

# Monte Carlo Financial Models on U50

Group 7

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Github 連結: [https://github.com/EvanLu0815/Final\\_monteCarloFinancialModel](https://github.com/EvanLu0815/Final_monteCarloFinancialModel)

## Introduction

In this project, I am going to implement Black-Scholes Model on the payoff price of European vanilla option. In the Black-Scholes model, the price can be considered as geometric Brownian motion. Then we can obtain (1).

$$dS = rSdt + \sigma Sdz \quad (1)$$

In (1),  $S$  is stock price,  $r$  is the fixed interest rate,  $\sigma$  is the constant volatility and  $z$  is a Wiener process. The analytical solution for the stochastic differential equation (1) is

$$S_{t+\Delta t} = S_t e^{(r - \frac{1}{2}\sigma^2)\Delta t + \sigma\epsilon\sqrt{\Delta t}} \quad (2)$$

In (2),  $\epsilon \sim N(0, 1)$  is the standard normal distribution.

The European vanilla option can be exercised only at expiration date. As a result, only the stock price at the expiration date can affect the payoff price. Then the payoff price can be implemented as (3).

$$P_{call} = \max\{S_T - K, 0\} \quad (3)$$

In (3),  $T$  is the pre-set time,  $S_T$  is the stock price at expiration date and  $K$  is the strike price.

## Algorithm

Black-Scholes model includes three main steps. Each time interval  $(0, T)$  is first divided into  $M$  steps, and denoted as  $t_0, t_1, \dots, t_M$ . Secondly,  $M$  standard normally distributed independent random numbers  $\epsilon$  are generated. Finally,  $S_{t_M}$  is computed by (2) from  $S_{t_0}$ . After going through the three steps, one "path" is completed. In the model, it needs to compute  $N$  paths. The algorithm is shown below.

---

**Algorithm 1** Black-Scholes model

---

**Input:** parameters for the stock and option  
**Output:** payoff price  
*Initialization:* Random number generators  
**for**  $i = 1$  to  $N$  **do**  
    **for**  $k = 1$  to  $M$  **do**  
         $U_1, U_2 \leftarrow \text{MersenneTwist}()$   
         $\epsilon_1, \epsilon_2 \leftarrow \text{BoxMuller}(U_1, U_2)$   
         $S_{t_{k+2}}, S_{t_{k+1}} \leftarrow \text{Price}(S_t, \epsilon_1, \epsilon_2)$   
         $k++ = 2$   
    **end for**  
     $P_{\text{option}}[i] \leftarrow \text{Option}(S_t[], K)$   
     $i++$   
**end for**  
**return**  $P_{\text{Call}} = \text{ave}(P_{\text{option}})$

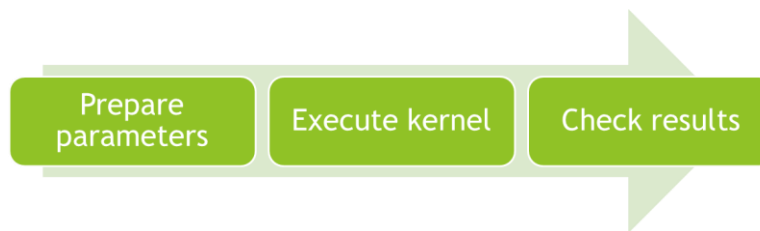
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The random numbers  $\epsilon$  is generated by Mersenne-Twister algorithm followed by Box-Muller transformation.

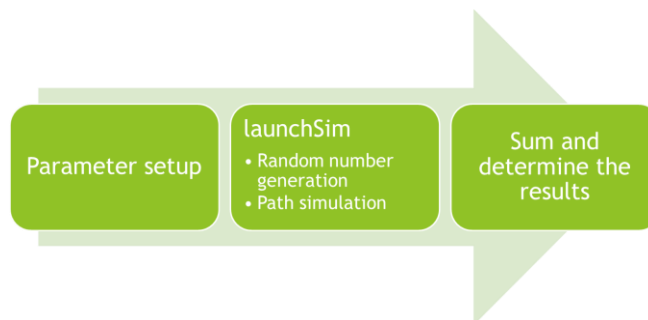
## Hardware Implementation

In this project, I re-write the whole host program and adjust some of the pragma in order to make the project workable on the vitis 2021.2 and U50 platform.

### System Structure



### Kernel Execution Structure



#### 1. Parameter setup

The kernel is first setup the parameters. It uses sd to transfer all the float data into blackScholes model.

```

60 static const int SIMS_PER_GROUP =32;
61 stockData<float> sd(timeT,freeRate,volatility,initPrice,strikePrice);
62
63 float call0, put0;
64 blackScholes<SIMS_PER_GROUP,EuropeanOptionStatus<float>, float> bs0(sd, steps);
  
```

#### 2. LaunchSim

The kernel is then use launchSimulation in lauchSim.h to generate random number using box-Muller algorithm and use simulation offered by the class

blackScholes to do path simulation. In launchSim, three functions are called, prng, BOX\_MULLER, and simulation. I will introduce them in the following.

```
launchSimulation(call0, put0, g_id+0, bs0, sims*steps>>4, sims>>4);
```

```
19 void launchSim(DATA_T &pCall, DATA_T &pPut, RNG<DATA_T> &rng0, RNG<DATA_T> &rng1, Model &m, int numR, int sims){
20 #pragma HLS DATAFLOW
21     hls::stream<unsigned int> s_num0;
22     hls::stream<unsigned int> s_num1;
23 #pragma HLS STREAM variable=s_num0 depth=4 dim=1
24 #pragma HLS STREAM variable=s_num1 depth=4 dim=1
25     hls::stream<DATA_T> sRNG0;
26     hls::stream<DATA_T> sRNG1;
27 #pragma HLS STREAM variable=sRNG0 depth=4 dim=1
28 #pragma HLS STREAM variable=sRNG1 depth=4 dim=1
29
30     prng(rng0, rng1, s_num0, s_num1, numR);
31
32     RNG<DATA_T>::BOX_MULLER(s_num0, s_num1, sRNG0, sRNG1, numR>>1);
33
34     m.simulation(sRNG0, sRNG1, sims, pCall, pPut);
35 }
```

Prng:

```
6 void prng(RNG<DATA_T> &rng0, RNG<DATA_T> &rng1, hls::stream<unsigned int> &sRNG0, hls::stream<unsigned int> &sRNG1, int nums
7     for(int i = 0; i < nums>>2; i++){
8 #pragma HLS PIPELINE
9     unsigned int r0, r1, r2, r3;
10    rng0.extract_number(&r0, &r1);
11    rng1.extract_number(&r2, &r3);
12    sRNG0.write(r0);
13    sRNG0.write(r2);
14    sRNG1.write(r1);
15    sRNG1.write(r3);
16 }
17 }
```

extract\_number is used to prepare the seed for box-muller algorithm. The INLINE pragma is used to break the function structure to decrease the use of hardware resources.

```
98 void extract_number(uint* num1, uint* num2){
99 #pragma HLS INLINE
100     uint id1=increase(1), idm=increase(RNG_MH), idm1=increase(RNG_MH1);
101
102     uint x = this->seed, x1=this->mt_o[this->index], x2=this->mt_e[id1],
103           xm=this->mt_o[idm], xm1=this->mt_e[idm1];
104
105     x = (x & upper_mask) + (x1 & lower_mask);
106     uint xp = x >> 1;
107     if ((x & 0x01) != 0)
108         xp ^= RNG_A;
109     x = xm ^ xp;
110
111     uint y = x;
112     y ^= ((y >> RNG_U) & RNG_D);
113     y ^= ((y << RNG_S) & RNG_B);
114     y ^= ((y << RNG_T) & RNG_C);
115     y ^= (y >> RNG_L);
116     *num1 = y;
117     mt_o[this->index]=x;
118
119     x1 = (x1 & upper_mask) + (x2 & lower_mask);
120     uint xt = x1 >> 1;
121     if ((x1 & 0x01) != 0)
122         xt ^= RNG_A;
123     x1 = xm1 ^ xt;
124
125     uint y1 = x1;
126     y1 ^= ((y1 >> RNG_U) & RNG_D);
127     y1 ^= ((y1 << RNG_S) & RNG_B);
128     y1 ^= ((y1 << RNG_T) & RNG_C);
129     y1 ^= (y1 >> RNG_L);
130     *num2 = y1;
131     mt_o[this->index]=x1;
132
133     this->index=id1;
134     this->seed=x2;
135 }
```

BOX\_MULLER:

In this function, INLINE is still used to break function structure.

```
156 void BOX_MULLER(DATA_T*data1, DATA_T*data2, DATA_T ave, DATA_T deviation){
157 #pragma HLS INLINE
158     static const DATA_T _2PI= 2*3.14159265358979323846f;
159     // static const DATA_T MINI_RNG = 2.328306e-10;
160
161     uint num1, num2;
162     DATA_T tp, tmp1, tmp2;
163     extract_number(&num1, &num2);
164     ap_ufixed<32,0> f_tmp1, f_tmp2;
165     f_tmp1(31, 0)=num1;
166     f_tmp2(31, 0)=num2;
167     tmp1 = f_tmp1.to_float();
168     tmp2 = f_tmp2.to_float();
169 #ifdef __DOUBLE_PRECISION__
170     tp=sqrt(fmax(-2*log(tmp1), 0)*deviation);
171     *data1=cos(_2PI*tmp2)*tp+ave;
172     *data2=sin(_2PI*tmp2)*tp+ave;
173 #else
174     tp=sqrtf(fmaxf(-2.0f*logf(tmp1), 0.0f)*deviation);
175     *data1=cosf(_2PI*tmp2)*tp+ave;
176     *data2=sinf(_2PI*tmp2)*tp+ave;
177 #endif
178 }
```

Simulation:

In simulation, path\_sum and sum are called to complete the algorithm we have explained in algorithm section.

```

45 void simulation(hls::stream<DATA_T>& s_RNG0, hls::stream<DATA_T>& s_RNG1, int sims, DATA_T &pCall, DATA_T &pPut)
46 {
47     DATA_T call = 0, put = 0;
48     hls::stream<DATA_T> prices;
49 #pragma HLS STREAM variable=prices depth=NUM_SIMS dim=1
50 #pragma HLS DATAFLOW
51     path_sim(s_RNG0, s_RNG1, prices, sims);
52     sum(prices, call, put, sims);
53     pCall = call;
54     pPut = put;
55 }

```

```

56 void path_sim(hls::stream<DATA_T>& s_RNG0, hls::stream<DATA_T>& s_RNG1, hls::stream<DATA_T>& prices, int sims){
57     OptionStatus stockPrice[NUM_SIMS];
58 #pragma HLS ARRAY_PARTITION variable=stockPrice cyclic factor=2 dim=1
59     for(int j=0; j<NUM_SIMS; j++){
60 #pragma HLS PIPELINE
61         stockPrice[j].init(data.price);
62     }
63     for(int k=0; k<sims/NUM_SIMS; k++){
64         for(int s=0; s<NUM_STEPS; s++){
65             for(int j=0; j<NUM_SIMS/2; j++){
66 #pragma HLS PIPELINE
67                 DATA_T r0 = s_RNG0.read();
68                 DATA_T r1 = s_RNG1.read();
69                 update(stockPrice[j*2], r0);
70                 update(stockPrice[j*2+1], r1);
71             }
72         }
73     }
74 #pragma HLS DEPENDENCE variable=stockPrice array inter RAW false
75 #pragma HLS PIPELINE
76     DATA_T price = stockPrice[j].valid? stockPrice[j].price():data.strikePrice;
77     prices.write(price);
78     stockPrice[j].init(data.price);
79 }
80 }
81 }

```

```

82 void update(OptionStatus &option, DATA_T r){
83 #pragma HLS INLINE
84     const DATA_T Dt = data.timeT / (DATA_T)NUM_STEPS,
85     Rdt = 1+data.freeRate*Dt,
86     SqrtV = data.volatility * sqrtf(Dt);
87     option.stockPrice *= Rdt +r *SqrtV;
88     option.update();
89 }
90 void sum(hls::stream<DATA_T> &prices, DATA_T &call, DATA_T &put, int sims){
91     for(int j=0; j<sims; j++){
92 #pragma HLS PIPELINE
93         DATA_T price = prices.read();
94         call+=executeCall(price);
95         put+=executePut(price);
96     }
97 }

```

In sum function, the executeCall and executePut are called to determine which price result should be kept as shown in formula (3).

```

98 DATA_T executeCall(DATA_T& price){
99 #pragma HLS INLINE
100     if(price > data.strikePrice){
101         return (price - data.strikePrice);
102     }
103     else
104         return 0;
105 }
106 DATA_T executePut(DATA_T& price){
107 #pragma HLS INLINE
108     if(price < data.strikePrice){
109         return (data.strikePrice - price);
110     }
111     else
112         return 0;
113 }
114 };

```

### 3. Sum and determine the results

<pre> pCall[g_id] = (call0 +call1 +call2 +call3 +call4 +call5 +call6 +call7 +call8 +call9 +call10 +call11 +call12 +call13 +call14 +call15 )/sims; </pre>	<pre> pPut[g_id] =(put0 +put1 +put2 +put3 +put4 +put5 +put6 +put7 +put8 +put9 +put10 +put11 +put12 +put13 +put14 +put15 )/sims; </pre>
--	--

## Main function

I use the host code from lab3 and adjust the kernel-related part.

The kernel interface is shown below. According to the kernel interface, the host function needs to prepare 2 axi master for pCall and pPut and 8 axi lite for the rest of parameters.

```
33 void blackEuro(float *pCall, float *pPut, // call price and put price
34               float timeT, // time period of options
35               float freeRate, // interest rate of the riskless asset
36               float volatility, // volatility of the risky asset
37               float initPrice, // stock price at time 0
38               float strikePrice, // strike price
39               int steps,
40               int sims,
41               int g_id)
42 {
43     #pragma HLS INTERFACE m_axi port=pCall bundle=gmem
44     #pragma HLS INTERFACE s_axilite port=pCall bundle=control
45     #pragma HLS INTERFACE m_axi port=pPut bundle=gmem
46     #pragma HLS INTERFACE s_axilite port=pPut bundle=control
47     #pragma HLS INTERFACE s_axilite port=timeT bundle=control
48     #pragma HLS INTERFACE s_axilite port=freeRate bundle=control
49     #pragma HLS INTERFACE s_axilite port=volatility bundle=control
50     #pragma HLS INTERFACE s_axilite port=initPrice bundle=control
51     #pragma HLS INTERFACE s_axilite port=strikePrice bundle=control
52     #pragma HLS INTERFACE s_axilite port=steps bundle=control
53     #pragma HLS INTERFACE s_axilite port=sims bundle=control
54     #pragma HLS INTERFACE s_axilite port=g_id bundle=control
55     #pragma HLS INTERFACE s_axilite port=return bundle=control
```

The code below allocates memory for storing pCall and pPut and create write only buffer for them.

```
604     cout << "All parameters are successfully generated. ";
605
606     cout << "HOST-Info: Allocating memory for h_call ... ";
607     void *ptr=nullptr;
608     if (posix_memalign(&ptr,4096,num_runs*sizeof(float))) {
609         cout << endl << "HOST-Error: Out of Memory during memory allocation for h_call" << endl << endl;
610         return EXIT_FAILURE;
611     }
612     cout << "h_call Allocated" << endl;
613     h_call = reinterpret_cast<float*>(ptr);
614
615     cout << endl;
616
617     cout << "HOST-Info: Allocating memory for h_put ... ";
618     if (posix_memalign(&ptr,4096,num_runs*sizeof(float))) {
619         cout << endl << "HOST-Error: Out of Memory during memory allocation for h_put" << endl << endl;
620         return EXIT_FAILURE;
621     }
622     cout << "h_put Allocated" << endl;
623     h_put = reinterpret_cast<float*>(ptr);
```

```

625 // -----
626 // Step 4.2: Create Buffers in Global Memory to store data
627 //         o) d_call    - stores h_call (W)
628 //         o) d_put     - stores h_put (W)
629 // -----
630 cl_mem d_call, d_put;
631
632 d_call = clCreateBuffer(Context, CL_MEM_WRITE_ONLY | CL_MEM_USE_HOST_PTR, num_runs * sizeof(float), \
633                          h_call, &errCode);
634 if (errCode != CL_SUCCESS) {
635     cout << endl << "Host-Error: Failed to allocate Global Memory for d_call" << endl << endl;
636     return EXIT_FAILURE;
637 }
638
639 d_put = clCreateBuffer(Context, CL_MEM_WRITE_ONLY | CL_MEM_USE_HOST_PTR, num_runs * sizeof(float), \
640                        h_put, &errCode);
641 if (errCode != CL_SUCCESS) {
642     cout << endl << "Host-Error: Failed to allocate Global Memory for d_put" << endl << endl;
643     return EXIT_FAILURE;
644 }

```

The code below prepares the rest of the parameters and set kernel arguments.

```

594 cout << "HOST-Info: generate parameters    ... ";
595 cl_float initprice = 100;                // -s
596 cl_float strikeprice = 110;              // -k
597 cl_float rate = 0.05;                   // -r
598 cl_float volatility = 0.2;              // -v
599 cl_float time = 1.0;                    // -t
600 int num_runs=16;
601 cl_uint sims = 1024, steps=1024;

```

```

668 int Nb_Of_Mem_Events = 4,
669     Nb_Of_Exe_Events = num_runs;
670
671 cl_event Mem_op_event[Nb_Of_Mem_Events],
672         K_exe_event[Nb_Of_Exe_Events];
673
674 #ifdef ALL_MESSAGES
675 cout << endl;
676 cout << "HOST-Info: ===== " << endl;
677 cout << "HOST-Info: (Step 5) Run Application " << endl;
678 cout << "HOST-Info: ===== " << endl;
679 #endif

```

```

681 // -----
682 // Step 5.1: Set Kernel Arguments
683 // -----
684 #ifdef ALL_MESSAGES
685 cout << "HOST-Info: Setting Kernel arguments ..." << endl;
686 #endif
687 errCode = false;
688
689 errCode |= clSetKernelArg(K_blackEuro, 0, sizeof(cl_mem), &d_call);
690 errCode |= clSetKernelArg(K_blackEuro, 1, sizeof(cl_mem), &d_put);
691 errCode |= clSetKernelArg(K_blackEuro, 2, sizeof(cl_float), &time);
692 errCode |= clSetKernelArg(K_blackEuro, 3, sizeof(cl_float), &rate);
693 errCode |= clSetKernelArg(K_blackEuro, 4, sizeof(cl_float), &volatility);
694 errCode |= clSetKernelArg(K_blackEuro, 5, sizeof(cl_float), &initprice);
695 errCode |= clSetKernelArg(K_blackEuro, 6, sizeof(cl_float), &strikeprice);
696 errCode |= clSetKernelArg(K_blackEuro, 7, sizeof(cl_uint), &steps);
697 errCode |= clSetKernelArg(K_blackEuro, 8, sizeof(cl_uint), &sims);
698
699 if (errCode != CL_SUCCESS) {
700     cout << endl << "Host-ERROR: Failed to set Kernel arguments from 0 to 8" << endl << endl;
701     return EXIT_FAILURE;
702 }

```

```

704 errCode = clEnqueueMigrateMemObjects(Command_Queue, 1, &d_call, CL_MIGRATE_MEM_OBJECT_CONTENT_UNDEFINED, \
705     0, NULL, &Mem_op_event[0]);
706 if (errCode != CL_SUCCESS) {
707     cout << endl << "Host-Error: Failed Migrate d_call without migrating content" << endl << endl;
708     return EXIT_FAILURE;
709 }
710
711 // -----
712
713 errCode = clEnqueueMigrateMemObjects(Command_Queue, 1, &d_put, CL_MIGRATE_MEM_OBJECT_CONTENT_UNDEFINED, \
714     0, NULL, &Mem_op_event[1]);
715 if (errCode != CL_SUCCESS) {
716     cout << endl << "Host-Error: Failed Migrate d_put without migrating content" << endl << endl;
717     return EXIT_FAILURE;
718 }

```

The code below is submitting kernel for execution

```

728 // -----
729 // Step 5.3: Submit Kernels for Execution
730 // -----
731
732 cout << "HOST-Info: Submitting Kernel K_blackEuro ..." << endl;
733 errCode = false;
734 for (int i=0; i < num_runs; i++) {
735     errCode |= clSetKernelArg(K_blackEuro, 9, sizeof(int), &i);
736     errCode |= clEnqueueTask(Command_Queue, K_blackEuro, 0, NULL, &K_exe_event[i]);
737 }
738 if (errCode != CL_SUCCESS) {
739     cout << endl << "HOST-Error: Failed to submit K_blackEuro" << endl << endl;
740     return EXIT_FAILURE;
741 }

```

## Kernel Function

HLS allocation:

The origin pragma has wrong syntax:

```

56 #pragma HLS ALLOCATION instances=mul limit=1 operation
57 #pragma HLS ALLOCATION instances=fmul limit=1 operation
58 #pragma HLS ALLOCATION instances=fexp limit=1 operation
59 #pragma HLS ALLOCATION instances=fdiv limit=1 operation

```



```

1 WARNING: [HLS 207-5551] unexpected pragma argument 'instances', expects function/operation
  (/users/course/2022S/HLS17000000/g110061562/final/Vitis_V3/blackEuro_kernels/src/launchSim.h:39:24)
1 WARNING: [HLS 207-5551] unexpected pragma argument 'instances', expects function/operation
  (/users/course/2022S/HLS17000000/g110061562/final/Vitis_V3/blackEuro_kernels/src/blackEuro.cpp:57:24)
1 WARNING: [HLS 207-5551] unexpected pragma argument 'instances', expects function/operation
  (/users/course/2022S/HLS17000000/g110061562/final/Vitis_V3/blackEuro_kernels/src/blackEuro.cpp:58:24)
1 WARNING: [HLS 207-5551] unexpected pragma argument 'instances', expects function/operation
  (/users/course/2022S/HLS17000000/g110061562/final/Vitis_V3/blackEuro_kernels/src/blackEuro.cpp:59:24)
1 WARNING: [HLS 207-5551] unexpected pragma argument 'instances', expects function/operation
  (/users/course/2022S/HLS17000000/g110061562/final/Vitis_V3/blackEuro_kernels/src/blackEuro.cpp:60:24)

```

The adjusted pragma:

```

62 #pragma HLS ALLOCATION operation instances=mul limit=1
63 #pragma HLS ALLOCATION operation instances=fmul limit=1
64 #pragma HLS ALLOCATION operation instances=fexp limit=1
65 #pragma HLS ALLOCATION operation instances=fdiv limit=1

```

Stream:

The origin pragma:

```

49 #pragma HLS STREAM variable=prices depth=NUM_SIMS dim=1
...
1 WARNING: [HLS 207-5505] the 'dim' option to 'Stream' pragma is not supported and will be ignored
  (/users/course/2022S/HLS17000000/g110061562/final/Vitis_V3/blackEuro_kernels/src/blackScholes.h:49:56)
1 WARNING: [HLS 207-5505] the 'dim' option to 'Stream' pragma is not supported and will be ignored
  (/users/course/2022S/HLS17000000/g110061562/final/Vitis_V3/blackEuro_kernels/src/launchSim.h:23:49)
1 WARNING: [HLS 207-5505] the 'dim' option to 'Stream' pragma is not supported and will be ignored
  (/users/course/2022S/HLS17000000/g110061562/final/Vitis_V3/blackEuro_kernels/src/launchSim.h:24:49)
1 WARNING: [HLS 207-5505] the 'dim' option to 'Stream' pragma is not supported and will be ignored
  (/users/course/2022S/HLS17000000/g110061562/final/Vitis_V3/blackEuro_kernels/src/launchSim.h:27:48)
1 WARNING: [HLS 207-5505] the 'dim' option to 'Stream' pragma is not supported and will be ignored
  (/users/course/2022S/HLS17000000/g110061562/final/Vitis_V3/blackEuro_kernels/src/launchSim.h:28:48)

```

The adjusted pragma:

```

50 #pragma HLS STREAM variable=prices depth=NUM_SIMS

```

Function extract:

The origin pragma:

```

95 {
96 #pragma HLS FUNCTION_EXTRACT
97 #pragma HLS DATAFLOW
98     launchSimulation(call0, put0, g_id+0, bs0, sims*steps>>4, sims>>4);
99     launchSimulation(call1, put1, g_id+1, bs1, sims*steps>>4, sims>>4);
100    launchSimulation(call2, put2, g_id+2, bs2, sims*steps>>4, sims>>4);
101    launchSimulation(call3, put3, g_id+3, bs3, sims*steps>>4, sims>>4);
102    launchSimulation(call4, put4, g_id+4, bs4, sims*steps>>4, sims>>4);
103    launchSimulation(call5, put5, g_id+5, bs5, sims*steps>>4, sims>>4);
104    launchSimulation(call6, put6, g_id+6, bs6, sims*steps>>4, sims>>4);
105    launchSimulation(call7, put7, g_id+7, bs7, sims*steps>>4, sims>>4);
106    launchSimulation(call8, put8, g_id+8, bs8, sims*steps>>4, sims>>4);
107    launchSimulation(call9, put9, g_id+9, bs9, sims*steps>>4, sims>>4);
108    launchSimulation(call10, put10, g_id+10, bs10, sims*steps>>4, sims>>4);
109    launchSimulation(call11, put11, g_id+11, bs11, sims*steps>>4, sims>>4);
110    launchSimulation(call12, put12, g_id+12, bs12, sims*steps>>4, sims>>4);
111    launchSimulation(call13, put13, g_id+13, bs13, sims*steps>>4, sims>>4);
112    launchSimulation(call14, put14, g_id+14, bs14, sims*steps>>4, sims>>4);
113    launchSimulation(call15, put15, g_id+15, bs15, sims*steps>>4, sims>>4);
114 }
...
1 WARNING: [HLS 207-5566] unknown HLS pragma ignored
  (/users/course/2022S/HLS17000000/g110061562/final/Vitis_V3/blackEuro_kernels/src/blackEuro.cpp:97:9)
1 WARNING: [HLS 207-5554] Only for-loops and functions support the dataflow
  (/users/course/2022S/HLS17000000/g110061562/final/Vitis_V3/blackEuro_kernels/src/blackEuro.cpp:98:9)

```

The adjusted pragma:



```

102 // {
103 // #pragma HLS FUNCTION_EXTRACT
104 // #pragma HLS DATAFLOW
105     launchSimulation(call0, put0, g_id+0, bs0, sims*steps>>4, sims>>4);
106     launchSimulation(call1, put1, g_id+1, bs1, sims*steps>>4, sims>>4);
107     launchSimulation(call2, put2, g_id+2, bs2, sims*steps>>4, sims>>4);
108     launchSimulation(call3, put3, g_id+3, bs3, sims*steps>>4, sims>>4);
109     launchSimulation(call4, put4, g_id+4, bs4, sims*steps>>4, sims>>4);
110     launchSimulation(call5, put5, g_id+5, bs5, sims*steps>>4, sims>>4);
111     launchSimulation(call6, put6, g_id+6, bs6, sims*steps>>4, sims>>4);
112     launchSimulation(call7, put7, g_id+7, bs7, sims*steps>>4, sims>>4);
113     launchSimulation(call8, put8, g_id+8, bs8, sims*steps>>4, sims>>4);
114     launchSimulation(call9, put9, g_id+9, bs9, sims*steps>>4, sims>>4);
115     launchSimulation(call10, put10, g_id+10, bs10, sims*steps>>4, sims>>4);
116     launchSimulation(call11, put11, g_id+11, bs11, sims*steps>>4, sims>>4);
117     launchSimulation(call12, put12, g_id+12, bs12, sims*steps>>4, sims>>4);
118     launchSimulation(call13, put13, g_id+13, bs13, sims*steps>>4, sims>>4);
119     launchSimulation(call14, put14, g_id+14, bs14, sims*steps>>4, sims>>4);
120     launchSimulation(call15, put15, g_id+15, bs15, sims*steps>>4, sims>>4);
121 // }

```

```

18     template<typename DATA_T, typename Model>
19     void launchSim(DATA_T &pCall, DATA_T &pPut, RNG<DATA_T> &rng0, RNG<DATA_T> &rng1, Model &m, int numR, int sims){
20     #pragma HLS function_instantiate variable=rng0
21     #pragma HLS DATAFLOW

```

I add function\_instantiate to make 16 launchSimulation run in parallel.

## Results

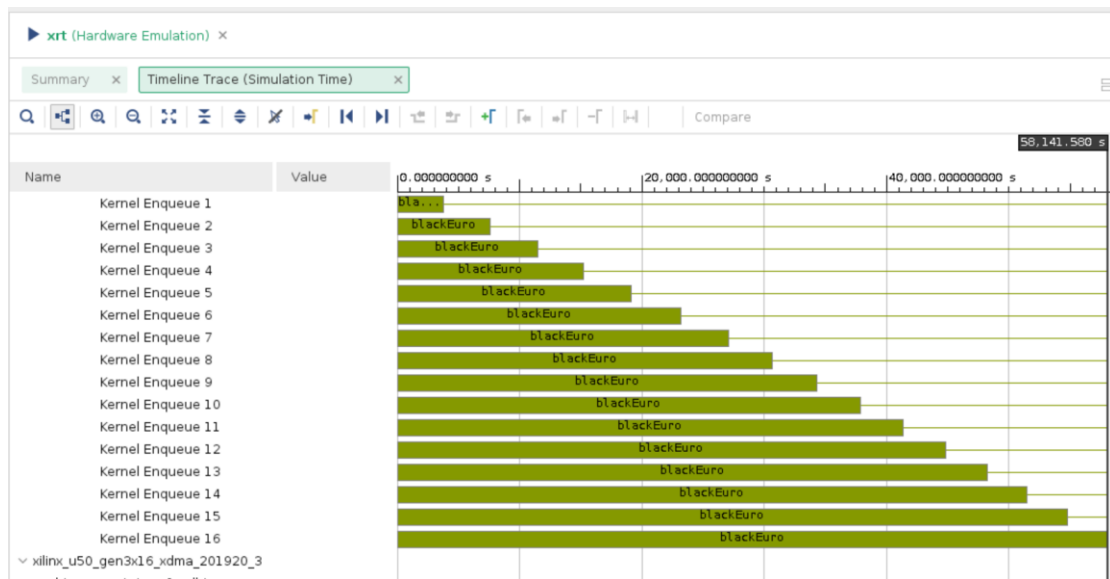
```

HOST_Info: Waiting for application to be completed ...
The 1st call price is 6.26604
The 1st put price is 10.8582
The 2nd call price is 6.4935
The 2nd put price is 10.7894
The 3th call price is 6.45818
The 3th put price is 10.7916
The 4th call price is 6.36644
The 4th put price is 11.173
The 5th call price is 6.3803
The 5th put price is 11.2333
The 6th call price is 6.42416
The 6th put price is 11.3428
The 7th call price is 6.49111
The 7th put price is 11.2489
The 8th call price is 6.46597
The 8th put price is 11.3446
The 9th call price is 6.28576
The 9th put price is 11.4276
The 10th call price is 6.26392
The 10th put price is 11.5545
The 11th call price is 1.34525e-43
The 11th put price is 1.66313e+22
The 12th call price is 6.31635
The 12th put price is 11.4937
The 13th call price is 6.40219

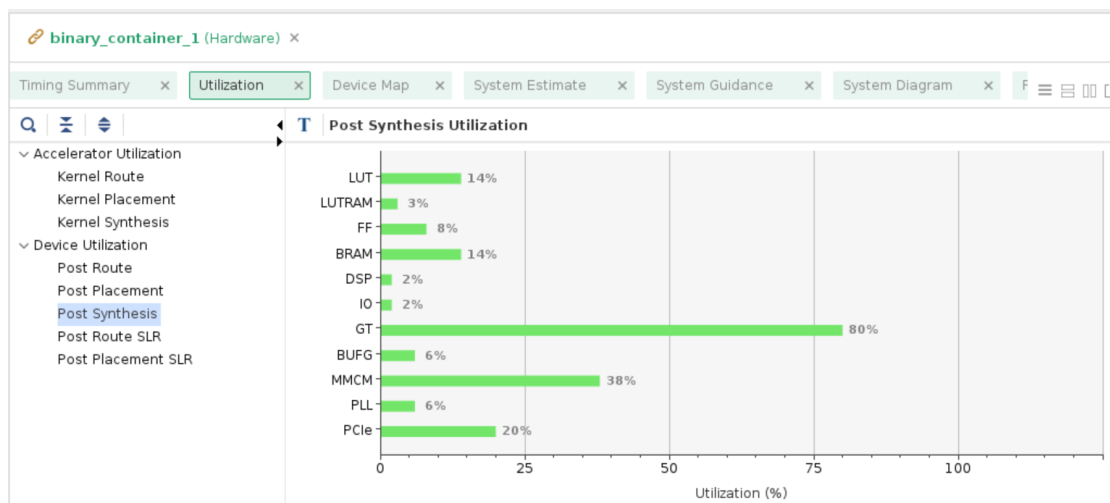
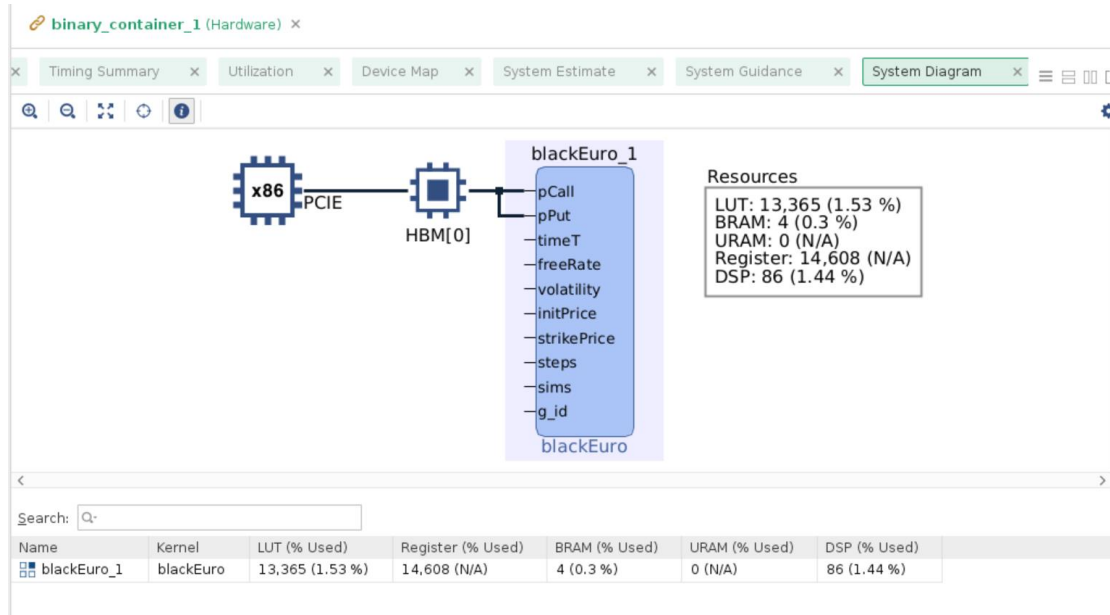
The 14th call price is 0
The 14th put price is 7.18483e+22
The 15th call price is 0
The 15th put price is 0
The 16th call price is 6.26251
The 16th put price is 11.8452
the sum of call price is: 82.8764
the sum of put price is: 8.84795e+22
the call price is: 4.92716    the difference with the reference value is 592.716%
the put price is: 5.26027e+21    the difference with the reference value is 1185.82%

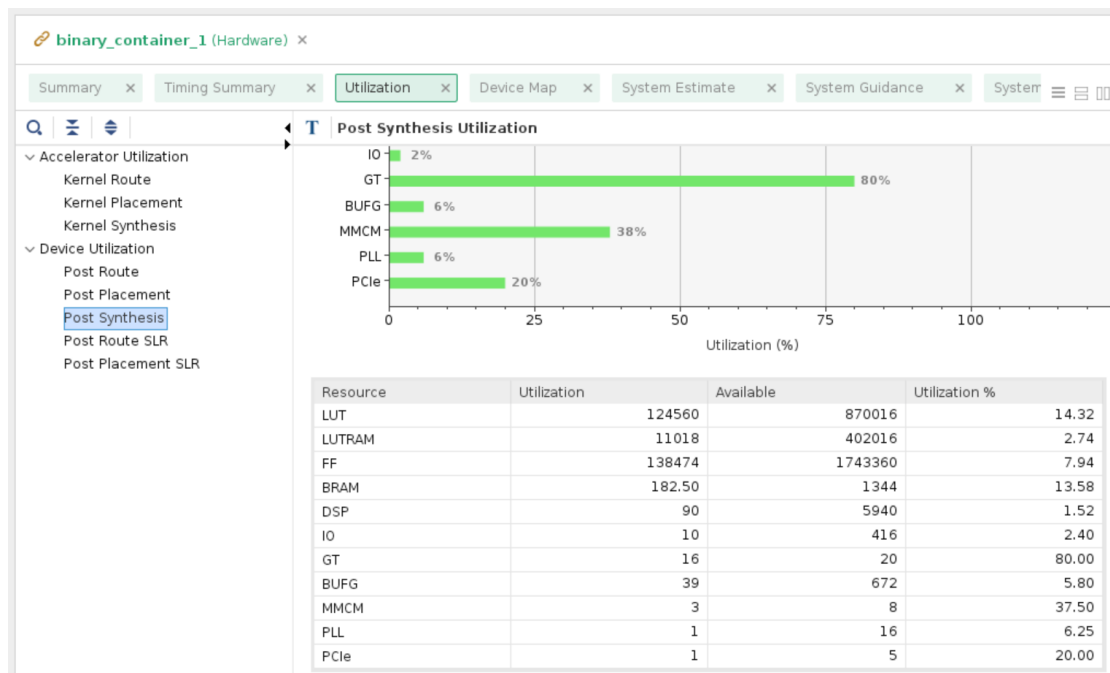
```

Hardware emulation timeline trace:



Hardware utilization:





binary\_container\_1 (Hardware) x

Timing Summary x **Utilization** x Device Map x System Estimate x System Guidance x System Diagram x F

Q [ ] [ ] [ ] T **Kernel Synthesis Utilization**

Accelerator Utilization

- Kernel Route
- Kernel Placement
- Kernel Synthesis**

Device Utilization

- Post Route
- Post Placement
- Post Synthesis
- Post Route SLR
- Post Placement SLR

Name	LUT	LUTAsMem	REG	BRAM	URAM	DSP
Platform	111195	9832	123868	178	0	4
User Budget	758821	392184	1619492	1166	640	5936
Used Resources	13365	1186	14608	4	0	86
Unused Resources	745456	390998	1604884	1162	640	5850
blackEuro (1)	13365	1186	14608	4	0	86
blackEuro_1	13365	1186	14608	4	0	86

binary\_container\_1 (Hardware) x

Timing Summary x **Utilization** x Device Map x System Estimate x System Guidance x System Diagram x F

Q [ ] [ ] [ ] T **Kernel Synthesis Utilization**

Accelerator Utilization

- Kernel Route
- Kernel Placement
- Kernel Synthesis**

Device Utilization

- Post Route
- Post Placement
- Post Synthesis
- Post Route SLR
- Post Placement SLR

Name	LUT	LUTAsMem	REG	BRAM	URAM	DSP
Platform	12.78%	2.45%	7.11%	13.24%	0.00%	0.07%
User Budget	100.00%	100.00%	100.00%	100.00%	100.00%	100.00%
Used Resources	1.76%	0.30%	0.90%	0.34%	0.00%	1.45%
Unused Resources	98.24%	99.70%	99.10%	99.66%	100.00%	98.55%
blackEuro (1)	1.76%	0.30%	0.90%	0.34%	0.00%	1.45%
blackEuro_1	1.76%	0.30%	0.90%	0.34%	0.00%	1.45%

## Reference

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10.1109/EMS.2016.036.

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<https://docs.xilinx.com/r/en-US/ug1399-vitis-hls/pragma-HLS-allocation>

<https://www.boledu.org/textbooks/hls-textbook/io-interface/axi-lite>

[https://github.com/dr-liangma/FinancialModels\\_AmazonF1](https://github.com/dr-liangma/FinancialModels_AmazonF1)