# Math & Mystery Chronicles

2016 US Election Analysis

Bayesian Hospital Insights

Flying Through Borealia

# The Enigmatic Anomaly

Where Clues Lead to Questions

Meet Jenny, the brilliant lead investigator on a quest to unravel the unexplained and peculiar arrival and departure delays that unfolded at US airports in 2019. Today, her relentless pursuit stands on the brink of a chilling revelation. Brace yourself for an electrifying journey as they navigate the labyrinth of this unsolved mystery.



An Investigation into Mysterious Flight Patterns by Jenny Lewis

Unravel the method behind her madness, but be warned – once you're in, there's no turning back.

# Testimonies Reveal the Unusual

By Jenny Lewis

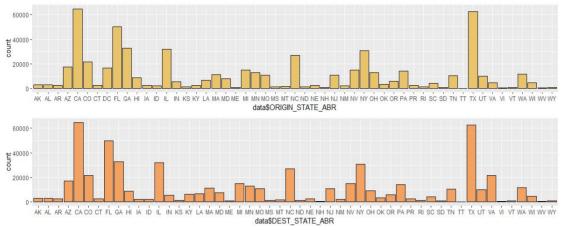
As I was handed a large amount of data on flights in the US from January of 2019, something initially seemed off to me. I began to notice some flights that had very long delays, unlike the others at the same airport. For many years, I was stumped. I could not figure out what was happening that might cause such irregular flights. I knew I had to dig deeper and get to the bottom of this sticky situation.

I started by doing a general exploration of the data by visualizing the flights to see what the patterns were (if any) and if I could find an explanation. Once I found potential exceptions to patterns, I wanted to take a closer look at a random subset of flights and investigate further into the causes. I talked to many witnesses and interrogated many suspects as I was putting all of the pieces of this puzzle together. Read along further if you're curious to see how I embarked on this adventure into the world of flying in the United States and proved that not every flight will go as expected.

# Witness 1 Speaks

Our First Witness Recalls Their Initial Encounter With the Data

"I knew something was wrong with the data"



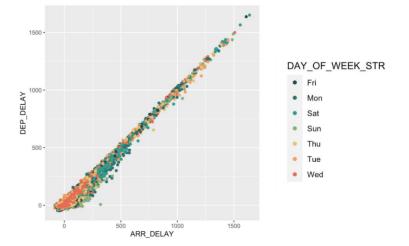
Intriguingly, the witness disclosed that the most popular origin and destination states were California, Texas, Florida, Illinois, Georgia, New York, and North Carolina. These states seemed to be the primary hubs of air travel, attracting a significant

amount of flights. On the other hand, the witness also revealed the least popular origin and destination states. Surprisingly, Hampshire, Trust Territories, Virgin Islands, West Virginia, Vermont, Wyoming, and Maine appeared fewer connections, making them less frequented

by flights. The first witness proved to be a valuable source information, shedding light crucial on insights about the US airports. They introduced two important terms: ORIGIN\_STATE\_AB R, representing the two-letter State abbreviations for the origin airports, and DEST\_STATE\_ABR, denoting the two-letter State abbreviations for the destination airports.

The ARR\_DELAY and DEP\_DELAY data revealed delays or advancements in either the arrival or departure flights, respectively. Where negative values indicate delays and positive values indicate early arrivals. The witness also shared the

DAY\_OF\_WEEK\_STR, a shortened representation of the days of the week when the flights occurred.

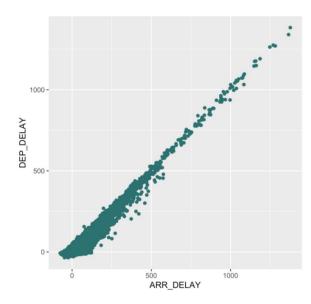


Here's where things got interesting - anomalous activities seemed to be concentrated mostly on Sundays, Mondays, and Thursdays. These particular days appeared to have a higher incidence of delays or advancements in both arrivals and departures.

# Witness 2 Exposes

Anomaly Analysis Leads to Justice

The revelations from the second witness added a new layer of intrigue to the investigation, focusing on the arrival and departure delays on specific days of the week - Monday, Sunday, and Thursday, which had been the three days previously identified as the most anomalous by witness 1. While all three days exhibited similar cluster patterns, it was their anomalies that set them apart. In general, the arrival and departure times were typically delayed by the same amount.

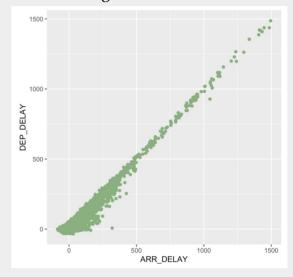


Delays of flights when travelling on Mondays.

I was informed by the witness to start with Mondays, as they believed there might be something peculiar happening. At a first glance, I noticed there were several data points that fell slightly below and out of the general pattern of the delays. In particular, there were quite a few flights with arrival delays between 200 and 600 minutes that didn't have quite as high of a departure delay as the rest of the flights. I took note of this strange behaviour that might be able to help me piece this story together further.

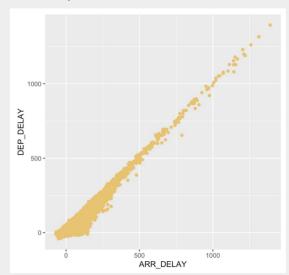
#### What's Happening on Sundays?

As we continued the investigation with witness 2 we were lead in the direction of the flights on Sundays, as it was one of the most frequent travel days, and there may be some potential outliers hiding there.



Delays of flights when travelling on Sundays

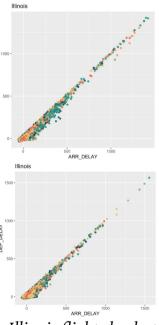
As the witness continued to provide more information, there was a slight indication that something abnormal might be happening on Mondays. As I looked at its delays, I noticed there were a few Monday flights that weren't quite following the pattern of the others, noting them down to potentially look into.



Delays of flights when travelling on Thursdays

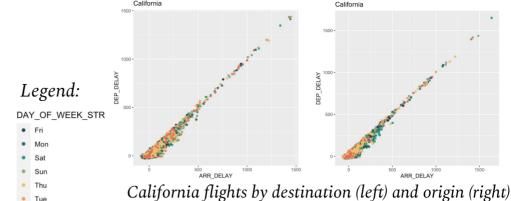
# Witness 3 Breaks Silence

With our next witness, they wanted to bring light to some possible abnormalities may have arisen from the states that have the most travellers passing through. ARR\_DELAY, Using DEP\_DELAY, DEST\_STATE\_ABR, and ORIGIN STATE ABR, the witness helped identify a few states that had many travellers with some flights looking strange.



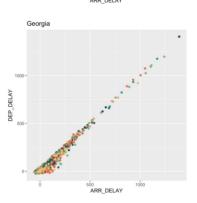
Illinois
was one of
the states
the
witness
provided
insight on
potential
outliers
that didn't
follow the
pattern.

Illinois flights by destination (top) and origin (bottom)



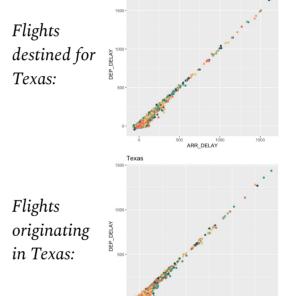
With California being the most popular state to fly into and out of, the witness recalled seeing some passengers waiting for abnormal amounts of time while travelling

there.

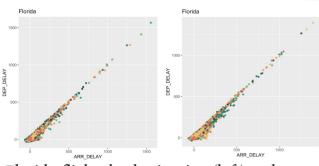


Georgia flights by destination (top) and origin (bottom)

The witness had indicated that Georgia might have a few flights that had some irregular delay times, as indicated above.



Since Texas was the second highest travelled through state, the witness identified some points that fell out of the general pattern of the delays indicating we should take note.

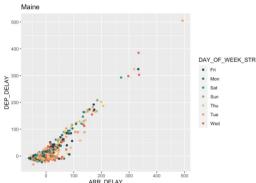


Florida flights by destination (left) and origin (right)

Although the witness provided Florida as a state with potential outliers, when I looked into the dataset I noticed most of the points for flights originating in Florida seemed to follow the general pattern of delays. That being said, when I looked into the flights destined for Florida, there were quite a few flights that fell below the others.

# Witness 4's Breakthrough

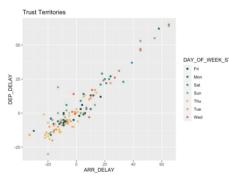
The disclosure from witness 4 led me to investigate states with the lowest number of flights. Among them were Maine, Trust Territories,

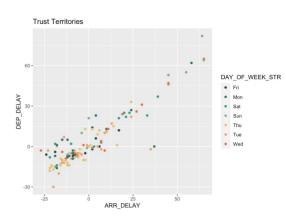


Flights originating in Maine
and New Hampshire, each exhibiting intriguing anomalies. Maine's data showed sparsity, but the

general shape of arrival and departure delays remained consistent.

Trust Territories. For originating both arrival flights displayed behavior, erratic deviating from the patterns seen before. Sparse data points and a of sufficient evidence made it challenging to establish





Flights originating in the Trust Territories

a clear relationship between arrival and departure delays. However, interestingly, Trust Territories consistently showed Thursdays with flights typically delayed by a smaller amount, observed at the bottom left of the scatter plot.

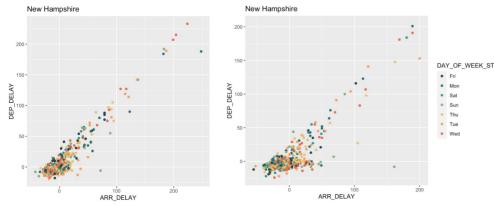
Flights destined for the Trust Territories (left)

### New Hampshire's Unusual Patterns

New Hampshire, although having more data points than Trust Territories but fewer than Maine, had

presented significant with numerous issues outliers and gaping disparities. Destined flights New to Hampshire had concentration of outliers

on Sunday, Tuesday, and Monday. On the other hand, origin flights from New Hampshire exhibited outliers on Sunday, Thursday, Wednesday, and Tuesday.



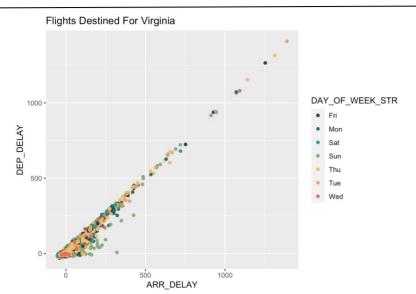
New Hampshire flights by destination (left) and origin (right)

Decoding the States, Seeking the Missing Piece

Each state's unique behavior provided valuable clues that I knew I must unravel to decipher the puzzling anomalies hidden within the flight data.

### A Crucial Lead in the Investigation

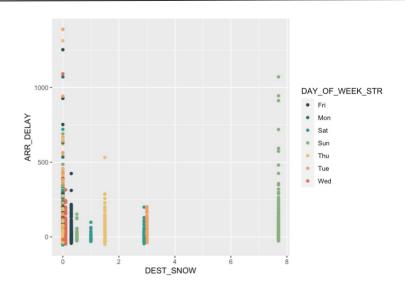
Unraveling Virginia's Flight Anomalies



After consulting the four witnesses, I set out to investigate the erratic arrival and departure delays. A vital clue emerged when I received evidence from an airport, redirecting my focus to Virginia. Discussions with Virginia airport attendees revealed that Sundays showed the most anomalies in flights destined for the state. Taking a closer look, I noticed many gaping issues possible indicating removed, lost, or unknown recorded destination flights.

intriguing An pattern emerged as I analyzed the flights destined Virginia. Up to a certain value, both arrival departure delays showed a positively correlated path. However, beyond value of "1000," I noticed a significant drop in the frequency of flights, indicating that those with larger delays were a rare occurrence. This finding added of a layer fascination to the investigation, leaving me explore the to eager behind this reasons distinctive behavior.

The airport attendees also introduced the term "DEST\_SNOW," representing the amount of snowfall in inches (in) that each state received. Interestingly, behavior confined was January, suggesting the typical assumption of weather delays. Snowfall in the region was predominantly below 1 inch. However, what caught my attention were the gaps where seemed to recorded snow of 4-6 inches.



Indeed, further investigation revealed that Sundays experienced the highest snowfall. This correlation between snowfall and irregular flight delays provided a compelling lead to follow.

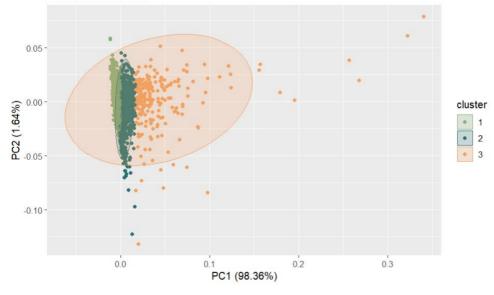
Coming Up Next: How I used a smaller subset to pinpoint the outliers.

### **PCA**

The first suspect identified

Patrick C. Adams (PCA), a prime suspect in the case, has been linked to the irregular behavior observed at the US airports in 2019. The pressing question that lingers whether Patrick C. Adams alone, there acted or was someone else involved in his stealthy activities?

Patrick exposed three distinct clusters in the data. Cluster 1 flight formed a scattered line slightly pointing while Cluster 2 displayed points in a straight line. Cluster 3, on the other hand, had scattered points spread across the plot. Additionally, it was revealed that PC1 (Principal Component 1)



Principal Component Analysis (PCA) clustered scatter plot

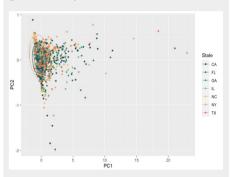
represented the overall departure delay, while PC2 (Principal Component symbolized the arrival delay of flights U.S. airports. at Remarkably, PC1 alone 98.36% explained of the variation in the flight data. During the investigation, Patrick confessed deliberately crafting certain points within the clusters identified by their X values.

# Patrick Confessed to Crafting Outliers

Confessed Outliers: 93182, 477922, 259286, 467791, 42767, 479941, 312513, 381994, 451093, 259423, 270720, 352242, 382028, 46425, 93004.

#### Algorithm Triumph!

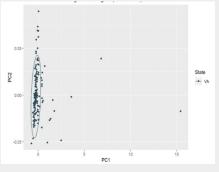
As I dug into the flight data, I noticed striking outliers from prominent destination states like California, Florida, Texas, and Georgia - precisely the



PCA - Largest Origin States states that the third witness had mentioned were the most frequent on the list.

#### Chasing the Clues

My curiosity led me to focus on Virginia, one of the largest destination states. As suspected, there were indeed numerous outliers among the destination flights for Virginia.

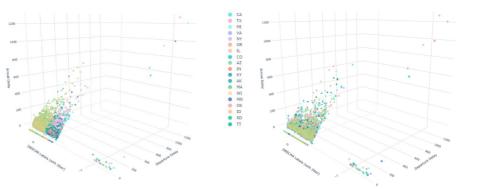


PCA - Virgina Destination

#### **DBSCAN**

The second suspects brought in for questioning

The suspects I brought in were Debs & Candie, also DBSCAN. known as dvnamic duo known for (density based spatial clustering of applications of noise) looks at clusters within the dataset identified potentially possible outliers. Debs and Candie provided me with the DEST STATE ABR (destination abbreviation), ORIGIN STATE ABR (origin state abbreviation),



detecting outliers. DBSCAN with flight delays by destination (left) and origin (right) states.

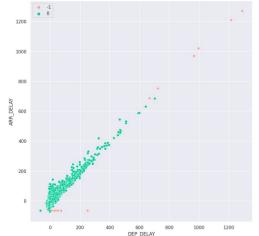
DEP\_DELAY (departure delay), and ARR\_DELAY (arrival delay).

Where Are These Potential Outliers Coming From?

state I asked Debs and Candie where all the these flights were coming from and on), going to and asked them to provide us with graphs that

(departure show potential outliers. If Debs or Candie provided us with a flight labelled as "-1". we had a strong indication that the flight was a potential outlier. All other flights were labelled as "0" and were not believe have any anomalous behaviours. Many of the potential outliers strayed far from the other flights and significantly higher had

### Outliers Debs & Candie Confessed To and Their Delays



Confessed outliers (pink) and non-outliers (green) from Debs & Candie

After interrogating Debs and Candie, we looked at flights and their our delays. I investigated the behaviour of all of the flights in the data and those separated that Debs and Candie confessed to from the From confession, I were able to the identify possible outliers, with many of them not following the general pattern of the flight delays.

### <del>delays.</del>

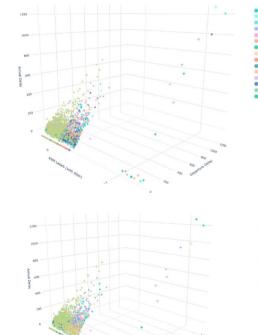
# They Confessed to Many Outliers!

490158,	259286,	282050,
113891,	473726,	250208,
42767,	219580,	239692,
477922,	93182,	259372,
417185,	449318,	210546,
469875,	54463,	354955,
529616,	479941,	467791,
544652,	469356,	171352,
256452,	228490,	526012,
82692,	11902,	501614,
492652,	121347,	77196,
240		

#### **KNN**

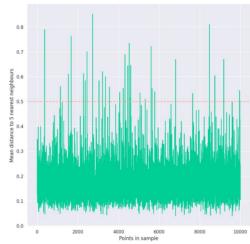
Our Third Suspected Individual

The next suspect interviewed Kevin was Noah Newman, an expert the K-Nearest in Neighbours algorithm (KNN), who grouped flights together based on different characteristics and classifications. Kevin was the second suspect interviewed who had background in using clusters to analyse data and find potential outliers. The two of used us ARR DELAY (arrival delay) and DEP DELAY (departure delay) in our clusters.



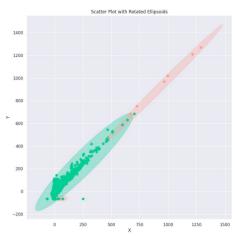
KNN by destination (top) and origin (bottom) state

Kevin produced two graphs with his initial findings, one based on DEST STATE ABR (destination state abbreviation) and one based on ORIGIN STATE ABR (origin state abbreviation), where those labelled as "-1" were found to be potential outliers. those labelled as "0" were not.



Mean distance to 5 nearest neighbours

Kevin chose K = 5 for his clustering, and provided me with the mean distance to 5 neighbours. The nearest points above the pink line were found to be outliers, and those below were not. I found that most of the data fell below the 0.5 line, with only about 30 points rising above it. Those 30 points classified as were not following the pattern of flight delays as the rest.



Scatter plot with rotated ellipsoids

Kevin provided me with some very insight data by different showing me clusters, or neighbourhoods, of datapoints. The points that are in pink have been identified as potential outliers, whereas the points that are green were not. There were two clusters potential that contained outliers, those with high delays and those with very low delays.

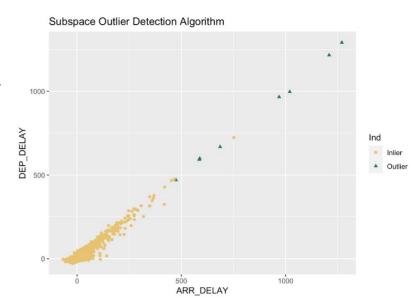
# Outliers Kevin Confessed To!

	<i>J</i>	
259286,	282050,	113891,
473726,	42767,	239692,
477922,	93182,	259372,
417185,	449318,	381994,
337032,	354955,	529616,
479941,	467791,	268199,
544652,	171352,	256452,
228490,	266925,	262613,
82692,	502920,	501614,
121347,	77196,	454429,
92801		

#### SOD

#### The Fourth and Final Suspect

The final suspect I interviewed was Sarah Oliver-Davids, also known SOD. She was linked to many irregularities in the US flights January of 2019. Now that the three other identified suspects have provided me with incredibly useful information, I want to ask the final suspect what she may know about these irregular flights. When talking with Sarah about them, I about the DEP DELAY asked her (departure delay), ARR\_DELAY (arrival delay), and X values that were uniquely associated to each flight in the dataset. SOD (subspace outlier detection) help use my subset to look at potential outliers in the delayed flights.



Throughout Sarah's interrogation, we were able to pinpoint 10 anomalous flights and identified them by their unique X values. Sarah confessed to the following outliers:

259286,	467279,	527628,	381994,
42767,	477922,	467791,	312513,
93182,	467358		

### The Verdict: Guilty

Case Closed - Joint Efforts to Individual Actions

	230	11902	28250	12	647	54463	77196	82692	92801	10000	3	93182	113891	121347	7135	133	1054	13	219580	228490	0000	2000	2020	256452	259286	259372	5047		979	266952	268199	270720	282050	312513	227022	5076	5224	354955	381994	382028	718	102	1001	451093	454429	467279	467358	201104	469356	469875	473726	477922	44	490158	492652	501614	502920	526012	527628	1 3	2961	544652
DBSCAN					П									Г							Т					Г		Т	$\neg$						Т	$\Box$				Г							Т															
KNN																					Т																										Т															
PCA																					Т																					Т					Т					Į.										
SOD																										9					,										, .																					

It seems that a few outliers, specifically #42767, #93182, #259286, #467791, and #477922, stood out as instances where all four suspects collaborated, highlighted in green. These are the outliers that I can confirm since they were consistently identified by multiple accomplices. There were additional outliers that were associated with the involvement of three suspects.

For example, #381994 was identified by PCA, SOD, and KNN, while #479941 was identified by DBSCAN, KNN, and PCA. Furthermore, there were other potential outliers where two suspects collaborated, or where a suspect acted alone, which makes these outliers remain as *potential* anomalies.

