Methods Comparison

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Introduction

This vignette provides a comparison of the 12 variables selected by the 3 methods: coda_logistic_lasso, clr+logistic_lasso, selbal.

First, let us install and load the packages.

1.1 Packages installation and loading

```
#cran.packages = c('knitr', 'MASS', 'VennDiagram', 'gplots', 'glmnet')
#install.packages(cran.packages)
#devtools::install_github(repo = "UVic-omics/selbal")

library(knitr)
library(MASS)
library(VennDiagram)
library(gplots)
library(glmnet)
library(selbal)
```

1.2 Simulations

The way we simulate datasets.

1.3 Example datasets

We have two case studies.

1.3.1 Crohn disease data

```
load("./datasets/Crohn_data.rda")
dim(x_Crohn)
```

[1] 975 48



The Crohn data have 975 samples and 48 taxa.

summary(y_Crohn)

CD no ## 662 313

Among 975 samples, 662 samples are labeled as 'CD', the other 313 are labeled as 'no'.

Methods implementation

2.1 LOGISTIC LASSO

```
With linear constraint: \sum \beta_j = 0 (for j > 1)
# y: dependent variable, binary, vector of length n
# X: matrix of k covarites (positive values, taxa abundances in counts, proportions, intensities, ...),
coda_logistic_lasso<-function(y,X,lambda, maxiter=400, maxiter2=50, r=10,</pre>
                                tol=1.e-4, tol2=1.e-6){
  #install.packages("MASS")
 library(MASS)
                 # for the computation of the generalized inverse ginv()
# library(tictoc)
  if (!is.numeric(y)){
    y < -as.numeric(y) - 1
  #source("functions_coda_logistic_lasso.R")
  # Transform initial data
  ztransformation(X)
  #initial values for beta
  # p<<-ncol(X) # p: number of covariates after filtering</pre>
  {\it \# n<<-nrow(X); \# both \ defined \ on \ ztransformation \ function}
  \#beta\_ini \leftarrow rep(1,p+1)/(p+1) \# uniform values
  beta_ini<-c(\log(mean(y)/(1-mean(y))), rep(1/p,p)) # b0 related to mean(y) and uniform values for the
 #null deviance
 nulldev<-glm(y~1, family=binomial())[[10]]</pre>
  #initialization parameters
  k<-1
  epsilon<-0.1
```



```
beta_ant<-beta_ini
beta<-beta_ant
y_ant<-beta_ant
y_k<-y_ant
d_k<-y_ant
dev_explained_ant<-0
# Optimization with constraint
start_iter = Sys.time();
while((abs(epsilon)>tol)&(k<=maxiter)){</pre>
      #print(append("loop",k))
           k0<-0
           t k < -10
           condition<-0.1
           while ((condition>0)&(k0<=maxiter2)){</pre>
                 k0 < -k0 + 1
                 #print(append("k0",k0))
                 d_k<-y_ant-t_k*grad_g(y_ant, z, y, n)</pre>
                 # Soft thresholding:
                 zproxi<-c(d_k[1],soft_thres(d_k[-1],lambda*t_k))</pre>
                 # Projection:
                 zproj<-projection(zproxi,p_c)</pre>
                 # line search condition
                 Gt<-(y_ant-zproj)/t_k</pre>
                 condition < -g(y_ant-t_k*Gt,z, y, n) - g(y_ant,z, y, n) + t_k*t(grad_g(y_ant,z, y, n)) %*%Gt-t_k/2*normalised for the state of the st
                 #print(append("condition", condition))
                 \#print(append("t_k", t_k))
                 t_k<-t_k/2
            beta<-zproj
           y_k<-beta+(k-1)/(k+r-1)*(beta-beta_ant)
            dev_explained<-1-(nrow(X)*2*g(beta,z, y, n)/nulldev)</pre>
            epsilon<-abs(dev_explained-dev_explained_ant)</pre>
           y_ant<-y_k
           beta_ant<-beta
           dev_explained_ant<-dev_explained
           k < -k + 1
#print(append("epsilon",epsilon))
end_iter = Sys.time();
sprintf("iter time = %f",end_iter-start_iter)
#Projection of the optimal beta to fulfil the constraint sum(beta[j])=0, for j>1
```



```
indx<-which(abs(zproxi)>tol2)
  if (abs(zproxi[1])>0) indx<-indx[-1]</pre>
  c0<-rep(1,(length(indx)))</pre>
  c0<-c0/sqrt(normSqr(c0))
  p_c0<-c0%*%t(c0)
  #beta1<-as.numeric(projection(beta[indx],p_c0))</pre>
  beta1<-projection(beta[indx],p_c0)</pre>
  beta_res<-c(beta[1],rep(0,p))</pre>
  beta res[indx] <-beta1
  # print("beta coefficients:")
  # beta_res
  #print("taxa with non-zero coeff:")
  # selec<-colnames(z)[abs(beta res)>0]
  #print("beta non-zero coefficients:")
  # beta_res[abs(beta_res)>0]
  #print("proportion of explained deviance")
  # dev_explained
  #print("proportion of explained deviance beta_res")
  dev_explained_beta_res<-1-(nrow(X)*2*g(beta_res,z, y, n)/nulldev)</pre>
  # dev_explained_beta_res
  results<-list(
     "number of iterations"=k,
       "number of selected taxa"=
         sum(abs(beta_res)>0)-1,
       "indices of taxa with non-zero coeff"=
       which(abs(beta_res)>0)-1,
       "taxa with non-zero coeff"=
       colnames(z)[abs(beta_res)>0],
       "beta non-zero coefficients"=
       beta_res[abs(beta_res)>0],
       "proportion of explained deviance"=
       dev_explained_beta_res,
     "betas"=
     beta_res)
  return(results)
} # END function coda logistic lasso
```

2.2 LOGISTIC ELASTIC NET

##-----



```
coda_logistic_elasticNet<-function(y,X,lambda, alpha=0.5, maxiter=1000, maxiter2=50, r=10,
                                      tol=1.e-4, tol2=1.e-6){
  #install.packages("MASS")
 library (MASS) # for the computation of the generalized inverse ginu()
# library(tictoc)
# source("functions_coda_logistic_lasso.R")
  # Transform initial data
  ztransformation(X)
  #initial values for beta
  \#beta\_ini \leftarrow rep(1,p+1)/(p+1) \# uniform values
  beta_ini<-c(log(mean(y)/(1-mean(y))),rep(1/p,p)) # b0 related to mean(y) and uniform values for the
  #null deviance
  nulldev<-glm(y~1, family=binomial())[[10]]</pre>
  \#initialization\ parameters
  k<-1
  epsilon<-0.1
  beta_ant<-beta_ini
  beta<-beta ant
  y_ant<-beta_ant
  y_k<-y_ant
  d_k<-y_ant
  dev_explained_ant<-0
  # elastic parameters
  lambda=alpha*lambda;
  gamma=2*(1-alpha)/alpha;
  # Optimization with constraint
  start_iter = Sys.time()
  while((abs(epsilon)>tol)&(k<=maxiter)){</pre>
    #print(append("loop",k))
    k0<-0
    t_k<-10
    condition<-0.1
    while ((condition>0)&(k0<=maxiter2)){</pre>
      k0 < -k0 + 1
      #print(append("k0",k0))
      d_k<-y_ant-t_k*grad_g(y_ant, z, y, n)</pre>
      # Soft thresholding:
       \begin{tabular}{ll} \# zproxi <-c (d_k[1], soft\_thres(d_k[-1], lambda*t\_k)) \\ \end{tabular} 
      # zproxi = zproxi/(1+gamma*lambda);
```



```
zproxi < -c(d_k[1], soft_thres(d_k[-1], lambda*t_k)/(1+gamma*lambda*t_k))
           # Projection:
           zproj<-projection(zproxi,p_c)</pre>
           # line search condition
          Gt<-(y_ant-zproj)/t_k
           condition < -g(y_ant-t_k*Gt,z, y, n) - g(y_ant,z, y, n) + t_k*t(grad_g(y_ant,z, y, n))%*%Gt-t_k/2*normStart(y, y, n)) + t_k*t(grad_g(y_ant,z, y, n))%*%Gt-t_k/2*normStart(y, y, n)) + t_k*t(grad_g(y_ant,z, y, n)) + t_k*t(grad_
           #print(append("condition", condition))
           \#print(append("t_k", t_k))
          t_k<-t_k/2
     }
     beta<-zproj
     y_k \leftarrow beta+(k-1)/(k+r-1)*(beta-beta_ant)
     dev_explained<-1-(nrow(X)*2*g(beta,z, y, n)/nulldev)</pre>
     epsilon <- abs (dev_explained-dev_explained_ant)
     y_ant<-y_k
     beta_ant<-beta
     dev_explained_ant<-dev_explained
     k < -k + 1
     #print(append("epsilon", epsilon))
end_iter = Sys.time()
sprintf("iter time = %f",end_iter - start_iter)
#Projection of the optimal beta to fulfil the constraint sum(beta[j])=0, for j>1
indx<-which(abs(zproxi)>tol2)
if (abs(zproxi[1])>0) indx<-indx[-1]</pre>
c0<-rep(1,(length(indx)))</pre>
c0<-c0/sqrt(normSqr(c0))
p_c0<-c0%*%t(c0)
#beta1<-as.numeric(projection(beta[indx],p_c0))</pre>
beta1<-projection(beta[indx],p_c0)</pre>
#beta1
beta_res<-c(beta[1],rep(0,p))</pre>
beta_res[indx] <-beta1</pre>
#print("beta coefficients:")
# beta_res
#print("taxa with non-zero coeff:")
# selec<-colnames(z)[abs(beta_res)>0]
#return(selec)
```



```
#print("beta non-zero coefficients:")
  # beta_res[abs(beta_res)>0]
  #print("proportion of explained deviance")
  # dev_explained
  #print("proportion of explained deviance beta_res")
  dev_explained_beta_res<-1-(nrow(X)*2*g(beta_res,z, y, n)/nulldev)</pre>
  # dev_explained_beta_res
  results <-list("number of iterations"=k,
                "number of selected taxa"=
                  sum(abs(beta res)>0)-1,
                "indices of taxa with non-zero coeff"=
                  which(abs(beta res)>0)-1,
                "name of taxa with non-zero coeff"=
                  colnames(z)[abs(beta_res)>0],
                "beta non-zero coefficients"=
                 beta_res[abs(beta_res)>0],
                "proportion of explained deviance"=
                  dev_explained_beta_res,
                "betas"=
                  beta_res)
 return(results)
} # END function coda_logistic_ElasticNet
```

2.3 rangLambda

It provides a rang of lambda values corresponding to a given number of variables to be selected (numVar).

The default initial lambda is lambdaIni=1.

```
##-----
rangLambda <- function(y,X,numVar, lambdaIni =1){</pre>
 lambdaB = lambdaIni;
 lambdaA = 0;
 #lambda=0.5*(lambdaB+lambdaA);
 lambda=lambdaIni;
 results <- coda_logistic_lasso(y,X,lambda, maxiter = 100);
 numVarAct = results[[2]];
 if (numVarAct > numVar){
   lambda=lambda+0.5;
   #lambda=lambda+1;
   lambdaB =lambda;
 }else{
   lambdaB =lambda;
 nIter=1;
 presentLambda = NULL;
```



```
presentnumVar = NULL;
presentLambda[nIter] = lambda;
presentnumVar[nIter] = numVarAct;
numvarA=ncol(X);
numvarB=numVarAct;
print(c(lambdaA, lambdaB, numvarA, numvarB))
diffNvar = abs(numvarB-numvarA);
while ((diffNvar>1) & (abs(numVarAct-numVar)>0) & (nIter < 6)){</pre>
 nIter=nIter+1;
 lambda=0.5*(lambdaB+lambdaA);
 results <- coda_logistic_lasso(y,X,lambda, maxiter = 100);</pre>
 numVarAct = results[[2]];
 if (numVarAct < numVar) {</pre>
    lambdaB = lambda;
   numvarB = numVarAct;
 }else{
    lambdaA = lambda;
    numvarA = numVarAct;
 presentLambda[nIter] = lambda;
 presentnumVar[nIter] = numVarAct;
 diffNvar = abs(numvarB-numvarA);
 print(c(lambdaA, lambdaB, numvarA, numvarB))
indx=which(presentnumVar >= 0);
results = list( 'rang lambdas'=c(lambdaA,lambdaB), 'num selected variables'=c(numvarA,numvarB))
return(results);
```

2.4 Soft thresholding

http://www.simonlucey.com/soft-thresholding/

```
soft_thres<-function(b, lambda){
    x<-rep(0,length(b))
    # Set the threshold
    th = lambda/2;

#First find elements that are larger than the threshold
    k <- which(b > th)
    x[k] <- b[k] - th

# Next find elements that are less than abs
    k <-which(abs(b) <= th)
    x[k] <- 0

# Finally find elements that are less than -th
    k <-which(b < -th)
    x[k] = b[k] + th

return(x)
}</pre>
```



2.5 Other functions

```
norm1<-function(x){</pre>
  return(sum(abs(x)))
normSqr<-function(x){</pre>
  return(sum(x^2))
}
ztransformation<-function(X){</pre>
  p << -ncol(X)
                # p: number of covariates after filtering
  n << -nrow(X);
  # log transformation Z=log(X)
  z < -log(X)
  # z=matrix of covariates: add a first column of 1's for beta0
  z<-cbind(rep(1,nrow(z)),z)</pre>
  z<-as.matrix(z)</pre>
  # c=linear constraint sum(betas)=0 (except beta0)
  <-c(0,rep(1,ncol(X)))
  c<-c/sqrt(sum(c^2))</pre>
  c<-as.matrix(c)</pre>
  p_c<<-c\*\t(c)
  # z transformation (centering) for improvement of optimization
  # this transformation does not affect the estimation since the linear predictor is the same
  z << -(z-(z\%*\%p_c))
  colnames(z)<<-c("beta0",colnames(X))</pre>
  return(z)
}
A<-function(x){
  y < -log(1 + exp(x))
  return(y)
}
mu_beta<-function(x, Z){</pre>
  zetabybeta<-Z\*\x
  res<-rep(1,length(zetabybeta))
  indzb<-which(zetabybeta<=100)</pre>
  res[indzb]<-exp(zetabybeta[indzb])/(1+exp(zetabybeta[indzb]))</pre>
  return(res)
}
g<-function(x,Z,Y,n){</pre>
```



```
res<- (t(Y))%*%Z%*%x
  res<-res-sum(log(1+exp(Z_{*}x)))
 res<- as.vector((-res)/n)
 return(res)
h<-function(x, lambda){</pre>
  lambda*norm1(x)
grad_g<-function(x, Z, Y, n){</pre>
 res<- (t(Y-mu_beta(x,Z)))%*%Z
 res<- as.vector((-res)/n)
 return(res)
}
# Projection
projection<-function(x, M){</pre>
  if (ncol(M)*nrow(M)>0){
    res<-x-ginv(M)%*%M%*%x
  } else {res<-rep(0,length(x))}</pre>
  return(res)
}
F<-function(x,t_k,d_k){</pre>
  lambda*t_k*norm1(x[-1])+normSqr(d_k-x)/2
}
F2<-function(x,Z,Y,n,lambda){
  g(x,Z,Y,n)+lambda*norm1(x[-1])
trapezInteg <- function(x,y) {</pre>
# Compute AUC using trapezoid numerical method
 n = length(x);
  sumArea = 0;
  for (i in 1:(n-1)){
    h=x[i+1]-x[i];
    if (abs(h) > 1.e-7){
      sumArea = sumArea + 0.5*(y[i+1]+y[i])*h;
    }else{
      sumArea = sumArea;
    }
  }
  return(sumArea)
```





CODA_LOGISTIC_LASSO

3.1 Crohn disease data

```
y<-y_Crohn
summary(y)

## CD no
## 662 313

y is the binary outcome, can be numerical (values 0 and 1), factor (2 levels) or categorical (2 categories)
x<-x_Crohn
```

x is the matrix of microbiome abundances, either absolute abundances (counts) or relative abundances (proportions);

x should not be the matrix of log(counts) or log(proportions). The method itself performs the log-transformation of the abundances.

```
dim(x)
## [1] 975 48
```

The rows of x are individuals/samples, the columns are taxa

```
rangLambda(y,x,numVar=12, lambdaIni =0.15)
```

```
## [1] 0.00 0.65 48.00 17.00
## [1] 0.000 0.325 48.000 2.000
## [1] 0.1625 0.3250 12.0000 2.0000
## $`rang lambdas`
## [1] 0.1625 0.3250
##
## $`num selected variables`
## [1] 12 2
```

It provides a rang of lambda values corresponding to a given number of variables to be selected (numVar).

The default initial lambda is lambdaIni=1.

```
results_codalasso<-coda_logistic_lasso(y,x,lambda=0.19)
```

lambda is the penalization parameter: the larger the value of lambda the fewer number of variables will be selected.



```
results_codalasso
## $`number of iterations`
## [1] 23
##
## $`number of selected taxa`
## [1] 11
## $`indices of taxa with non-zero coeff`
 [1] 0 2 5 9 19 27 31 32 33 39 40 48
##
## $`taxa with non-zero coeff`
## [1] "beta0"
                          "g__Parabacteroides"
 [3] "f_Peptostreptococcaceae_g_" "g_Eggerthella"
## [5] "g__Dialister"
                          "o_Lactobacillales_g__"
## [7] "g__Prevotella"
                          "g__Roseburia"
## [9] "g__Lachnospira"
                          "g__Streptococcus"
## [11] "g__Aggregatibacter"
                          "g__Bilophila"
##
## $`beta non-zero coefficients`
## [1] -1.0023255478 -0.0057464016 0.0202907034 -0.0184875313 -0.0992393846
## [6] -0.0159418386 -0.0030842274 0.2530005235 -0.0085670215 -0.0818265310
## [11] -0.0406982632 0.0002999724
## $`proportion of explained deviance`
## [1] 0.1542276
##
## $betas
## [26] 0.0000000000 0.000000000 -0.0159418386 0.0000000000 0.0000000000
## [31] 0.000000000 -0.0030842274 0.2530005235 -0.0085670215 0.0000000000
## [46] 0.000000000 0.000000000 0.000000000 0.0002999724
selected_codalasso<-results_codalasso[[4]][-1]
columns_selected_codalasso<-results_codalasso[[3]][-1]</pre>
#coef<-results[[5]][-1]
write.csv(data.frame(columns_selected_codalasso, selected_codalasso), "./Generated_datasets/results_codal
```



CLR_LOGISTIC_LASSO

4.1 Crohn disease data

```
y<-y_Crohn_numeric
```

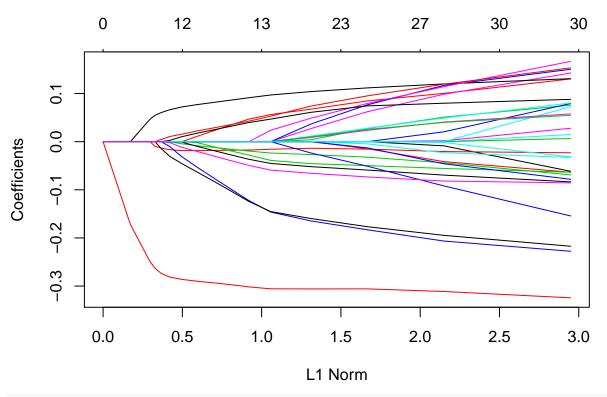
glmnet() requires y to be numeric.

```
x<-as.matrix(x_Crohn)

# CLR transformation Z=log(x)
z<-log(x)
clrx<- apply(z,2,function (x) x-rowMeans(z))
#rowMeans(clrx)

clrlasso <- glmnet(clrx, y, standardize=FALSE , alpha=1,family="binomial", lambda=seq(0.015,2,0.01))
plot(clrlasso)</pre>
```





print(clrlasso)

```
## Call: glmnet(x = clrx, y = y, family = "binomial", alpha = 1, lambda = seq(0.015,
                                                                                            2, 0.01), st
##
                  %Dev Lambda
##
          Df
##
          0 1.769e-15 1.995
     [1,]
##
     [2,]
          0 1.769e-15 1.985
     [3,]
          0 1.769e-15 1.975
##
##
     [4,]
          0 1.769e-15
                       1.965
##
     [5,]
          0 1.769e-15
                       1.955
     [6,]
           0 1.769e-15
##
                        1.945
          0 1.769e-15
##
     [7,]
                       1.935
     [8,]
          0 1.769e-15
##
                       1.925
##
     [9,]
           0 7.783e-15 1.915
          0 1.769e-15
##
    [10,]
                       1.905
##
    [11,]
          0 1.769e-15 1.895
##
    [12,]
          0 1.769e-15
                       1.885
    [13,]
           0 1.769e-15
                       1.875
##
    [14,]
          0 1.769e-15
                        1.865
##
##
   [15,]
          0 1.769e-15
                       1.855
##
    [16,]
           0 1.769e-15
                       1.845
##
    [17,]
           0 1.769e-15
                       1.835
##
    [18,]
          0 1.769e-15
                       1.825
          0 1.769e-15
                       1.815
##
   [19,]
          0 1.769e-15
                       1.805
##
   [20,]
    [21,]
           0 7.783e-15
                       1.795
##
##
    [22,]
          0 1.769e-15
                       1.785
##
    [23,]
           0 1.769e-15 1.775
##
   [24,] 0 1.769e-15 1.765
```



```
[25,] 0 1.769e-15 1.755
          0 1.769e-15 1.745
##
   [26,]
##
   [27,]
          0 1.769e-15 1.735
##
   [28,]
          0 1.769e-15 1.725
##
   [29,]
          0 1.769e-15 1.715
##
   [30,]
          0 1.769e-15 1.705
          0 1.769e-15 1.695
##
   [31,]
##
   [32,]
          0 1.769e-15 1.685
##
   [33,]
          0 7.783e-15
                      1.675
          0 1.769e-15 1.665
##
   [34,]
##
   [35,]
          0 1.769e-15 1.655
##
   [36,]
          0 1.769e-15 1.645
##
   [37,]
          0 1.769e-15 1.635
##
   [38,]
          0 1.769e-15 1.625
##
   [39,]
          0 1.769e-15 1.615
##
   [40,]
          0 1.769e-15
                      1.605
##
   [41,]
          0 1.769e-15
                      1.595
          0 1.769e-15 1.585
##
   [42,]
          0 1.769e-15 1.575
##
   [43,]
##
   [44,]
          0 1.769e-15 1.565
##
   [45,]
          0 7.783e-15 1.555
##
   [46,]
          0 1.769e-15 1.545
##
   [47,]
          0 1.769e-15 1.535
          0 1.769e-15 1.525
##
   [48,]
##
   [49,]
          0 1.769e-15 1.515
##
   [50,]
          0 1.769e-15 1.505
##
   [51,]
          0 1.769e-15 1.495
##
    [52,]
          0 1.769e-15 1.485
##
   [53,]
          0 1.769e-15 1.475
##
   [54,]
          0 1.769e-15
                      1.465
   [55,]
          0 1.769e-15
##
                      1.455
##
   [56,]
          0 1.769e-15
                       1.445
##
          0 7.783e-15
                      1.435
   [57,]
          0 1.769e-15 1.425
##
   [58,]
          0 1.769e-15 1.415
##
   [59,]
          0 1.769e-15 1.405
##
   [60,]
##
   [61,]
          0 1.769e-15 1.395
##
   [62,]
          0 1.769e-15 1.385
##
   [63,]
          0 1.769e-15 1.375
##
   [64,]
          0 1.769e-15 1.365
##
   [65,]
          0 1.769e-15 1.355
##
   [66,]
          0 1.769e-15 1.345
##
    [67,]
          0 1.769e-15 1.335
##
   [68,]
          0 1.769e-15 1.325
##
   [69,]
          0 7.783e-15 1.315
   [70,]
          0 1.769e-15
                      1.305
##
##
    [71,]
          0 1.769e-15
                       1.295
          0 1.769e-15
##
   [72,]
                      1.285
##
   [73,]
          0 1.769e-15 1.275
##
   [74,]
          0 1.769e-15 1.265
##
   [75,]
         0 1.769e-15 1.255
##
   [76,] 0 1.769e-15 1.245
   [77,] 0 1.769e-15 1.235
##
   [78,] 0 1.769e-15 1.225
```



```
[79,] 0 1.769e-15 1.215
##
   [80,]
          0 1.769e-15 1.205
##
   [81,]
          0 7.783e-15 1.195
##
   [82,]
          0 1.769e-15 1.185
##
   [83,]
          0 1.769e-15 1.175
##
   [84,]
          0 1.769e-15 1.165
##
   [85,]
          0 1.769e-15 1.155
##
   [86,]
          0 1.769e-15 1.145
##
   [87,]
          0 1.769e-15
                      1.135
##
   [88,]
         0 1.769e-15 1.125
##
   [89,]
          0 1.769e-15 1.115
##
   [90,]
          0 1.769e-15 1.105
   [91,]
          0 1.769e-15 1.095
##
##
   [92,]
          0 1.769e-15
                      1.085
##
   [93,]
          0 7.783e-15 1.075
##
   [94,]
          0 1.769e-15
                      1.065
##
   [95,]
          0 1.769e-15
                      1.055
##
   [96,]
          0 1.769e-15 1.045
##
   [97,]
          0 1.769e-15 1.035
##
   [98,]
          0 1.769e-15 1.025
##
   [99,]
          0 1.769e-15 1.015
## [100,]
          0 1.769e-15 1.005
## [101,]
          0 1.769e-15 0.995
## [102,]
          0 1.769e-15
                       0.985
## [103,]
         0 1.769e-15 0.975
## [104,]
          0 1.769e-15 0.965
## [105,]
          0 7.783e-15 0.955
## [106,]
          0 1.769e-15
                       0.945
## [107,]
          0 1.769e-15 0.935
## [108,]
          0 1.769e-15
                       0.925
## [109,]
          0 1.769e-15
                       0.915
## [110,]
          0 1.769e-15
                       0.905
## [111,]
          0 1.769e-15
                      0.895
## [112,]
          0 1.769e-15
                       0.885
## [113,]
          0 1.769e-15
                       0.875
## [114,]
          0 1.769e-15
                       0.865
## [115,]
          0 1.769e-15
                       0.855
## [116,]
          0 1.769e-15
                       0.845
## [117,]
          0 7.783e-15
                       0.835
## [118,]
          0 1.769e-15 0.825
## [119,]
          0 1.769e-15 0.815
## [120,]
          0 1.769e-15 0.805
## [121,]
          0 1.769e-15
                       0.795
## [122,]
          0 1.769e-15 0.785
## [123,]
          0 1.769e-15
                       0.775
## [124,]
          0 1.769e-15
                       0.765
## [125,]
          0 1.769e-15
                       0.755
## [126,]
          0 1.769e-15
                       0.745
## [127,]
          0 1.769e-15
                       0.735
## [128,]
          0 1.769e-15
                       0.725
## [129,]
          0 7.783e-15
                       0.715
## [130,]
          0 1.769e-15
                       0.705
## [131,]
         0 1.769e-15
                       0.695
## [132,] 0 1.769e-15 0.685
```



```
## [133,] 0 1.769e-15 0.675
## [134,] 0 1.769e-15 0.665
## [135,]
          0 1.769e-15 0.655
## [136,]
          0 1.769e-15 0.645
## [137,]
          0 1.769e-15
                       0.635
## [138,]
          0 1.769e-15 0.625
## [139,]
          0 1.769e-15
                      0.615
## [140,]
          0 1.769e-15
                       0.605
## [141,]
          0 7.783e-15
                       0.595
## [142,]
          0 1.769e-15 0.585
## [143,]
          0 1.769e-15 0.575
## [144,]
          0 1.769e-15 0.565
## [145,]
          0 1.769e-15
                       0.555
## [146,]
          0 1.769e-15
                      0.545
## [147,]
          0 1.769e-15
                       0.535
## [148,]
          0 1.769e-15
                       0.525
## [149,]
          0 1.769e-15
                       0.515
## [150,]
          0 1.769e-15
                      0.505
## [151,]
          0 1.769e-15
                       0.495
## [152,]
          0 1.769e-15
                       0.485
## [153,]
          0 7.783e-15 0.475
## [154,]
          0 1.769e-15 0.465
## [155,]
          0 1.769e-15
                       0.455
## [156,]
          0 1.769e-15
                       0.445
## [157,]
          0 1.769e-15 0.435
## [158,]
          0 1.769e-15 0.425
## [159,]
          0 1.769e-15 0.415
## [160,]
          0 1.769e-15
                       0.405
## [161,]
          0 1.769e-15
                      0.395
## [162,]
          0 1.769e-15
                       0.385
## [163,]
          1 1.275e-03
                       0.375
## [164,]
          1 7.497e-03
                       0.365
## [165,]
          1 1.355e-02 0.355
## [166,]
          1 1.944e-02 0.345
## [167,]
          1 2.517e-02 0.335
## [168,]
          1 3.074e-02 0.325
## [169,]
          1 3.615e-02 0.315
## [170,]
          1 4.141e-02
                       0.305
## [171,]
          1 4.651e-02
                       0.295
## [172,]
          1 5.146e-02 0.285
## [173,]
          1 5.626e-02 0.275
## [174,]
          1 6.091e-02 0.265
## [175,]
          1 6.541e-02
                       0.255
## [176,]
          1 6.976e-02 0.245
## [177,]
          1 7.396e-02 0.235
## [178,]
          1 7.802e-02
                       0.225
## [179,]
          2 8.230e-02
                       0.215
## [180,]
          2 8.806e-02 0.205
## [181,]
          2 9.359e-02
                      0.195
## [182,]
          2 9.891e-02 0.185
## [183,]
          2 1.040e-01 0.175
## [184,]
          2 1.089e-01 0.165
## [185,] 2 1.135e-01 0.155
## [186,] 3 1.181e-01 0.145
```



```
## [187,] 3 1.240e-01 0.135
## [188,] 5 1.319e-01 0.125
## [189,] 8 1.422e-01 0.115
## [190,] 10 1.557e-01 0.105
## [191,] 12 1.711e-01 0.095
## [192,] 12 1.860e-01 0.085
## [193,] 12 1.999e-01 0.075
## [194,] 12 2.125e-01 0.065
## [195,] 13 2.256e-01 0.055
## [196,] 20 2.457e-01 0.045
## [197,] 23 2.683e-01 0.035
## [198,] 27 2.910e-01 0.025
## [199,] 30 3.162e-01 0.015
clrlasso_coef<-coef(clrlasso,s=0.10)</pre>
sum(abs(clrlasso_coef)>0)
## [1] 13
selected_clrlasso<-which(as.numeric(abs(coef(clrlasso, s=0.1)))>0)[-1];
The indices of selected variables (abs(coef)>0)
selected_clrlasso<-selected_clrlasso-1</pre>
taxa_id<-colnames(x_Crohn)[selected_clrlasso]</pre>
write.csv(data.frame(selected_clrlasso,taxa_id),"./Generated_datasets/results_clrlasso_Crohn12.csv")
```

Selbal: selection of balances

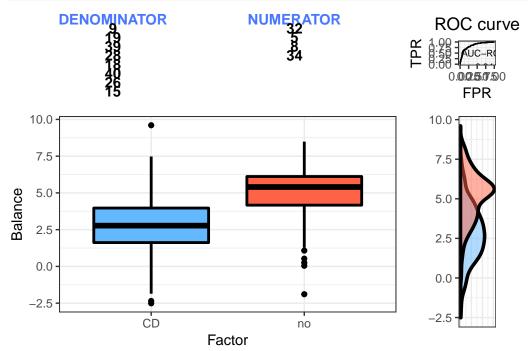
5.1 Crohn disease data

```
y<-y_Crohn
```

For binary outcomes (logistic regression), selbal requires y to be factor.

If y is numeric selbal implements linear regression.

```
x<-x_Crohn
colnames(x)<-(1:ncol(x))
selbal_Crohn<-selbal(x = x, y = y, logt=T, maxV=12)</pre>
```



selected_selbal<-as.numeric(c(selbal_Crohn[[6]][,1],selbal_Crohn[[6]][,2]))</pre>

Warning: NAs introduced by coercion



```
id.na<-which(is.na(selected_selbal))
selected_selbal<-selected_selbal[-id.na]
selected_selbal<-as.character(selected_selbal)

columns_selected_selbal<-which(colnames(x)%in% selected_selbal)
taxa_id<-colnames(x_Crohn)[columns_selected_selbal]

write.csv(data.frame(columns_selected_selbal, taxa_id),"./Generated_datasets/results_selbal_Crohn12.csv</pre>
```

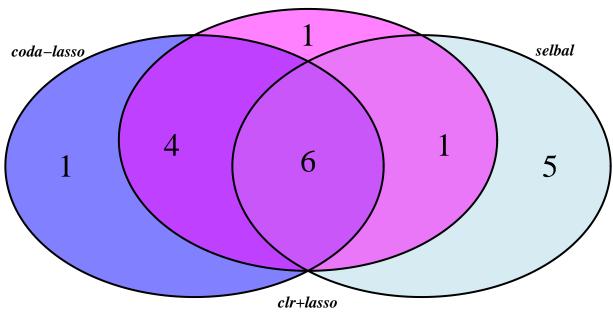


Concordance of variables selected by the three methods

6.1 Crohn disease data



Concordance of selected taxa for Crohn data



```
taxa.id <- venn(taxa.id_selected, show.plot=FALSE)
taxa <- venn(taxa_selected, show.plot=FALSE)
inters_taxa.id <- attr(taxa.id, "intersections")
inters_taxa <- attr(taxa, "intersections")
lapply(inters_taxa, head)</pre>
```

```
## $A
## [1] "10"
##
## $B
## [1] "27"
##
## $C
## [1] "15" "18" "26" "28" "34"
## $`A:B`
## [1] "2" "31" "33" "48"
##
## $`A:C`
## [1] "8"
##
## $`A:B:C`
## [1] "5" "9" "19" "32" "39" "40"
lapply(inters_taxa.id, head)
```

\$A



```
## [1] "g__Faecalibacterium"
##
## $B
## [1] "o__Lactobacillales_g__"
##
## $C
## [1] "g__Blautia" "g__Dorea" "g__Oscillospira"
## [4] "g__Adlercreutzia" "o__Clostridiales_g__"
##
## $^A:B^
## [1] "g__Parabacteroides" "g__Prevotella" "g__Lachnospira"
## [4] "g__Bilophila"
##
#* $^A:C^
## [1] "g__Bacteroides"
##
## $^A:B:C^
## [1] "f__Peptostreptococcaceae_g__" "g__Eggerthella"
## [3] "g__Dialister" "g__Roseburia"
## [5] "g__Streptococcus" "g__Aggregatibacter"
```