

# GNSS Outlines for RPD Challenge

## TECH DAY, RPD Challenge 2020

### 7<sup>th</sup> NOV 2020

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# What is GNSS?

Global Navigation Satellite System (GNSS) is the standard generic term for all navigation satellites systems like GPS, GLONASS, GALILEO, BeiDou, QZSS, NAVIC.

- Global Constellation

- GPS USA
- GLONASS, Russia
- Galileo, Europe
- BeiDou (COMPASS) / BDS, China

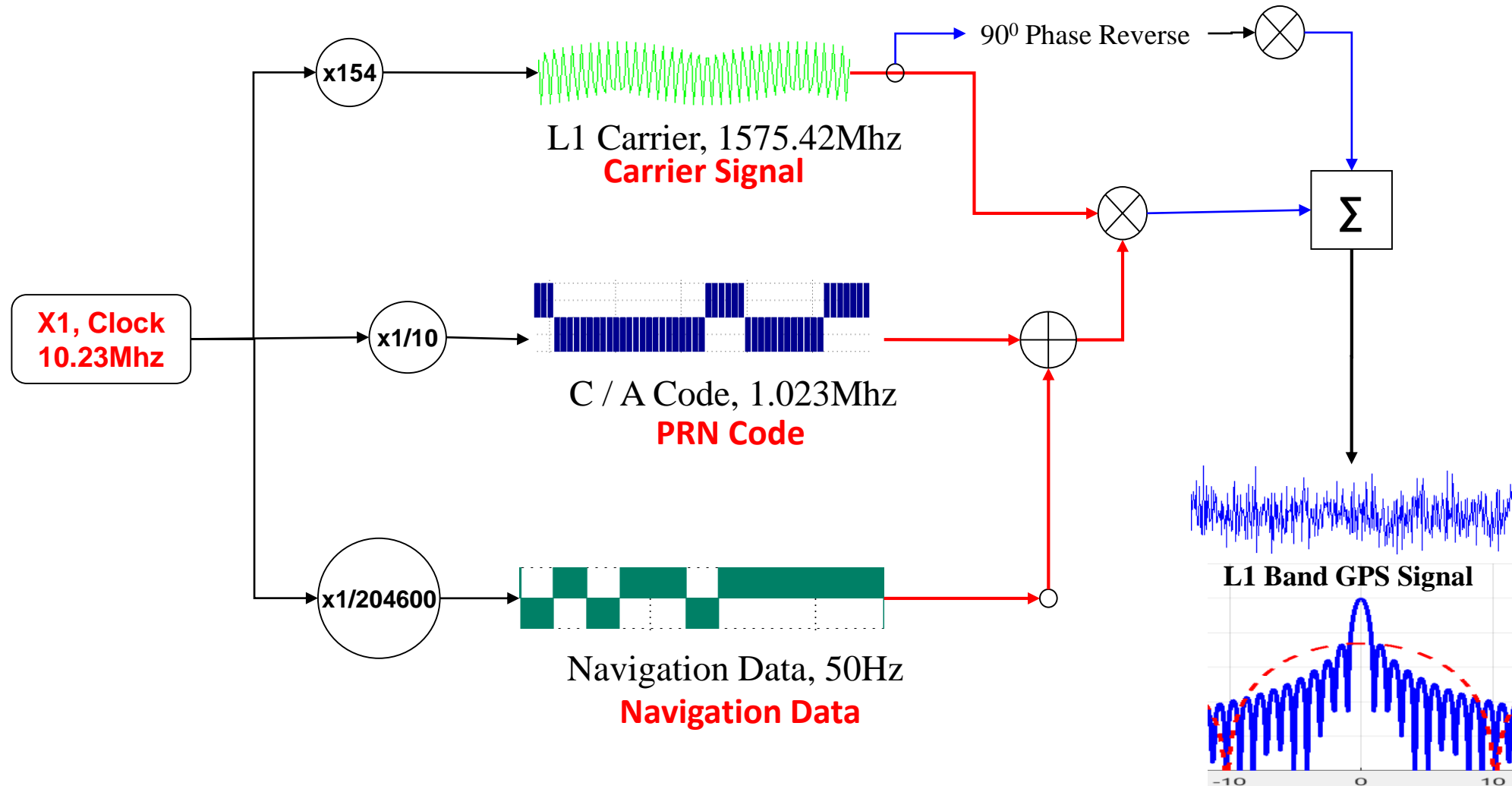
- Regional Constellation

- QZSS, Japan
- NAVIC (IRNSS), India

# GPS L1C/A Signal Structure

- Carrier Signal
  - It defines the frequency of the signal
  - For example:
    - GPS L1 is 1575.42MHz, L2 is 1227.60MHz and L5 is 1176.45MHz
- PRN Code
  - Used to identify satellite ID in CDMA
  - Requires to modulate the data
  - Should have good auto-correlation and cross-correlation properties
- Navigation Data
  - Includes satellite orbit related data (ephemeris data)
  - Includes satellite clock related information (clock errors etc)

# GPS, QZSS L1C/A Signal Structure

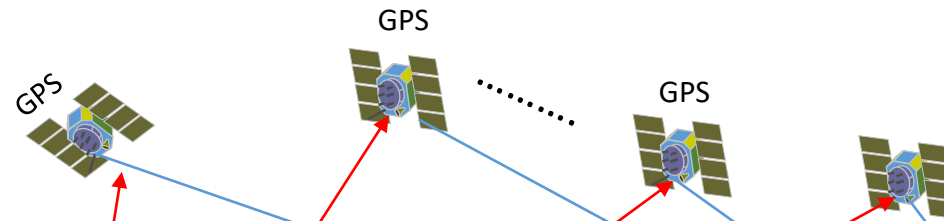
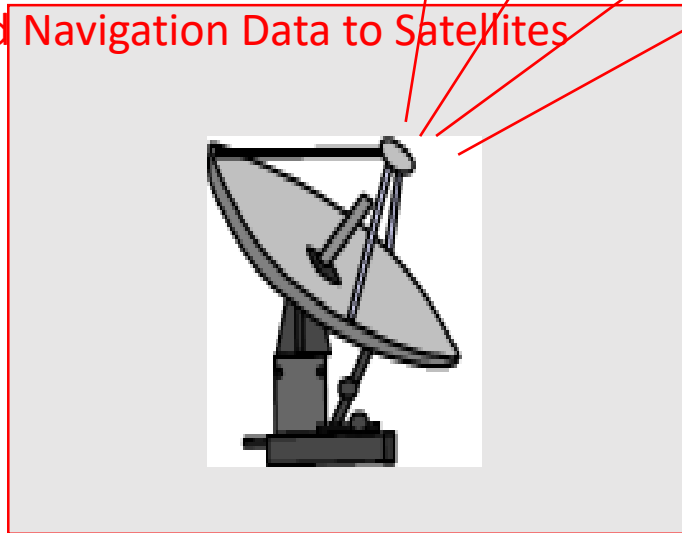


# GNSS Architecture

Space Segment  
GNSS Satellites

Control Segment

Monitor Satellite Health, Orbit, Clock etc  
Upload Navigation Data to Satellites



User Segment

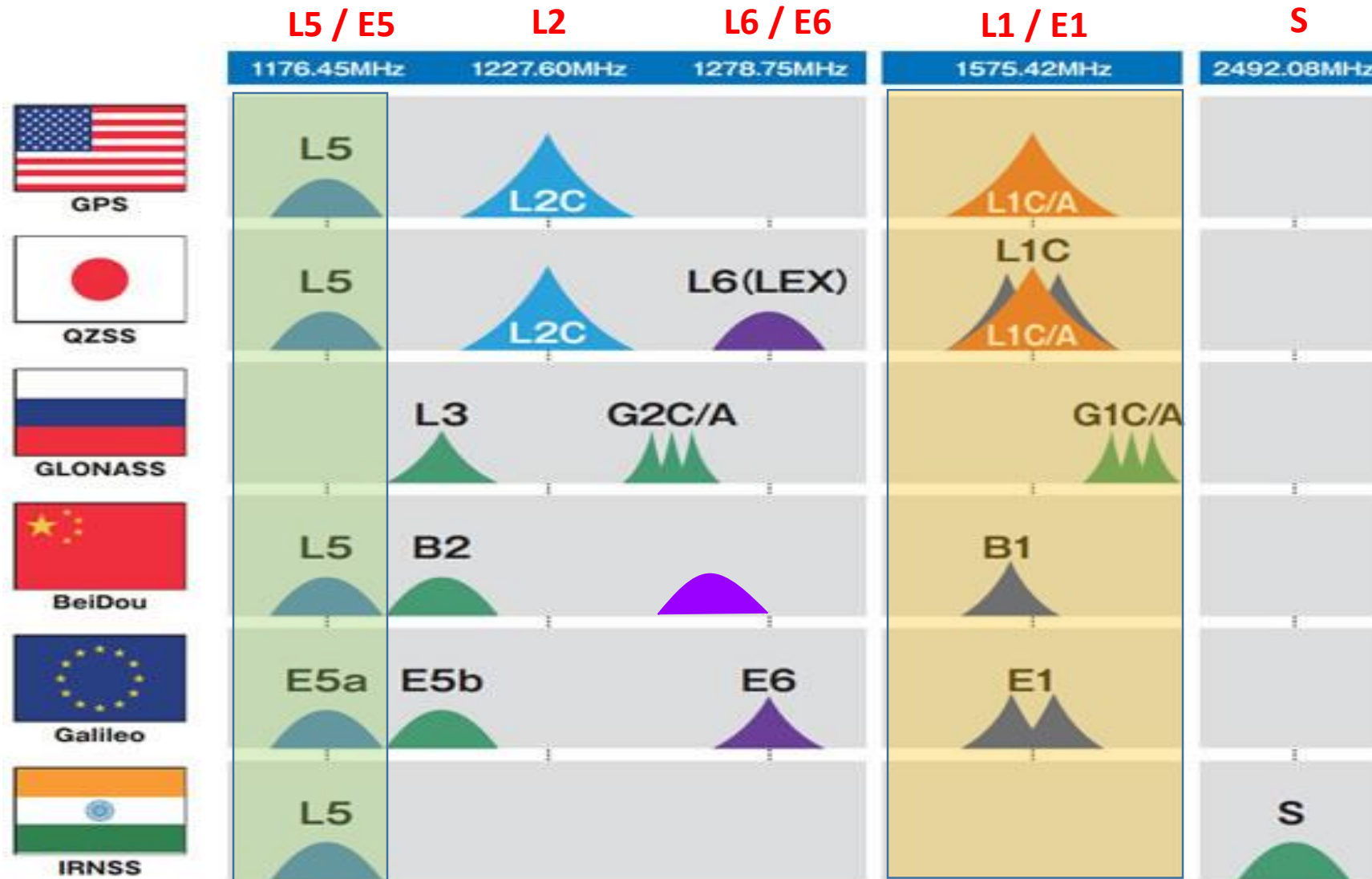
GNSS Receivers  
Applications that use GNSS

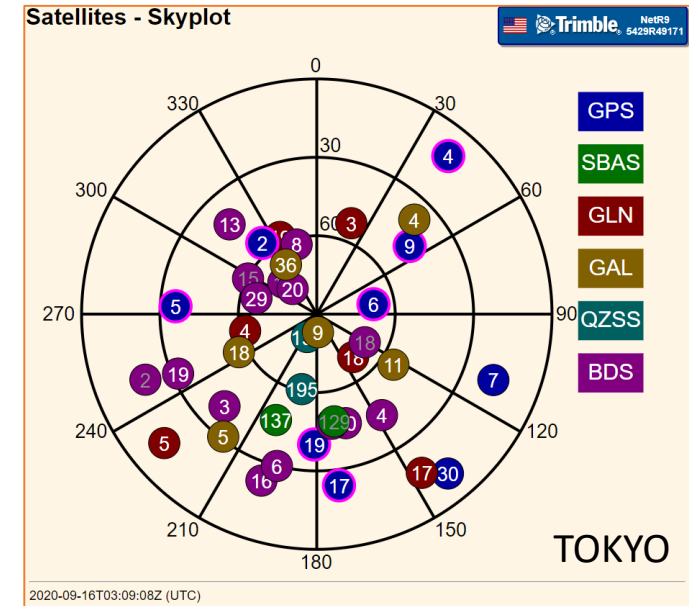
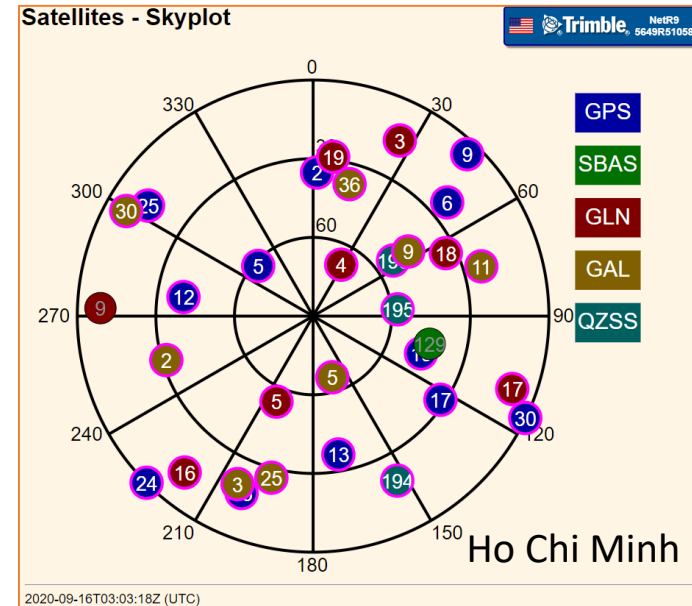
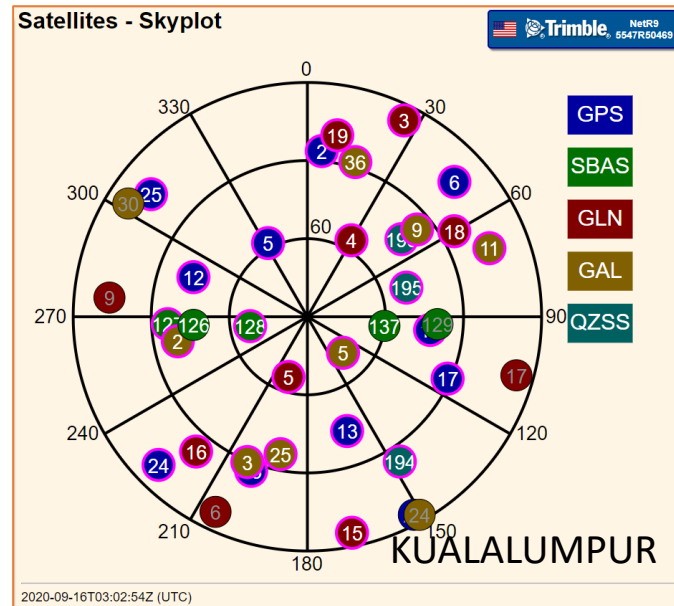
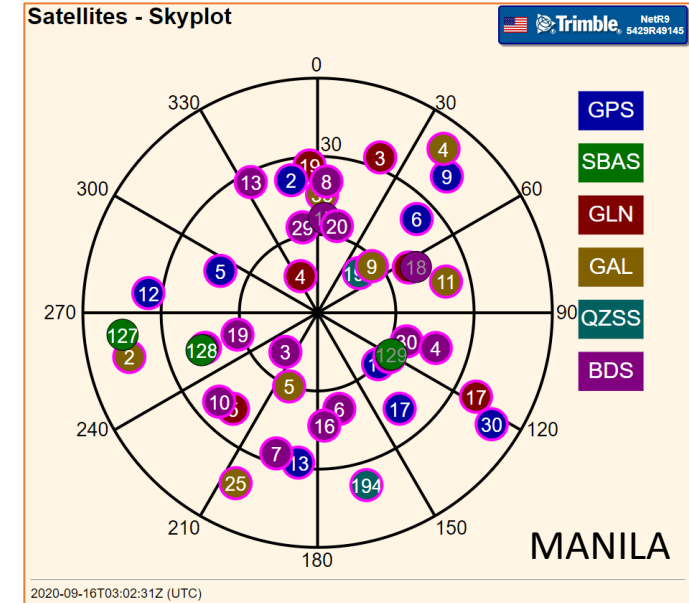
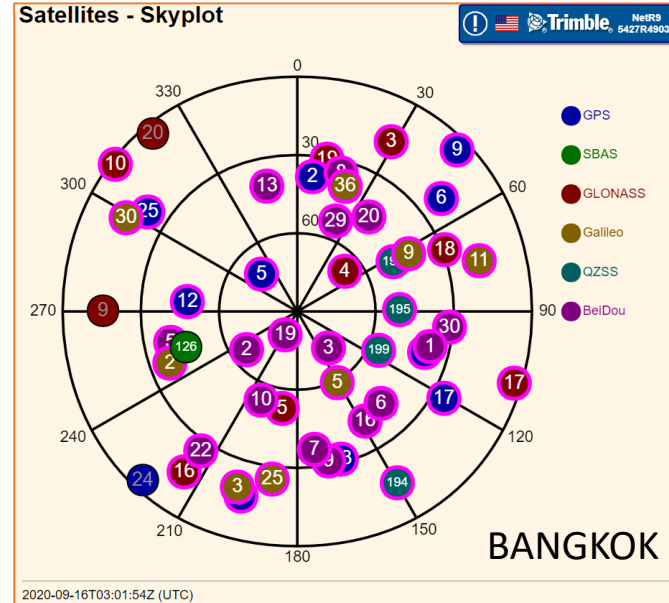
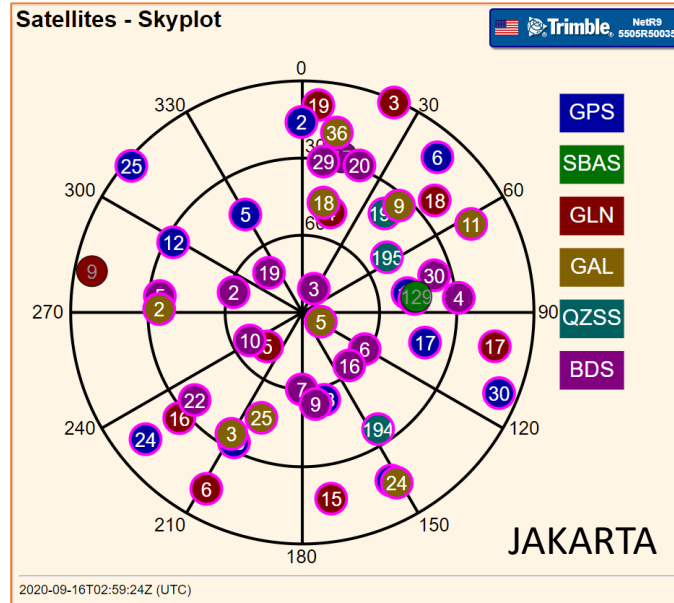


# GPS Signals

Band	Frequency, MHz	Signal Type	Code Length msec	Chip Rate, MHz	Modulation Type	Data / Symbol Rate, bps/sps	Notes
L1	1575.42	C/A	1	1.023	BPSK	50	Legacy Signal
		C <sub>Data</sub>	10	1.023	BOC(1,1)	50 / 100	From 2014
		C <sub>Pilot</sub>	10	1.023	TMBOC	No Data	BOC(1,1) & BOC(6,1)
		P(Y)	7 days	10.23	BPSK		Restricted
L2	1227.60	CM	20	0.5115	BPSK	25 / 50	Modulated by TDM of (L2CM xor Data) and L2CL
		CL	1500	0.5115		No Data	
		P(Y)	7days	10.23	BPSK		
L5	1176.45	I	1	10.23	BPSK	50 / 100	Provides Higher Accuracy
		Q	1			No Data	

# Multi-GNSS Signals

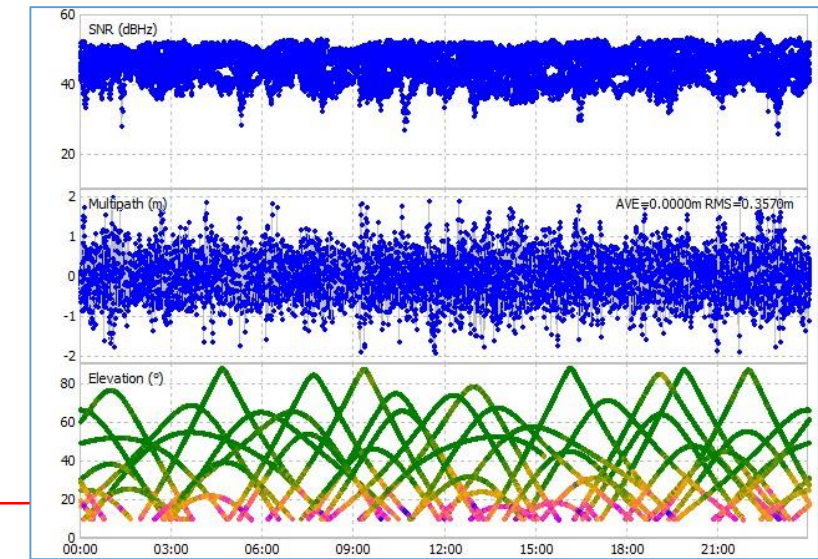
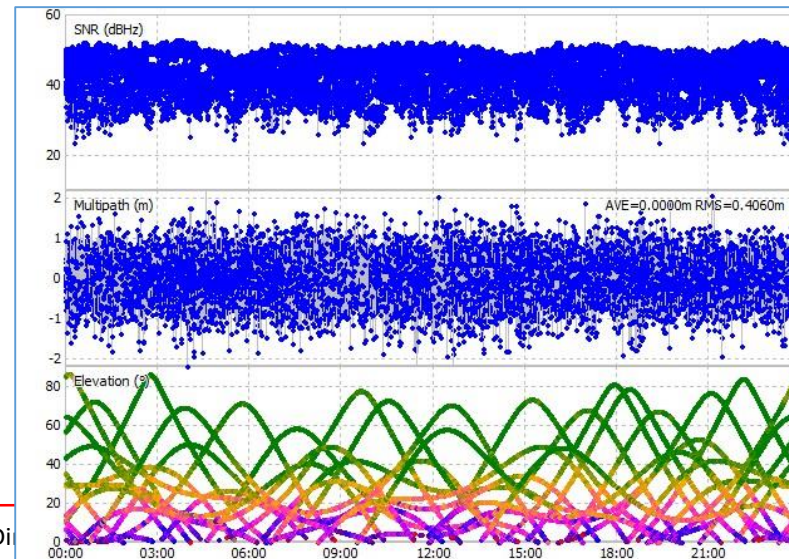
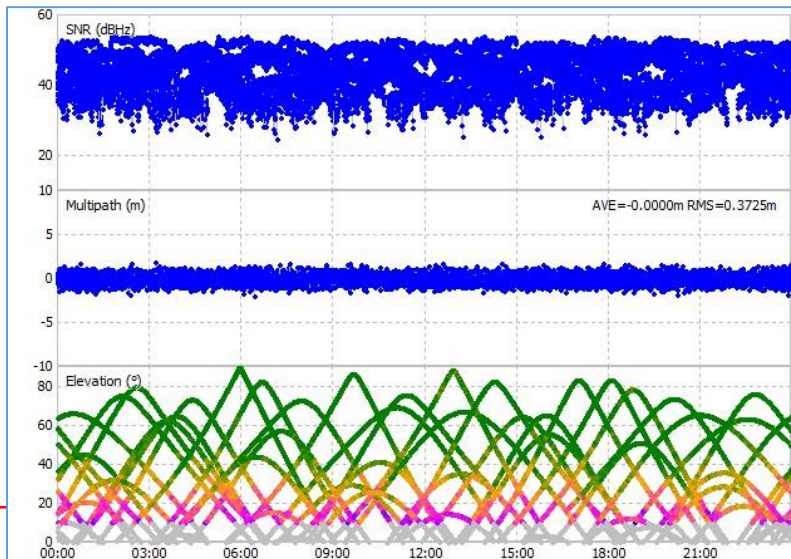
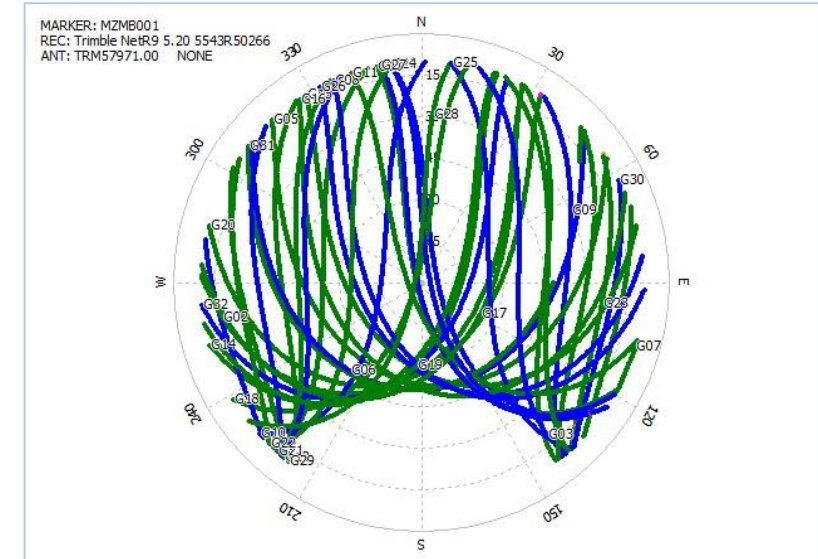
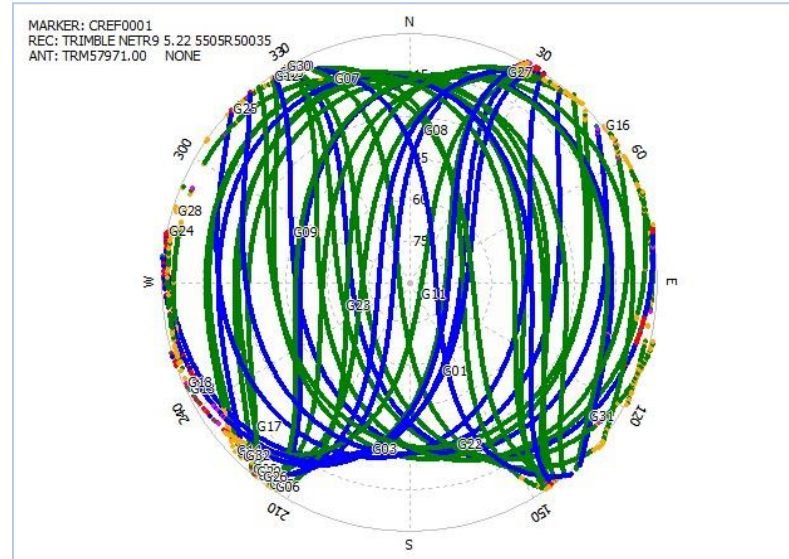
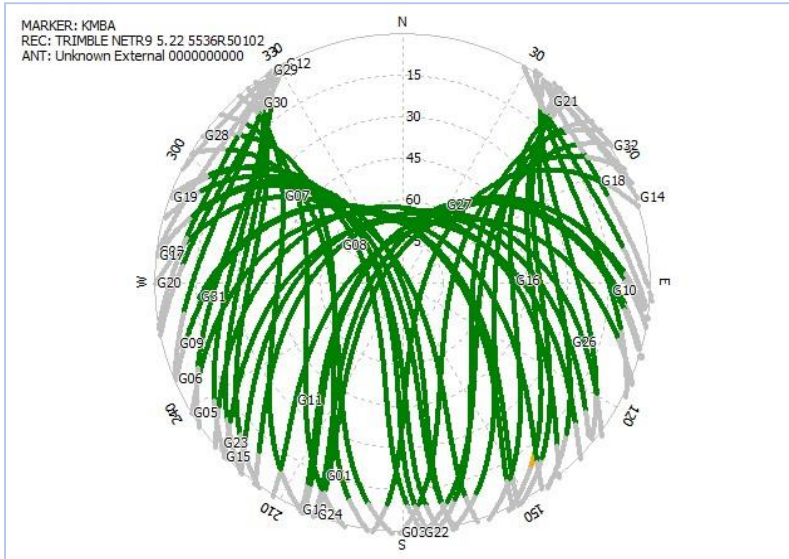






# GPS Skyplots: Tokyo, Jakarta and Maputo

## Tokyo-A Base-Station      Jakarta Base-Station      Maputo Base-Station



# Data Formats: NMEA, RINEX, RTCM

References: <https://www.nmea.org/>  
<http://freenmea.net/docs>

# National Marine Electronics Association (NMEA) Format

- NMEA is format to output measurement data from a sensor in a pre-defined format in ASCII
- In the case of GPS, It outputs GPS position, velocity, time and satellite related data
- NMEA sentences (output) begins with a “Talker ID” and “Message Description”
  - Example:
  - `$GPGGA,123519,4807.038,N,01131.000,E,1,08,0.9,545.4,M,46.9,M,,*47`
    - Position, Time and Fix Status Data
    - “\$GP” is Talker ID
    - “GGA” is Message Description to indicate for Position Data
  - `$GPRMC,123519,A,4807.038,N,01131.000,E,022.4,084.4,230394,003.1,W*6A`
    - Position, Velocity and Time Data



# NMEA Data Format

**GGA - Fix data which provide 3D location and accuracy data.**

**\$GPGGA,123519,4807.038,N,01131.000,E,1,08,0.9,545.4,M,46.9,M,,\*47**

Where: GGA Global Positioning System Fix Data

123519                      Fix taken at 12:35:19 UTC

4807.038, N              Latitude 48 deg 07.038' N

01131.000, E              Longitude 11 deg 31.000' E

1 Fix quality:

0 = invalid ,

1 = GPS fix (SPS),

2 = DGPS fix,

3 = PPS fix,

4 = Real Time Kinematic

5 = Float RTK

6 = estimated (dead reckoning) (2.3 feature)

7 = Manual input mode

8 = Simulation mode

08                      Number of satellites being tracked

0.9                      Horizontal dilution of position

545.4,M                  Altitude, Meters, above mean sea level

46.9,M                  Height of geoid (mean sea level) above WGS84 ellipsoid

(empty field)              time in seconds since last DGPS update (empty field) DGPS station ID number

\*47                      the checksum data, always begins with \*

# NMEA Data Format

**RMC - Fix data which provide 3D location and accuracy data.**

**\$GPRMC,123519,A,4807.038,N,01131.000,E,022.4,084.4,230394,003.1,W\*6A**

RMC	Position, Velocity and Time Data
123519	Fix taken at 12:35:19 UTC
A	Status A = Active or V = Void
4807.038, N	Latitude 48 deg 07.038' N
01131.000, E	Longitude 11 deg 31.000' E
022.4	Speed over the ground in knots
084.4	Track angle in degrees (True)
230394	Date (DDMMYY)
003.1	Magnetic variation in degrees
*6A	the checksum data, always begins with *

# RINEX Data Format

- RINEX: Receiver Independent Exchange Format is a data exchange format for raw satellite data among different types of receivers.
  - Different types of receivers may output position and raw data in proprietary formats
  - For post-processing of data using DGPS or RTK it is necessary to use data from different types of receivers. A common data format is necessary for this purpose.
  - Example: How to post process data from Trimble, Novatel and Septentrio receivers to compute a position?
- RINEX only provides Raw Data. It does not provide position output.
  - User has to post-process RINEX data to compute position
  - Raw data consists of Pseudorange, Carrierphase, Doppler, SNR
- RINEX basically consists of two data types
  - “\*.N” file for Satellite and Ephemeris Related data.
    - Also called Navigation Data
  - “\*.O” file for Signal Observation Data like Pseudorange, Carrier Phase, Doppler, SNR
    - Also called Observation Data
- The latest RINEX version is 3.04, 23 NOV 2018
  - Note: Not all the software and receivers are yet compatible with the latest version
  - Make sure which version of RINEX works the best with your software

# RINEX "N" File for GPS

```

2.11      NAVIGATION DATA      GPS (GPS)      RINEX VERSION / TYPE
cnvtToRINEX 2.90.0  convertToRINEX OPR  05-Jul-17 03:38 UTC PGM / RUN BY / DATE
-----
0.8382D-08 0.2235D-07 -0.5960D-07 -0.1192D-06      ION ALPHA
0.8602D+05 0.6554D+05 -0.1311D+06 -0.4588D+06      ION BETA
-0.931322574615D-09-0.355271367880D-14  405504      1947 DELTA-UTC: A0,A1,T,W
18      LEAP SECONDS
      END OF HEADER
32 17 05 01 00 00 0.0-0.400723423809D-03-0.110276232590D-10 0.000000000000D+00
0.370000000000D+02-0.806250000000D+01 0.455840416154D-08-0.192420920137D+01
-0.353902578354D-06 0.111064908560D-02 0.826455652714D-05 0.515371503258D+04
0.864000000000D+05-0.782310962677D-07 0.675647076441D-01-0.838190317154D-07
0.958529124300D+00 0.221156250000D+03-0.265074890978D+01-0.796390315710D-08
-0.389659088008D-09 0.100000000000D+01 0.194700000000D+04 0.000000000000D+00
0.240000000000D+01 0.000000000000D+00 0.465661287308D-09 0.370000000000D+02
0.795120000000D+05 0.400000000000D+01 0.000000000000D+00 0.000000000000D+00
24 17 05 01 00 00 0.0-0.341213308275D-04-0.454747350886D-12 0.000000000000D+00
0.100000000000D+02 0.787812500000D+02 0.459340561950D-08 0.167267059468D+01
0.404566526413D-05 0.564297637902D-02 0.102464109659D-04 0.515370226479D+04
0.864000000000D+05-0.782310962677D-07 0.108986675687D+01 0.484287738800D-07
0.945651423640D+00 0.170906250000D+03 0.490563049326D+00-0.815641117584D-08
-0.128933942045D-09 0.100000000000D+01 0.194700000000D+04 0.000000000000D+00
0.240000000000D+01 0.000000000000D+00 0.279396772385D-08 0.100000000000D+02
0.792180000000D+05 0.400000000000D+01 0.000000000000D+00 0.000000000000D+00

```

# RINEX “O” File GPS, GLONASS, GALILEO, QZSS, SBAS

2.11		OBSERVATION DATA		Mixed(MIXED)		RINEX VERSION / TYPE	
cnvtToRINEX 2.90.0		convertToRINEX OPR		05-Jul-17 03:38 UTC		PGM / RUN BY / DATE	
-----						COMMENT	
KMBA						MARKER NAME	
KMBA						MARKER NUMBER	
DM						OBSERVER / AGENCY	
5536R50102						REC # / TYPE / VERS	
UT						ANT # / TYPE	
TRIMBLE NETR9						APPROX POSITION XYZ	
5.20						ANTENNA: DELTA H/E/N	
UNKNOWN EXT						WAVELENGTH FACT L1/2	
-3955510.8982 3357111.6791 3697796.5495						# / TYPES OF OBSERV	
0.0000 0.0000 0.0000						INTERVAL	
1 1 0						TIME OF FIRST OBS	
8 C1 C2 C3 L1 L2 L3 P1 P2						TIME OF LAST OBS	
1.000						RCV CLOCK OFFS APPL	
2017 5 1 0 0 0.0000000 GPS						LEAP SECONDS	
2017 5 1 23 59 59.0000000 GPS						# OF SATELLITES	
0						PRN / # OF OBS	
18						PRN / # OF OBS	
59						PRN / # OF OBS	
G01 23351 23350 0 23350 46694 0 0 23344						PRN / # OF OBS	
G02 22293 0 0 22293 22286 0 0 22286						PRN / # OF OBS	
G03 19633 19632 0 19632 39259 0 0 19627						PRN / # OF OBS	
G05 25303 25302 0 25299 50599 0 0 25297						PRN / # OF OBS	
G06 24709 24708 0 24709 49411 0 0 24703						PRN / # OF OBS	
G07 27766 27764 0 27764 55505 0 0 27741						PRN / # OF OBS	



# RINEX "O" File, Continued from previous slide

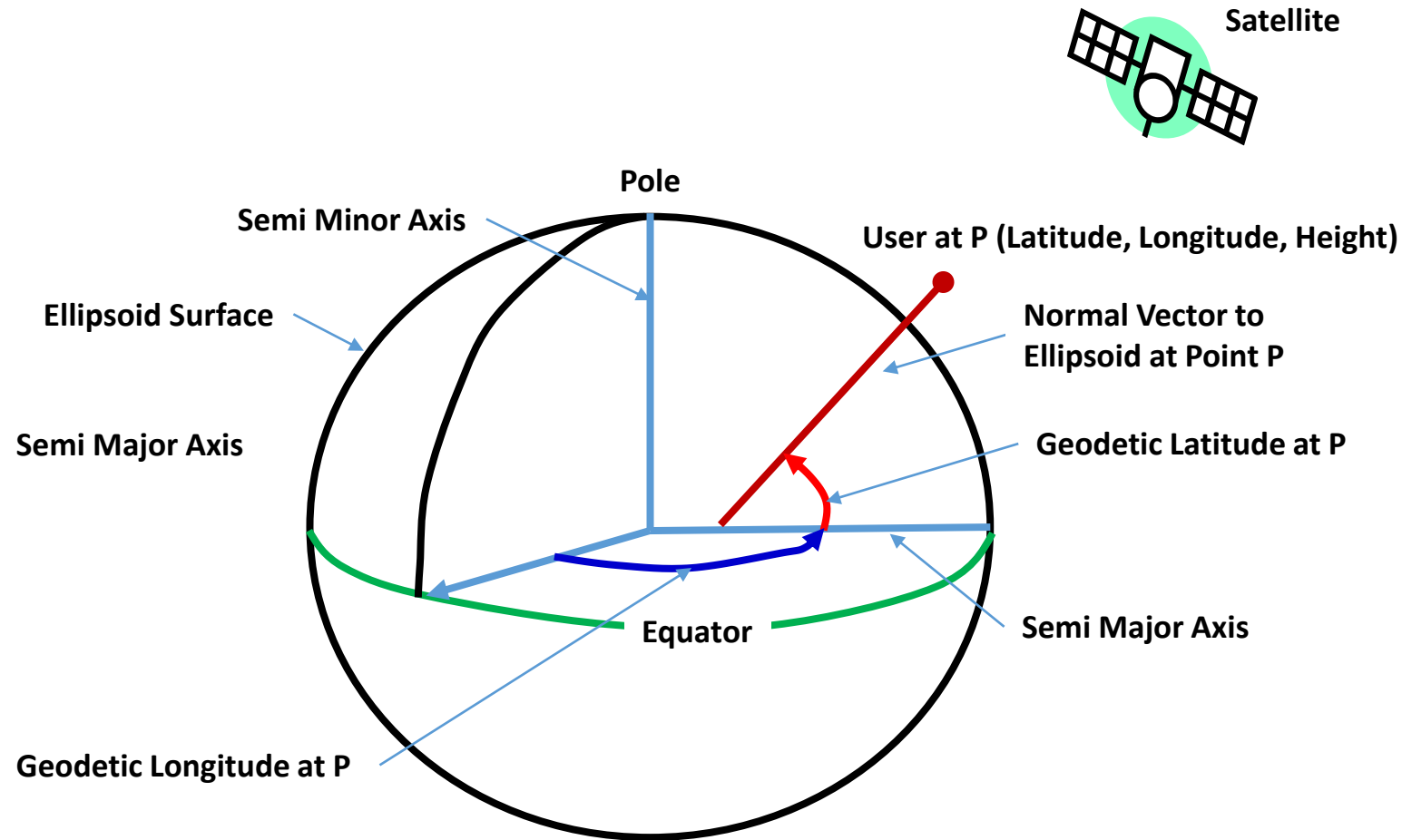
S37	86400	0	0	86400	0	0	0	0	PRN / # OF OBS
S40	56700	0	0	56700	0	0	0	0	PRN / # OF OBS
CARRIER PHASE MEASUREMENTS: PHASE SHIFTS REMOVED									COMMENT
									END OF HEADER
17	5	1	0	0	0.0000000	0	19G10G12G14G15G18G24G25G31G32R01R02R03		
R11R12R13S28S29S37S40									
21375379.406	7	21375388.078	9				112328384.475	7	87528640.180 9
						21375388.41448			
20991588.469	7	20991594.418	9				110311559.942	7	85957091.970 9
						20991594.71548			
23097788.500	6						121379711.146	6	94581624.25147
						23097793.85247			
24539464.648	6	24539473.480	8				128955722.954	6	100484989.893 8
						24539473.66046			
21890081.000	6						115033147.870	6	89636240.02147
						21890086.53547			
22760846.398	6	22760855.313	9				119609048.681	6	93201876.319 9
						22760854.86347			
20303284.266	7	20303294.227	9				106694510.219	7	83138615.317 9
						20303294.01248			
23440741.258	6	23440748.211	8				123181935.734	6	95985961.100 8
						23440748.62147			
21395760.742	7	21395769.145	9				112435502.496	7	87612113.685 9
						21395769.30548			

# RTCM

- RTCM : Radio Technical Commission for Maritime Services
  - An internationally accepted data transmission standard for base-station data transmission to a rover defined. The standards are defined and maintained by RTCM SC-104
- RTCM SC-104 (Special Committee 104)
  - Defines data formats for Differential GPS and
  - RTK (Real-Time Kinematic Operations)
- The Current Version is RTCM-3 (10403.3)
- Refer <https://www.rtcn.org/> for detail information and document
  - Documents are not free
  - A normal user does not need RTCM document.
  - GNSS receivers with base-station capabilities will setup necessary messages for RTK
  - If you are developing a system or application you may need it

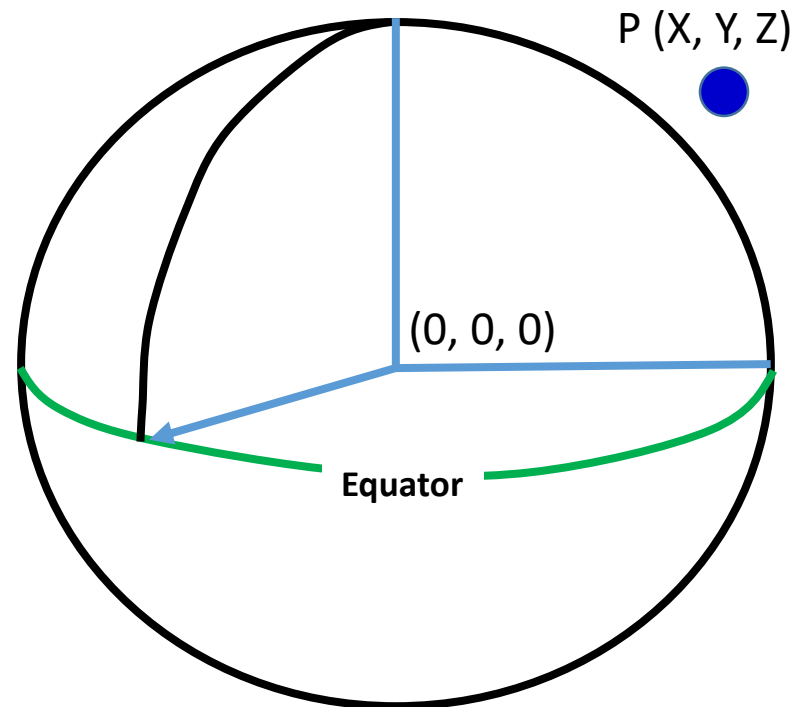
# Coordinate Systems

# Geodetic Coordinate System



# ECEF (Earth Centered, Earth Fixed)

ECEF Coordinate System is expressed by assuming the center of the earth coordinate as  $(0, 0, 0)$



# Coordinate Conversion from ECEF to Geodetic and vice versa

Geodetic Latitude, Longitude & Height to  
ECEF (X, Y, Z)

$$X = (N + h) \cos \varphi \cos \lambda$$

$$Y = (N + h) \cos \varphi \sin \lambda$$

$$Z = [N(1 - e^2) + h] \sin \varphi$$

$\varphi = \text{Latitude}$

$\lambda = \text{Longitude}$

$h = \text{Height above Ellipsoid}$

ECEF (X, Y, Z) to  
Geodetic Latitude, Longitude & Height

$$\varphi = \text{atan}\left(\frac{Z + e^2 b \sin^3 \theta}{p - e^2 a \cos^3 \theta}\right)$$

$$\lambda = \text{atan2}(y, x)$$

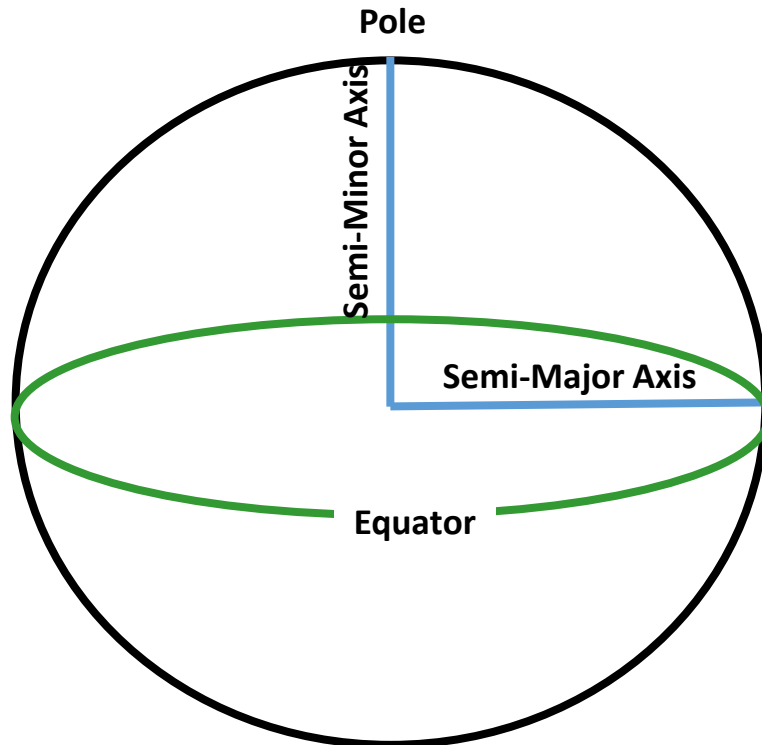
$$h = \frac{P}{\cos \varphi} - N(\varphi)$$

$$P = \sqrt{x^2 + y^2}$$

$$\theta = \text{atan}\left(\frac{Za}{Pb}\right)$$

$$N(\varphi) = \frac{a}{\sqrt{1 - e^2 \sin^2 \varphi}}$$

# Geodetic Datum: Geometric Earth Model



## GPS uses WGS-84 Datum

But, topographic maps and many other maps use different datum. Before using GPS data on these maps, it's necessary to convert GPS coordinates from WGS-84 to local coordinate system and datum. Many GPS software have this tool. Also, GPS receivers have built-in datum selection capabilities.

Check your receiver settings before using.

## WGS-84 Geodetic Datum Ellipsoidal Parameters

**Semi-Minor Axis,  $b = 6356752.3142\text{m}$**

**Semi-Major Axis,  $a = 6378137.0\text{m}$**

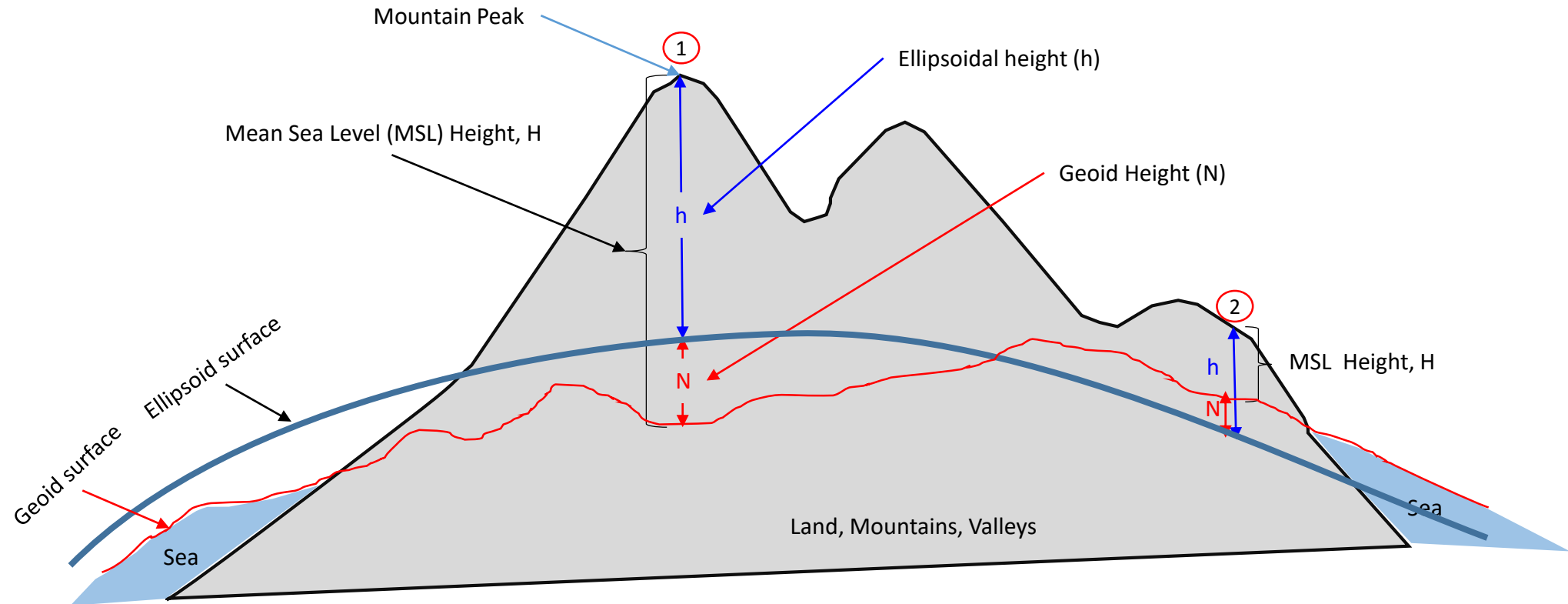
**Flattening,  $f = (a-b)/a$**

**$= 1/298.257223563$**

**First Eccentricity Square =  $e^2 = 2f-f^2$**

**$= 0.00669437999013$**

# Ellipsoid, Geoid and Mean Sea Level (MSL)



MSL Height (H) = Ellipsoidal height (h) – Geoid height (N)  
Geoid Height is negative if its below Ellipsoidal height

Example at point (1) :  $h = 1200\text{m}$ ,  $N = -30\text{m}$   
 $H = h - N = 1200 - (-30) = 1200 + 30 = 1230\text{m}$

Example at point (2) :  $h = 300\text{m}$ ,  $N = +15\text{m}$   
 $H = h - N = 300 - 15 = 285\text{m}$



# Height Data Output in u-blox Receiver, NMEA Sentence, \$GNGGA Sentence

\$GNVTG,,T,,M,0.010,N,0.018,K,D\*30

\$GNGGA,012039.00,3554.18235,N,13956.35867,E,2,12,0.48,54.4,M,39.6,M,0.0,0000\*5D

\$GNGSA,A,3,03,04,06,09,17,19,22,28,194,195,02,,0.92,0.48,0.78,1\*06

\$GNGSA,A,3,11,12,04,24,19,31,33,,,,,0.92,0.48,0.78,3\*00

\$GNGSA,A,3,30,01,03,14,08,28,33,04,02,07,10,13,0.92,0.48,0.78,4\*08

\$GPGSV,5,1,17,01,18,076,,02,04,279,36,03,43,045,43,04,34,109,41,1\*6C

\$GPGSV,5,2,17,06,38,295,43,09,26,152,40,11,02,107,29,17,74,330,47,1\*67

\$GPGSV,5,3,17,19,53,320,45,22,22,048,39,28,36,213,43,41,18,249,39,1\*6D

\$GPGSV,5,4,17,50,46,201,40,193,52,172,43,194,16,193,40,195,85,163,46,1\*5E

\$GPGSV,5,5,17,199,46,201,37,1\*66

\$GAGSV,2,1,07,04,25,175,40,11,28,299,37,12,65,007,43,19,50,105,40,7\*72

\$GAGSV,2,2,07,24,27,245,41,31,09,198,36,33,33,082,42,7\*43

\$GBGSV,4,1,15,01,48,172,43,02,19,248,36,03,39,225,43,04,44,148,42,1\*7C

\$GBGSV,4,2,15,06,00,185,29,07,39,214,41,08,53,305,43,10,44,248,42,1\*7C

\$GBGSV,4,3,15,13,33,283,42,14,23,043,38,27,55,323,48,28,61,092,48,1\*71

\$GBGSV,4,4,15,30,05,306,36,32,17,206,42,33,48,055,46,1\*4F

\$GNGLL,3554.18235,N,13956.35867,E,012039.00,A,D\*76

MSL (Altitude)

Geoid Separation  
Geoid Height

Parameter	Value	Unit	Description
UTC	012040.00	hhmmss.sss	Universal time coordinated
Lat	3554.18235	ddmm.mmmm	Latitude
Northing Indicator	N		N=North, S=South
Lon	13956.35868	ddmm.mmmm	Longitude
Easting Indicator	E		E=East, W=West
Status	2		0=Invalid, 1=2D/3D, 2=DGNSS, 4=Fixed RTK, 5=Float RTK, 6=Dead Reckoning
SVs Used	12		Number of SVs used for Navigation
HDOP	0.48		Horizontal Dilution of Precision
Alt (MSL)	54.4	m	Altitude (above means sea level)
Unit	M		M=Meters
Geoid Sep.	39.6	m	Geoid Separation = Alt(HAE) - Alt(MSL)
Unit	M		M=Meters
Age of DGNSS Corr	0.0	s	Age of Differential Corrections
DGNSS Ref Station	0000		ID of DGNSS Reference Station

The NMEA sentences in this figure are from u-blox receiver.

NMEA format uses "Mean Sea Level" for height data (shown in blue texts).

Also it provides Geoid Height (Geoid Separation) value.

GPS by default is Ellipsoidal height and this height is converted to Mean Sea Level height using the geoid Height (shown in red texts).

This means, u-blox receiver uses a built-in database of Geoid Height.

U-blox also outputs Ellipsoidal height in proprietary message \$PUBX,00 (marked as altRef)  
\$PUBX,00,time,lat,NS,long,EW,altRef,navStat,hAcc,vAcc,SOG,COG,vVel,diffAge,HDOP,VDO  
P,TDOP,numSvs,reserved,DR,\*cs<CR><LF>

altRef → Altitude above user datum ellipsoid

## Height Data Output in u-blox Receiver, NMEA Sentence, \$GNGGA Sentence

\$GNVTG,,T,,M,0.010,N,0.018,K,D\*30

\$GNGGA,012039.00,3554.18235,N,13956.35867,E,2,12,0.48,54.4,M,39.6,M,0.0,0000\*5D

\$GNGSA,A,3,03,04,06,09,17,19,22,28,194,195,02,,0.92,0.48,0.78,1\*06

\$GNGSA,A,3,11,12,04,24,19,31,33,,,,,0.92,0.48,0.78,3\*00

\$GNGSA,A,3,30,01,03,14,08,28,33,04,02,07,10,13,0.92,0.48,0.78,4\*08

\$GPGSV,5,1,17,01,18,076,,02,04,279,36,03,43,045,43,04,34,109,41,1\*6C

\$GPGSV,5,2,17,06,38,295,43,09,26,152,40,11,02,107,29,17,74,330,47,1\*67

\$GPGSV,5,3,17,19,53,320,45,22,22,048,39,28,36,213,43,41,18,249,39,1\*6D

\$GPGSV,5,4,17,50,46,201,40,193,52,172,43,194,16,193,40,195,85,163,46,1\*5E

\$GPGSV,5,5,17,199,46,201,37,1\*66

\$GAGSV,2,1,07,04,25,175,40,11,28,299,37,12,65,007,43,19,50,105,40,7\*72

\$GAGSV,2,2,07,24,27,245,41,31,09,198,36,33,33,082,42,7\*43

\$GBGSV,4,1,15,01,48,172,43,02,19,248,36,03,39,225,43,04,44,148,42,1\*7C

\$GBGSV,4,2,15,06,00,185,29,07,39,214,41,08,53,305,43,10,44,248,42,1\*7C

\$GBGSV,4,3,15,13,33,283,42,14,23,043,38,27,55,323,48,28,61,092,48,1\*71

\$GBGSV,4,4,15,30,05,306,36,32,17,206,42,33,48,055,46,1\*4F

\$GNGLL,3554.18235,N,13956.35867,E,012039.00,A,D\*76

MSL (Altitude)  
Geoid Separation  
Geoid Height

Parameter	Value	Unit	Description
UTC	012040.00	hhmmss.sss	Universal time coordinated
Lat	3554.18235	ddmm.mmmm	Latitude
Northing Indicator	N		N=North, S=South
Lon	13956.35868	ddmm.mmmm	Longitude
Easting Indicator	E		E=East, W=West
Status	2		0=Invalid, 1=2D/3D, 2=DGNSS, 4=Fixed RTK, 5=Float RTK, 6=Dead Reckoning
SVs Used	12		Number of SVs used for Navigation
HDOP	0.48		Horizontal Dilution of Precision
Alt (MSL)	54.4	m	Altitude (above means sea level)
Unit	M		M=Meters
Geoid Sep.	39.6	m	Geoid Separation = Alt(HAE) - Alt(MSL)
Unit	M		M=Meters
Age of DGNSS Corr	0.0	s	Age of Differential Corrections
DGNSS Ref Station	0000		ID of DGNSS Reference Station

The NMEA sentences in this figure are from u-blox receiver.

NMEA format uses "Mean Sea Level" for height data (shown in blue texts).

Also it provides Geoid Height (Geoid Separation) value.

GPS by default is Ellipsoidal height and this height is converted to Mean Sea Level height using the geoid Height (shown in red texts).

This means, u-blox receiver uses a built-in database of Geoid Height.

U-blox also outputs Ellipsoidal height in proprietary message \$PUBX,00 (marked as altRef)  
\$PUBX,00,time,lat,NS,long,EW,altRef,navStat,hAcc,vAcc,SOG,COG,vVel,diffAge,HDOP,VDO  
P,TDOP,numSvs,reserved,DR,\*cs<CR><LF>

altRef → Altitude above user datum ellipsoid

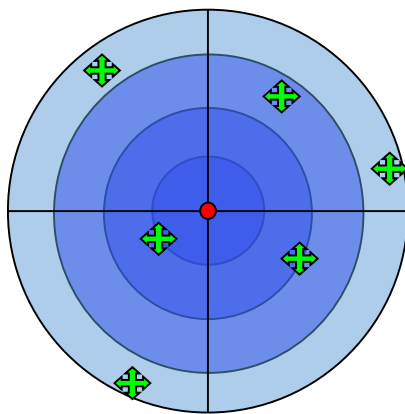
# Points to Be Careful in GPS Survey

- Datum
  - Which Datum is used for GPS Survey?
  - By default, GPS uses WGS-84
  - But, your Map may be using different datum like Everest
    - Make Sure that Your Map and Your Coordinates from the GPS are in the same Datum, if not, datum conversion is necessary
    - You can get necessary transformation parameters from your country's survey department
- Height
  - Which Height is used?
  - By default GPS uses Ellipsoidal Height
  - But, your Map may be using Mean Sea Level (MSL or Topographic) Height
    - You need to convert from Ellipsoidal Height into MSL Height
    - Use Ellipsoidal and Geoid height Difference Data for your survey region
      - You can get it from your country's survey office

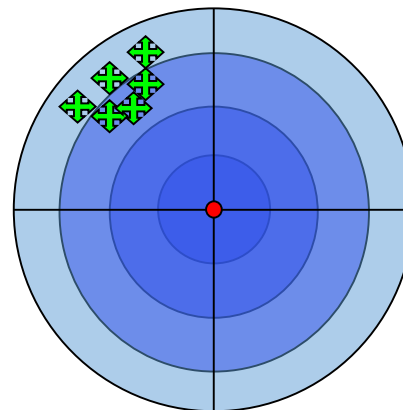
# GNSS Errors

# Background Information: Accuracy vs. Precision

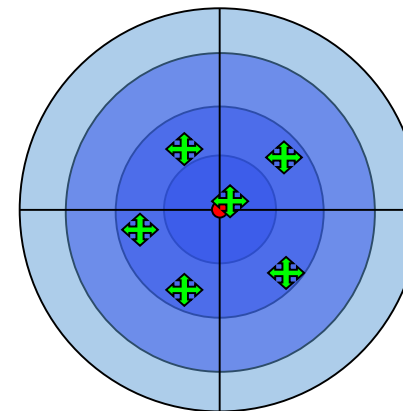
- Accuracy
  - Capable of providing a correct measurement
  - Measurement is compared with true value
  - Affected by systematic error
- Precision
  - Capable of providing repeatable and reliable measurement
  - Statistical analysis of measurement provides the precision
  - Measure of random error
  - Systematic error has no effect



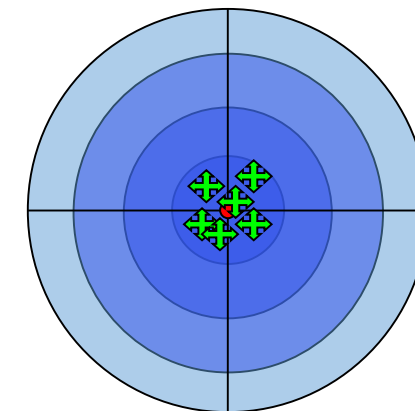
Neither Precise nor Accurate



Precise but Not Accurate



Accurate but Not Precise



Precise and Accurate

# GNSS Measurement Errors

Measure	Abbreviation	Definition
Root Mean Square	RMS	The square root of the average of the squared errors
Twice Distance RMS	2D RMS	Twice the RMS of the horizontal errors
Circular Error Probable	CEP	A circle's radius, centered at the true antenna position, containing 50% of the points in the horizontal scatter plot
Horizontal 95% Accuracy	R95	A circle's radius, centered at the true antenna position, containing 95% of the points in the horizontal scatter plot
Spherical Error Probable	SEP	A sphere's radius centered at the true antenna position, containing 50% of the points in the three dimensional scatter plot

Source: [GPS Accuracy: Lies, Damn Lies, and Statistics, GPS World, JAN 1998](https://www.gpsworld.com/gps-accuracy-lies-damn-lies-and-statistics/)  
<https://www.gpsworld.com/gps-accuracy-lies-damn-lies-and-statistics/>

# Commonly Used GNSS Performance Measurements

- TTFF
  - True Time to First Fix
  - Parameter: Cold Start, Warm Start, Hot Start
- Standard Accuracy
  - Accuracy attainable without any correction techniques
  - Few meters of accuracy, normally within 10m in open sky
- DGPS Accuracy
  - Accuracy attainable by differential correction data
  - Code-phase correction
  - 1 – 3m accuracy
- RTK / PPK Accuracy
  - Accuracy attainable by differential correction data
  - Use both Code-Phase and Carrier Phase correction
  - Centimeter level accuracy
  - RTK: Real Time Kinematic
  - PPK: Post Processing Kinematic
- PPP Accuracy
  - Precise Point Positioning
  - Centimeter to decimeter level accuracy
  - Various modes of PPP available
  - QZSS MADOCA PPP
    - 10 – 20 CM accuracy
  - QZSS CLAS
    - Few centimeter accuracy

# TTFF and Typical Example Values

- TTFF
  - Cold Start : < 36 seconds
    - Time required to output first position data since the receiver power is on
    - No reference data like time or almanac are available
  - Warm Start : < 6 seconds
    - Time required to output first position data since the receiver power is on with the latest satellite almanac data in the receiver's memory
    - Time and almanac related reference data are already known
  - Hot Start : < 1 second
    - Receiver has already output position data
    - Time to reacquire an already tracked satellite due to temporary blockage by buildings or trees



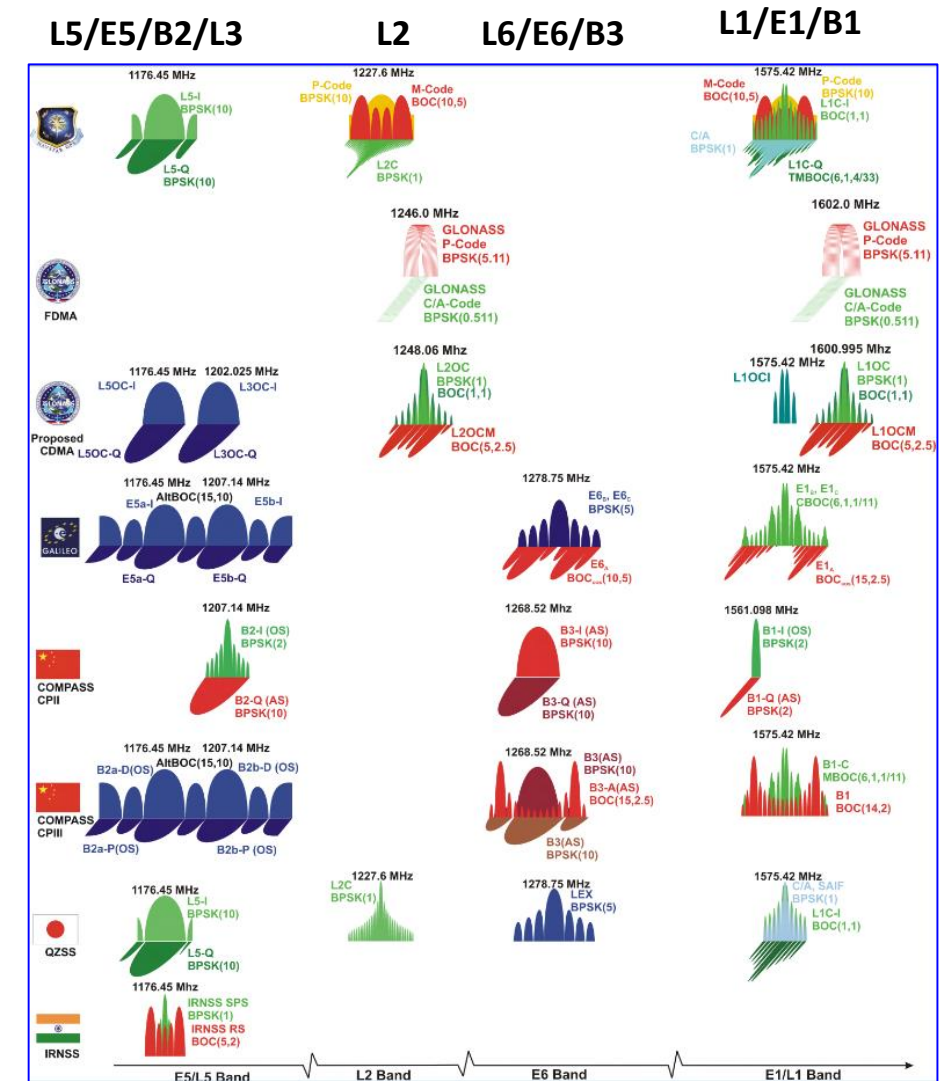
# Performance Measurement of RTK Accuracy

- A fix error and a variable error with respect to base-length is given
  - Such as :  $x \text{ cm} + y \text{ ppm}$
  - Example:  $2\text{cm} + 1\text{ppm}$ 
    - There is a fix error of 2cm plus 1ppm error due to base-length between the Base and Rover
    - 1ppm  $\rightarrow$  1 parts per million
    - $\rightarrow$  1cm of error in 1 million centimeter distance between the Base and the Rover
    - $\rightarrow$  1cm of error in 1000000 centimeter distance between the Base and the Rover
    - $\rightarrow$  1cm of error in 10000 meter distance between the Base and the Rover
    - $\rightarrow$  1cm of error in 10 kilometer distance between the Base and the Rover
    - $\rightarrow$  **1cm of error for every 10Km of distance between the Base and the Rover**
    - $\rightarrow$  4cm of error for 40Km of distance between the Base and the Rover
    - **Thus the total error is : 2cm + 4cm due to 40Km of base length**
  - The longer the base-length, the larger the error
    - Do not assume that this error is linear
    - And it may not be valid for longer base-lines
    - Normally the recommended base-length for RTK for a Geodetic Receiver is 40Km

# Low-Cost Receiver Systems

# High-End Survey Grade Receivers

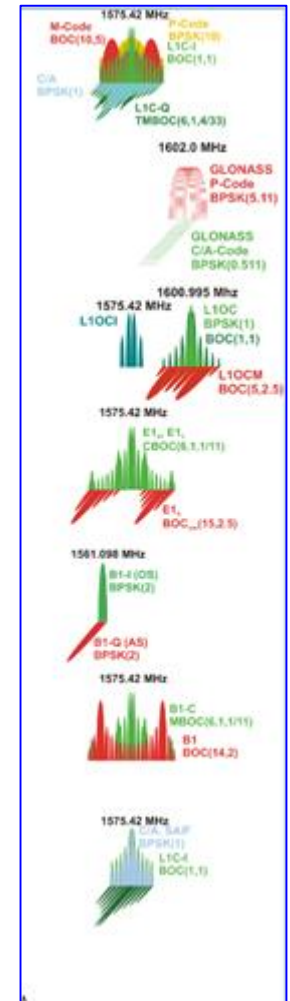
- Multi-frequency
  - GPS : L1/L2/L5
  - GLONASS : L1/L2/L3
  - GALILEO : E1/E5/E6
  - BDS : B1/B2/B3
  - QZSS : L1/L2/L5/L6
  - NAVIC : L5/S
- Multi-system
  - GPS, GLONASS, GALILEO, BeiDou, QZSS, NAVIC, SBAS etc
- Price varies from \$3, 000 to \$30,000 or more



# Low-Cost Receivers

- Multi-System
  - GPS, GLONASS, GALILEO, BeiDou, QZSS, SBAS etc
- Basically Single Frequency
  - L1/E1/B1-Band
  - Very soon: Multi-System, Multi Frequency, L1/L2 or L1/L5
    - Future trend for Mass Market System will be L1/L5
  - Some chip makers have already announced Multi-System, Multi-Frequency GNSS Chips for Mass Market
- Low Cost:
  - Less than \$300 (Multi-GNSS, L1 Only) including Antenna and all necessary Hardware, Software
    - Our target is within \$100 or less including everything

L1/E1/B1\*



\*Note: Only one signal type from each system is processed  
e.g. GPS has L1C/A and L1C in L1, ,but only L1C/A is used in Low-Cost Receiver

## Our Definition of Low-Cost Receiver

- Price : \$100 or less
- Accuracy : Better than 100cm
- Weight : 100g or less  
(Without Battery)

100<sup>3</sup>

\$100 x 100cm x 100g

Will it be possible?

# Question?

Although the Normal Accuracy of GPS is about 10m,  
why can we get Centimeter Level Accuracy?

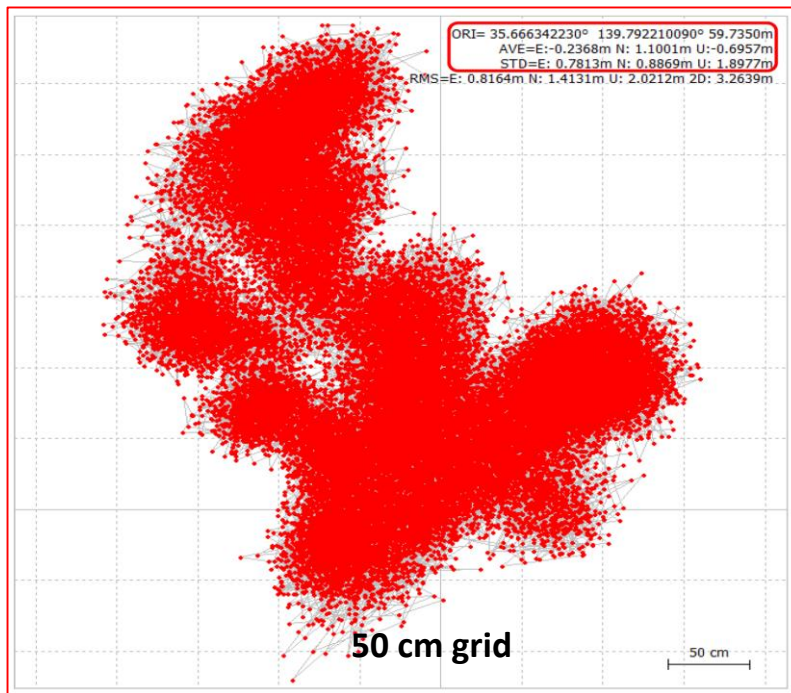
# GPS Position Accuracy

How to achieve accuracy from few meters to few centimeters?

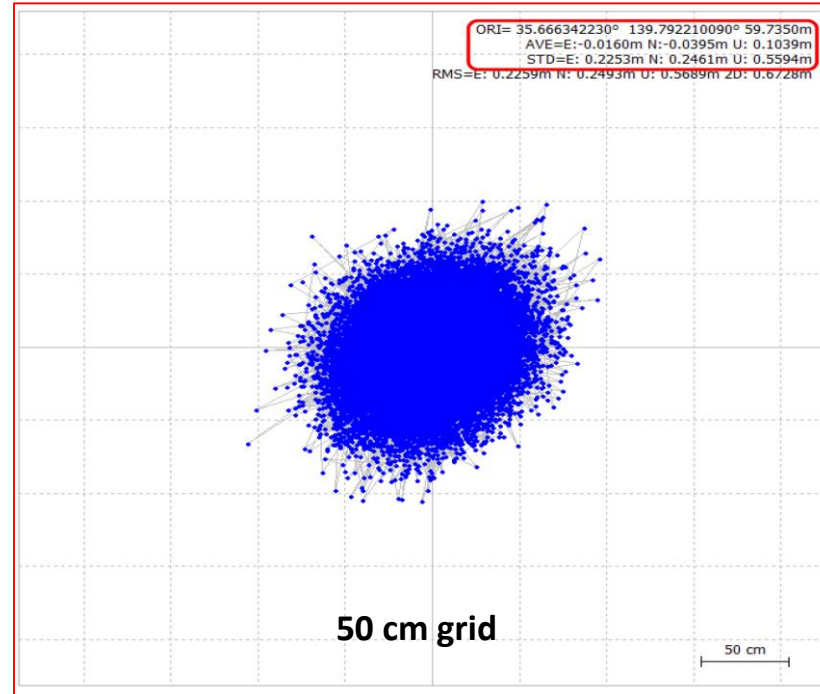
meter



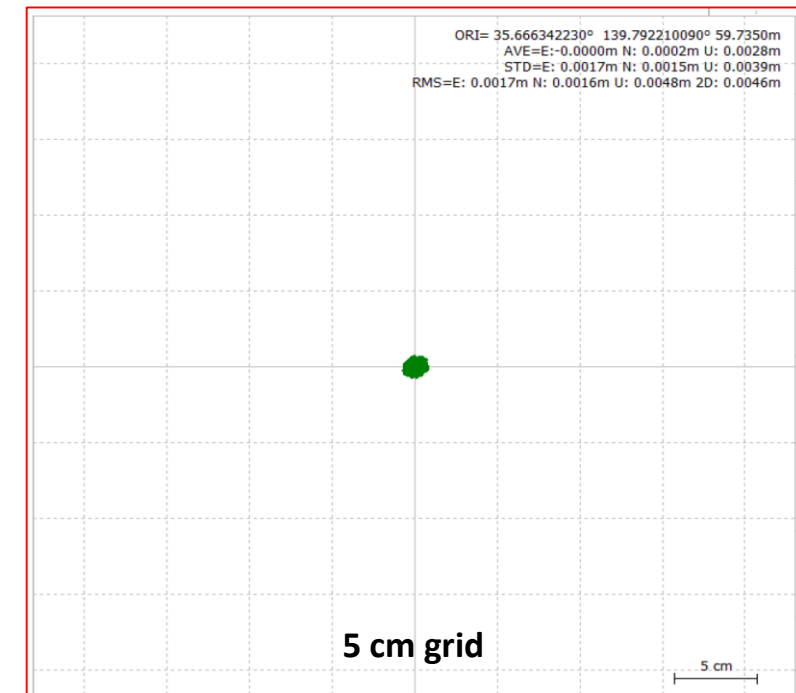
centimeter



SPP (Single Point Position)



DGPS (Differential GPS)  
Code-phase observation



RTK (Real Time Kinematic)  
Carrier-phase observation

# Errors in GPS Observation (L1C/A Signal)

Error Sources	One-Sigma Error , m		Comments
	Total	DGPS	
Satellite Orbit	2.0	0.0	Common errors are removed
Satellite Clock	2.0	0.0	
Ionosphere Error	4.0	0.4	Common errors are reduced
Troposphere Error	0.7	0.2	
Multipath	1.4	1.4	
Receiver Circuits	0.5	0.5	

**If we can remove common errors, position accuracy can be increased.**

**Common errors are: Satellite Orbit Errors, Satellite Clock Errors and Atmospheric Errors (within few km)**

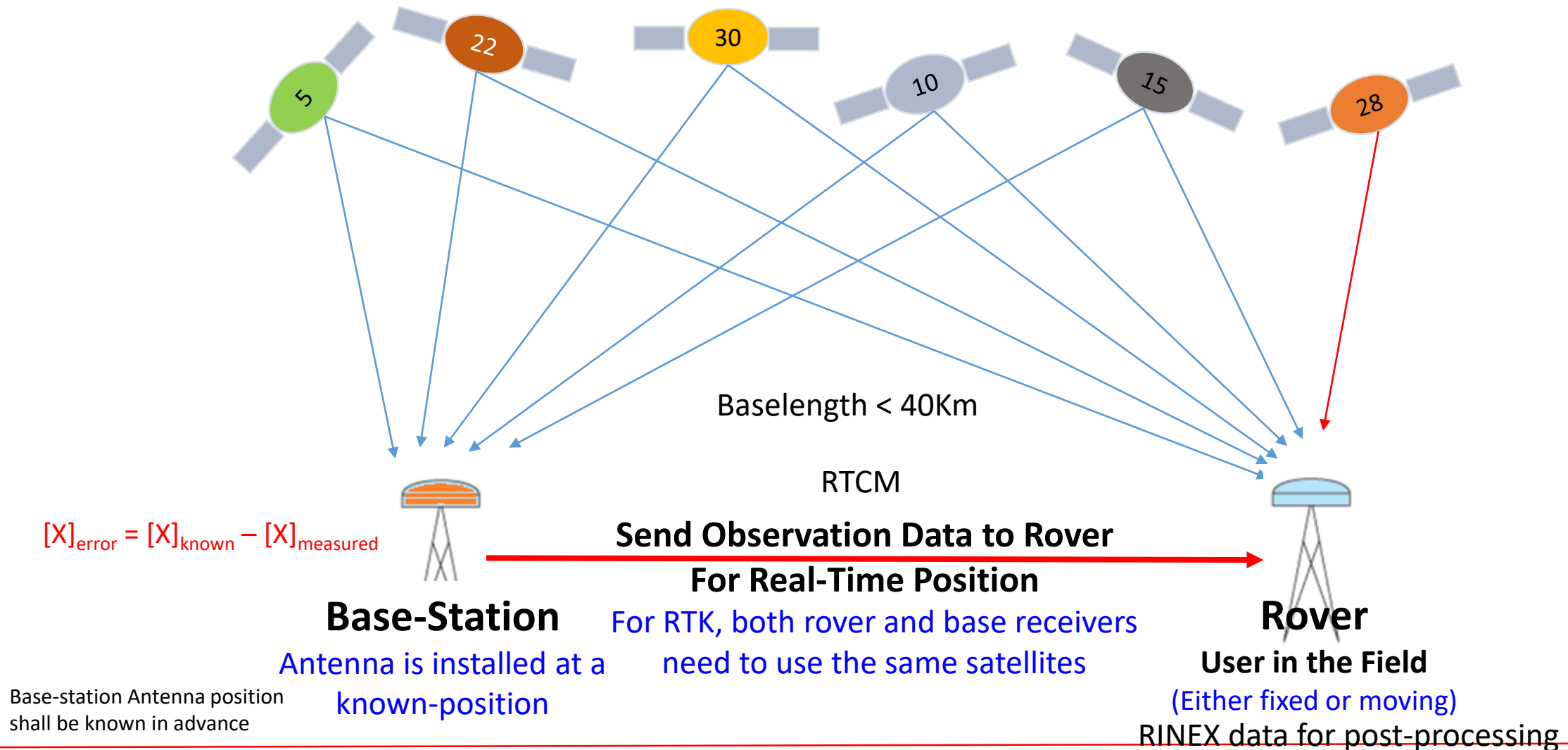
Values in the Table are just for illustrative purpose, not the exact measured values.

Table Source : [http://www.edu-observatory.org/gps/gps\\_accuracy.html#Multipath](http://www.edu-observatory.org/gps/gps_accuracy.html#Multipath)



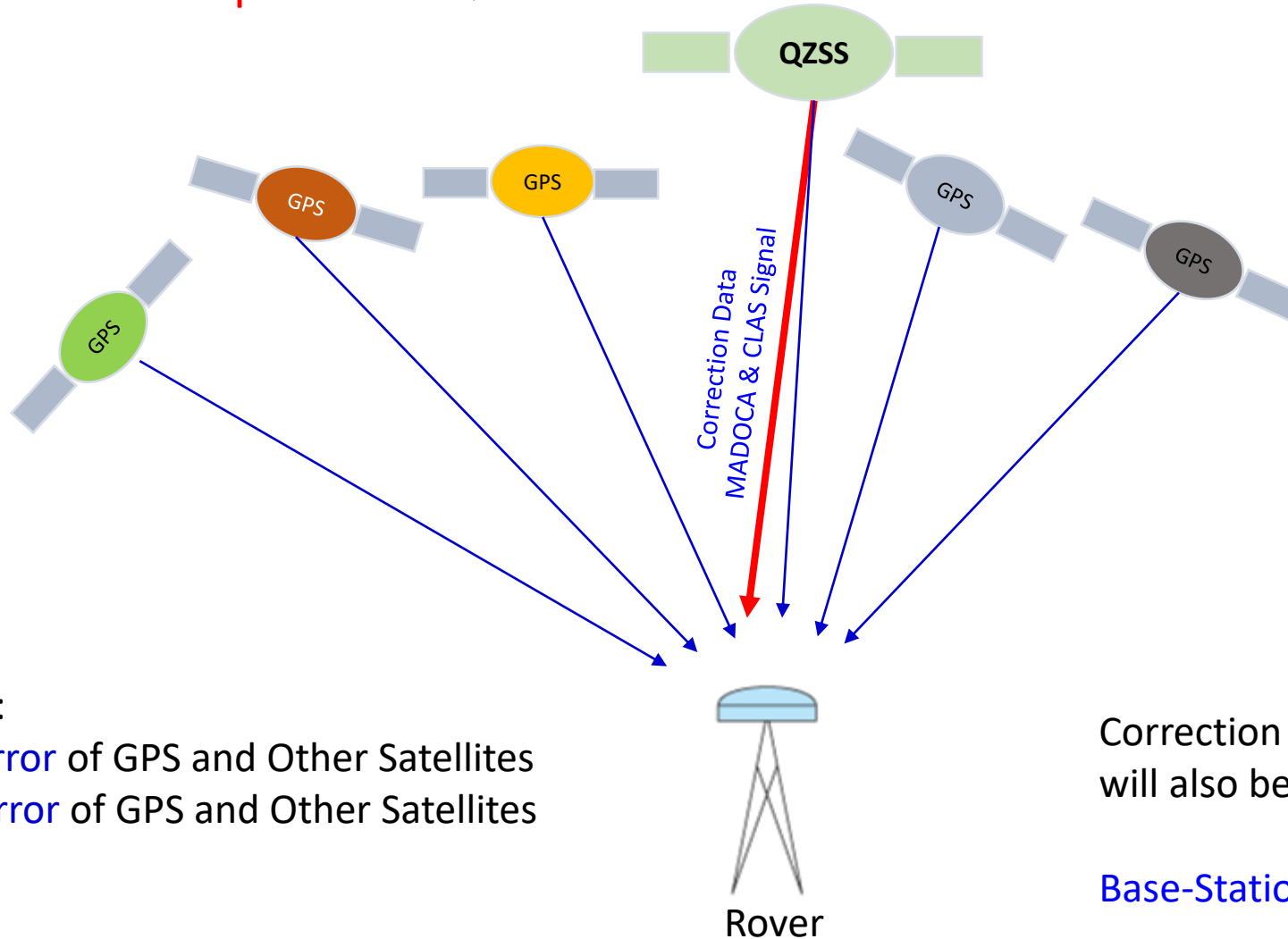
# How to Remove or Minimize Common Errors?

## Use Differential Correction



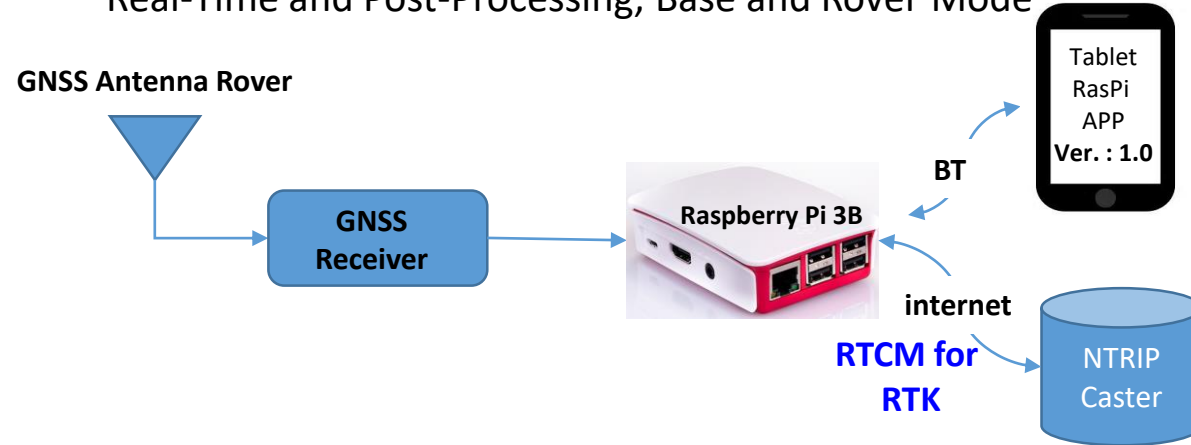
# How to Remove or Minimize Common Errors?

## Principle of QZSS MADOCA and CLAS Services

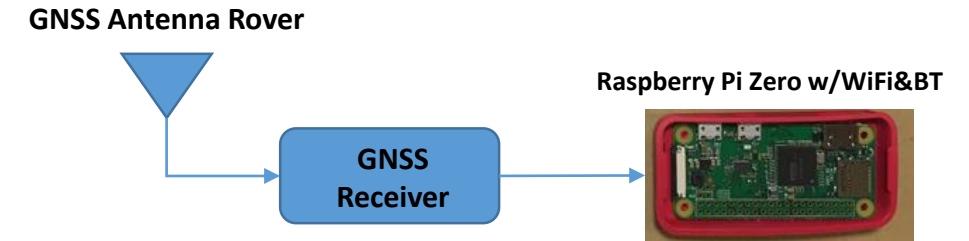


# Low-Cost RTK Receiver System

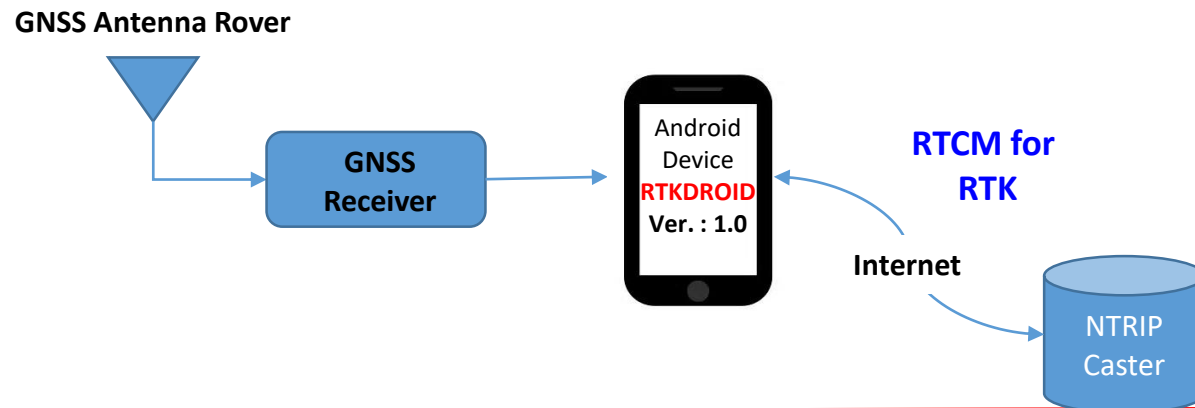
**TYPE R1** Type A: Low-Cost, High-Accuracy Receiver System  
Real-Time and Post-Processing, Base and Rover Mode



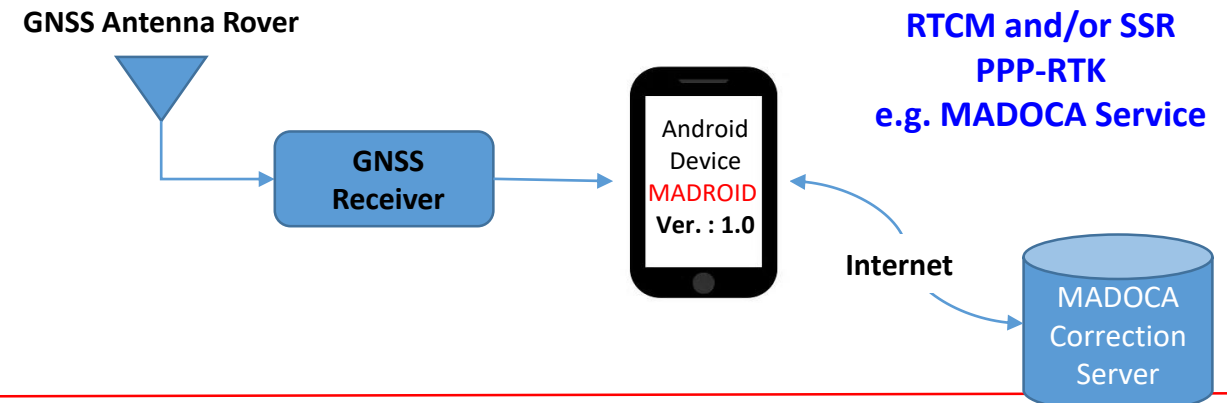
**TYPE R2** Type B: Low-Cost, High-Accuracy Receiver System  
For Post-Processing & Rover Mode Only



**TYPE A1** Type C: Low-Cost, High-Accuracy Receiver System  
Real-Time and Post-Processing, Rover Mode Only



**TYPE MA** Type D: Low-Cost, High-Accuracy Receiver System  
Real-Time and Post-Processing, Rover Mode Only

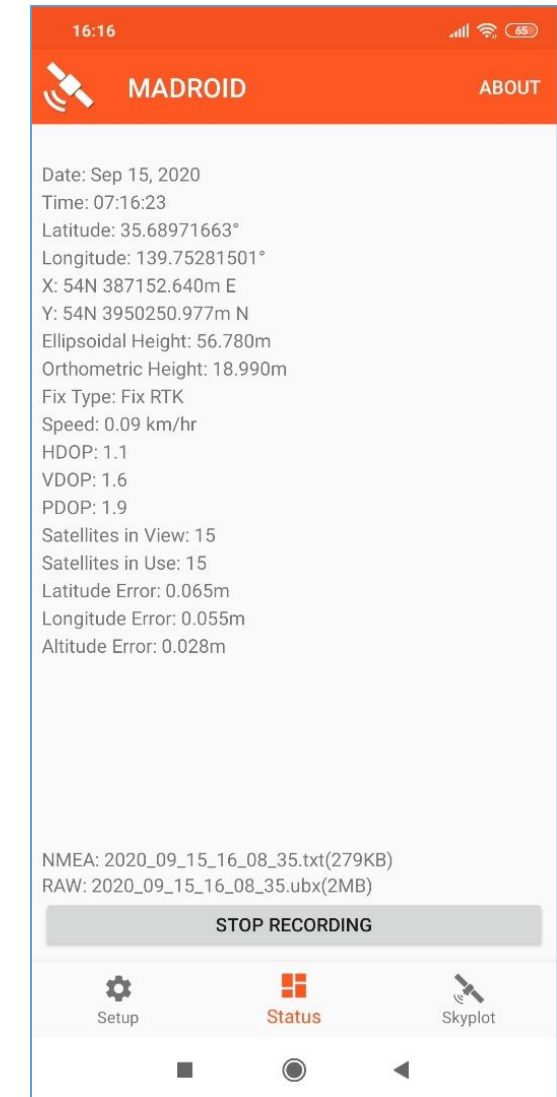
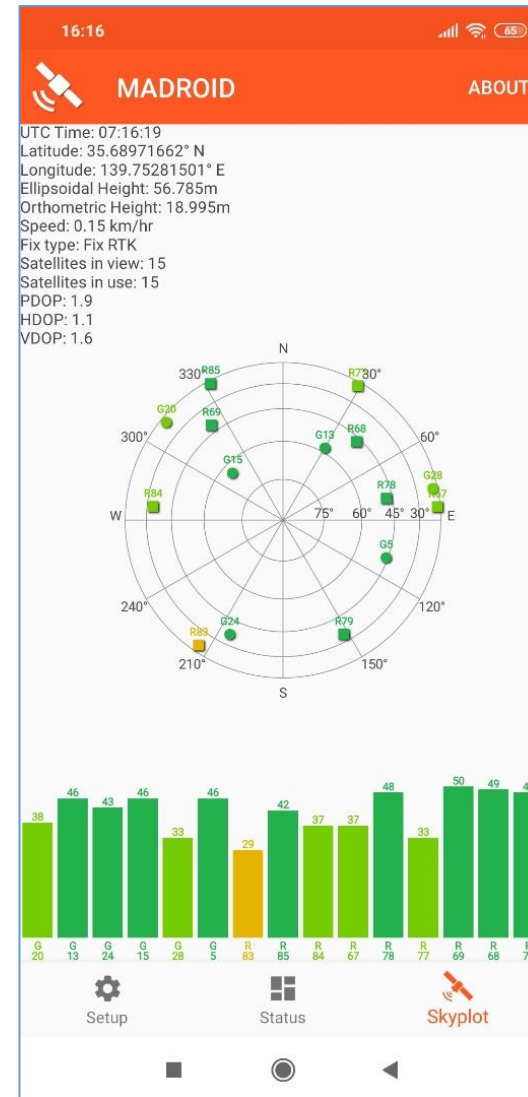
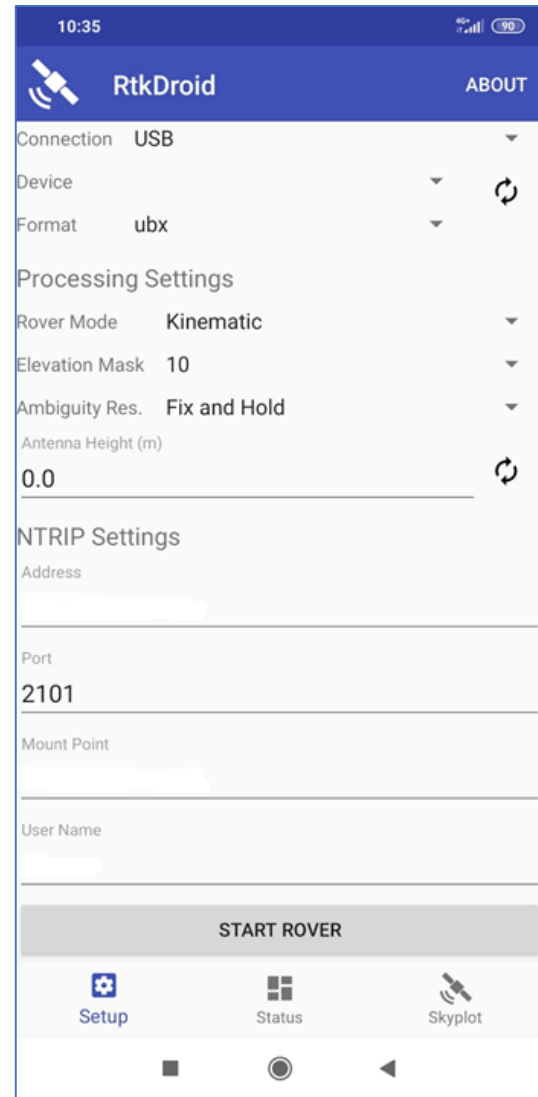


# Screen Shots of RTKDROID and MADROID

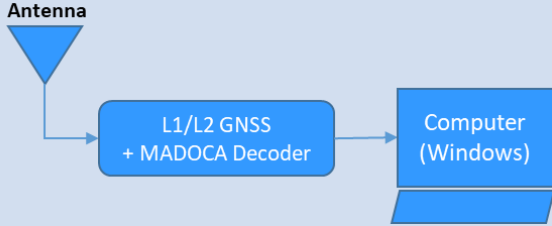
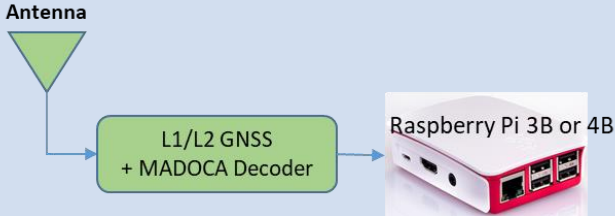
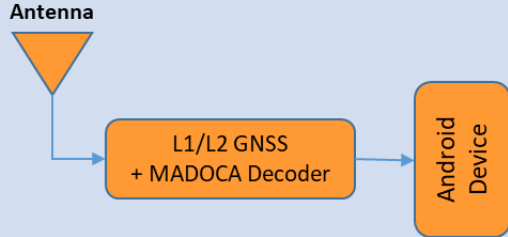
Connect GNSS receiver to  
Android device

(1) RTKDROID :  
For RTK or PPK

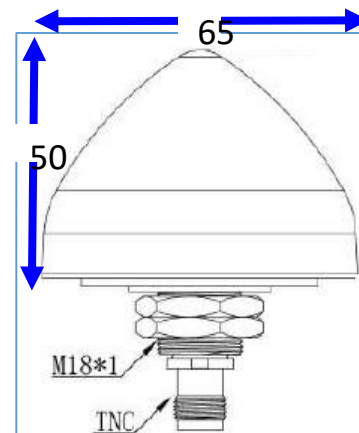
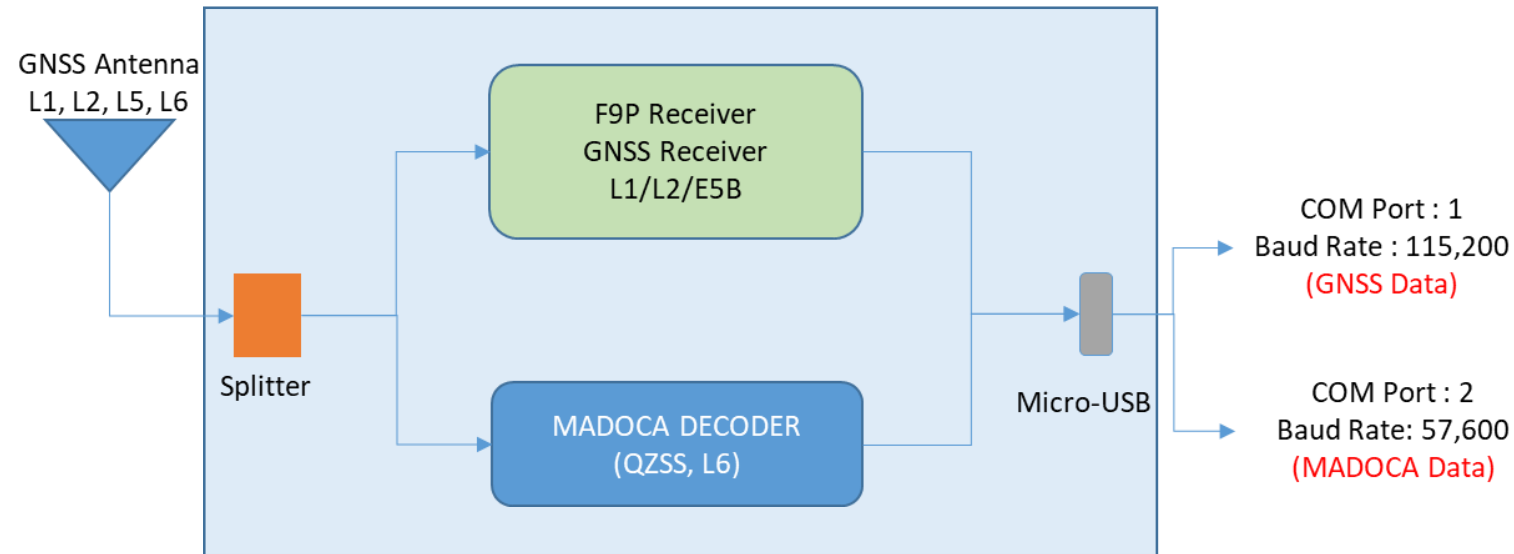
(2) MADROID:  
for MADOCA-PPP,  
MADOCA-PPP/AR (future)



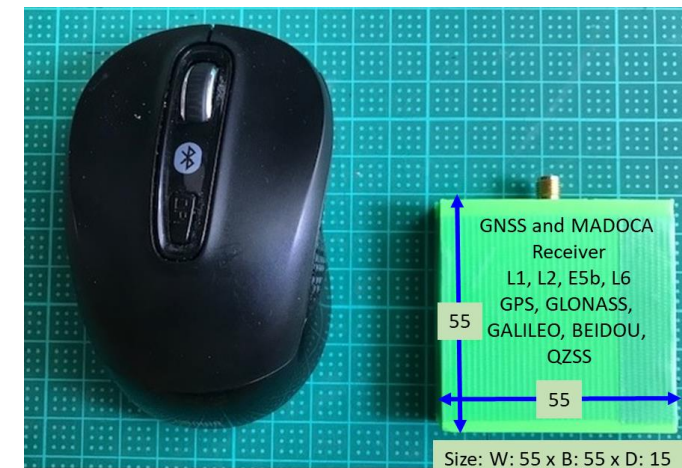
# Low-Cost MADOCA Receiver Systems: Product Types

	MAD-WIN	MAD- $\pi$	MADROID
Platform / OS	Windows	RaspberryPi 3B or 4B	Android Device
GNSS Receiver	Default : u-blox F9P Other: Any dual-frequency Receiver	Default : u-blox F9P only	Default : u-blox F9P Other: Any dual-frequency Receiver
MADOCA Receiver	U-blox D9 only	U-blox D9 only	NA (MADOCA Online Correction Data only)
GNSS Receiver Data Format	UBX, SBF, RTCM3	UBX SBF, RTCM3 (For online GNSS data)	UBX
MADOCA Correction Data Format (Satellite)	UBX only	UBX only	NA
MADOCA Correction Data Format (Online)	Online Services from GPAS, UTokyo (Test Level) UBX or RTCM3	Online Services from GPAS, UTokyo (Test Level) Online Services UBX or RTCM3	GPAS Services, RTCM3 UTokyo Online Service in the next release
System Architecture			

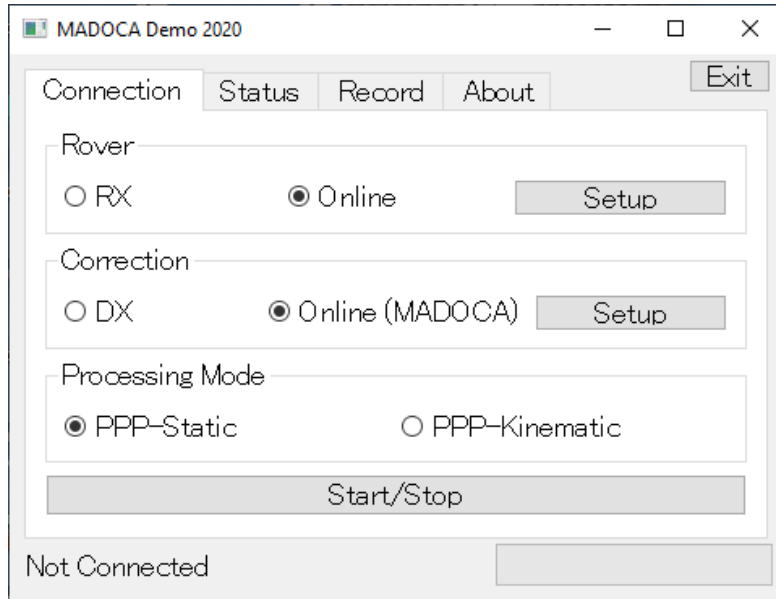
# Low-Cost MADOCA Receiver System: Antenna and Receiver



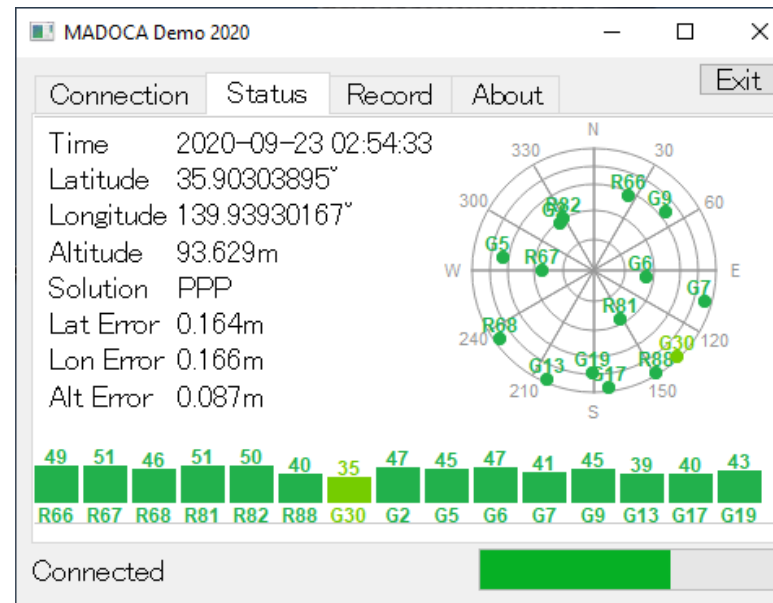
GNSS Antenna



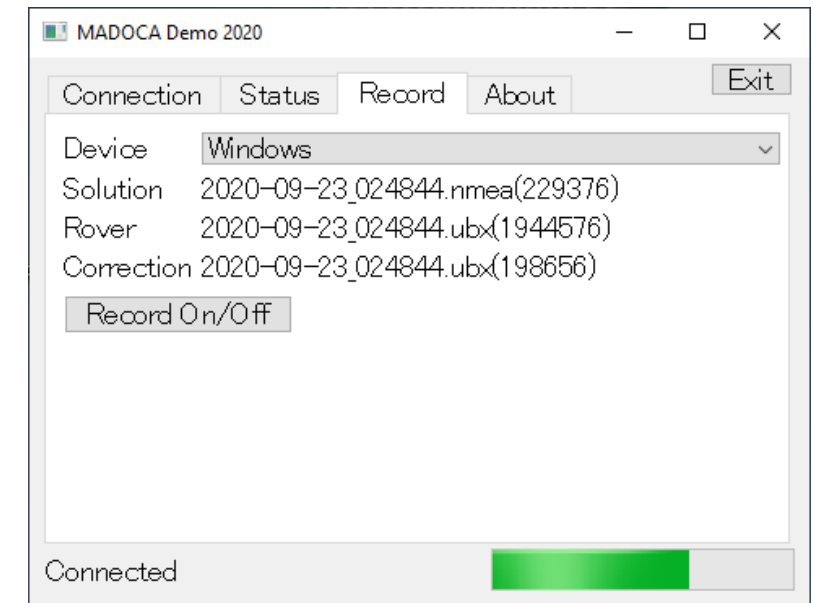
# MAD-WIN and MAD- $\pi$ Screen Shots



Receiver and MADOCA Correction Data Setup Menu



MADOCA PPP Output Display

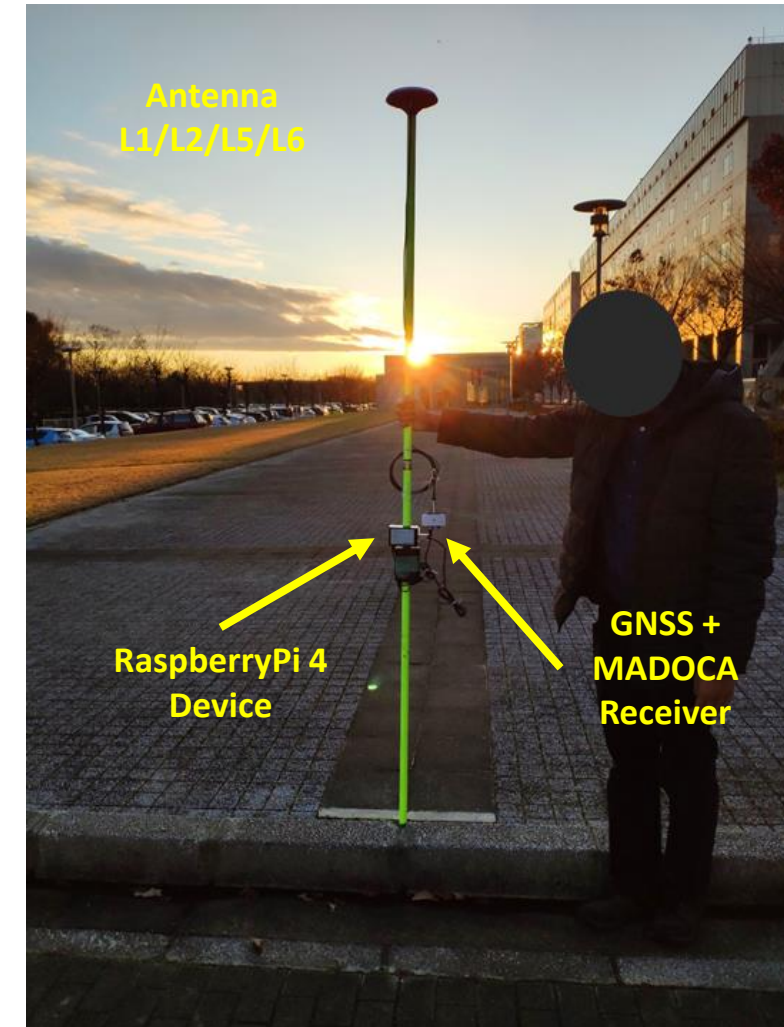


Log of MADOCA PPP Solution, Receiver Raw Data and MADOCA Correction Data



# MAD- $\pi$

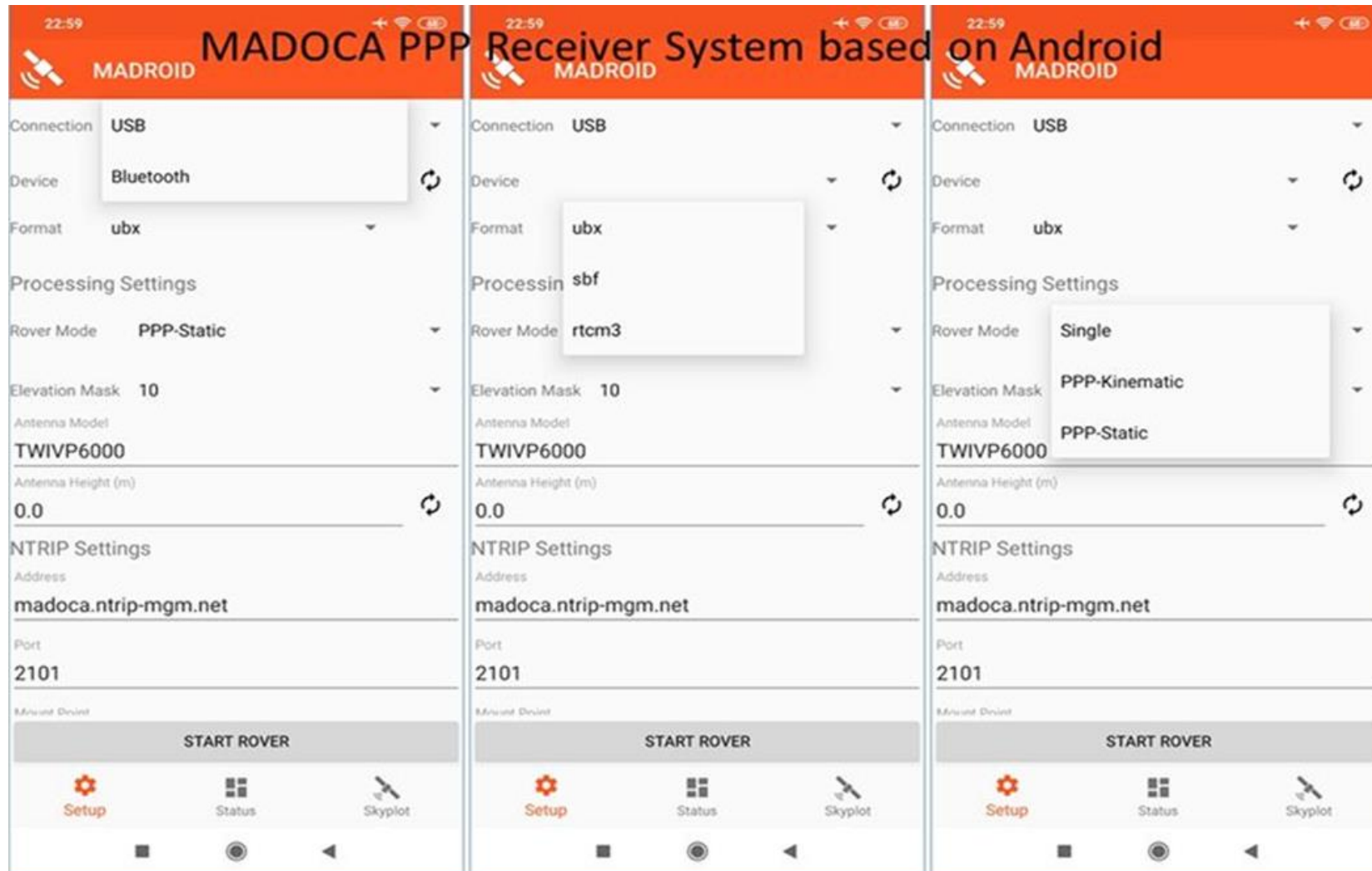
MADOCA Receiver based on RaspberryPi / Dual Frequency Receiver + MADOCA Decoder





# MADROID Screenshots

## MADOCA PPP based on Android Dual Frequency Receiver + Online MADOCA Data



# MADROID TEST Results : Tokyo

16:16

**MADROID** ABOUT

Connection USB

Device u-blox GNSS receiver

Format ubx

Processing Settings

Rover Mode PPP-Static

Elevation Mask 10

Antenna Model TWIVP6000

Antenna Height (m) 0.0

NTRIP Settings

Address madoca.ntrip-mgm.net

Port 2101

STOP ROVER

Setup Status Skyplot

16:16

**MADROID** ABOUT

NTRIP Settings

Address madoca.ntrip-mgm.net

Port 2101

Mount Point MDC0

User Name dinesh@csis.u-tokyo.ac.jp

Password \*\*\*\*\*

☒ Use Local Correction

Local Correction Settings

Address 163.43.29.167

Port 80

Mount Point

STOP ROVER

Setup Status Skyplot

16:16

**MADROID** ABOUT

Mount Point MDC0

User Name dinesh@csis.u-tokyo.ac.jp

Password \*\*\*\*\*

☒ Use Local Correction

Local Correction Settings

Address 163.43.29.167

Port 80

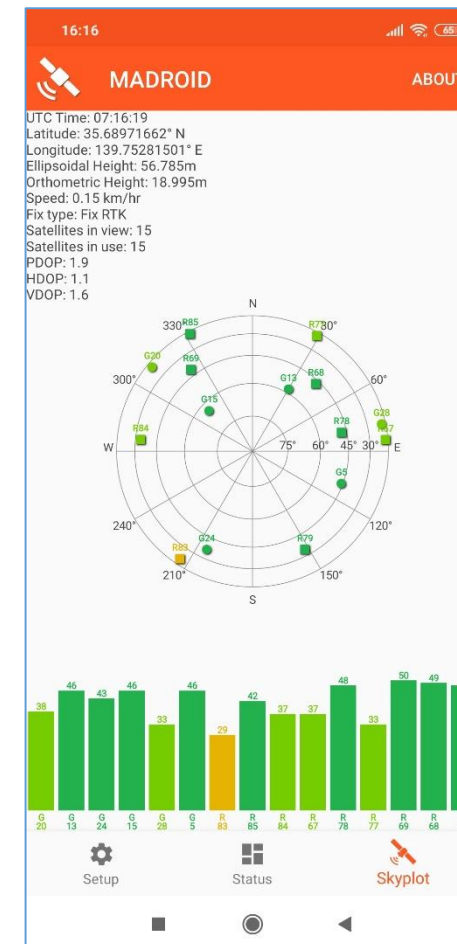
Mount Point GPASLOCAL\_T2

User Name gpas

Password \*\*\*\*\*

STOP ROVER

Setup Status Skyplot



16:16

**MADROID** ABOUT

Date: Sep 15, 2020  
Time: 07:16:23  
Latitude: 35.68971663°  
Longitude: 139.75281501°  
X: 54N 387152.640m E  
Y: 54N 3950250.977m N  
Ellipsoidal Height: 56.780m  
Orthometric Height: 18.990m  
Fix Type: Fix RTK  
Speed: 0.09 km/hr  
HDOP: 1.1  
VDOP: 1.6  
PDOP: 1.9  
Satellites in View: 15  
Satellites in Use: 15  
Latitude Error: 0.065m  
Longitude Error: 0.055m  
Altitude Error: 0.028m

NMEA: 2020\_09\_15\_16\_08\_35.txt(279KB)  
RAW: 2020\_09\_15\_16\_08\_35.ubx(2MB)

STOP RECORDING

Setup Status Skyplot

# GNSS Applications

# GNSS Applications - 1

- Surveying, Mapping and Geodesy
- Transportation
  - Car Navigation, ITS, ADAS, V2X
  - Railway Network
  - Marine : AIS, VMS
  - Aviation : SBAS / GBAS
  - UAV / DRONE
    - 3-D Mapping without GCP
- Vehicle Accidents / Emergency Services
  - eCall/ ERA-GLONASS / E-911
- Taxation / Insurance
  - Taxation based on location or distance traveled

# GNSS Applications - 2

- Legal and Law Enforcement
  - Fishing Zone Management, Illegal Fishing Control
  - Crime Prevention
- Agriculture
  - Precise farming, Auto or Semi-Auto Driving of Tractors
  - Product Supply-Chain Management
- Location Based Applications
  - Services, Entertainment, Advertisement, Gaming, Marketing
- Warning during Disasters
  - EWS of QZSS, SAR of GALILEO
- Geo-Fencing / Geo-Securities
- Robotics
  - Navigation, Actions based on Location
- Scientific Applications
  - Space Weather : Scintillation, Radio Occultation, Plasma Bubble

# GNSS Applications - 3

- Telecommunication
  - Synchronize cell towers, microsecond order for CDMA
  - Network Time Protocol , millisecond order
- Power Grid
  - Phase Synchronization between grids is required for higher efficiency and avoid power failures
- Time Stamping of
  - Financial and Banking Transactions
  - Legal, Clerical, Shipping Documents
- Scientific Timing Applications
  - Time stamping of events
    - e. g. Global VLBI Observation, earthquake occurrences, arrival of neutrino in particle physics

# Contact and Additional Information

- Homepage

- Main Page : <https://home.csis.u-tokyo.ac.jp/~dinesh/>
- Webinar Page : <https://home.csis.u-tokyo.ac.jp/~dinesh/WEBINAR.htm>  
<https://gnss.peatix.com/>
- Training Data etc. : [https://home.csis.u-tokyo.ac.jp/~dinesh/GNSS\\_Train.htm](https://home.csis.u-tokyo.ac.jp/~dinesh/GNSS_Train.htm)
- Low-Cost Receiver : <https://home.csis.u-tokyo.ac.jp/~dinesh/LCHAR.htm>
- Facebook : <https://www.facebook.com/gnss.lab/>

- Contact

- E-mail : [dinesh@csis.u-tokyo.ac.jp](mailto:dinesh@csis.u-tokyo.ac.jp)
- Skype : mobilemap