

1. Αξιολόγηση & Μετρικές

Confusion Matrix: $Acc = \frac{TP+TN}{N}$ | $Prec = \frac{TP}{TP+FP}$
 $Rec = \frac{TP}{TP+FN}$ | $Spec = \frac{TN}{TN+FP}$ | $F1 = \frac{2PR}{P+R}$.
Medical Bayes: $\frac{P(Disease|+)}{P(Disease|+) + \frac{Sens \cdot Prev}{Sens \cdot Prev + (1-Spec)(1-Prev)}}$ =
Errors: $MSE = \frac{1}{N} \sum (y - \hat{y})^2$. $R^2 = 1 - \frac{RSS}{TSS}$.
Bias-Var: $Err = Bias^2 + Var + Noise$.
• High Bias \rightarrow Underfit (Simple). • High Var \rightarrow Overfit (Complex).
ROC/AUC: Plot TPR vs FPR. Random=0.5, Perfect=1.
Cross-Val: k-Fold (Low Bias/Var est), Hold-out (Fast).

2. Probabilities & Info

Bayes: $P(h|d) \propto P(d|h)P(h)$ (Post Lik Prior).
Bayes Risk: Choose action w/ min exp. loss.
Gauss: $\mathcal{N} \sim |\Sigma|^{-1/2} e^{-\frac{1}{2}(x-\mu)^T \Sigma^{-1}(x-\mu)}$.
MLE: $\hat{\mu} = \bar{x}$, $\hat{\sigma}^2 = \frac{1}{N} \sum (x-\mu)^2$ (Biased). Unbiased: divide $N-1$.
Entropy: $H(P) = -\sum P \log P$. Max at uniform.
KL Div: $D_{KL} = \sum P \ln \frac{P}{Q}$. **CrossEnt:** $H(P, Q) = H(P) + D_{KL}$.
MLE: $\max \sum \ln P(x|\theta)$. $\nabla \ln L = 0$.

3. Γραμμικά Μοντέλα

LinReg: $w = (X^T X)^{-1} X^T y$. ($O(N^3)$).
LogReg: $P = \sigma(w^T x) = \frac{1}{1+e^{-z}}$. Convex Loss.
 $\sigma' = \sigma(1-\sigma)$. Update: $w \leftarrow w + \eta(y - \hat{y})x$.
LDA: Max Sep $J(w) = \frac{w^T S_B w}{w^T S_W w}$.
 $S_B = (m_2 - m_1)(m_2 - m_1)^T$. $S_W = \sum S_i$.
Opt: $w \propto S_W^{-1}(m_2 - m_1)$. Assumes equal Σ .
Geometry: Hyperplane $w^T x + w_0 = 0$.
Dist $r = y(x)/\|w\|$. $w \perp$ surface.
Regularization (Shrinkage):
L1 (Lasso): $\lambda|w|$ (Sparsity/Selection).
L2 (Ridge): λw^2 (Small weights).

4. SVM & Kernels

Primal: $\min \frac{1}{2}\|w\|^2 + C \sum \xi_i$ s.t. $y_i(w^T x_i + b) \geq 1 - \xi_i$.
Convex: Global minimum guaranteed.
Support Vectors: Points on margin ($y(\cdot) = 1$) or errors. Only these affect w .
Margin: $2/\|w\|$. Larger $C \rightarrow$ Harder (Sm margin).
Slacks ξ : 0 (correct), $0 < \xi < 1$ (margin vio), $\xi > 1$ (error).
Kernel Trick: $x^T z \rightarrow K(x, z)$. Implicit high dim.
• Poly: $(x^T z + c)^d$. Dim $\approx d$ -order terms.
• RBF: $e^{-\gamma\|x-z\|^2}$. Dim ∞ . (Taylor exp).
Geometry: Max margin boundary is \perp bisector of closest points from classes.

5. Neural Networks

Non-Convex: Local optima possible.
Unit: $z = \sum w_i x_i + b \rightarrow a = g(z)$.
Activ: ReLU $\max(0, z)$ (Fast, no vanish grad).
Sigmoid $(0,1)$, Tanh $(-1,1)$ (Sat at limits).
Softmax: $y_k = e^{z_k} / \sum e^{z_j}$. For Multi-class.
Forward: $Z^{[l]} = W^{[l]} A^{[l-1]} + b^{[l]}$, $A^{[l]} = g(Z^{[l]})$.
Backprop: Chain rule $\frac{\partial J}{\partial W}$.
 $\delta^L = (a^L - y)$, $\delta^l = (W^{l+1})^T \delta^{l+1} \cdot g'(z^l)$.
 $\partial J / \partial W^l = \delta^l (a^{l-1})^T$.
Params: FC: $(N_{in} + 1)N_{out}$.
CNN: $Out = \lfloor \frac{W-K+2P}{S} \rfloor + 1$.
Params: $F \times F \times C_{in} \times C_{out} + C_{out}$.
Optim: SGD (Noisy), Batch (Slow), Mini-batch.
Momentum (Velocity), Adam (Adapt LR).

6. Ensembles

Bagging: Bootstrap (replace) + Parallel Models.
Reduces **Variance**. Ex: Random Forest.
Random Forest: Bagging + Feature subset (\sqrt{p}).
Decorrelates trees \rightarrow Better reduction of var.
Boosting: Sequential. Fix prev errors.
Reduces **Bias** (and Var). Ex: AdaBoost, XGB.
AdaBoost: Weights $\alpha_t = \frac{1}{2} \ln \frac{1-\epsilon}{\epsilon}$.
Data weights $D_{t+1} \propto D_t e^{-\alpha y \hat{y}}$ (Focus Hard).

Trees: Split: Max InfoGain ($H_{pre} - H_{post}$).

Entropy $= -\sum p \log p$, Gini $1 - \sum p^2$.

7. Unsupervised & PCA

PCA: Max Variance directions (Ortho).
1. Center ($x - \mu$). 2. Cov $\Sigma = \frac{1}{N} X^T X$. 3. Eigendecomp $U \Lambda U^T$.
Proj $z = U_k^T x$. Var ratio $\sum_1^k \lambda_i / \sum \lambda_{all}$.
Included '1' feature doesn't change PCA (const var=0).
K-Means: Iterate: Assign closest, Update centroids.
Converges finite steps. Spherical clusters. Sensitive to K/Init.
GMM: Soft K-means. Probabilistic (π, μ, Σ).
EM Algo: Max Likelihood (local max).
E-step: Calc responsibilities γ . M-step: Update params.
DBSCAN: Density. core/horder/noise. Args: eps, minPts.
Hierarchical: Agglomerative.
Linkage: Single (min dist), Complete (max), Avg.
Silhouette: $\frac{b-a}{\max(a,b)}$. +1 Good, 0 Border, -1 Wrong.

8. KNN & Dim Reduction

KNN: Lazy. Distances (L_2).
Small $k \rightarrow$ High Var (Noise). Large $k \rightarrow$ High Bias (Smooth).
Curse of Dim: Vol grows exp. Points equidistant.
Need exp data. Solutions: PCA, Feature Sel.

9. True/False Exam Bible (1/2)

-- SVM Objective: Convex Quadratic (Global Min).
-- NN Objective: Non-Convex (Local Min).
-- EM Algo: Maximizes Likelihood (Local Max).
-- K-Means: Loss decreases monotonically. Converges.
-- RBF Feature Space: Infinite dimensional.
-- PCA: Adding const feature \rightarrow No change.
-- Perceptron: Oscillates if not lin sep.
-- Hard Margin SVM: Requires lin sep.
-- Bootstrapping: Sampling WITH replacement.

10. True/False Exam Bible (2/2)

-- L1 Reg: Sparsity (Feat Sel). L2: Small weights.
-- Bias-Var: 1-NN (High Var), K-NN (High Bias).
-- Kernel Trick: w is lin comb of data (Representer).
-- Softmax: Used for Multi-class Output.
-- Linear Activ in Hidden: Collapse to linear model.
-- Generative: Naive Bayes, GMM, LDA.
-- Discriminative: LogReg, SVM, NN, KNN.
-- Decision Trees: Pruning reduces overfitting.

11. Quick Math/Formulas

Logarithms: $\ln(xy) = \ln x + \ln y$, $\ln(e^x) = x$.
Derivatives: $\frac{d}{dx} \sigma(x) = \sigma(1-\sigma)$.
Matrix: $(AB)^T = B^T A^T$. $\nabla_x w^T x = w$.
 $\nabla_x x^T A x = (A + A^T)x$.
Distances: L_1 Manhattan $\sum |x|$, L_2 Euclidean $\sqrt{\sum x^2}$.
Eigen: $A v = \lambda v$. $\det(A - \lambda I) = 0$.
Normal: 68% (1σ), 95% (2σ), 99.7% (3σ).

12. Algorithm Summary

Naive Bayes: $P(y|x) \propto P(y) \prod P(x_i|y)$. Fast, High Bias.
LogReg: Linear boundary. Interpretable. P-values.
SVM: Max Margin. Robust. Kernels \rightarrow Non-Lin.
DT: Non-parametric. Interp. Orthogonal splits.
RF/GDM: Black-box. High Acc. Robust.
NN: Univ approx. Needs data/compute. Non-convex.
K-Means: Simple. Scalable. Convex clusters only.