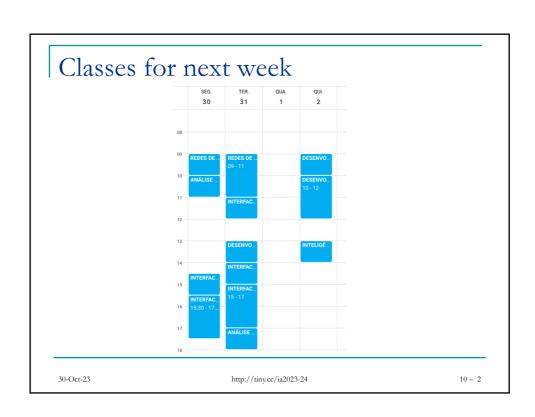
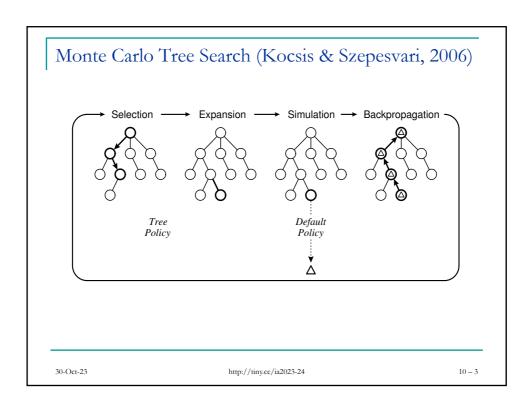
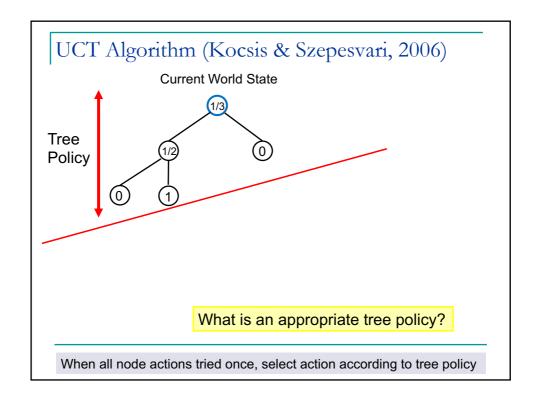


Monte Carlo Tree Search (cont.)







Played them again...



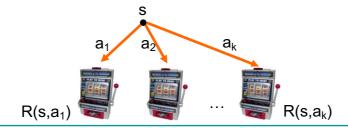
Problem: which machine should you play next?

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Multi-armed Bandit Problem, informally

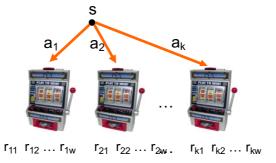
- Find an arm-pulling strategy such that the expected total reward at time n is close to the best possible (i.e., always pulling the best arm)
 - Must balance exploring machines to find good payoffs and exploiting current knowledge



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Uniform (Naïve) bandit algorithm (Even-Dar et. al., 2002)

- 1. Pull each arm w times (uniform pulling).
- 2. Return arm with best average reward.



Uniform is a poor choice – waste of time on bad arms

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Exploration vs. exploitation

- When to explore (try a new machine)?
- When to stop exploring and start exploiting (play the apparently best machine)?

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UCT Algorithm (Kocsis & Szepesvari, 2006)

■ Tree policy is guided by:
$$\pi_{UCT}(s) = \arg\max_{a} Q(s, a) + c \sqrt{\frac{\ln n(s)}{n(s, a)}}$$

- Q(s,a): average reward received in current trajectories after taking action a in state s, Q(s,a)=wins(s,a)/n(s,a)
- n(s): number of times s encountered in the sims
- n(s,a): number of times action a taken in s

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UCT Algorithm (Kocsis & Szepesvari, 2006)

- \square Q(s,a)=wins(s,a)/n(s,a)
- n(s): number of times s encountered in the sims
- n(s,a): number of times action a taken in s

Exploration Parameter

Exploration Parameter

$$\pi_{UCT}(s) = \arg\max_{a} Q(s, a) + c \sqrt{\frac{\ln n(s)}{n(s, a)}}$$

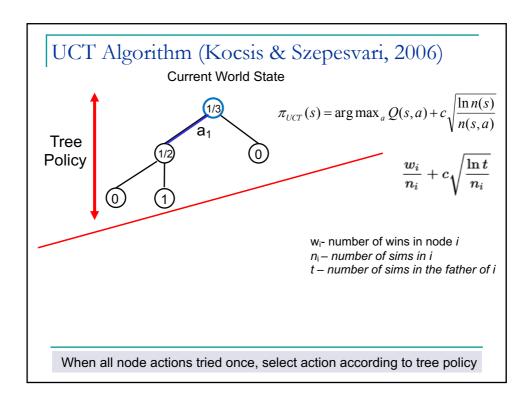
Value Term:

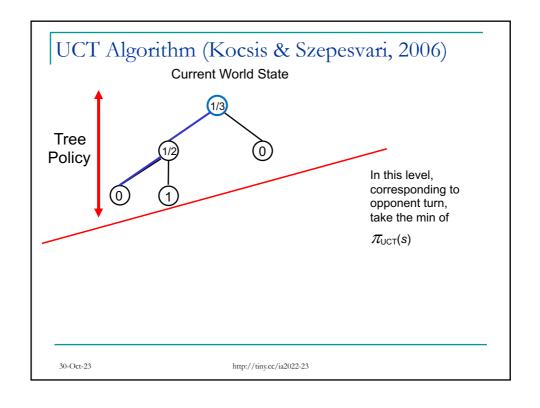
favors actions that looked good historically

Exploration Term:

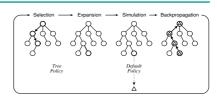
actions get an exploration bonus that grows with $\ln n(s)$

Doesn't waste much time on sub-optimal arms unlike uniform!





UCT Recap



- To select an action at a state s
 - Build a tree using N iterations of monte-carlo tree search
 - Default policy is uniform random
 - Tree policy is based on UCT rule, i.e., select action a that maximizes

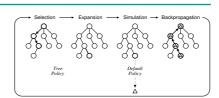
$$\pi_{UCT}(s) = \arg\max_{a} Q(s, a) + c \sqrt{\frac{\ln n(s)}{n(s, a)}}$$

$$\frac{w_i}{n_i} + c \sqrt{\frac{\ln t}{n_i}}$$

More simulations more accuracy

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UCT Recap



Algorithm 1 General MCTS approach.

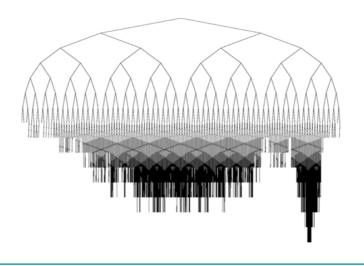
function MCTSSEARCH(s_0)

create root node v_0 with state s_0 while within computational budget do $v_l \leftarrow \text{TREEPOLICY}(v_0)$ $\Delta \leftarrow \text{DEFAULTPOLICY}(s(v_l))$ BACKUP(v_l, Δ)

return $a(\text{BESTCHILD}(v_0))$

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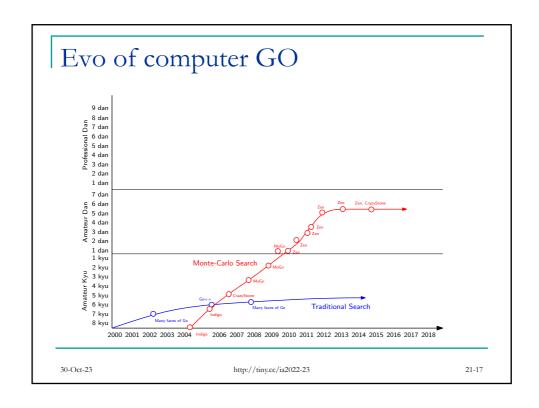
Some Improvements

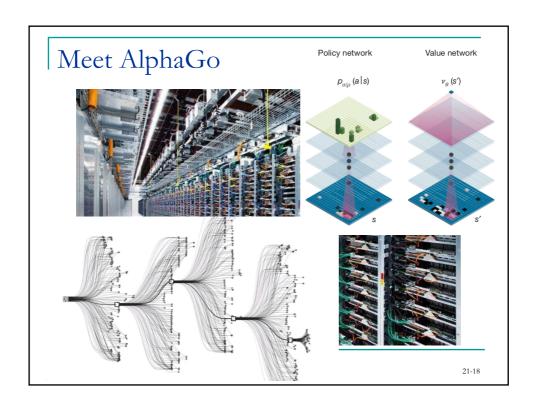
- Use domain knowledge to figure out a better than random (rollout) policy
 - e.g., don't choose obviously bad actions
- Use domain knowledge to predict the opponent actions
- Learn a heuristic function to evaluate positions and use it to evaluate and select leaf nodes for further simulations

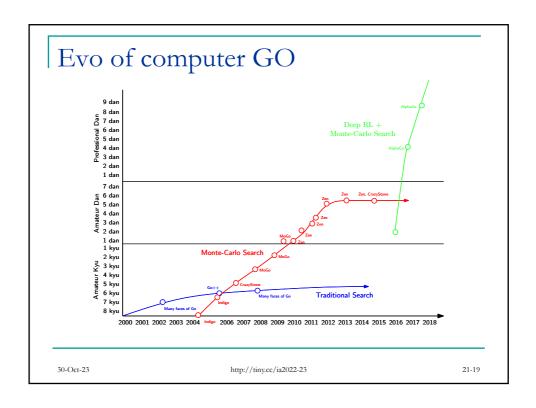
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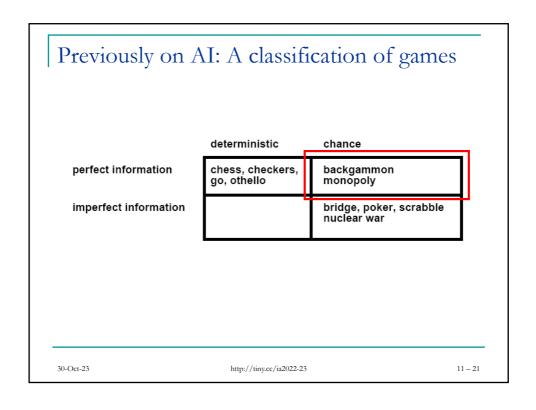


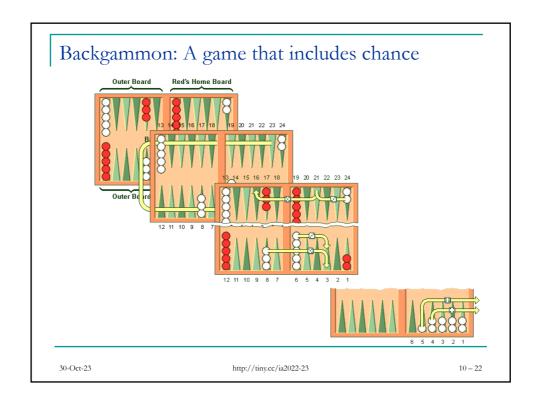


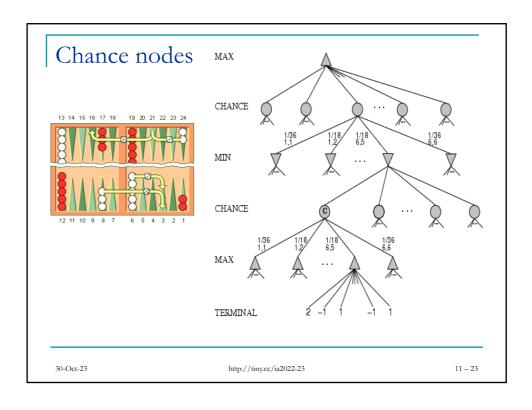
MCTS/UCT take home points

 State of the Art any-time look-ahead probabilistic search for sequential decisions in the presence of uncertainty.

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Expected minimax value

EXPECTED-MINIMAX-VALUE(n) =

 $\begin{cases} & \text{UTILITY}(n) \\ & \max_{s \in successors(n)} \text{MINIMAX-VALUE}(s) \\ & \min_{s \in successors(n)} \text{MINIMAX-VALUE}(s) \\ & \sum_{s \in successors(n)} P(s) * \text{EXPECTEDMINIMAX}(s) \end{cases}$

If *n* is a terminal
If *n* is a max node
If *n* is a min node
If *n* is a chance node

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Minimax: exact values of Eval are irrelevant

MAX

A2 is the best move

MIN

1

2

1

20

400

Behavior is preserved under any monotonic transformation of Eval function.

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Expected minimax value, example of A2 is the best move MAX DICE 2.1 1.3 2 outcomes with prob {.9, .1} 1.3 2 outcomes with prob {.9, .1} 9 1 40.9 2 2 3 3 1 1 4 4 20 20 30 30 1 1 400 400

Backgammon in practice

- Dice rolls increase the branching factor: 21 possible outcomes with 2 dices
- α-β pruning becomes much less effective.
- TDGammon: uses depth-2 search + very good Eval (neural-network with reinforcement learning);

ranked among the top three players in the world

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