       | 32.8        | 41.6        | +ReSCORE                  | 23.4        | 32.7         | 46       |
| IQATR (Llama-3.1-8B+Contriever trained w/ ReSCORE) | <u>23.4</u> | 32.7       | 47.2        | 59.3       | 50.0        | <b>59.7</b> |                           |             | Hotpot(      | QA       |
|  |             |            |             |            |             |             |                           |             | 4=0          |          |

| Method                   |      | MQ   |      |      | HQA  |      |      | 2WQ  |      |
|--------------------------|------|------|------|------|------|------|------|------|------|
|                          | cEM  | EM   | F1   | cEM  | EM   | F1   | cEM  | EM   | F1   |
| Self-Ask                 | -    | 13.8 | 27.0 | -    | -    | -    | -    | 30.0 | 36.1 |
| Self-Ask + Search Engine | -    | 15.2 | 27.2 | -    | -    | -    | -    | 40.1 | 52.6 |
| SearChain + colBERT      | 17.1 | -    | -    | 56.9 | -    | -    | 46.3 | -    | -    |
| IQATR (Ours)             | 30.4 | 23.4 | 32.7 | 59.6 | 47.2 | 59.3 | 57.0 | 50.0 | 59.7 |

| Self-RAG*     | 5.6  | 17.9 | 36.1 | 36.5 | 36.5 |  |  |  |  |
|---------------|------|------|------|------|------|--|--|--|--|
| +ReSCORE      | 8.7  | 19.2 | 33.8 | 37.2 | 37.2 |  |  |  |  |
| FLARE         | 27.5 | 38.9 | 37.2 | 48.4 | 48.4 |  |  |  |  |
| +ReSCORE      | 31.4 | 42.5 | 39.2 | 48.5 | 51.7 |  |  |  |  |
| Adaptive-Note | 42.0 | 55.3 | 44.8 | 49.8 | 50.1 |  |  |  |  |
| +ReSCORE      | 43.8 | 58.0 | 47.3 | 63.3 | 77.2 |  |  |  |  |
| Our Baseline  | 39.4 | 52.3 | 44.8 | 47.5 | 47.5 |  |  |  |  |
| +ReSCORE      | 47.2 | 59.3 | 46.6 | 69.3 | 72.4 |  |  |  |  |
| 2WikiMHQA     |      |      |      |      |      |  |  |  |  |
| Self-RAG*     | 3.0  | 19.1 | 26.3 | 27.1 | 27.1 |  |  |  |  |
| +ReSCORE      | 5.6  | 21.2 | 25.9 | 28.4 | 32.8 |  |  |  |  |
| FLARE         | 23.2 | 35.0 | 32.5 | 42.9 | 42.9 |  |  |  |  |
| +ReSCORE      | 26.5 | 38.0 | 33.2 | 45.6 | 45.6 |  |  |  |  |
| Adaptive-Note | 35.7 | 46.1 | 45.7 | 59.2 | 59.2 |  |  |  |  |
| +ReSCORE      | 37.4 | 49.3 | 49.8 | 63.2 | 67.5 |  |  |  |  |
| Our Baseline  | 32.8 | 41.6 | 45.7 | 56.9 | 56.9 |  |  |  |  |
| +ReSCORE      | 50.0 | 59.7 | 51.2 | 81.2 | 88.0 |  |  |  |  |
|               |      |      |      |      |      |  |  |  |  |

 $\mathbf{MHR}_{i} @ \mathbf{8}$   $i = 1 \quad i = 2 \quad i = \eta_{n}$ 

25.8

31.6

37.1

40.1

50.2

49.8

51.6

63.0

25.8 24.9

31.0

30.9

45.1 44.9

46.8

25.8

31.6

37.1

43.3

50.2

55.3

51.6

65.2

#### Pseudo-GT Supervision Ablation

|          | MQ   |      |      | HQA  |      |      | 2WQ  |      |      |
|----------|------|------|------|------|------|------|------|------|------|
|          | R@8  | EM   | F1   | R@8  | EM   | F1   | R@8  | EM   | F1   |
| None     | 47.1 | 15.2 | 23.8 |      |      | 52.3 | 58.9 | 32.8 | 41.6 |
| P(a d,q) | 41.4 | 5.8  | 12.3 |      | 19.2 | 26.4 | 41.9 | 18.8 | 26.5 |
| P(q d)   | 47.9 | 15.9 | 25.9 |      | 42.0 | 53.9 | 63.2 | 39.2 | 47.9 |
| P(q,a d) | 55.7 | 16.4 | 26.3 | 68.3 | 43.6 | 56.4 | 67.1 | 41.4 | 51.7 |

$$P_{QA}(A|Q) = \sum_{D} P(A, D|Q)$$

$$P_{RAG}(A, D|Q) = P_{generate}(A|D, Q) P_{retrieve}(D|Q)$$

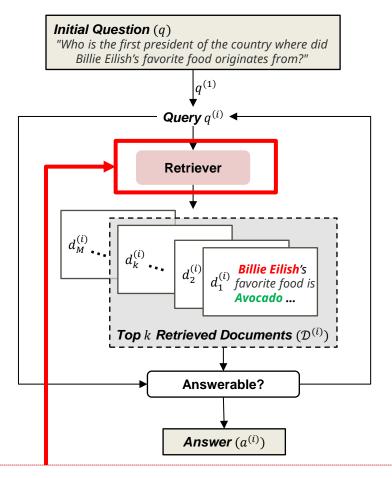
$$P_{Retriever}(D|Q) \propto \frac{P_{LLM}(A,Q|D)}{P_{LLM}(A,Q|D)}$$

$$P_{LLM}(A, Q|D) = P_{Consistency}(A|D, Q) P_{Relevance}(Q|D)$$



| Pseudo-GT Label                | R@2   | R@4   | R@8   | R@16  |  |  |  |  |  |
|--------------------------------|-------|-------|-------|-------|--|--|--|--|--|
| rseudo-G1 Label                | K@Z   | K@4   | K@o   | K@10  |  |  |  |  |  |
| MuSiQue                        |       |       |       |       |  |  |  |  |  |
| None                           | 32.71 | 40.10 | 47.06 | 53.61 |  |  |  |  |  |
| $P_{LM}(q \mid d)$             | 34.64 | 41.09 | 47.93 | 54.24 |  |  |  |  |  |
| $P_{\mathrm{LM}}(a \mid q, d)$ | 28.94 | 35.10 | 41.41 | 47.84 |  |  |  |  |  |
| $P_{LM}(q,a\mid d)$            | 42.68 | 50.31 | 55.66 | 60.38 |  |  |  |  |  |
| HotpotQA                       |       |       |       |       |  |  |  |  |  |
| None                           | 49.40 | 56.45 | 61.65 | 66.25 |  |  |  |  |  |
| $P_{\text{LM}}(q \mid d)$      | 55.15 | 62.35 | 65.85 | 69.10 |  |  |  |  |  |
| $P_{LM}(a \mid q, d)$          | 27.50 | 34.35 | 42.75 | 52.50 |  |  |  |  |  |
| $P_{LM}(q,a\mid d)$            | 58.05 | 64.60 | 68.30 | 70.65 |  |  |  |  |  |
| 2WikiMHQA                      |       |       |       |       |  |  |  |  |  |
| None                           | 46.40 | 54.30 | 58.85 | 63.35 |  |  |  |  |  |
| $P_{LM}(q \mid d)$             | 50.78 | 59.08 | 63.23 | 66.13 |  |  |  |  |  |
| $P_{\mathrm{LM}}(a \mid q, d)$ | 26.10 | 33.26 | 41.85 | 51.20 |  |  |  |  |  |
| $P_{LM}(q,a\mid d)$            | 53.73 | 62.98 | 67.10 | 68.73 |  |  |  |  |  |

## Comparison with GT

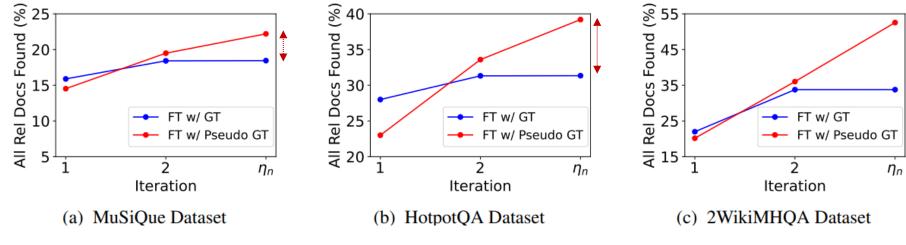


Replaced the Retriever with GT-trained

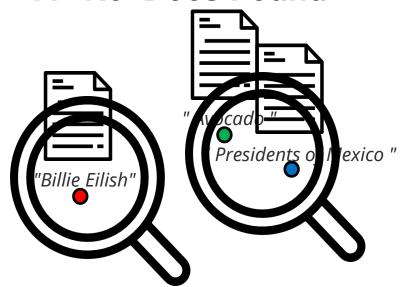
|           | QA   |           |       | $\mathrm{MHR}_i$ @8 |              |  |  |  |  |
|-----------|------|-----------|-------|---------------------|--------------|--|--|--|--|
| Label     | EM   | <b>F1</b> | i = 1 | i = 2               | $i = \eta_n$ |  |  |  |  |
| MuSiQue   |      |           |       |                     |              |  |  |  |  |
| None      | 15.2 | 23.8      | 44.9  | 51.6                | 51.6         |  |  |  |  |
| GT        | 15.8 | 24.9      | 46.7  | 54.8                | 54.8         |  |  |  |  |
| Pseudo-GT | 23.4 | 32.7      | 46.8  | 63.0                | 65.2         |  |  |  |  |
| HotpotQA  |      |           |       |                     |              |  |  |  |  |
| None      | 39.4 | 52.3      | 44.8  | 47.5                | 47.5         |  |  |  |  |
| GT        | 39.2 | 45.8      | 48.7  | 52.7                | 52.7         |  |  |  |  |
| Pseudo-GT | 47.2 | 59.3      | 46.6  | 69.3                | 72.4         |  |  |  |  |
| 2WikiMHQA |      |           |       |                     |              |  |  |  |  |
| None      | 32.8 | 41.6      | 45.7  | 56.9                | 56.9         |  |  |  |  |
| GT        | 37.1 | 46.2      | 48.5  | 61.7                | 61.7         |  |  |  |  |
| Pseudo-GT | 50.0 | 59.7      | 51.2  | 81.2                | 88.0         |  |  |  |  |

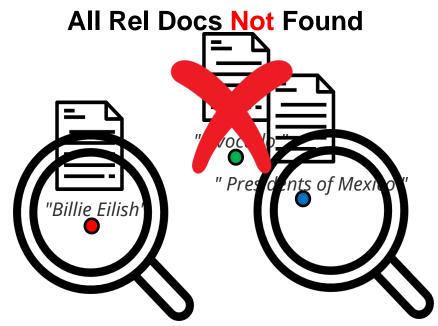


#### Comparison of GT and Pseudo-GT Labels



#### **All Rel Docs Found**





#### Query Reformulation Ablation



#### **Query Reformulation**

None

" Who is the first president of the country where did Billie Eilish's favorite food originates from?"

OR

**LLM-rewrite** 

"Who is the first president of the country where did **Avocado** originates from?"

OR

"Who is the first president of the country where did **Thought-concat** Billie Eilish's favorite food originates from? **Billie Eilish**'s favorite food is **Avocado**."

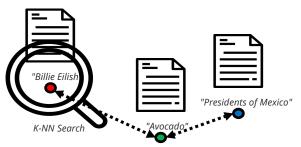
| Reformulation  | Q     | A    | $\mathbf{MHR}_i@8$ |       |              |  |  |  |  |
|----------------|-------|------|--------------------|-------|--------------|--|--|--|--|
| Method         | EM F1 |      | i = 1              | i = 2 | $i = \eta_n$ |  |  |  |  |
| MuSiQue        |       |      |                    |       |              |  |  |  |  |
| None           | 10.8  | 17.8 | 44.7               | 45.4  | 47.4         |  |  |  |  |
| LLM-rewrite    | 21.2  | 30.5 | 45.1               | 56.7  | 63.7         |  |  |  |  |
| Thought-concat | 23.4  | 32.7 | 46.8               | 63.0  | 65.2         |  |  |  |  |
| HotpotQA       |       |      |                    |       |              |  |  |  |  |
| None           | 29.4  | 41.1 | 42.8               | 43.6  | 43.8         |  |  |  |  |
| LLM-rewrite    | 44.2  | 57.4 | 41.9               | 54.8  | 64.7         |  |  |  |  |
| Thought-concat | 47.2  | 59.3 | 46.6               | 69.3  | 72.4         |  |  |  |  |
| 2WikiMHQA      |       |      |                    |       |              |  |  |  |  |
| None           | 35.6  | 44.7 | 48.6               | 49.7  | 49.8         |  |  |  |  |
| LLM-rewrite    | 51.7  | 60.1 | 50.0               | 86.0  | 89.5         |  |  |  |  |
| Thought-concat | 50.0  | 59.7 | 51.2               | 81.2  | 88.0         |  |  |  |  |

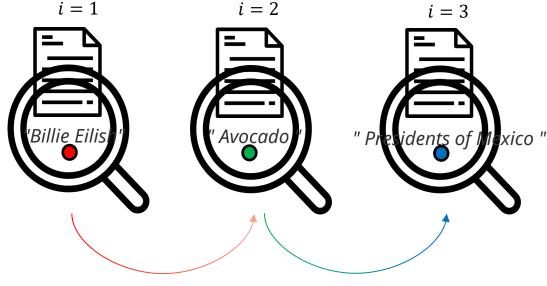
#### Summary











"Billie Eilish's favorite food is Avocado"

"Avocado originated from Mexico"



"Who is the first president of the country where did Billie Eilish's favorite food originates from?"









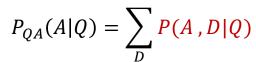


" Avocado"









 $P_{RAG}(A, D|Q) = P_{generate}(A|D, Q) P_{retrieve}(D|Q)$ 

 $P_{Retriever}(D|Q) \propto P_{LLM}(A,Q|D)$ 

 $P_{LLM}(A, Q|D) = P_{Consistency}(A|D, Q) P_{Relevance}(Q|D)$ 





"South Korea"

## E.O.D.