Eric Pitman Summer Workshop in Computational Science



3. Descriptive Statistics



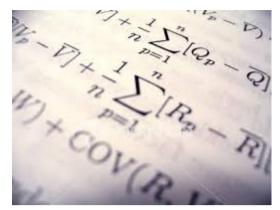
Descriptive Statistics



Explore a dataset:

- What's in the dataset?
- What does it mean?
- What if there's a lot of it?

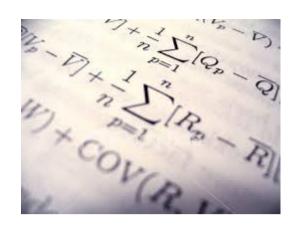
Basic Statistical Functions in R



Wanted: measures of the center and the spread of our numeric data.

- mean()
- median()
- range()
- var() and sd() # variance, standard deviation
- summary() # combination of measures

mean()



A measure of the data's "most typical" value.

- Arithmetic mean == average
- Divide sum of values by number of values

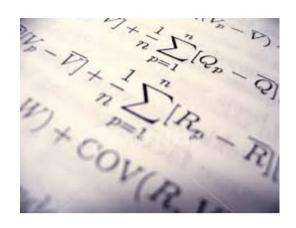
$$\overline{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

mean()

A measure of the data's "most typical" value.

$$\overline{x} = \frac{1}{n} \sum_{i=1}^{n} x_{i}$$
> f <- c(3, 2, 4, 1)
> mean(f) # == sum(f)/length(f) == (3+2+4+1)/4
[1] 2.5

median()

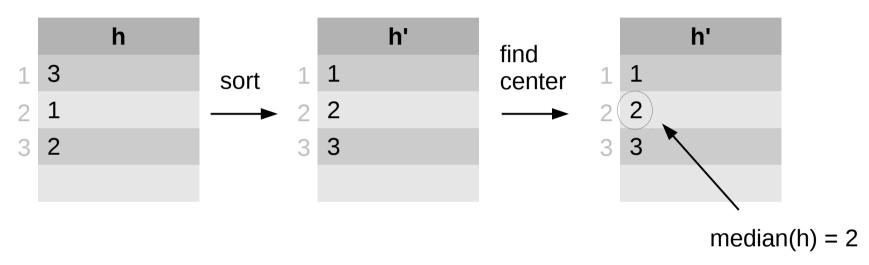


A measure of the data's center value. To find it:

- Sort the contents of the data structure
- Compute the value at the center of the data:
 - For odd number of elements, take the center element's value.
 - For even number of elements, take mean around center.

median()

Odd number of values:



$$> h <- c(3, 1, 2)$$

> median(h)

[1] 2

median()

Even number of values: need to find mean()

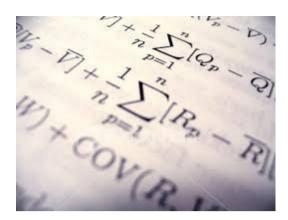


$$> f <- c(3, 2, 4, 1)$$

> median(f)

[1] 2.50

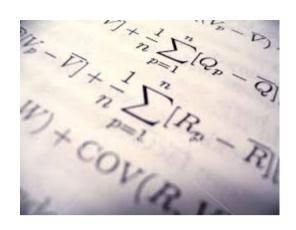
range(): min() and max()



range() reports the minimum and maximum values found in the data structure.

```
> f <- c(3, 2, 4, 1)
> range(f) # reports min(f) and max(f)
[1] 1 4
```

var() and sd()



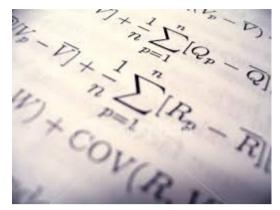
 Variance: a measure of the spread of the values relative to their mean:

$$Var = s_n^2 = \frac{1}{n} \sum_{i=1}^n (y_i - \overline{y})^2$$
 Sample variance

Standard deviation: square root of the variance

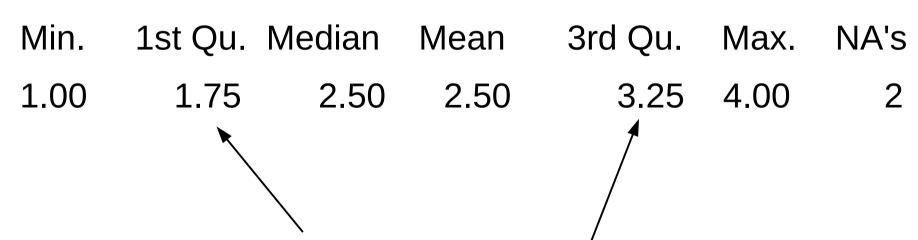
$$s_n = \sqrt{Var}$$
 Sample standard deviation

R's summary() Function



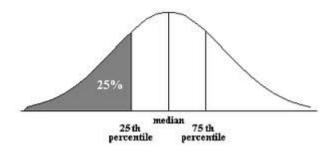
Provides several useful descriptive statistics about the data:

- > g <- c(3, NA, 2, NA, 4, 1)
- > summary(g)



Quartiles: Sort the data set and divide it up into quarters...

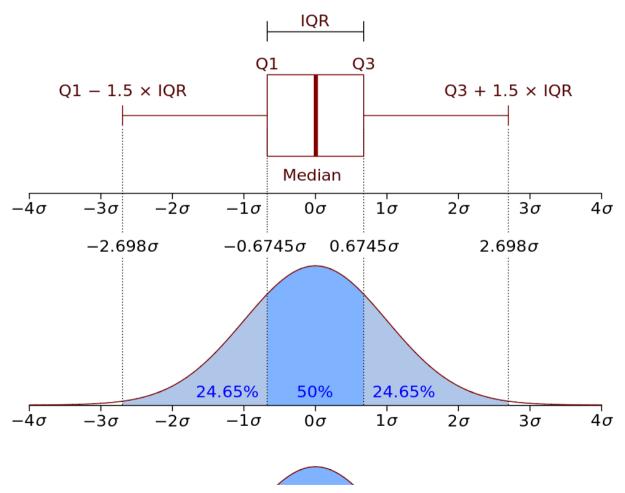
Quartiles



Quartiles are the *three points* that divide ordered data into four equal-sized groups:

- Q1 marks the boundary just above the lowest 25% of the data
- Q2 (the median) cuts the data set in half
- Q3 marks the boundary just below the highest 25% of data

Quartiles



Boxplot and probability distribution function of Normal N(0,1 σ^2) population

Summary: Basic Statistical Functions

- Characterize the center and the spread of our numeric data.
- Comparing these measures can give us a good sense of our dataset.

Statistics and Missing Data

If NAs are present, specify na.rm=TRUE to call:

- mean()
- median()
- range()
- sum()
- ...and some other functions

R disregards NAs, then proceeds with the calculation.

Diamonds Data



50,000 diamonds, for example:

carat	cut col	or	clarity	depth	table	price	X	У	Z
1 0.23	Ideal	Ε	SI2	61.5	55	326	3.95	3.98	2.43
2 0.21	Premium	Ε	SI1	59.8	61	326	3.89	3.84	2.31
3 0.23	Good	Ε	VS2	L 56.9	65	327	4.05	4.07	2.31

What can we learn about these data?

Diamonds Data



This dataset is part of the ggplot2 library.

To enable access to the dataset, just load the library:

```
> library("ggplot2")
> str(diamonds)
'data.frame': 53940 obs. of 10 variables:
$ carat : num  0.23 0.21 0.23 0.29
0.31 ...
```

Diamonds Data summary()

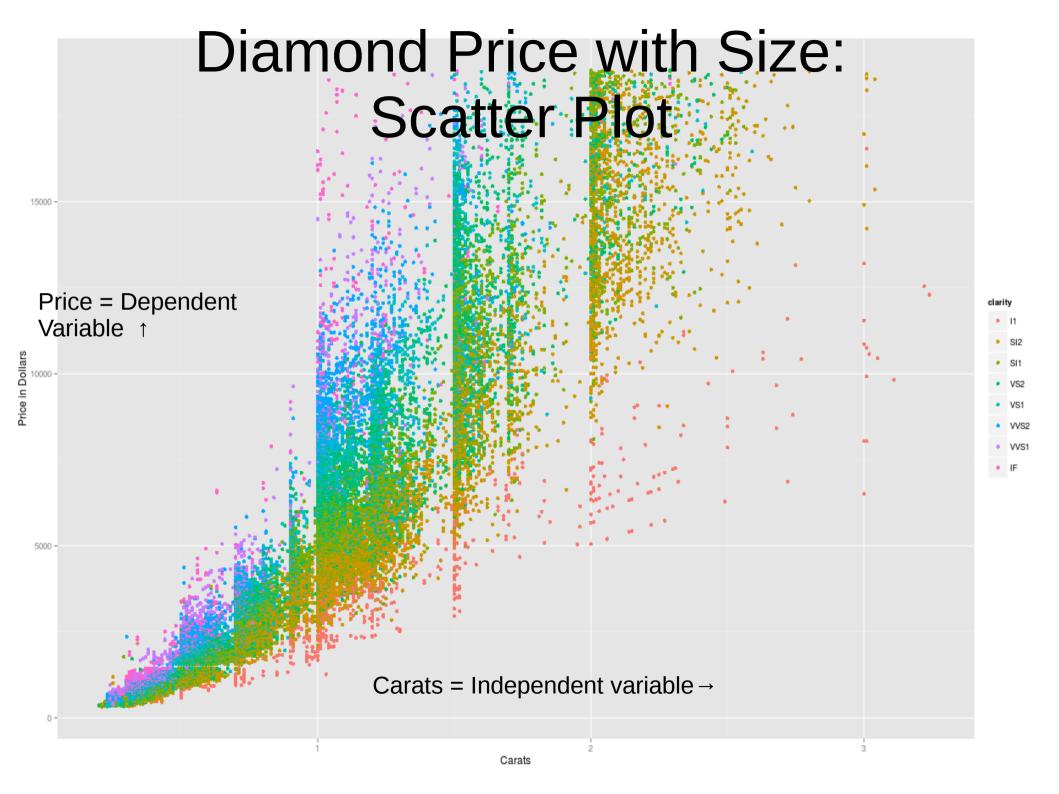


Information provided by summary() depends on the type of data, by column:

carat	cut	color	price		
Min. :0.2000 1st Qu.:0.4000 Median :0.7000 Mean :0.7979 3rd Qu.:1.0400 Max. :5.0100	Fair : 1610 Good : 4906 Very Good:12082 Premium :13791 Ideal :21551	H: 8304 I: 5422	Min. : 326 1st Qu.: 950 Median : 2401 Mean : 3933 3rd Qu.: 5324 Max. :18823		
		J: 2808			
numeric data:	categorical (factor	r) data:			

counts

statistical summary



table() Function

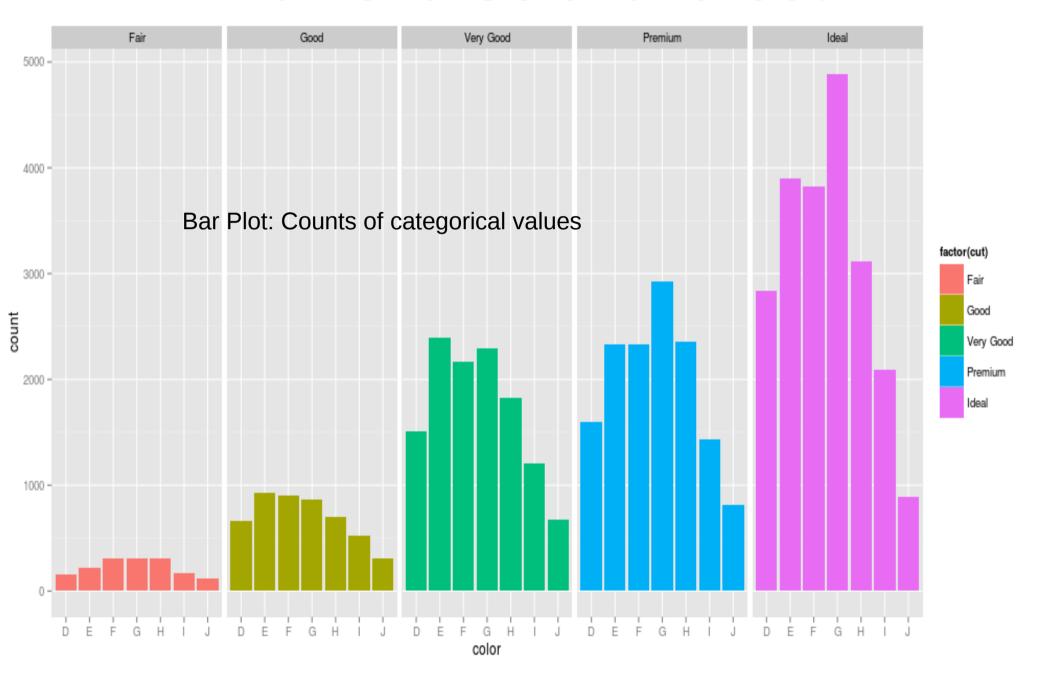


Contingency table: counts of categorical values for selected columns

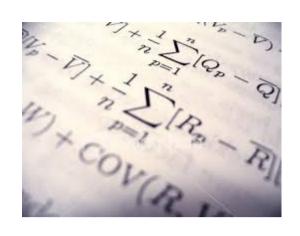
> table(diamonds\$cut, diamonds\$color)

	D	Ε	F	G	Н	1	J	
Fair	163	224	312	314	303	175	119	
Good	662	933	909	871	702	522	307	
Very Good	1513	2400	2164	2299	1824	1204	678	
Premium	1603	2337	2331	2924	2360	1428	808	
Ideal	2834	390	03 38	26 48	84 31	15 20	93 896	3

Diamond Color and Cut



Correlation



Do the two quantities X and Y vary together?

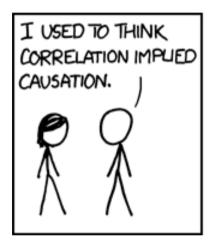
- Positively:
$$0<\rho<1$$
 - Or negatively:
$$-1<\rho<0$$

- Or negatively:
$$-1 < \rho < 0$$

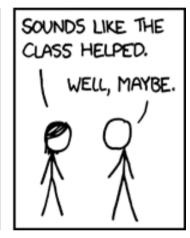
$$\rho_{X,Y} = corr(X,Y) = \frac{cov(X,Y)}{\sigma_X \sigma_Y} = \frac{E[(X - \mu_X)(Y - \mu_Y)]}{\sigma_X \sigma_Y}$$

A pairwise, *statistical* relationship between quantities

Correlation







$$\rho_{X,Y} = corr(X,Y) = \frac{cov(X,Y)}{\sigma_X \sigma_Y} = \frac{E[(X - \mu_X)(Y - \mu_Y)]}{\sigma_X \sigma_Y}$$

NOTE: Correlation does not imply causation...

Looking for Correlations



diamonds data frame: 50,000 diamonds

- carat: weight of the diamond (0.2–5.01)
- table: width of top of diamond relative to widest point (43–95)
- price: price in US dollars
- x: length in mm (0–10.74)
- y: width in mm (0–58.9)
- z: depth in mm (0–31.8)

cor() Function



Look at pairwise, *statistical* relationships between numeric data:

> cor(diamonds[c(1,6:10)])

	carat	table	price	X	У	Z
carat	1.0000000	0.1816175	0.9215913	0.9750942	0.9517222	0.9533874
table	0.1816175	1.0000000	0.1271339	0.1953443	0.1837601	0.1509287
price	0.9215913	0.1271339	1.0000000	0.8844352	0.8654209	0.8612494
X	0.9750942	0.1953443	0.8844352	1.0000000	0.9747015	0.9707718
у	0.9517222	0.1837601	0.8654209	0.9747015	1.0000000	0.9520057
Z	0.9533874	0.1509287	0.8612494	0.9707718	0.9520057	1.0000000

Student Dataset Example



Now we can write some R to perform some descriptive statistics on our student data:

- Contingency table of school and handedness?
- Correlation between age and height?
- Some descriptive statistics about height (only comparing apples to apples!)

OK...but what's the problem here? Small dataset!

Interlude

Complete descriptive statistics exercises.



Open in the RStudio source editor:

<workshop>/exercises/3-exercises-descriptive-statistics.R