CSC 212: Data Structures and Abstractions Binary Search Trees

Marco Alvarez

Department of Computer Science and Statistics University of Rhode Island

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k-ary Trees

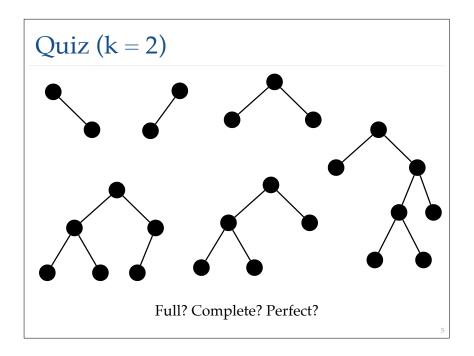
Quick notes

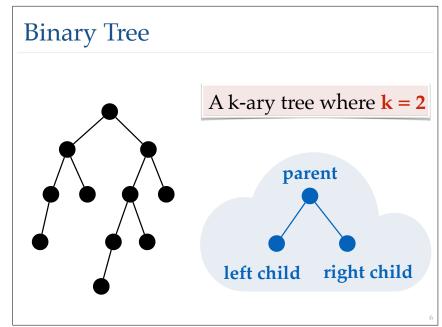
- Final Project (about 5 weeks)
 - √ requires planning and long coding hours
 - ✓ there is a lot to learn
- · Team Work
 - √ motivate each other
 - ✓ all team members must understand the topic and code
 - a presentation to the class will follow by the end of the semester
- Info Session (optional)
 - √ tomorrow during lab hours

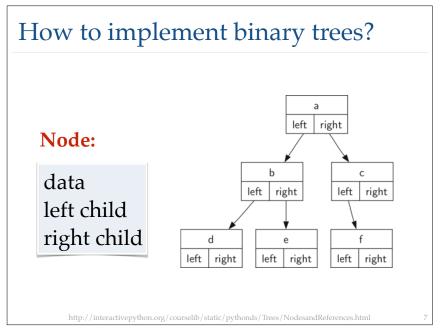
k-ary Trees

- In a **k-ary tree**, every node has between 0 and k children
- In a **full (proper)** k-ary tree, every node has exactly 0 or k children
- In a **complete** k-ary tree, every level is entirely filled, except possibly the deepest, where all nodes are as far left as possible
- In a **perfect** k-ary tree, every leaf has the same depth and the tree is full

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Binary Search Trees

Binary Search Tree

- A BST is a binary tree
- · A BST has symmetric order
 - \checkmark each node x in a BST has a key key(x)
 - \checkmark for all nodes y in the left subtree of x, key(y) < key(x) **
 - \checkmark for all nodes y in the right subtree of x, key(y) > key(x) **

(**) assume that the keys of a BST are pairwise distinct

```
50
20
40
60
80
75
```

```
class BSTNode {
    private:
        int data;
        BSTNode *left;
        BSTNode *right;

    public:
        BSTNode(int d);
        ~BSTNode();

    friend class BSTree;
};
```

```
class BSTree {
    private:
        BSTNode *root;
    void destroy(BSTNode *p);

public:
    BSTree();
    ~BSTree();

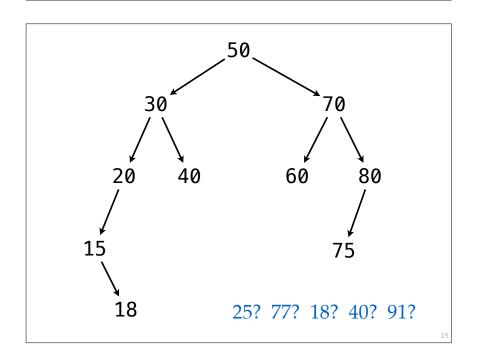
    void insert(int d);
    void remove(int d);
    BSTNode *search(int d);
};
```

Search into BSTs

Search

- · Start at root node
- If the search key matches the current node's key then **found**
- If search key is greater than current node's key search on right child
- If search key is less than current node's search on left child
- Stop when current node is NULL (not found)

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Insert into BSTs

Insert

- · Perform a Search operation
- If **found**, no need to insert (may increase counter)
- If **not found**, insert node where Search stopped

50 70 20 40 60 80 75 18 65? 27? 90? 11? 51?

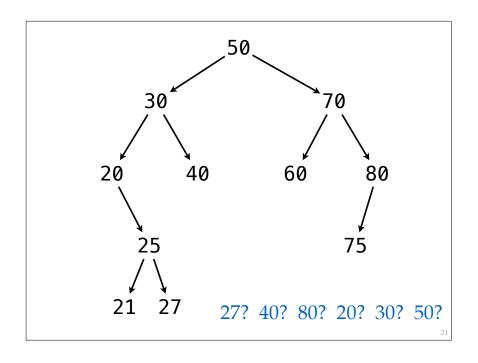
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Remove from BSTs

Remove

- Case 1: node is a leaf
 - √ trivial, delete node and set parent's pointer to NULL
- Case 2: node has 1 child
 - ' trivial, set parent's pointer to the only child and delete node
- Case 3: node has 2 children
 - find **successor** can also use predecessor
 - √ copy successor's data to node
 - √ delete successor

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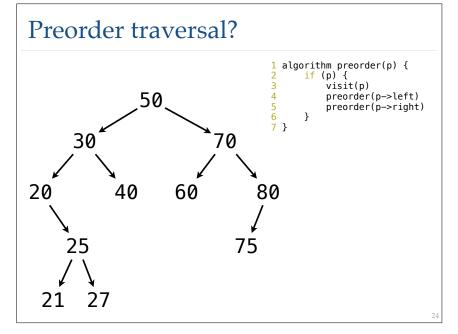
BST Traversals

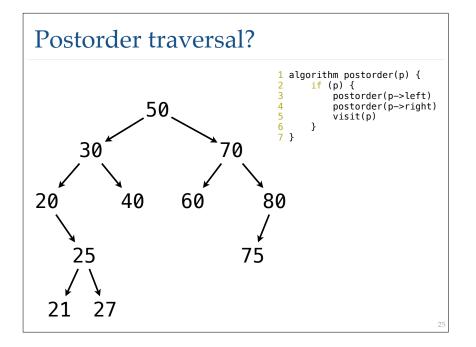
Traversals • Preorder traversal

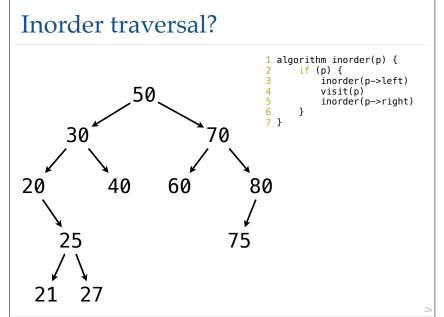
· Inorder traversal



· Postorder traversal



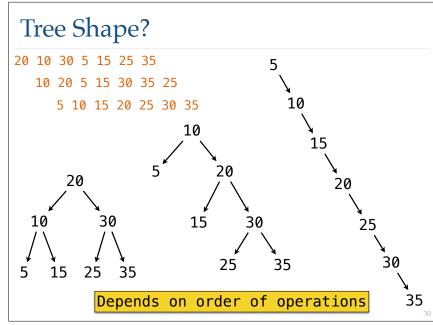


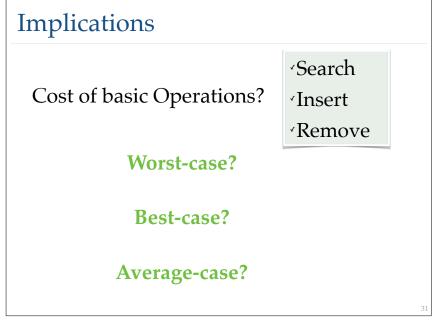


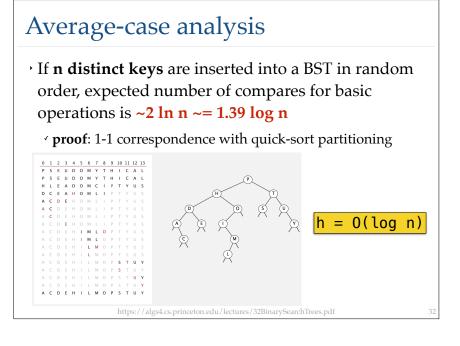
How to destroy a binary tree?

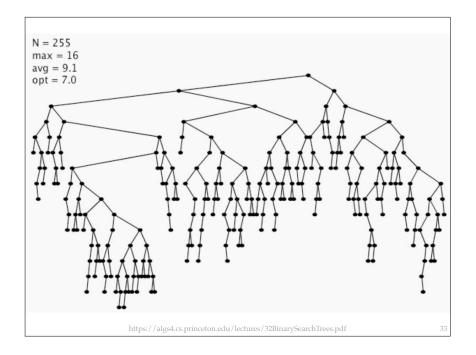
How to print all elements in increasing order?











Collections/Dictionaries

	What?	Sequential (unordered)	Sequential (ordered)	BST
search	search for a key	0(n)	O(log n)	0(h)
insert	insert a key	0(n)	0(n)	0(h)
delete	delete a key	0(n)	0(n)	0(h)
min/max	smallest/largest key	0(n)	0(1)	0(h)
floor/ ceiling	predecessor/ successor	0(n)	O(log n)	0(h)
rank	number of keys less than key	0(n)	O(log n)	0(h)**

(**) requires the use of 'size' at every node

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