

CS 2200 Spring 2019 HW 05

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Due Tuesday, April 2, 2019, 11:59PM

Submit your HW as a SINGLE PDF file that includes your answers, your programs, and their output. Also include any data files if you used them. Please make sure that your PDF is well-organized so we can quickly find all the pieces of each problem that belong together.

PROBLEMS

1. (10 points) Find a deterministic finite-state automaton that recognizes the language, L , consisting of all strings in $\{a, b\}^*$ that contain an odd number of b 's such that there is at least one a between every two b 's in the string. Verify your solution by running some non-trivial cases on your simulator. Include your graphviz drawing, your `.gv` file, and your `.ndfsa` file.
2. (5 points) Construct a regular expression that generates the language, L , defined in Problem 1.
3. (10 points) Let $A = \{c, d\}$. Let $L_2 \subseteq A^*$ be the language consisting of all strings not in the language, L_3 , which is generated by the regular expression $c^*d^*c^*$. Find a deterministic finite-state automaton that recognizes L_2 . Verify your solution by running some non-trivial cases on your simulator. Include your graphviz drawing, your `.gv` file, and your `.ndfsa` file.
4. (5 points) Find a regular expression that generates the language, L_2 , defined in Problem 3
5. (10 points) Let $L_3 \subseteq \{f, g\}^*$ be the language of all strings generated by the regular expression $(fg + ffg + fgf)^*$. Construct a non-deterministic finite-state machine that recognizes L_3 . Verify your solution by running some non-trivial cases on your simulator. Include your graphviz drawing, your `.gv` file, and your `.ndfsa` file.
6. (10 points) Using the subset construction described in class, construct a deterministic finite-state machine based on the non-deterministic finite-state machine that

you constructed in Problem 5. Verify your solution by running some non-trivial cases on your simulator. Include your graphviz drawing, your .gv file, and your .fsa file.

7. (10 points) Let G be the context-free grammar $\{ \{Q, V\}, \{c, d\}, \{ Q \rightarrow QQ|V, V \rightarrow cVd|cd \}, Q \}$.
 - (a) (5 points) Describe the language $L_6 = L(G)$. Prove that G is ambiguous.
 - (b) (5 points) Give an unambiguous grammar H , such that $L(H) = L(G)$. Give some justification for the claim that H is unambiguous.
8. (20 points) Consider the CFG $G = \{ \{S\}, \{a, b\}, \{S \rightarrow aSbS|bSaS|\epsilon\}, S \}$. Prove by induction that $L(G) = \{ w \in \{a, b\}^* \mid \text{the number of a's in } w = \text{the number of b's in } w \}$. Note that there are two things to prove here. First, you have to prove that if a string of terminals is generated by G , then the number of a's in it is equal to the number of b's. Second, you have to prove that if a string of a's and b's has an equal number of a's and b's, then it can be generated by G .
9. (20 points) Let $G = (\text{Vars}, \text{Alph}, \text{Rules}, \text{Start})$ be a CFG as described below. Using the algorithms discussed in class, convert G into an equivalent grammar that is in Chomsky Normal Form.
 - (a) $\text{Vars} = \{ P, Q, R, S, T, U, V, W, X, Y, Z \}$.
 - (b) $\text{Alph} = \{ a, b, c \}$.
 - (c) $\text{Start} = S$.
 - (d) $\text{Rules} =$
 - i. $S \rightarrow aXT|YbT|UbZ|UWc|PQT$.
 - ii. $P \rightarrow aT$.
 - iii. $Q \rightarrow QT|aQ$.
 - iv. $T \rightarrow cT|\epsilon$.
 - v. $U \rightarrow aU|\epsilon$.
 - vi. $X \rightarrow aX|R|\epsilon$.
 - vii. $R \rightarrow aRb|\epsilon$.
 - viii. $Y \rightarrow Yb|R|\epsilon$.
 - ix. $V \rightarrow bVc|\epsilon$.
 - x. $W \rightarrow Wc|V|\epsilon$.
 - xi. $Z \rightarrow bZ|V|\epsilon$.