

Why teaching functional programming to undergraduates at CUNY is important

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If functors mean that something can be mapped over...

- then calling 'fmap' on a functor should
 - map a function over the functor

Functor Law intuition

If functors mean that something can be mapped over...

- then calling 'fmap' on a functor should
 - map a function over the functor
- Nothing else

The First Functor Laws

Definition (The First Functor Law)

states that if we map the identity (`id`) function over a functor, we get the functor

- $\text{fmap id} = \text{id}$

Identity in the Repl

Identity functions in the repl

```
fmap id (Just 3)
```

```
id (Just 3)
```

```
fmap id [1..5]
```

```
id [1..5]
```

```
fmap id []
```

```
fmap id Nothing
```

```
1==1
```

```
Just 3
```

```
Just 3
```

```
[1,2,3,4,5]
```

```
[1,2,3,4,5]
```

```
[]
```

```
Nothing
```

The Second Functor Law

Definition (The Second Functor Law says)

The Second Functor Law says that composing two functions and then mapping the composed function over a functor is the same as first mapping one function over the functor and then mapping the other one.

- $\text{fmap } (f.g) = \text{fmap } f . \text{fmap } g$
- $\text{fmap } (f.g) F = \text{fmap } f (\text{fmap } g F)$

Composition in the Repl

Composition functions in the repl

```
fmap ((+1).(*2)) (Just 3)
fmap (+1) (fmap (*2) (Just 3))
fmap ((+1).(*2)) [1..5]
fmap (+1) (fmap (*2) [1..5])
1==1
```

```
Just 7
```

```
Just 7
```

```
[3,5,7,9,11]
```

```
[3,5,7,9,11]
```