




# How Can Countries Increase Their Life Expectancy

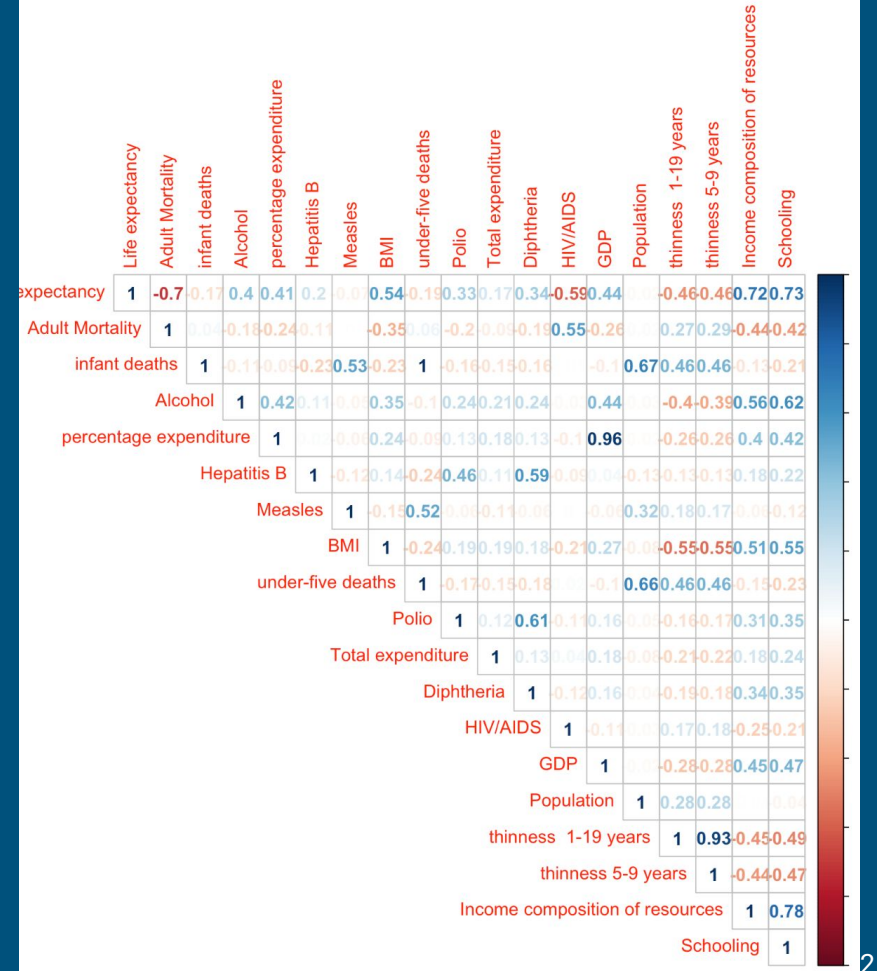


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# The Data

- Sourced from the World Health Organization (WHO)
- Contains 2,938 observations of 22 variables
  - 193 countries
  - 2000 - 2015
- Selected variables
  - **ID (3):** Year, Country, Development Status
  - **Response (1):** Life Expectancy
  - **Predictors (10):** Schooling, GDP, Alcohol, BMI, Percentage Expenditure, Income composition of resources, HIV/AIDS, Thinness 10-19 years (and 5-9 years), adult mortality
- Correlation plot (right)



# Variable Selection

```
call:
lm(formula = Life.expectancy ~ Schooling + GDP + Alcohol + BMI +
  percentage.expenditure + Income.composition.of.resources +
  HIV.AIDS + thinness.5.9.years + thinness.10.19.years, data = life)

Residuals:
    Min       1Q   Median       3Q      Max
-27.5813  -2.5470  -0.0207   2.6412  25.4956

Coefficients:
                Estimate Std. Error t value Pr(>|t|)
(Intercept)    4.980e+01  4.985e-01  99.895 < 2e-16 ***
Schooling       1.078e+00  5.206e-02  20.702 < 2e-16 ***
GDP             4.434e-05  1.709e-05   2.594 0.009537 **
Alcohol        -1.009e-01  2.961e-02  -3.407 0.000668 ***
BMI             5.476e-02  6.336e-03   8.642 < 2e-16 ***
percentage.expenditure
1.773e-04  1.111e-04   1.596 0.110670
Income.composition.of.resources
9.957e+00  7.498e-01  13.279 < 2e-16 ***
HIV.AIDS        -6.609e-01  1.768e-02 -37.389 < 2e-16 ***
thinness.5.9.years
-4.548e-02  5.638e-02  -0.807 0.419871
thinness.10.19.years
-7.606e-02  5.757e-02  -1.321 0.186593
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4.522 on 2301 degrees of freedom
Multiple R-squared:  0.7837,    Adjusted R-squared:  0.7829
F-statistic: 926.5 on 9 and 2301 DF,  p-value: < 2.2e-16
```

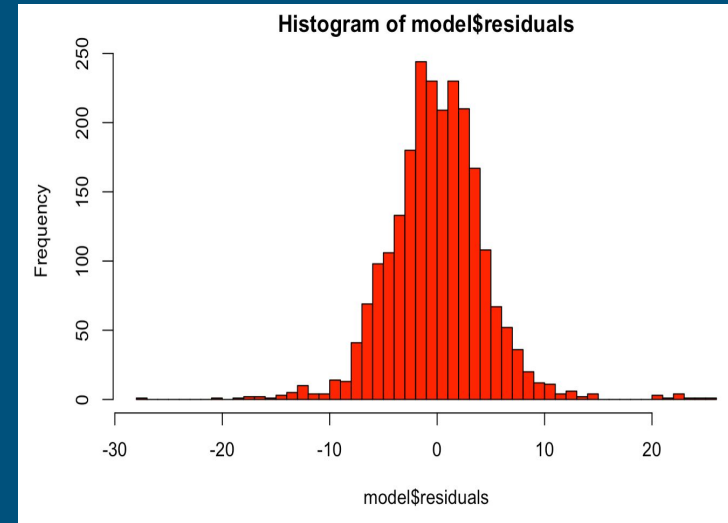
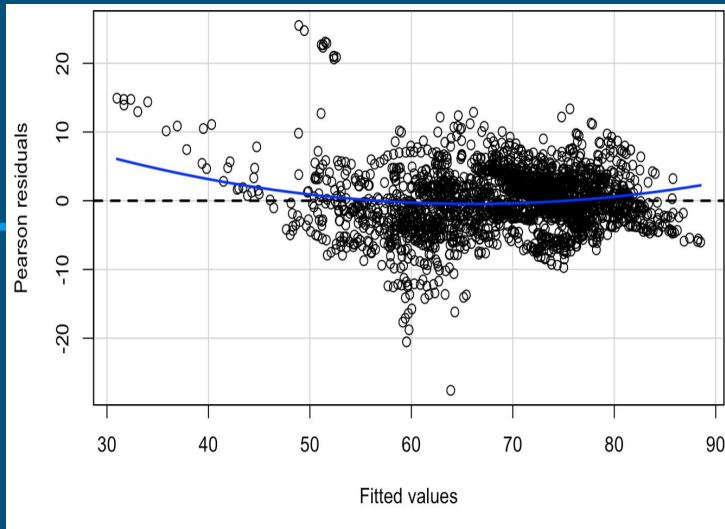
Initial model with all 9 predictors (2 later trimmed)

- We began with the 10 predictors most correlated with life expectancy (simple  $R^2 > 0.4$ )
  - Later excluded adult mortality, as it is part of the life expectancy calculation
- Then we employed **backward selection** to trim down the model until all predictors had a significance  $< 0.05$ 
  - This was in line with removing the most mutually correlated variables (highest VIFs  $\sim 7$ )
- The best overall model had **7 predictors**, though the other 2 predictors were still useful for other parts of the analysis
- Observations containing missing values were excluded for simplicity and consistency
  - Our subset therefore had 2,311 observations of 13 variables

# Question 3

*Given these predictors, how accurately can one predict life expectancy with a linear model?*





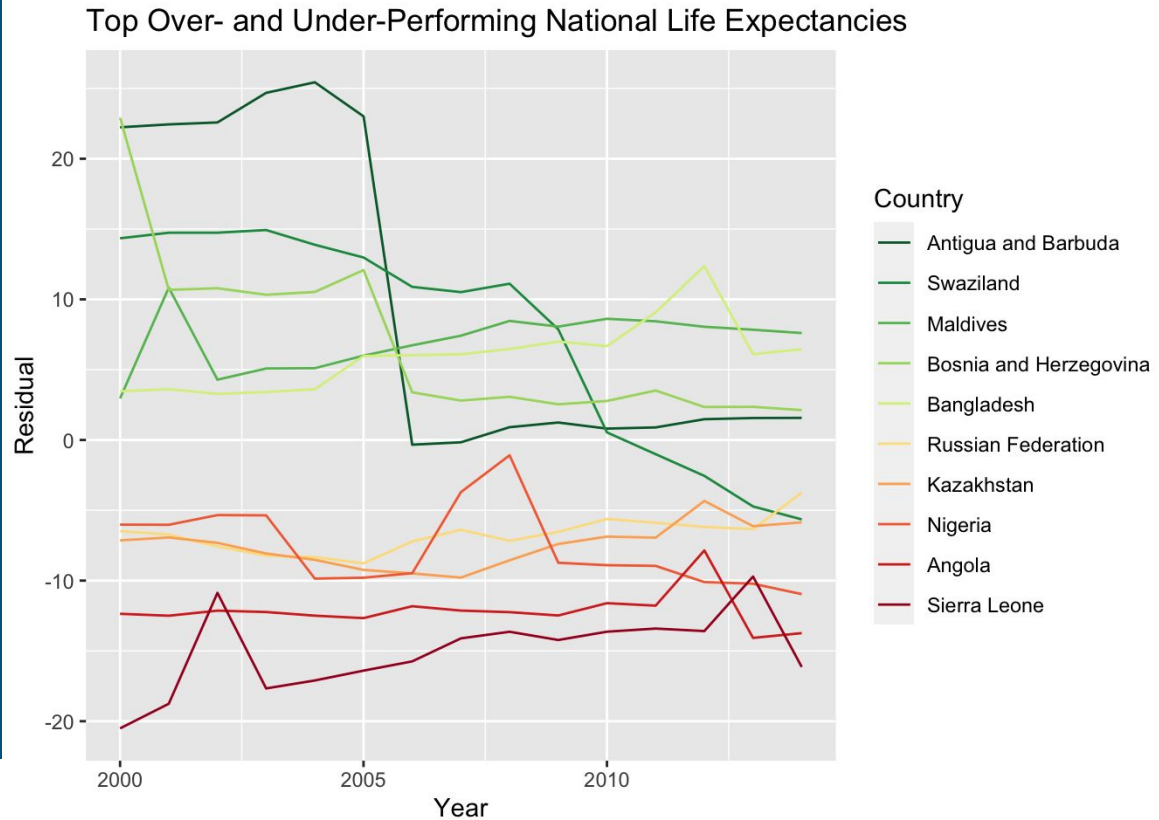
- We have obtained an accuracy 78.28% from the trimmed model.
- We can note that the points (left) are “equally” spread across the x-axis indicating that our model does not have any non-linear relationships.
- Constructed a histogram (right), from the linear model that the residuals are normally distributed.

# Question 5

*Which countries over- or under-perform in life expectancy relative to what our linear model would predict? What might account for this difference?*



- Overall residual distribution is approximately normal
- The distribution of average national errors suggests outliers\*
- We calculated p-values for each nation's average error (equivalent to sampling a mean under  $H_0$ )
- There were **43 significant outliers** for average error
- The top over- and under-performers are shown here
- Only external conditions can account for these consistent differences from the model



$$H_0 : \epsilon \sim N(0, \sigma^2) \text{ for all countries}$$

$$H_1 : \epsilon \sim N(0, \sigma^2) \text{ for at least one country}$$

$$z_j = \frac{1}{n_j} \sum_{i=1}^{n_j} \epsilon = \frac{1}{n_j} \sum_{i=1}^{n_j} N(0, \sigma^2) \sim N(0, \sigma^2/n_j) \text{ for each country } j$$

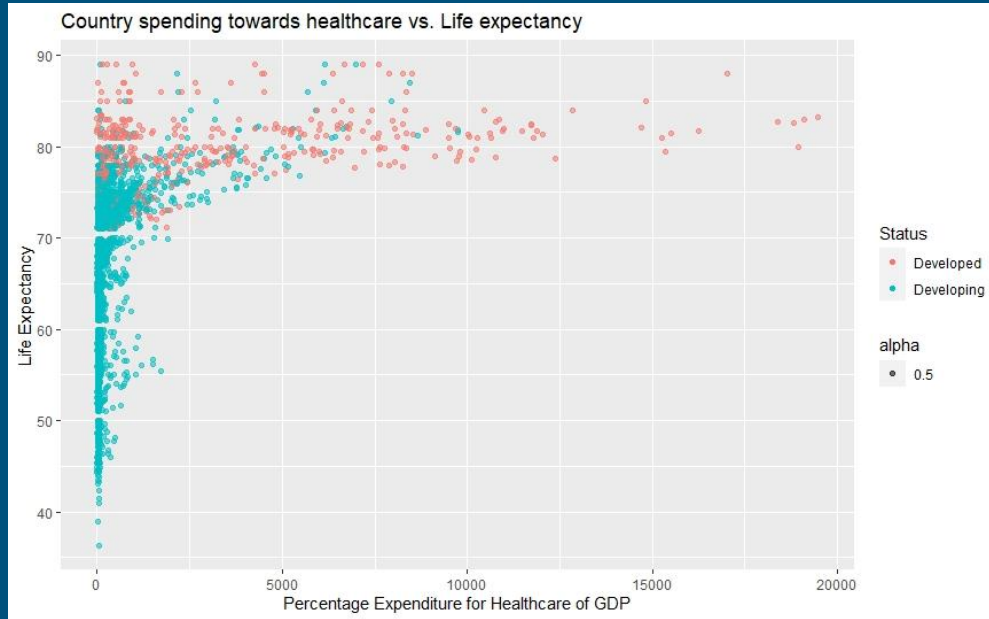
\* residual variance did not significantly decrease when averaged by nation, in disagreement with the CLT

# Question 7

To improve the lifespan of a country with low life expectancy( $<65$ ), should they improve on their healthcare expenditure? Does it differ between developing and developed countries?







- ❖ Choice is seemingly obvious before analysis
- ❖ After analysis, results are mixed
- ❖ After certain point in spending, country guaranteed high life expectancy
- ❖ Pattern differs between developing and developed countries
- ❖ Already high life expectancy for developed countries

# Conclusion

Overall Question this analysis is solving: *What are the key factors that improve life expectancy?*

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```
Call:
lm(formula = Life.expectancy ~ Schooling + GDP + Alcohol + BMI +
    Income.composition.of.resources + HIV.AIDS + thinness.10.19.years,
    data = data)

Residuals:
    Min       1Q   Median       3Q      Max
-27.5862  -2.5642  -0.0208   2.6258  25.4375

Coefficients:
                Estimate Std. Error t value Pr(>|t|)
(Intercept)    4.976e+01  4.959e-01  100.344 < 2e-16 ***
Schooling       1.078e+00  5.208e-02  20.710 < 2e-16 ***
GDP             6.913e-05  7.475e-06   9.247 < 2e-16 ***
Alcohol        -9.308e-02  2.927e-02  -3.180  0.00149 **
BMI             5.495e-02  6.281e-03   8.749 < 2e-16 ***
Income.composition.of.resources  9.872e+00  7.485e-01  13.189 < 2e-16 ***
HIV.AIDS       -6.614e-01  1.767e-02 -37.426 < 2e-16 ***
thinness.10.19.years -1.186e-01  2.616e-02  -4.533 6.11e-06 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4.523 on 2303 degrees of freedom
Multiple R-squared:  0.7834,    Adjusted R-squared:  0.7828
F-statistic: 1190 on 7 and 2303 DF,  p-value: < 2.2e-16
```

- Key factors for all countries are schooling, GDP, Alcohol, BMI, income composition of resources, and HIV/AIDS
- Removed percentage.expenditure and the thinness 5-9 categories, as they are not significant to the model.
- Very minute changes to R-squared value

```
call:
lm(formula = Life.expectancy ~ Schooling + GDP + Alcohol + BMI +
  percentage.expenditure + Income.composition.of.resources +
  HIV.AIDS + thinness.5.9.years + thinness.10.19.years, data = developed)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-4.8284	-1.6045	-0.4987	0.7789	9.2844

Coefficients: (1 not defined because of singularities)

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	5.327e+01	3.349e+00	15.908	< 2e-16 ***
Schooling	-4.088e-01	1.008e-01	-4.058	5.92e-05 ***
GDP	-1.913e-05	1.554e-05	-1.231	0.2191
Alcohol	-2.498e-01	4.716e-02	-5.298	1.91e-07 ***
BMI	-1.170e-02	7.807e-03	-1.498	0.1348
percentage.expenditure	1.082e-04	8.939e-05	1.211	0.2266
Income.composition.of.resources	4.473e+01	4.367e+00	10.241	< 2e-16 ***
HIV.AIDS	NA	NA	NA	NA
thinness.5.9.years	1.348e+00	1.139e+00	1.184	0.2372
thinness.10.19.years	-3.189e+00	1.234e+00	-2.584	0.0101 *

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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 2.536 on 414 degrees of freedom  
Multiple R-squared: 0.6094, Adjusted R-squared: 0.6018  
F-statistic: 80.74 on 8 and 414 DF, p-value: < 2.2e-16

```
call:
lm(formula = Life.expectancy ~ Schooling + GDP + Alcohol + BMI +
  percentage.expenditure + Income.composition.of.resources +
  HIV.AIDS + thinness.5.9.years + thinness.10.19.years, data = developing)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-27.3764	-2.6856	0.1231	2.6903	26.0064

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	4.951e+01	5.388e-01	91.898	< 2e-16 ***
Schooling	1.103e+00	5.777e-02	19.094	< 2e-16 ***
GDP	-4.149e-05	2.562e-05	-1.619	0.106
Alcohol	-1.667e-01	3.670e-02	-4.542	5.92e-06 ***
BMI	7.683e-02	7.533e-03	10.199	< 2e-16 ***
percentage.expenditure	1.327e-03	2.399e-04	5.531	3.63e-08 ***
Income.composition.of.resources	7.797e+00	7.882e-01	9.892	< 2e-16 ***
HIV.AIDS	-6.494e-01	1.821e-02	-35.667	< 2e-16 ***
thinness.5.9.years	6.692e-03	5.792e-02	0.116	0.908
thinness.10.19.years	-5.918e-02	5.895e-02	-1.004	0.316

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4.624 on 1878 degrees of freedom  
Multiple R-squared: 0.7473, Adjusted R-squared: 0.7461  
F-statistic: 617.1 on 9 and 1878 DF, p-value: < 2.2e-16

Developed

- ❑ Developed countries have fewer key factors to improve life expectancy
- ❑ Schooling, Alcohol, and income composition of resources
- ❑ average BMI, percentage expenditure on healthcare, income composition of resources, and HIV/AIDS cases

Developing



THANK YOU