

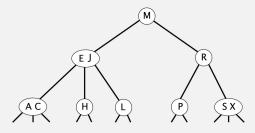
## 2-3 tree demo

#### Search.

- Compare search key against key(s) in node.
- Find interval containing search key.
- · Follow associated link (recursively).



search for H

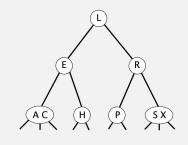


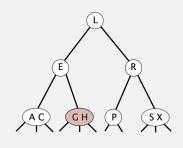
## 2-3 tree: insertion

Insertion into a 2-node at bottom.

• Add new key to 2-node to create a 3-node.

#### insert G



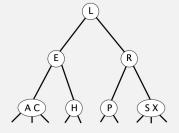


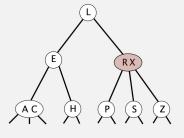
## 2-3 tree: insertion

### Insertion into a 3-node at bottom.

- Add new key to 3-node to create temporary 4-node.
- Move middle key in 4-node into parent.
- · Repeat up the tree, as necessary.
- If you reach the root and it's a 4-node, split it into three 2-nodes.

#### insert Z





## 2-3 tree construction demo



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# Balanced search trees: quiz 2



What is the maximum height of a 2-3 tree with n keys?

- A.  $\sim \log_3 n$
- **B.**  $\sim \log_2 n$
- C.  $\sim 2 \log_2 n$
- D. ~

ST implementations: summary

implementation	guarantee			average case			ordered	key
	search	insert	delete	search	insert	delete	ops?	interface
sequential search (unordered list)	n	n	n	n	n	n		equals()
binary search (ordered array)	$\log n$	n	n	$\log n$	n	n	V	compareTo()
BST	n	n	n	$\log n$	$\log n$	$\sqrt{n}$	~	compareTo()
2-3 tree	$\log n$	$\log n$	$\log n$	log n	log n	log n	~	compareTo()
but hidden constant $c$ is large (depends upon implementation)								
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# 2-3 tree: performance

Perfect balance. Every path from root to null link has same length.



## Tree height.

Min: log<sub>3</sub> n ≈ 0.631 log<sub>2</sub> n. [all 3-nodes]
 Max: log<sub>2</sub> n. [all 2-nodes]

- Between 12 and 20 for a million nodes.
- Between 18 and 30 for a billion nodes.

Bottom line. Guaranteed logarithmic performance for search and insert.

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# 2-3 tree: implementation?

### Direct implementation is complicated, because:

- · Maintaining multiple node types is cumbersome.
- · Need multiple compares to move down tree.
- Need to move back up the tree to split 4-nodes.
- · Large number of cases for splitting.

#### fantasy code

```
public void put(Key key, Value val)
{
  Node x = root;
  while (x.getTheCorrectChild(key) != null)
  {
      x = x.getTheCorrectChild(key();
      if (x.is4Node()) x.split();
    }
  if (x.is2Node()) x.make3Node(key, val);
  else if (x.is3Node()) x.make4Node(key, val);
}
```

Bottom line. Could do it, but there's a better way.

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