

# Package ‘CondDensReg’

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**Type** Package

**Title** Conditional density regression for individual-level data

**Version** 0.1.0

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**Description** Structured additive regression models for mixed (discrete/continuous) densities as response with scalar covariates, fitted via Poisson regression models based on 'mgcv', where the continuous part of the density is approximated via histograms. Implementation for Maier et al. (2025b) <doi:../arXiv...>.

**License** GPL-2

**Depends** mgcv

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data.table,  
dplyr,  
FDboost,  
ggplot2,  
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MASS,  
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reshape2,  
Rdpack,  
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weights

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## R topics documented:

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**Description**

Structured additive regression models for mixed densities as response and scalar covariates are fitted via Poisson regression models, where the continuous part of the density is approximated with histograms.

**Details**

This package is intended to fit regression models with densities in mixed (continuous/discrete) Bayes Hilbert spaces (including continuous and discrete ones as special cases) as response given scalar covariates, based on observed samples of the conditional distributions via a (penalized) maximum likelihood approach. The (penalized) log-likelihood function is approximated via the (penalized) log-likelihood of an appropriate poisson regression model, which is then fitted using `mgcv`'s `gam` with a new smooth for mixed densities. For details see Maier et al. (2023).

The main fitting function is `dens_reg`. Besides the (individual- level) data, it takes a variety of arguments related to specification of the underlying mixed Bayes Hilbert space, histogram construction for its continuous part, and partial effects (including penalties). We also provide `plot` and `predict` methods for the resulting fitted object.

**Author(s)**

Eva-Maria Maier, Lea Runge, and Alexander Fottner

**References**

Maier, E. M., Fottner, A., Stoecker, A., Okhrin, Y., & Greven, S. (2023): Conditional density regression for individual-level data.

**See Also**

`dens_reg` for the main fitting function.

dens\_reg

*Conditional density regression for individual-level data***Description**

This function implements the approach by Maier et al. (2025b) for fitting structured additive regression models with densities in a mixed (continuous/ discrete) Bayes Hilbert space  $B^2(\mu) = B^2(\mathcal{Y}, \mathcal{A}, \mu)$  as response given scalar covariates  $x_i$ , based on observations  $y_i$  from the conditional distributions given  $x_i$ , via a (penalized) maximum likelihood approach. The (penalized) log-likelihood function is approximated via the (penalized) log-likelihood of an appropriate poisson regression model, which (after constructing the count data appropriately) is then fitted using mgcv's [gam](#) with a new smooth for mixed densities in  $L_0^2(\mu)$ . We briefly summarize the approach below in the details.

Please see Maier et al. (2025b) for comprehensive description.

**Usage**

```
dens_reg(
  dta,
  y = NULL,
  sample_weights = NULL,
  counts = NULL,
  weighted_counts = NULL,
  values_discrete = c(0, 1),
  weights_discrete = 1,
  domain_continuous = c(0, 1),
  bin_number = NULL,
  bin_width = NULL,
  m_continuous = c(2, 2),
  k_continuous = 10,
  sp_y = NULL,
  method = "REML",
  penalty_discrete = NULL,
  group_specific_intercepts = NULL,
  linear_effects = NULL,
  smooth_effects = NULL,
  varying_coefficients = NULL,
  smooth_interactions = NULL,
  effects = TRUE,
  ...
)
```

**Arguments**

dta	Data set of type <a href="#">data.frame</a> or <a href="#">data.table</a> containing the observations $(y_i, x_i)$ of response and covariates as well as optional sample weights (compare <code>sample_weights</code> ) for each observation in the rows ( $i = 1, \dots, N$ ).
y	Variable in dta containing the response observations $y_i$ . Either the variable name can be given as string or the column position of the variable in dta as integer. If missing (NULL), if there is a unique column of dta not specified

	in <code>sample_weights</code> , <code>counts</code> , and <code>weighted_counts</code> and not used as covariate during effect specification (see below), this unique column is used.
<code>sample_weights</code>	(Optional) variable in <code>dta</code> which contains a sample weight for each observation. Either the variable name can be given as string or the column position of the variable in <code>dta</code> as integer. If missing (NULL), no sample weights are included per default (i.e., all observations have the same weight 1).
<code>counts</code>	(Optional) variable in <code>dta</code> which contains a count for each observation (for cases, where the available data contains counts instead of individual observations, which is common in particular for discrete data). Either the variable name can be given as string or the column position of the variable in <code>dta</code> as integer. If <code>bin_number</code> and <code>bin_width</code> are both NULL, midpoints of unique observations $y_i$ are used as boundaries of histogram bins (if $I$ is not empty, i.e., if there is a continuous component), which are then used to compute the bin widths (which are later required as offset in the regression model). If argument <code>counts</code> is missing (NULL; default), counts are constructed from individual observations (which is equivalent to each observation counted once). Note that if <code>counts</code> and <code>sample_weights</code> are both not NULL, the latter is ignored (also indicated via a warning message). Please use <code>weighted_counts</code> (additionally to <code>counts</code> ) to include possible weighted data.
<code>weighted_counts</code>	(Optional) variable in <code>dta</code> which contains a weighted count for each observation (compare Appendix D of Maier et al. (2025b)). In this case, also absolute counts have to be specified via <code>counts</code> . Otherwise, <code>weighted_counts</code> is ignored. Either the variable name can be given as string or the column position of the variable in <code>dta</code> as integer. If missing (NULL), counts are constructed from individual observations (which is equivalent to all observations counted once).
<code>values_discrete</code>	Vector of values in $\mathcal{D}$ (the subset of the domain corresponding to the discrete part of the densities). Defaults to missing (NULL) in which case it is set to $c(0, 1)$ . If set to FALSE, the discrete component is considered to be empty, i.e., the Lebesgue measure is used as reference measure (continuous special case).
<code>weights_discrete</code>	Vector of weights for the Dirac measures corresponding to <code>values_discrete</code> . If missing (NULL) it is set to 1 in all components as default. Can be a scalar for equal weights for all discrete values or a vector with specific weights for each corresponding discrete value.
<code>domain_continuous</code>	An interval (i.e., a vector of length 2) specifying $I$ (the subset of the domain corresponding to the continuous part of the densities). If missing (NULL) it is set to $c(0, 1)$ as default. If set to FALSE, the continuous component is considered to be empty, i.e., a weighted sum of dirac measures is used as reference measure (discrete special case).
<code>bin_number</code>	Number of equidistant histogram bins partitioning $I$ . Alternative to <code>bin_width</code> . If neither parameter is specified, <code>bin_number = 100</code> is used as default. If <code>bin_number</code> and <code>bin_width</code> are both given and the two values are not compatible, an error is returned.
<code>bin_width</code>	Width of histogram bins partitioning $I$ . Can be one scalar value (specifying an equidistant bin width), or a vector containing the width of each bin. The combined length of the specified bins must match the length of the continuous

	part of the domain. Alternative to <code>bin_number</code> . If <code>bin_number</code> and <code>bin_width</code> are both given and the two values are not compatible, an error is returned.
<code>m_continuous</code>	Vector of two integers specifying the order of the B-spline basis over $I$ and the order of the difference penalty (like the argument <code>m</code> for P-Spline smooth terms <code>bs = "ps"</code> in <a href="#">ti</a> , etc.) for basis functions in $L^2(\lambda)$ , before transformation to $L_0^2(\lambda)$ (compare details). If missing it is set to cubic splines with second order difference penalty, i.e., <code>m_continuous = c(2, 2)</code> , as default.
<code>k_continuous</code>	Integer specifying the number of B-spline basis functions in $L^2(\lambda)$ (like the argument <code>k</code> for P-Spline smooth terms <code>bs = "ps"</code> in <a href="#">ti</a> , etc.), before transformation to $L_0^2(\lambda)$ (compare details). Note that the transformation reduces the basis number by 1. The basis $b_Y b_Y$ in the mixed Bayes Hilbert space $B^2(\mu)$ will thus have <code>k_continuous - 1 + length(values_discrete)</code> elements. See also <a href="#">choose.k</a> for more information on choosing this parameter. If missing (NULL) it is set to 10.
<code>sp_y</code>	Integer or vector specifying the smoothing parameter for the marginal penalty matrix for $b_Y b_Y$ (anisotropic penalty; like the argument <code>sp</code> in <a href="#">ti</a> , etc.). If a vector is submitted, its length must be the number of partial effects (including the intercept), with the $j$ -th entry specifying the smoothing parameter for the $j$ -th partial effect. The order of parameters within this vector corresponds to the intercept followed by the partial effects in the order as specified below ( <code>group_specific_intercepts</code> , <code>linear_effects</code> , <code>smooth_effects</code> , <code>varying_coefficients</code> , and <code>smooth_interactions</code> ). Upenalized estimation is accomplished by setting <code>sp_y</code> to zero. If missing (NULL) or a negative value is supplied, the parameter will be estimated by <a href="#">gam</a> via the estimation method specified in <code>method</code> (with REML-estimation per default). Any positive or zero value is treated as fixed (see <a href="#">gam</a> ).
<code>method</code>	String characterizing the smoothing parameter estimation method as in <a href="#">gam</a> . Defaults to "REML" (REML-estimation).
<code>penalty_discrete</code>	<p>Integer or NULL giving the order of differences to be used for the penalty of the discrete component, with 0 corresponding to the identity matrix as penalty matrix (analogously to <code>m[2]</code> for the continuous component); Note that the order of differences must be smaller than the number of values in the discrete component, i.e., the length of <code>values_discrete</code>.</p> <p>If missing (NULL), the discrete component is estimated unpenalized (in the mixed case, by setting the discrete component of the penalty matrix to zero - with the continuous component non-zero -, in the discrete case by setting the smoothing parameter to zero (with a diagonal penalty matrix) since due to technical reasons it is not possible to set the whole penalty matrix to zero).</p>
<code>group_specific_intercepts</code>	Vector of the form <code>c("x_a", "x_b", ...)</code> of names of categorical covariates, i.e., <a href="#">factor</a> variables contained in <code>dta</code> for which group-specific intercepts $\beta_{x_a}, \beta_{x_b}, \dots$ (one per category of the respective covariate) shall be estimated. For <a href="#">ordered</a> factors, the first level is used as reference category (see <a href="#">gam.models</a> for more details). If missing (NULL), no group-specific intercept is included.
<code>linear_effects</code>	Vector of the form <code>c("x_a", "x_b", ...)</code> of names of numeric covariates contained in <code>dta</code> for which linear effects $x_a \odot \beta_{x_a}, x_b \odot \beta_{x_b}, \dots$ shall be estimated. If missing (NULL), no linear effect is included.
<code>smooth_effects</code>	List of (named) lists of the form <code>list(list(cov = "x_a", bs = bs_a, m = m_a, k = k_a, mc = mc_a, by = "x_b"), ...)</code> . If the lists are unnamed, the names are

assigned in the order of the given elements. The list is filled with NULL if it contains less than 6 elements. Each list is adding one (group-specific) smooth effect of the form  $g_{x_b}(x_a)$  to the model with:

- cov: Name of a numeric covariate contained in dta.
- bs: Character string specifying the type for the marginal basis in covariate direction. See [smooth.terms](#) for details and full list. If not specified or NULL, a P-spline basis "ps" is used.
- m: Vector of two integers or NULL giving the order of the marginal spline basis  $b_j$  in covariate direction and the order of its penalty (as in [ti](#)). If not specified or NULL, c(2,2) is used.
- k: Integer or NULL giving the dimension of the marginal basis  $b_j$  (as in [ti](#)). See [choose.k](#) for more information. If not specified or NULL, 10 is used.
- mc: Logical indicating if the marginal in covariate direction should have centering constraints applied. By default all marginals are constrained, i.e., mc = TRUE.
- by: Optional, name of a categorical covariate, i.e., [factor](#) variable contained in dta specifying whether the smooth effect should be modeled specifically for each level of the by-covariate (group-specific). For [ordered](#) factors, the first level is used as reference category (see [gam.models](#) for more details). If missing or NULL, the smooth effect is not depending on the level of an additional covariate.

If missing (NULL), no (group-specific) smooth effect is included.

#### varying\_coefficients

List of lists of the form `list(list(cov = "x_a", by = "x_b", bs = bs_a, m = m_a, k = k_a, mc = mc_a), ...)`. If the lists are unnamed, the names are assigned in the order of the given elements. The list is filled with NULL if it contains less than 6 elements. Each list is adding one varying coefficient of the form  $x_b \odot g(x_a)$  to the model with:

- cov: Name of a numeric covariate contained in dta.
- by: Name of a numeric covariate contained in dta.
- bs: Character string specifying the type for the marginal basis in covariate direction. See [smooth.terms](#) for details and full list. If not specified or NULL, a P-spline basis "ps" is used.
- m: Vector of two integers or NULL giving the order of the marginal spline basis  $b_j$  in covariate direction and the order of its penalty (as in [ti](#)). If not specified or NULL, c(2,2) is used
- k: Integer or NULL giving the dimension of the marginal basis  $b_j$  (as in [ti](#)). See [choose.k](#) for more information. If not specified or NULL, 10 is used.
- mc: Logical indicating if the marginal in the direction of the first covariate should have centering constraints applied. By default all marginals are constrained, i.e., mc = TRUE.

If missing (NULL), no varying coefficient is included.

#### smooth\_interactions

List of lists of the form `list(list(covs = c("x_a", "x_b", ...), bs = c(bs_a, bs_b, ...), m = list(m_a, m_b, ...), k = c(k_a, k_b, ...), mc = c(mc_a, mc_b, ...), by = "x_by"), list(...))`. If the lists are unnamed, the names are assigned in the order of the given elements. The list is filled with vectors/lists of NULL if it contains less than 6 elements. Each list is specifying a (group-specific) smooth interaction effect between at least two continuous covariates of the form  $g_{x_by}(x_a, x_b, \dots)$  in the model with:

- covs: Vector of names of numeric covariates contained in dta.
- bs: Vector of character strings specifying the types for each marginal basis of each covariate. See [smooth.terms](#) for details and full list. If not specified or NULL, a P-spline basis "ps" is used.
- m: List containing vectors of two integers or NULL giving the order of the marginal spline basis in direction of the respective covariate in covs for the smooth effect and the order of its penalty (as in [ti](#)). If not specified or NULL, a list of c(2, 2) is used.
- k: Vector of integers or NULL giving the dimension of the marginal basis in direction of the respective covariate in covs for the smooth effect. See [choose.k](#) for more information. If not specified or NULL, a vector specifying each parameter as 10 is used.
- mc: Logical vector indicating if the marginals in covariate direction should have centering constraints applied. By default all marginals are constrained, i.e., TRUE.
- by: Optional, name of a categorical covariate, i.e., [factor](#) variable contained in dta specifying whether the smooth interaction effect should be modeled specifically for each level of the by-covariate (group-specific). For [ordered](#) factors, the first level is used as reference category (see [gam.models](#) for more details). If missing or NULL, the smooth interaction effect is not depending on the level of an additional covariate.

If missing (NULL), no (group-specific) smooth interaction is included.

effects Indicates if estimated partial effects should be returned (TRUE; default) or not (FALSE).

... further arguments for passing on to [gam](#).

## Details

The function `dens_reg` estimates the densities  $f_{x_i}$  of conditional distributions of random variables  $Y_i|x_i$  from independent observations  $(y_i, x_i)$ , where  $y_i$  are realizations of  $Y_i|x_i$ , and  $x_i$  is a vector of covariate observations,  $i = 1, \dots, N$ . The densities are considered as elements of a mixed Bayes Hilbert space  $B^2(\mu) = B^2(\mathcal{Y}, \mathcal{A}, \mu)$  (including continuous and discrete ones as special cases). The subset of the domain  $\mathcal{Y}$  corresponding to the continuous part of the densities is denoted with  $I$ , the one corresponding to the discrete part with  $\mathcal{D}$ . The densities are modeled via a structured additive regression model

$$f_{x_i} = \bigoplus_{j=1}^J h_j(x_i)$$

with partial effects  $h_j(x_i) \in B^2(\mu)$  depending on no, one, or several covariates  $x_i$ . Each partial effect is represented using a tensor product basis, consisting of an appropriate vector of basis functions  $b_Y b_X$  in  $B^2(\mu)$  over the domain of  $B^2(\mu)$ , and a vector of basis functions  $b_{X,j}$  over the respective covariates. To obtain basis functions  $b_Y$  consider the orthogonal decomposition of the mixed Bayes Hilbert space  $B^2(\mu)$  into a discrete Bayes Hilbert space  $B^2(\delta^\bullet)$  and a continuous Bayes Hilbert space  $B^2(\lambda)$  developed in Section 3.4 of Maier et al. (2025a). Note that for the domain of the discrete Bayes Hilbert space, the discrete part  $\mathcal{D}$  has to be extended by an additional arbitrary discrete value (for the discrete summary of the continuous part). We construct basis functions in both these spaces by transforming appropriate basis functions in the corresponding (unconstrained)  $L^2$  spaces (more precisely, indicator functions with optional difference penalty for the discrete and a P-spline basis for the continuous Bayes Hilbert space), to the respective  $L_0^2$  spaces, i.e., the subspaces of  $L^2$  containing only functions that integrate to zero.

See appendix D of Maier et al. (2025a) for details on this transformation. Applying the inverse centered log-ratio (clr) transformation (which is an isometric isomorphism, allowing to consider densities in some  $B^2$  space equivalently in the respective  $L_0^2$  space) yields one basis in  $B^2(\delta^\bullet)$  and one in  $B^2(\lambda)$ . The basis in the actually considered mixed Bayes Hilbert space  $B^2(\mu)$  is then obtained by applying the respective embeddings to these two bases (compare Section 3.4 of Maier et al. (2025a) and Section 2.2 of Maier et al. (2025b)). The choice of  $b_{\mathcal{X},j}$  determines the type of the partial effect, e.g., linear or smooth for a continuous covariate. For smooth effects, the same marginal bases as in `gam` can be used. In particular, penalization is also possible. The resulting log-likelihood is then approximated by the log-likelihood of a corresponding multinomial model, which can equivalently be estimated by a Poisson model. The data for these models is obtained from the original observations  $y_1, \dots, y_N$  by combining all observations of the same conditional distribution into a vector of counts via a histogram on the continuous part of the domain of the densities and counts on the discrete part of the domain. For details, see Maier et al. (2025b). `dens_reg` constructs the respective count data from the individual observations and estimates the corresponding Poisson model. Furthermore, the resulting densities on pdf- and clr-level as well as the estimated partial effects on both levels are calculated.

## Value

The function returns an object of the class `dens_reg_obj`, which is a `list` with elements:

- `count_data`: `data.table`-object containing the count data obtained by using `preprocess` for the given data `dta` and covariates, which is also an object of the sub-class `histogram_count_data`. See `?preprocess` for more information.
- `model`: `gam`-object of the estimated model.
- `model_matrix`: Model matrix of the model.
- `theta_hat`: Estimated coefficient vector  $\hat{\theta}$ .
- `f_hat_clr`: Estimated conditional densities on clr-level  $clr(\hat{f})$  for every covariate combination in the order of the respective `group_id` in `count_data`.
- `f_hat`: Estimated conditional densities on pdf-level  $f(\hat{f})$  for every covariate combination in the order of the respective `group_id` in `count_data`.
- `effects`: Only contained, if `effects = TRUE`; List of lists. Each list gives one estimated partial effect. Both clr- and density-level are included.
- `params`: List of `domain_continuous`, `values_discrete` and `bin_number` as given to the function.
- `predicted_effects`: List of lists (`group_specific_intercepts`, `smooth effects`, `linear effects`, `varying`...) collecting the specification of all partial effects as given to the function in the respective parameters.
- `ID_covCombi`: Data frame which gives an overview over the assignment of the unique covariate combinations to the group IDs.

Note that `plot`- and `predict`-methods for objects of class `dens_reg_obj` are available via `CondDensReg::plot.dens_reg_obj` and `CondDensReg::predict.dens_reg_obj`, however, they are not exported, since they are not tested/documentated appropriately, yet.

## Author(s)

Lea Runge, Eva-Maria Maier



## References

Maier, E.-M., Fottner, A., Stoecker, A., Okhrin, Y., & Greven, S. (2025b): Conditional density regression for individual-level data. arXiv preprint arXiv:XXXX.XXXXX.

Maier, E.-M., Stoecker, A., Fitzenberger, B., Greven, S. (2025a): Additive Density-on-Scalar Regression in Bayes Hilbert Spaces with an Application to Gender Economics. Annals of Applied Statistics, 19(1), ???-???

## Examples

```
### Note that the following simulated data are only to illustrate
### function usage and do not possess significant covariate effects

# for further information on the parameters of the preprocessing step see ?preprocess

# create data for the mixed case
set.seed(101)

dta <- data.frame(obs_density = sample(0:2, 150, replace = TRUE, prob = c(0.15, 0.1, 0.75)),
                  covariate1 = sample(c("a", "b", "c"), 150, replace = TRUE),
                  covariate2 = sample(c("c", "d"), 150, replace = TRUE),
                  covariate3 = rep(rnorm(n = 15), 10),
                  covariate4 = rep(rnorm(n = 10), 15),
                  covariate5 = rep(rnorm(n = 10), 15), sample_weights = runif(150, 0, 2))
dta[which(dta$obs_density == 2), ]$obs_density <- rbeta(length(which(dta$obs_density == 2)),
                                                       shape1 = 3, shape2 = 3)

dta$covariate1 <- ordered(dta$covariate1)
dta$covariate2 <- ordered(dta$covariate2)

# create discrete data

dta_dis <- data.frame(obs_density = sample(0:2, 150, replace = TRUE, prob = c(0.25, 0.45, 0.3)),
                     covariate1 = sample(c("a", "b", "c"), 150, replace = TRUE),
                     covariate2 = sample(c("c", "d"), 150, replace = TRUE),
                     covariate3 = rep(rnorm(n = 15), 10),
                     covariate4 = rep(rnorm(n = 10), 15),
                     covariate5 = rep(rnorm(n = 10), 15),
                     sample_weights = runif(150, 0, 2))
dta_dis$covariate1 <- ordered(dta_dis$covariate1)
dta_dis$covariate2 <- ordered(dta_dis$covariate2)

# examples for different partial effects

## group specific intercepts
group_specific_intercepts <- c("covariate1", "covariate2")
## linear effects
linear_effects <- c("covariate4")
## smooth effects
smooth_effects <- list(list(cov = "covariate3", bs = "ps", m = c(2, 2), k = 4),
                       list(cov = "covariate3", bs = "ps", m = c(2, 2), k = 4,
                             mc = FALSE, by = "covariate1"))

## varying coefficient
varying_coef <- list(list(cov = "covariate3", by = "covariate4", bs = "ps", m = c(2, 2), k = 4))
## smooth interaction
smooth_inter <- list(list(covs = c("covariate3", "covariate4", "covariate5"),
                          bs = c("ps", "ps", "ps"),
                          m = list(c(2, 2), c(2, 2), c(2, 2)), k = c(4, 4, 5),
```

```

mc = c(TRUE, FALSE, TRUE), by = NULL))

# fit models (warning: calculation may take a few minutes)

## fit model for the mixed case with group specific intercepts and linear effects
### use fixed smoothing parameters in density direction and calculate also the partial effects

m_mixed <- dens_reg(dta = dta, y = 1, m_continuous = c(2, 2),
  k_continuous = 4, group_specific_intercepts = group_specific_intercepts,
  linear_effects = linear_effects, effects = TRUE, sp_y = c(1, 3, 5, 0.5))

## fit model for the discrete case with smooth effects and smooth interaction
### do not calculate effects

m_dis <- dens_reg(
  dta = dta_dis, y = 1, values_discrete = c(0, 1, 2),
  weights_discrete = c(1, 1, 1), domain_continuous = FALSE, m_continuous = c(2, 2),
  k_continuous = 4, group_specific_intercepts = group_specific_intercepts,
  smooth_effects = smooth_effects, smooth_interactions = smooth_inter, effects = FALSE)

# fit model for the continuous case with a functional varying coefficient

m_cont <- dens_reg(dta = dta[which(!(dta$obs_density %in% c(0, 1))), ],
  y = 1, values_discrete = FALSE, m_continuous = c(2, 2),
  k_continuous = 12, varying_coefficients = varying_coef, effects = TRUE)

```

---

Predict.matrix.mdspline.smooth

*Predict matrix method function for mixed density smooth*

---

## Description

[Predict.matrix](#) method function for smooth class `mdspline.smooth` to enable prediction from a model fitted with `mgcv`'s [gam](#).

## Usage

```
## S3 method for class 'mdspline.smooth'
Predict.matrix(object, data)
```

## Arguments

<code>object</code>	a smooth specification object, usually generated by a term <code>ti(x, bs="md", ...)</code>
<code>data</code>	A data frame containing the values of the (named) covariates at which the smooth term is to be evaluated. Exact requirements are as for <a href="#">smooth.construct</a> and <a href="#">smooth.construct2</a>

## Details

The Predict matrix function is not normally called directly, but is rather used internally by `mgcv`'s [predict.gam](#) etc. to predict from a fitted [gam](#) model. See [Predict.matrix](#) for more details, or [smooth.construct.md.smooth.spec](#) for details on the mixed density smooth "md".

**Value**

A matrix mapping the coefficients for the smooth term to its values at the supplied data values.

**Author(s)**

Eva-Maria Maier, Alexander Fottner

**References**

Maier, E.-M., Fottner, A., Stoecker, A., Okhrin, Y., & Greven, S. (2025b): Conditional density regression for individual-level data. arXiv preprint arXiv:XXXX.XXXXX.

**Examples**

```
### create data
set.seed(101)

N <- 100
dta <- data.frame(covariate1 = sample(c("a", "b", "c"), N, replace = TRUE),
                  covariate2 = rnorm(n = N))
dta$obs_density <- sapply(seq_len(N),
                          function(i) {
                            a_0 <- ifelse(dta$covariate1[i] == "a", 0.1,
                                           ifelse(dta$covariate1[i] == "b", 0.2, 0.3))
                            p_0 <- a_0 * sin(dta$covariate2[i]) + a_0 + 0.05
                            a_1 <- ifelse(dta$covariate1[i] == "a", 0.25,
                                           ifelse(dta$covariate1[i] == "b", 0.15, 0.05))
                            p_1 <- a_1 * cos(dta$covariate2[i]) + a_1 + 0.1
                            sample(0:2, 1, prob = c(p_0, p_1, 1 - p_0 - p_1))
                          })

dta$covariate1 <- ordered(dta$covariate1)

dta_mixed <- dta
ind_cont <- which(dta_mixed$obs_density == 2)
dta_mixed[ind_cont, ]$obs_density <-
  sapply(seq_along(ind_cont), function(i)
    rbeta(1, shape1 = 1 + exp(dta_mixed$covariate2[i]),
          shape2 = 1 + as.numeric(dta_mixed$covariate1[i])))
n_bins <- 20
dta_mixed <- preprocess(dta = dta_mixed, var_vec = c("covariate1", "covariate2"),
                        bin_number = n_bins, values_discrete = c(0, 1),
                        domain_continuous = c(0, 1))

### fit model
m_mixed <- gam(counts ~
  # no scalar global intercept (we add a density-intercept instead)
  - 1 +
  # intercept (corresponding to reference covariate1 = "a")
  ti(obs_density, bs = "md", m = list(c(2, 2)), k = 8,
    mc = FALSE, np = FALSE) +
  # group specific intercept for leveles "b" and "c" of covariate2
  ti(obs_density, bs = "md", m = list(c(2, 2)), k = 8,
    mc = FALSE, np = FALSE, by = covariate1) +
  # smooth effect of covariate2 (modeled via P-splines)
  ti(covariate2, obs_density, bs = c("ps", "md"),
```

```

        m = list(c(2, 2), c(2, 2)), k = c(8, 8), mc = c(TRUE, FALSE),
        np = FALSE) +
# intercepts per covariate combination (modeling absolute
# counts for poisson regression)
as.factor(group_id) +
# offsets: log(Delta) accounting for bin width, gam_offsets
# for weighted observations
offset(log(Delta)),
family = poisson(), method = "REML", data = dta_mixed)

### Functions using S3 Predict.matrix-method for class 'mdspline.smooth' are, e.g.,
### model.matrix and predict

# Using model.matrix (and internally Predict.matrix.mdspline.smooth) to extract
# design matrix and construct estimated densities thereof
X <- model.matrix(m_mixed)
# The design matrix includes intercepts per covariate combination modeling the
# absolute counts for the Poisson model, which are not of interest on density-level.
# Thus, we remove them.
intercepts <- which(grepl("group_id", colnames(X)))
X <- X[, -intercepts]
theta_hat <- m_mixed$coefficients[-intercepts]
# compute estimated conditional clr-transformed densities
f_hat_clr <- matrix(c(X %*% theta_hat), nrow = length(unique(dta_mixed$obs_density)))
f_hat <- apply(f_hat_clr, 2,
              FDboost::clr, w = c(1, rep(1/n_bins, n_bins), 1), inverse = TRUE)
t <- unique(dta_mixed$obs_density)
matplot(t[2:(length(t) - 1)], f_hat[2:(length(t) - 1), ], type = "l",
        col = rainbow(ncol(f_hat)), lty = rep(1:5, ceiling(ncol(f_hat) / 5)),
        ylim = range(f_hat))
matpoints(t[c(1, length(t))], f_hat[c(1, length(t)), ],
         col = rainbow(ncol(f_hat)), pch = 1)

# Using predict (and internally Predict.matrix.mdspline.smooth) to extract
# estimated partial effects
pred_terms <- predict(m_mixed, type = "terms")

```

---

preprocess

---

*From observations to a vector of observed (histogram) counts*


---

## Description

preprocess prepares data containing the original observations  $y_i$  appropriately to be used in Poisson models by combining all observations of the same conditional distribution (i.e., all observations sharing identical values in all covariates) into a vector of counts via a histogram on  $I \setminus D$  and counts on  $D$  where  $I$  is the interval of the continuous domain and  $D$  the set of discrete values.

## Usage

```

preprocess(
  dta,
  var_vec,

```

```

y = NULL,
sample_weights = NULL,
counts = NULL,
weighted_counts = NULL,
bin_width = NULL,
bin_number = NULL,
values_discrete = c(0, 1),
weights_discrete = 1,
domain_continuous = c(0, 1)
)

```

## Arguments

dta	Data set of type <code>data.frame</code> or <code>data.table</code> containing the observations $(y_i, x_i)$ of response and covariates as well as optional sample weights (compare <code>sample_weights</code> ) for each observation in the rows $(i = 1, \dots, N)$ .
var_vec	Vector of variables of dta on which the covariate combinations are based. The vector can either contain the variable names as strings or the column positions of the respective variables in dta.
y	Variable in dta containing the response observations $y_i$ . Either the variable name can be given as string or the column position of the variable in dta as integer. If missing (NULL), if there is a unique column of dta not specified in <code>var_vec</code> , <code>sample_weights</code> , <code>counts</code> , and <code>weighted_counts</code> (see below), this unique column is used.
sample_weights	(Optional) variable in dta which contains a sample weight for each observation. Either the variable name can be given as string or the column position of the variable in dta as integer. If missing (NULL), no sample weights are included per default (i.e., all observations have the same weight 1).
counts	(Optional) variable in dta which contains a count for each observation (for cases, where the available data contains counts instead of individual observations, which is common in particular for discrete data). Either the variable name can be given as string or the column position of the variable in dta as integer. If <code>bin_number</code> and <code>bin_width</code> are both NULL, midpoints of unique observations $y_i$ are used as boundaries of histogram bins (if <code>I</code> is not empty, i.e., if there is a continuous component), which are then used to compute the bin widths (which are later required as offset in the regression model). If argument <code>counts</code> is missing (NULL; default), counts are constructed from individual observations (which is equivalent to each observation counted once). Note that if <code>counts</code> and <code>sample_weights</code> are both not NULL, the latter is ignored (also indicated via a warning message). Please use <code>weighted_counts</code> (additionally to <code>counts</code> ) to include possible weighted data.
weighted_counts	(Optional) variable in dta which contains a weighted count for each observation (compare Appendix D of Maier et al. (2025b)). In this case, also absolute counts have to be specified via <code>counts</code> . Otherwise, <code>weighted_counts</code> is ignored. Either the variable name can be given as string or the column position of the variable in dta as integer. If missing (NULL), counts are constructed from individual observations (which is equivalent to all observations counted once).

<code>bin_width</code>	Width of histogram bins partitioning $I$ . Can be one scalar value (specifying an equidistant bin width), or a vector containing the width of each bin. The combined length of the specified bins must match the length of the continuous part of the domain. Alternative to <code>bin_number</code> . If <code>bin_number</code> and <code>bin_width</code> are both given and the two values are not compatible, an error is returned.
<code>bin_number</code>	Number of equidistant histogram bins partitioning $I$ . Alternative to <code>bin_width</code> . If neither parameter is specified, <code>bin_number = 100</code> is used as default. If <code>bin_number</code> and <code>bin_width</code> are both given and the two values are not compatible, an error is returned.
<code>values_discrete</code>	Vector of values in $\mathcal{D}$ (the subset of the domain corresponding to the discrete part of the densities). Defaults to missing (NULL) in which case it is set to <code>c(0, 1)</code> . If set to <code>FALSE</code> , the discrete component is considered to be empty, i.e., the Lebesgue measure is used as reference measure (continuous special case).
<code>weights_discrete</code>	Vector of weights for the Dirac measures corresponding to <code>values_discrete</code> . If missing (NULL) it is set to 1 in all components as default. Can be a scalar for equal weights for all discrete values or a vector with specific weights for each corresponding discrete value.
<code>domain_continuous</code>	An interval (i.e., a vector of length 2) specifying $I$ (the subset of the domain corresponding to the continuous part of the densities). If missing (NULL) it is set to <code>c(0, 1)</code> as default. If set to <code>FALSE</code> , the continuous component is considered to be empty, i.e., a weighted sum of dirac measures is used as reference measure (discrete special case).

## Value

The function returns an object of the class `histogram_count_data`, which is a [data.table](#) with columns:

- `counts` - For each by `var_vec` defined covariate combination the observed (histogram) counts in the first column.
- `weighted_counts` - If `sample_weights` is not NULL: Weighted (histogram) counts for the respective bin/discrete value incorporating the sample weights given by `sample_weights`.
- name of variable given to `y` - Marks the mid of the respective histogram bin (for values in  $I \setminus D$ ) or the discrete value. If a mid corresponds to a discrete value, the mid is shifted to the right by 0.0001 times the minimal distance to the next interval limit OR discrete value so that no mid is exactly corresponding to a discrete value. A warning message is generated in this case.
- names of all variable columns which were specified by `var_vec` - These columns contain the values of the respective variables.
- `group_id` - ID of each covariate combination.
- `gam_weights` - Vector to be passed to argument `weights` in [gam](#) when fitting the Poisson Model, if `dta` contains sample weights, see Appendix C of Maier et al. (2023).
- `gam_offset` - Negative logarithm of `gam_weights` to be used as offset to the predictor of the Poisson Model, if `dta` contains sample weights, see Appendix C of Maier et al. (2023).
- `Delta` - Width of the histogram bin or weight of the Dirac measure for a discrete value defined by `weights_discrete`. The Poisson model uses `offset(log(Delta))` to add the necessary additive term in the predictor that includes binwidths/dirac weights into the estimation.

- discrete - Logical value indicating whether the respective y is a discrete value in  $D$ .

Note that a plot-method for objects of class `histogram_count_data` is available via `CondDensReg:::histogram_count_data_plot` however, it is not exported, since it is not tested/documentated appropriately, yet.

### Author(s)

Lea Runge, Eva-Maria Maier

### References

Maier, E.-M., Fottner, A., Stoecker, A., Okhrin, Y., & Greven, S. (2025b): Conditional density regression for individual-level data. arXiv preprint arXiv:XXXX.XXXXX.

### Examples

```
set.seed(101)

# create data where 0 and 1 are the discrete observations, values
# equal 2 are replaced below by drawing from a beta distribution

dta <- data.frame(obs_density = sample(0:2, 100, replace = TRUE,
                                     prob = c(0.15, 0.1, 0.75)),
                 covariate1 = sample(c("a", "b"), 100, replace = TRUE),
                 covariate2 = sample(c("c", "d"), 100, replace = TRUE),
                 sample_weights = runif(100, 0, 2))
dta[which(dta$obs_density == 2), ]$obs_density <- rbeta(length(which(dta$obs_density == 2)),
                                                       shape1 = 3, shape2 = 3)

# Create histogram count dataset for dta using 10 equidistant
# bins and default values for continuous domain, discrete
# values and discrete weights while considering a mixed case
# of continuous and discrete domains. The following function calls are
# equivalent:

preprocess(dta, var_vec = c("covariate1", "covariate2"), y = "obs_density",
           sample_weights = "sample_weights", bin_number = 10)
preprocess(dta, var_vec = c(2, 3), y = 1, sample_weights = 4, bin_width = 0.1)

# Use the vector bin_width to define non-equidistant bins and
# specify with values_discrete and weights_discrete discrete values
# and weights besides the default (0,1) and weight 1:

preprocess(dta, var_vec = c(2, 3), y = 1, sample_weights = 4,
           bin_width = c(0.1, 0.5, 0.4), values_discrete = c(0, 1),
           weights_discrete = c(0.5, 2))

# The use of "values_discrete=FALSE" refers to histogram data in a
# purely continous setting (note that now the observations at 0 and 1 are
# counted towards the outer bins):

preprocess(dta, var_vec = c(2, 3), y = 1, sample_weights = 4, bin_width = 0.1,
           values_discrete = FALSE)

# filter data set for only observations valued in discrete domain

dta_discrete <- dta[which(dta$obs_density %in% c(0, 1)), ]
```

```
# The use of "domain_continuous=FALSE" refers to histogram data in a
# purely discrete setting:

preprocess(dta_discrete, var_vec = c(2, 3), y = 1, sample_weights = 4,
           bin_width = 0.1, values_discrete = c(0, 1),
           weights_discrete = c(0.5, 2), domain_continuous = FALSE)

# use the optional argument counts to "preprocess" already preprocessed
# data and select only one of two variables for the grouping
dta_discrete <- unique(dta_discrete[, 1:3])
dta_discrete$counts <- sample(0:10, nrow(dta_discrete), replace = TRUE)

preprocess(dta_discrete, var_vec = "covariate1", y = "obs_density",
           counts = "counts", bin_width = 0.1, values_discrete = c(0, 1),
           weights_discrete = c(0.5, 2), domain_continuous = FALSE)
```

---

smooth.construct.md.smooth.spec

*P-Splines with integrate-to-zero constraint for density regression*

---

## Description

Specifying `bs = "md"` in the tensor product smooth `ti` (setting `mc = FALSE`) constructs a smoother to be used in `mgcv`'s `gam` with `family = poisson()` for the case that the response variable of interest is a density in a mixed Bayes Hilbert space  $B^2(\mu) = B^2(\mathcal{Y}, \mathcal{A}, \mu)$  (including continuous or discrete ones as special cases) as in Maier et al. (2025b). The subset of the domain  $\mathcal{Y}$  corresponding to the continuous part of the densities is denoted with  $I$ , the one corresponding to the discrete part with  $\mathcal{D}$ . Corresponding covariate observations are the discrete values for the discrete component and the midpoints of the bins underlying the histograms approximating the densities for the continuous component. Response observations are the counts of the discrete observations and the histograms (the count data can easily be constructed from individual data with `preprocess`). Specification of basis and penalization details for the continuous component is as for `bs = "ps"`, see `mgcv`'s `smooth.construct.ps.smooth.spec`, which our implementation is oriented on. Specification of the domain and for the discrete component is possible via the argument `xt` in `ti` (see below).

Note that the implementation includes the integrate-to-zero constraint of  $L_0^2$ , i.e., further centering is not reasonable! This means, that the constructor should not be used with `s` or `te`, which always include centering (sum-to-zero) constraints for all marginals. Instead, it is supposed to be used with `ti`, setting `mc = FALSE` for the corresponding component.

We recommend to use `link{dens_reg}` to specify density regression models (based on `smooth.construct.md.smooth.spec`), instead of via `gam` directly, since the is quite cumbersome and specification has to be done with extreme care to obtain a reasonable model.

## Usage

```
## S3 method for class 'md.smooth.spec'
smooth.construct(object, data, knots)
```



## Arguments

object	a smooth specification object, usually generated by a term <code>ti(x, bs="md", ...)</code>
data	a list containing just the data (including any by variable) required by this term, with names corresponding to <code>object\$term</code> (and <code>object\$by</code> ). The by variable is the last element.
knots	a list containing any knots supplied for basis setup — in same order and with same names as data. Can be NULL. See details for further information.

## Details

The basis and penalty are constructed from a P-spline basis (continuous component) respectively indicator functions with optional difference penalty (discrete component) transformed to  $L_0^2$  as described in Appendix D of Maier et al. (2025a) and embedded to the mixed Bayes Hilbert space as described in Section 2.2 of Maier et al. (2025b). The argument `xt` in `ti` is used for further specification regarding the underlying Bayes Hilbert space. `xt` has to be a list of the same length as the vector `bs` specifying the marginal bases. For all "md" type marginal bases, the corresponding `xt`-list element is again a list with the following elements:

- `values_discrete`: Vector of values in  $\mathcal{D}$  (the subset of the domain corresponding to the discrete part of the densities). Defaults to missing (NULL) in which case it is set to `c(0, 1)`. If set to FALSE, the discrete component is considered to be empty, i.e., the Lebesgue measure is used as reference measure (continuous special case).
- `weights_discrete`: Vector of weights for the Dirac measures corresponding to `values_discrete`. If missing (NULL) it is set to 1 in all components as default. Can be a scalar for equal weights for all discrete values or a vector with specific weights for each corresponding discrete value.
- `domain_continuous`: An interval (i.e., a vector of length 2) specifying  $I$ . If missing (NULL) it is set to `c(0, 1)` as default. If set to FALSE, the continuous component is considered to be empty, i.e., a weighted sum of dirac measures is used as reference measure (discrete special case).
- `penalty_discrete`: integer (or NULL) giving the order of differences to be used for the penalty of the discrete component, with 0 corresponding to the identity matrix as penalty matrix (analogously to `m[2]` for the continuous component); Note that the order of differences must be smaller than the number of values in the discrete component, i.e., the length of `values_discrete`; if missing (NULL), in the mixed case, it is set to a zero matrix (corresponding to no penalization), while in the discrete case, it is set to a diagonal matrix (as in a ridge penalty). In the discrete case, please set the corresponding argument of `sp` in `ti` to 0 to estimate an unpenalized model.

## Value

An object of class "mdspline.smooth". See [smooth.construct](#), for the elements that this object will contain.

## Author(s)

Eva-Maria Maier, Alexander Fottner

## References

Maier, E.-M., Fottner, A., Stoecker, A., Okhrin, Y., & Greven, S. (2025b): Conditional density regression for individual-level data. arXiv preprint arXiv:XXXX.XXXXX.

Maier, E.-M., Stoecker, A., Fitzenberger, B., Greven, S. (2025a): Additive Density-on-Scalar Regression in Bayes Hilbert Spaces with an Application to Gender Economics. *Annals of Applied Statistics*, 19(1), ???-???

## Examples

```
#### create data
set.seed(101)

N <- 100
dta <- data.frame(covariate1 = sample(c("a", "b", "c"), N, replace = TRUE),
                  covariate2 = rnorm(n = N))
dta$obs_density <- sapply(seq_len(N),
                          function(i) {
                            a_0 <- ifelse(dta$covariate1[i] == "a", 0.1,
                                           ifelse(dta$covariate1[i] == "b", 0.2, 0.3))
                            p_0 <- a_0 * sin(dta$covariate2[i]) + a_0 + 0.05
                            a_1 <- ifelse(dta$covariate1[i] == "a", 0.25,
                                           ifelse(dta$covariate1[i] == "b", 0.15, 0.05))
                            p_1 <- a_1 * cos(dta$covariate2[i]) + a_1 + 0.1
                            sample(0:2, 1, prob = c(p_0, p_1, 1 - p_0 - p_1))
                          })

dta$covariate1 <- ordered(dta$covariate1)

# data for the mixed case
dta_mixed <- dta
ind_cont <- which(dta_mixed$obs_density == 2)
dta_mixed[ind_cont, ]$obs_density <-
  sapply(seq_along(ind_cont), function(i)
    rbeta(1, shape1 = 1 + exp(dta_mixed$covariate2[i]),
          shape2 = 1 + as.numeric(dta_mixed$covariate1[i])))
n_bins <- 20
dta_mixed <- preprocess(dta = dta_mixed, var_vec = c("covariate1", "covariate2"),
                       bin_number = n_bins, values_discrete = c(0, 1),
                       domain_continuous = c(0, 1))

# data for the continuous case
dta_cont <- dta_mixed[which(!dta_mixed$discrete), ]

# data for the discrete case
dta_dis <- preprocess(dta = dta, c("covariate1", "covariate2"),
                     values_discrete = c(0, 1, 2), domain_continuous = FALSE)

#### fit model in the mixed case
# All marginals in density-direction are specified via the mixed density basis "md",
# which per default uses a mixed Bayes Hilbert space with continuous domain (0, 1)
# and discrete values at 0 and 1. Since this is exactly our scenario, we don't
# actually need to specify xt here.

m_mixed <- gam(counts ~
  # no scalar global intercept (we add a density-intercept instead)
  - 1 +
  # intercept (corresponding to reference covariate1 = "a")
  ti(obs_density, bs = "md", m = list(c(2, 2)), k = 8,
    mc = FALSE, np = FALSE) +
  # group specific intercept for leveles "b" and "c" of covariate2
```

```

    ti(obs_density, bs = "md", m = list(c(2, 2)), k = 8,
       mc = FALSE, np = FALSE, by = covariate1) +
  # smooth effect of covariate2 (modeled via P-splines)
  ti(covariate2, obs_density, bs = c("ps", "md"),
     m = list(c(2, 2), c(2, 2)), k = c(8, 8), mc = c(TRUE, FALSE),
     np = FALSE) +
  # intercepts per covariate combination (modeling absolute
  # counts for poisson regression)
  as.factor(group_id) +
  # offsets: log(Delta) accounting for bin width, gam_offsets
  # for weighted observations
  offset(log(Delta)),
  family = poisson(), method = "REML", data = dta_mixed)

### fit model in the continuous case
# Continuous domain (0, 1) without discrete values
xt_c <- list(values_discrete = FALSE, domain_continuous = c(0, 1))

m_cont <- gam(counts ~
  # no scalar global intercept (we add a density-intercept instead)
  - 1 +
  # intercept (corresponding to reference covariate1 = "a")
  ti(obs_density, bs = "md", m = list(c(2, 2)), k = 8,
     mc = FALSE, np = FALSE, xt = list(xt_c)) +
  # group specific intercept for leveles "b" and "c" of covariate2
  ti(obs_density, bs = "md", m = list(c(2, 2)), k = 8,
     mc = FALSE, np = FALSE, xt = list(xt_c), by = covariate1) +
  # smooth effect of covariate2 (modeled via P-splines)
  ti(covariate2, obs_density, bs = c("ps", "md"), m = list(c(2,2), c(2,2)),
     k = c(8, 8), mc = c(TRUE, FALSE), np = FALSE,
     xt = list(NULL, xt_c)) +
  # intercepts per covariate combination (modeling absolute
  # counts for poisson regression)
  as.factor(group_id) +
  # offsets: log(Delta) accounting for bin width, gam_offsets
  # for weighted observations
  offset(log(Delta)),
  family = poisson(), method = "REML", data = dta_cont)

### fit model in the discrete case
# Continuous domain empty, discrete values 0, 1, 2
xt_d <- list(domain_continuous = FALSE, values_discrete = c(0, 1, 2))

m_dis <- gam(counts ~
  # no scalar global intercept (we add a density-intercept instead)
  - 1 +
  # intercept (corresponding to reference covariate1 = "a")
  ti(obs_density, bs = "md", m = list(c(2, 2)), k = 8,
     mc = FALSE, np = FALSE, xt = list(xt_d), sp = 0) +
  # group specific intercept for leveles "b" and "c" of covariate2
  ti(obs_density, bs = "md", m = list(c(2, 2)), k = 8,
     mc = FALSE, np = FALSE, xt = list(xt_d), sp = 0, by = covariate1) +
  # smooth effect of covariate2 (modeled via P-splines)
  ti(covariate2, obs_density, bs = c("ps", "md"), m = list(c(2,2), c(2,2)),
     k = c(8, 8), mc = c(TRUE, FALSE), np = FALSE,
     xt = list(NULL, xt_d), sp = c(-1, 0)) +
  # intercepts per covariate combination (modeling absolute

```

```
# counts for poisson regression)
as.factor(group_id) +
# offsets: log(Delta) accounting for bin width, gam_offsets
# for weighted observations
offset(log(Delta)),
family = poisson(), method = "REML", data = dta_dis)
```

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