

# Using a Stochastic Optimal Control Framework to Model the Control of Complex Human Movement: *Application to an Aerial Acrobatics*

Eve Charbonneau\*,<sup>1</sup>, Friedl De Groot<sup>2</sup>, Mickaël Begon<sup>1</sup>

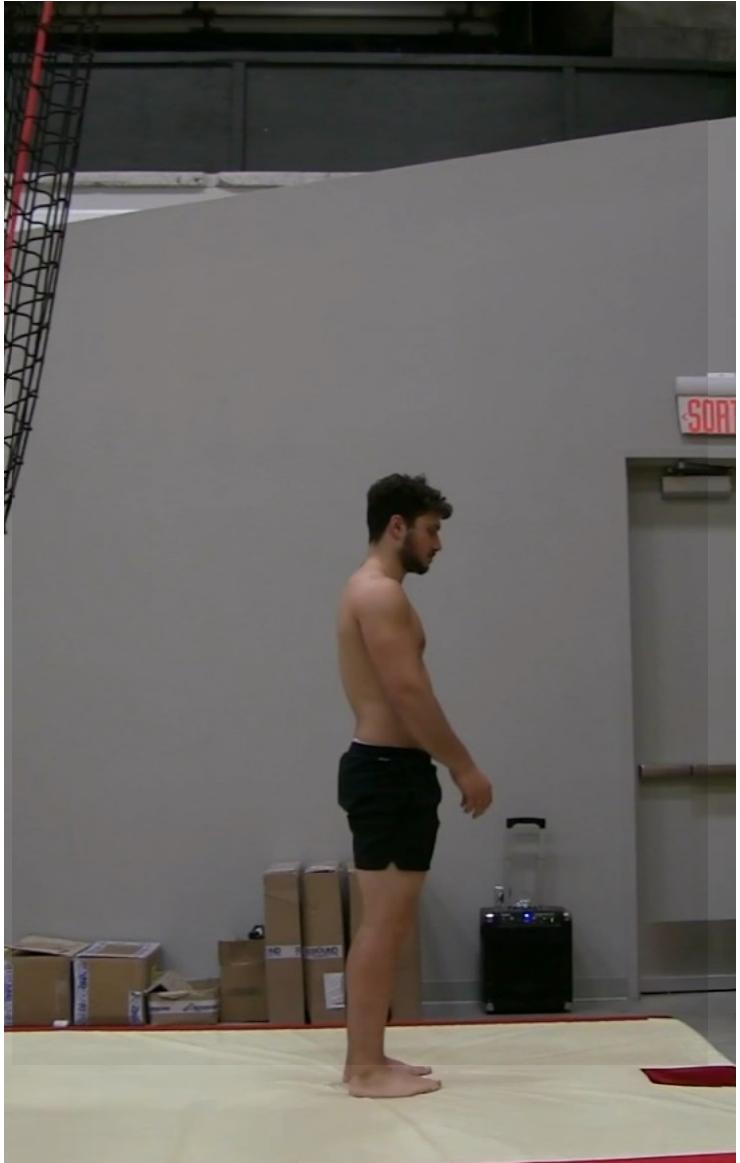
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# Project context



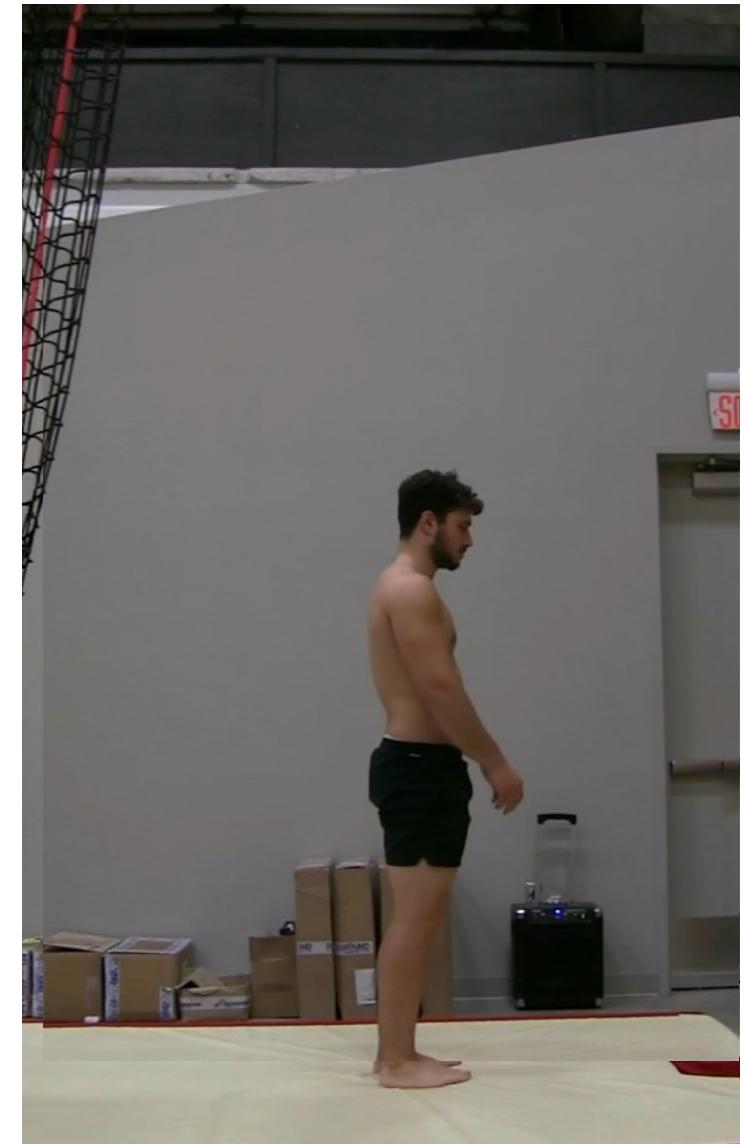
## What is limiting performance?

- Lack of strength
  - Lack of power
  - Lack of flexibility
- 
- Bad acrobatic technique
- 
- Poor coordination
  - Poor perception of spatial orientation
- } Physical conditioning
- } Change of technique
- } Sport-specific exercises

**Predictive simulations** can answer this question  
using “*what if*” scenarios

# How do athletes choose their strategy?

- Complete the acrobatic
    - ↳ Reach landing position
    - ↳ Adjust moment of inertia
  - Succeed consistently
    - ↳ Motor variability
    - ↳ Sensory feedback
  - Adjust the motor plan
    - ↳ Looking at the landing spot
    - ↳ Feedforward
- } Task description +  
Skeletal model
- } Feedback +  
Motor & sensory noise
- } Feedforward +  
Vision



# Literature

## Biomechanics

### Optimal Control theory

*Chow, C. K., & Jacobson, D. H. (1971)*  
*Ghosh, T. K., & Boykin Jr, W. H. (1976)*  
*Hatze, H. (1976)*

Goal: finding optimal motion

Open loop motor command

Complex musculoskeletal models  
and  
Complex movements

...but are these techniques feasible?

## Motor control

### Optimal Feedback Control theory

*Todorov, E., & Jordan, M. I. (2002)*

Goal: finding optimal feedback gains

Closed loop motor control policy  
Robust to motor and sensory noises

Simple models

...but is the model representative  
of the human movement ?

## Motor learning

### Perception-Action Coordination theory

*Gibson, J.J. (1979)*

Goal: Determining the role of  
perception & action in the  
execution of movements

Closed loop motor control policy where  
action is perceptually guided  
and perception is action-oriented

No model

...but how do we predict these  
sensory-motor strategies?

## Optimal Control theory



# Literature

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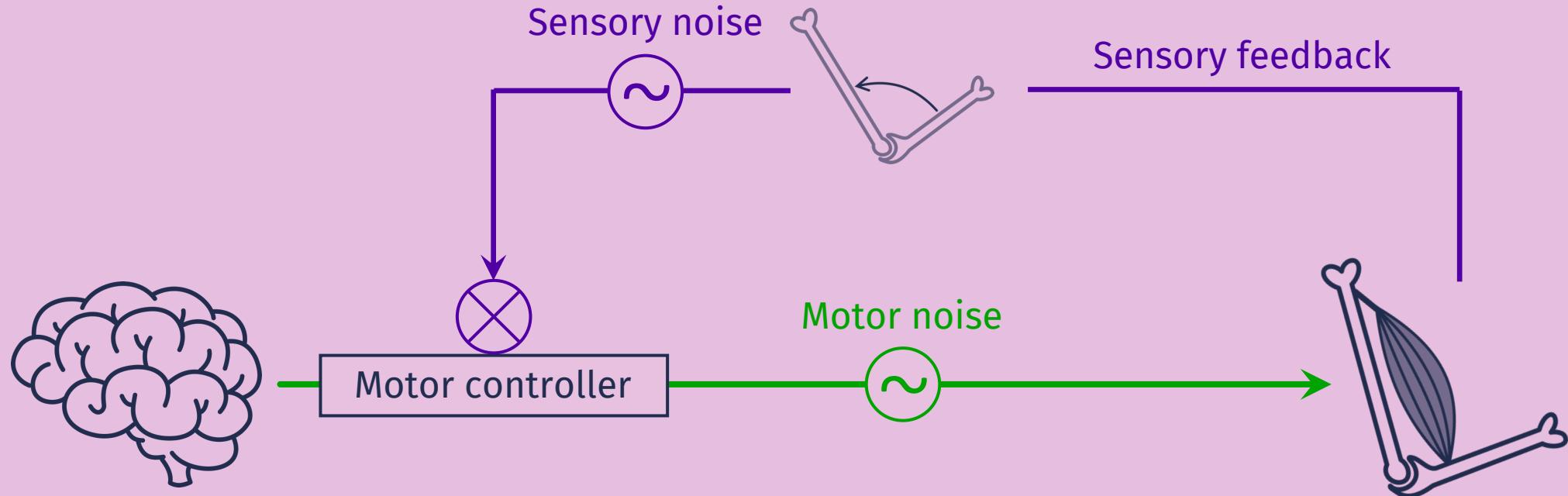
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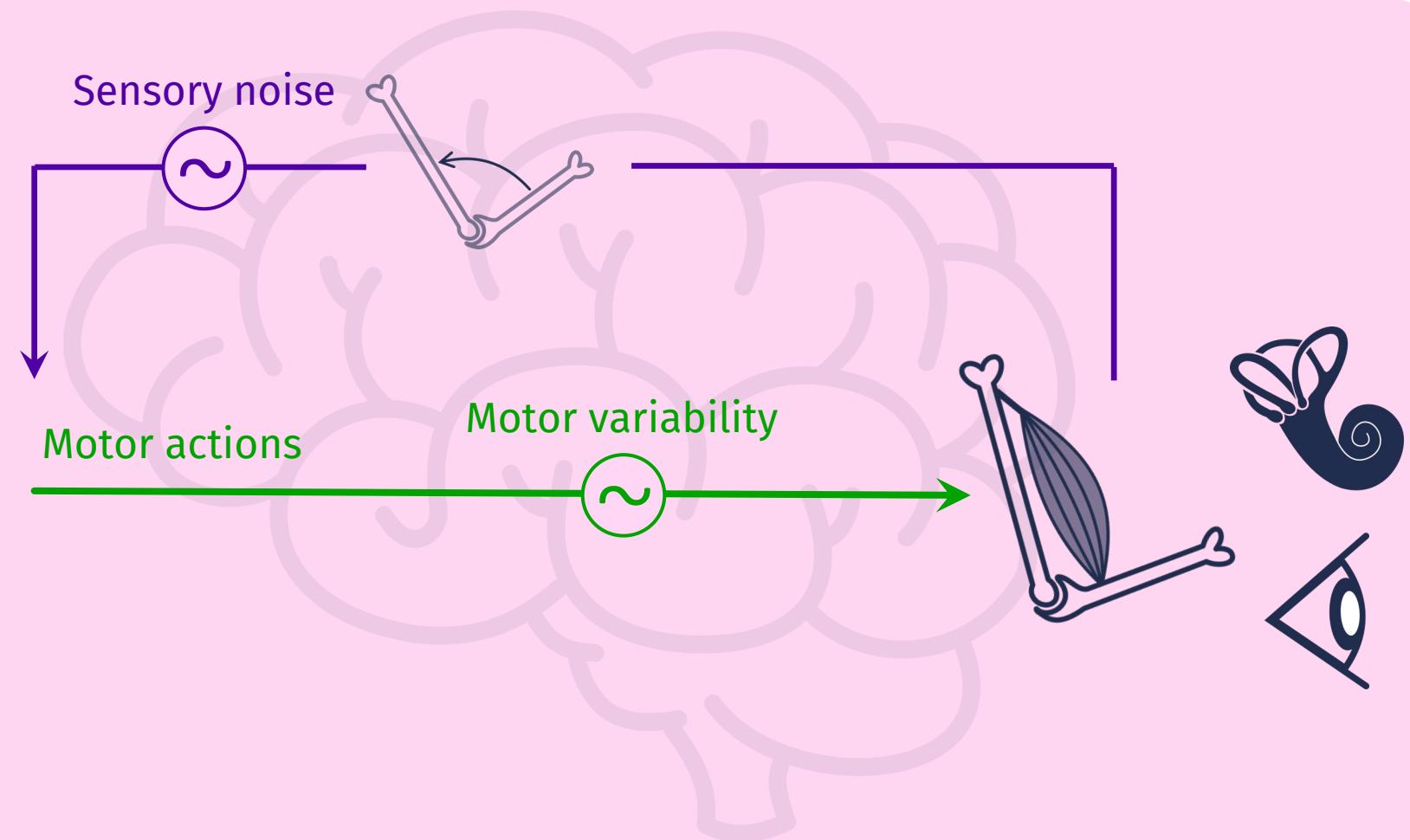
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## *Current study*

*Van Wouwe, T., Ting, L. H., & De Groot, F. (2022)*

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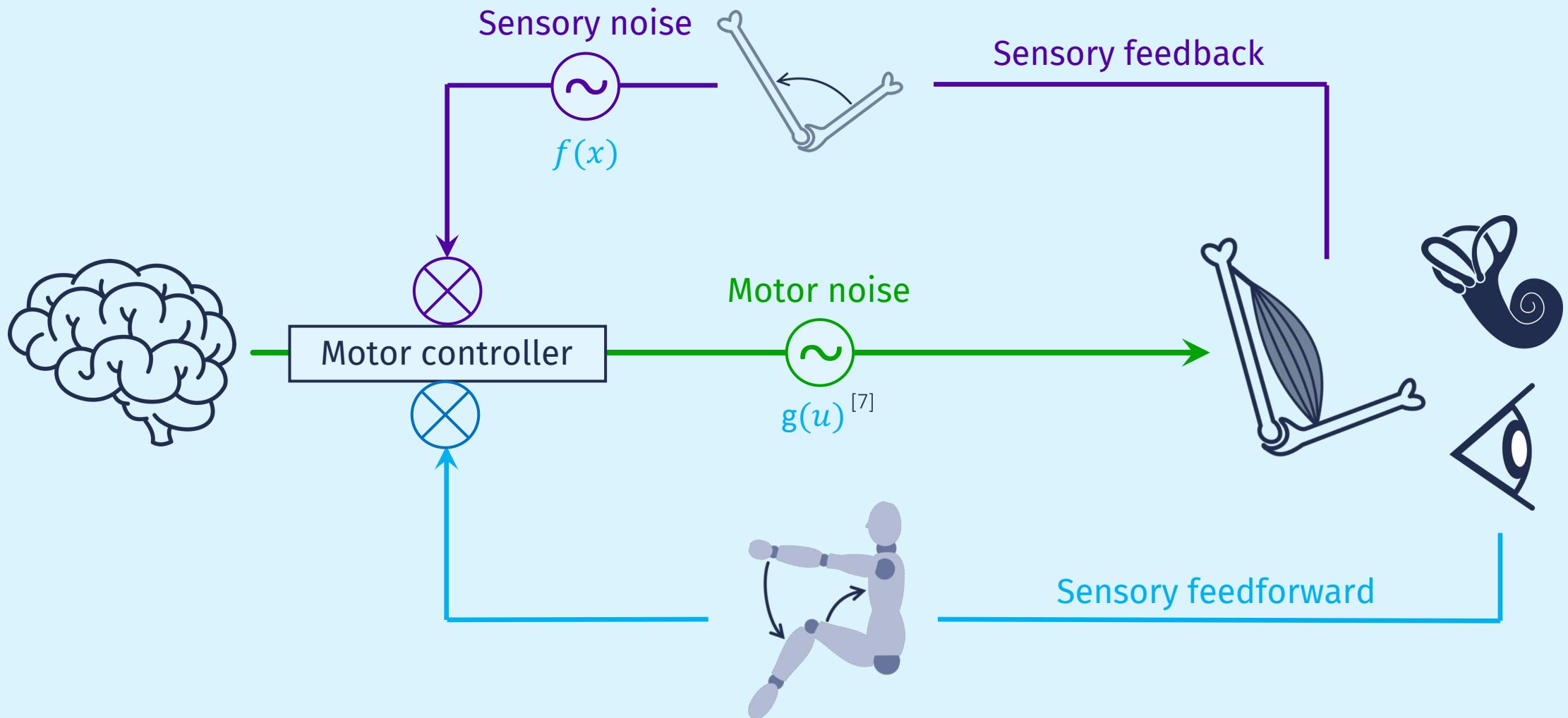
*Current study*

**Goal:** Mix these three theories together in a numerical method for stochastic predictive simulations.

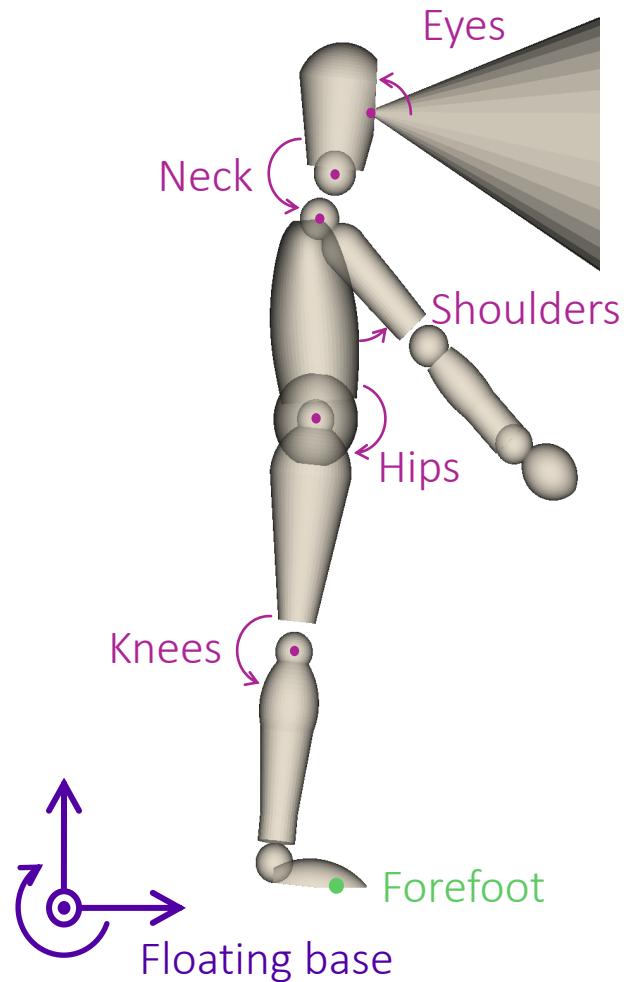
High numerical complexity → computational tricks

**Goal:** Mix these three theories together in a numerical method for stochastic predictive simulations.

High numerical complexity → computational tricks



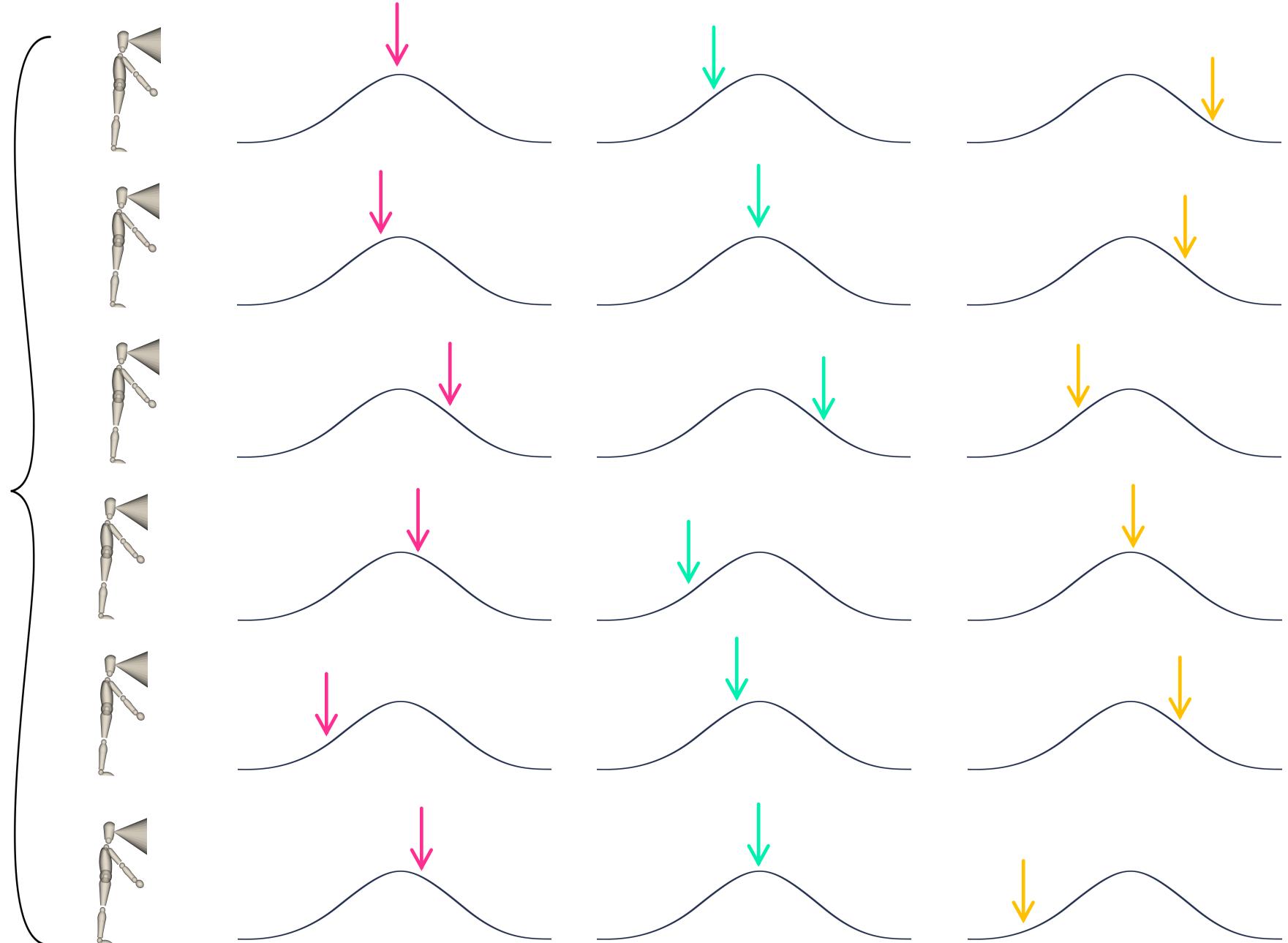
# Methods



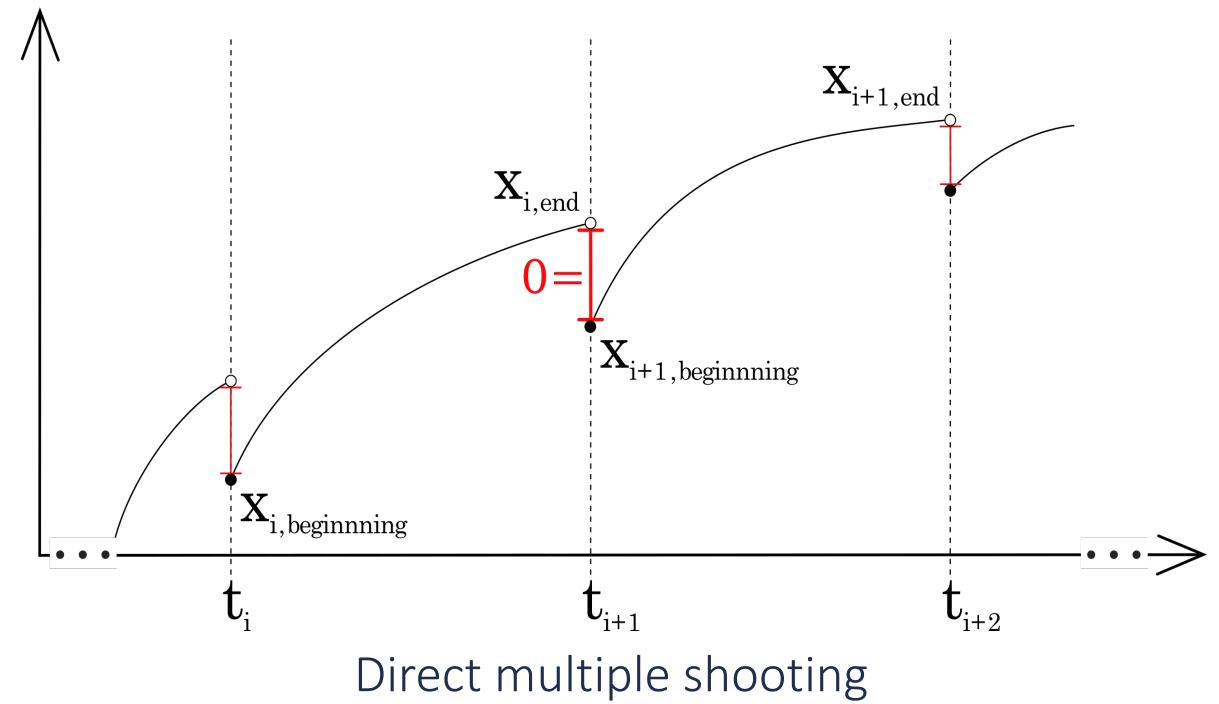
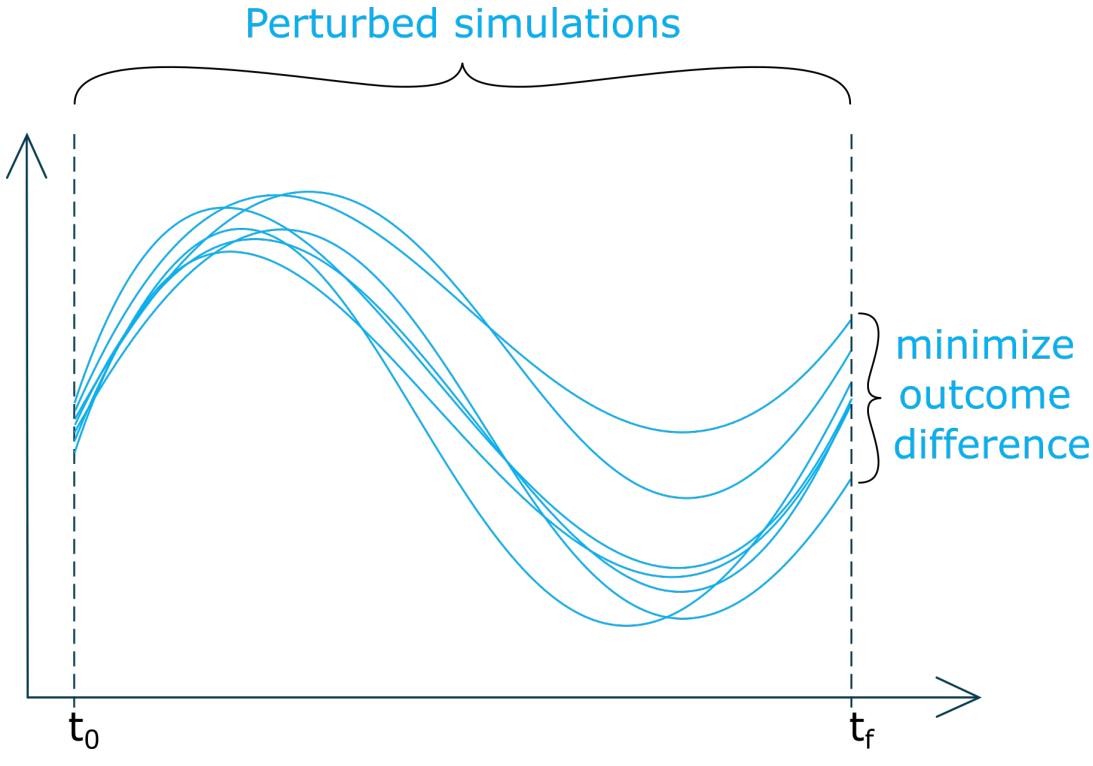
8 degrees of freedom (DoF)

# Methods

15 models  
**Same motor command**  
**Objective:**  
Minimize landing variability  
between models



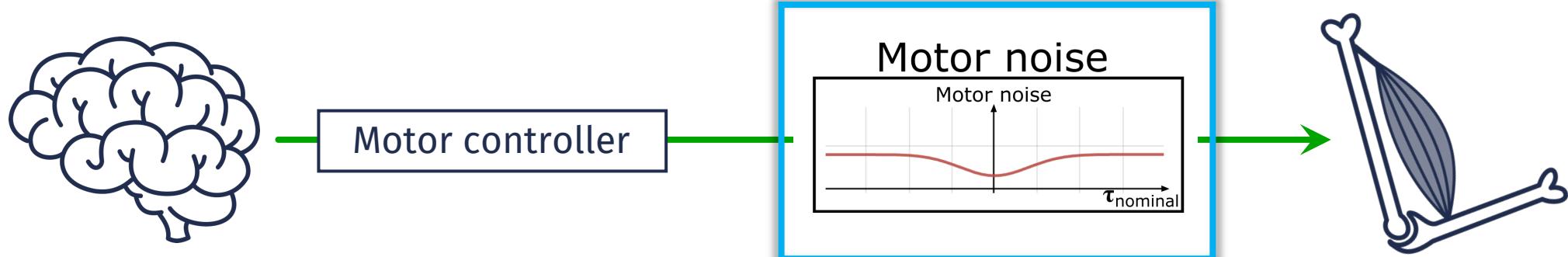
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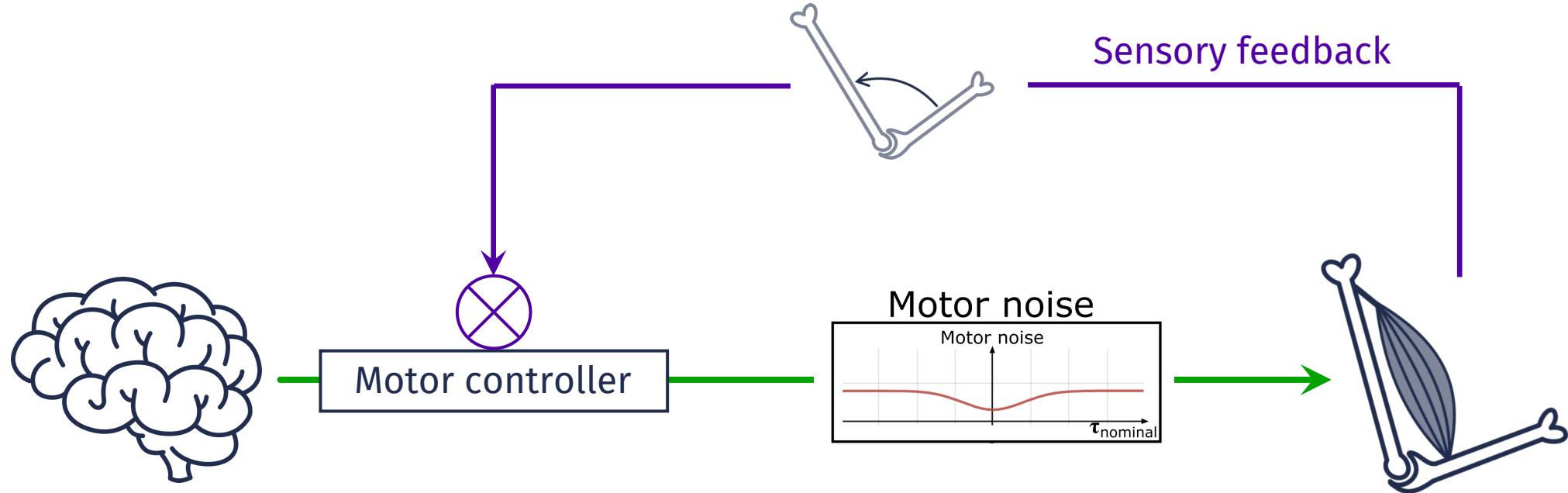


# Methods



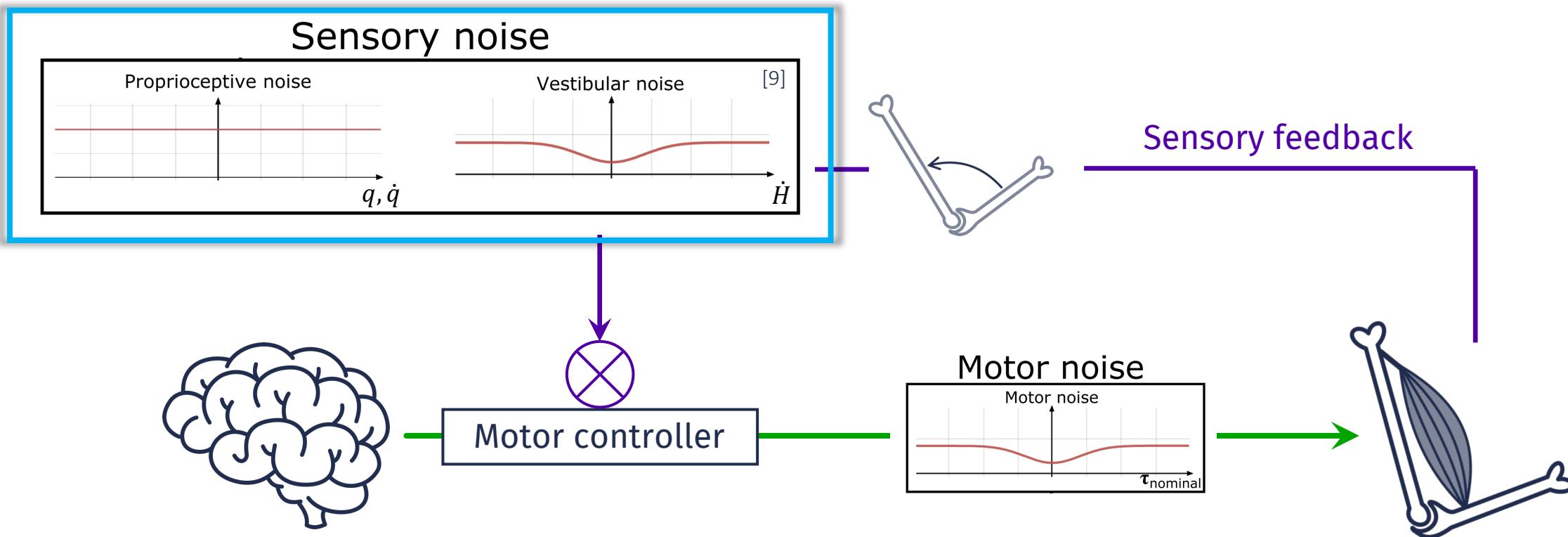
# Methods

Sensory feedback: Joints & head orientation  $(q, H)$   
Joints & head velocities  $(\dot{q}, \dot{H})$



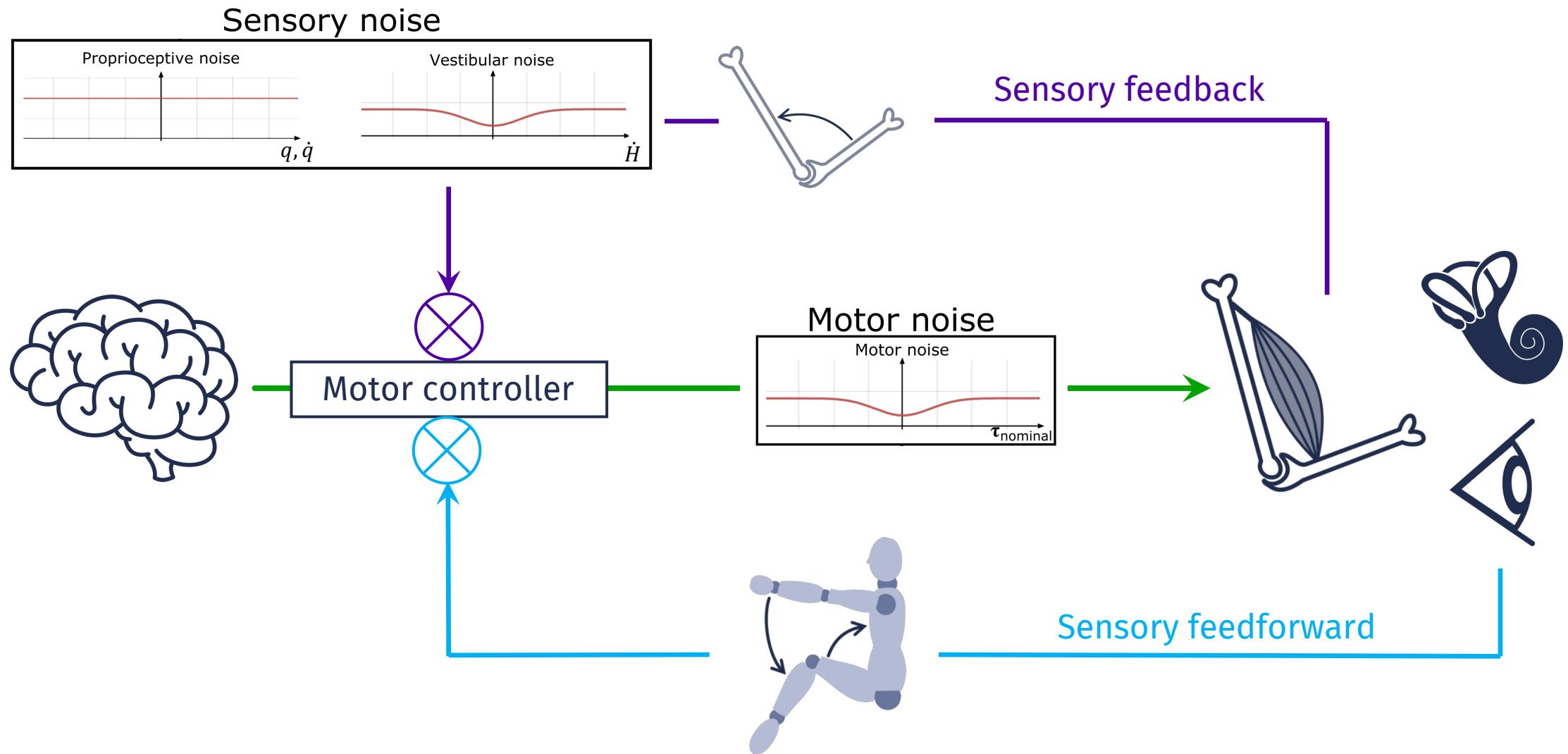
# Methods

Sensory feedback: Joints & head orientation ( $q, H$ )  
Joints & head velocities ( $\dot{q}, \dot{H}$ )



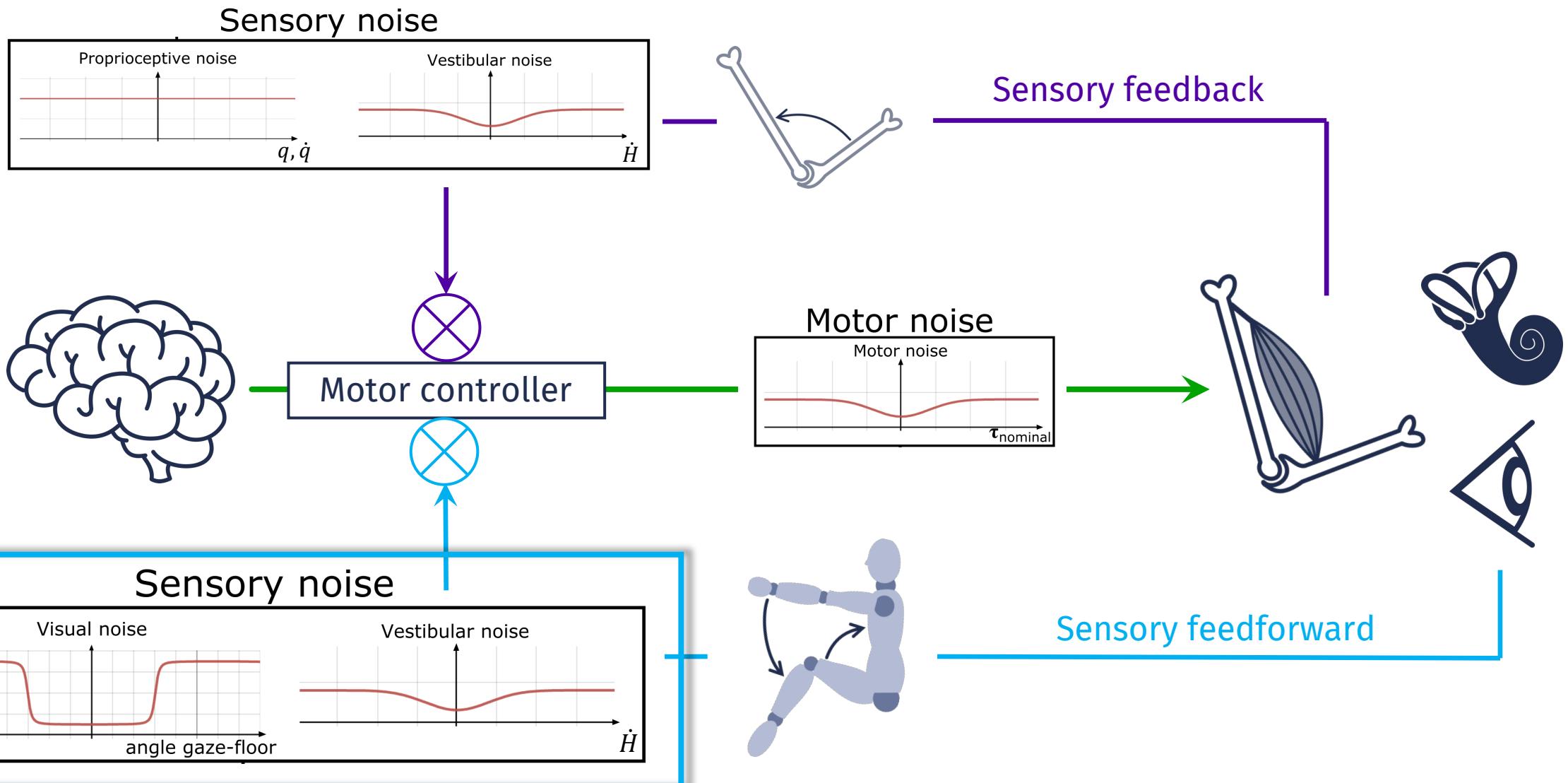
# Methods

Sensory feedforward: expected somerault at landing ( $\theta + \dot{\theta}\Delta t$ )<sup>[10]</sup>



# Methods

Sensory feedforward: expected somersault at landing ( $\theta + \dot{\theta}\Delta t$ )



# Methods

Optimal control  
(OCP)

Stochastic optimal control  
(SOCP)

Stochastic optimal control  
with variable noise and  
feedforward  
(SOCP+)

# Methods

## Optimal control (OCP)

## Stochastic optimal control (SOCP)

## Stochastic optimal control with variable noise and feedforward (SOCP+)

States:

Joint position :  $q(t)$   
Joint velocities:  $\dot{q}(t)$

Controls:

Nominal joint torques:  $u(t)$

$$\tau_{total} = u + \tau_{passive}$$

$$\min \quad \tau^2 + \dot{\tau}^2 + T$$

$$s.t. \quad x_{k+1} = F(x_k)$$

*Feet on the ground at the end*

*Center of mass over toes at the end*

# Methods

Optimal control  
(OCP)

States:  
Joint position :  $q(t)$   
Joint velocities:  $\dot{q}(t)$

x 15 models

Controls:  
Nominal joint torques:  $u(t)$

Others:  
Feedback reference:  $ref_{fb}(t)$   
Feedback gains:  $K_{fb}(t)$

$$\begin{aligned}\tau_{total} = & u + \tau_{passive} \\ & + K_{fb}(ref_{fb} - sensors + w_s) + w_M\end{aligned}$$

Stochastic optimal control  
(SOCP)

Stochastic optimal control  
with variable noise and  
feedforward  
(SOCP+)

$$\min \quad \tau^2 + \dot{\tau}^2 + T + \text{landing variability} + K^2 + \dot{K}^2$$

$$s.t. \quad x_{k+1} = F(x_k)$$

Feet on the ground at the end

Center of mass over toes at the end

$$ref_{fb} = \overline{sensors}$$

Somersault rate at landing:  $\dot{\theta}(T)$

# Methods

Optimal control  
(OCP)

Stochastic optimal control  
(SOCP)

**Stochastic optimal control  
with variable noise and  
feedforward  
(SOCP+)**

States:  
Joint position :  $q(t)$   
Joint velocities:  $\dot{q}(t)$   
  
  
 $x 15$  models

Controls:  
Nominal joint torques:  $u(t)$

Others:  
Feedback reference:  $ref_{fb}(t)$   
Feedback gains:  $K_{fb}(t)$   
Feedforward reference:  $ref_{ff}$   
Feedforward gains:  $K_{ff}(t)$

$$\begin{aligned}\tau_{total} = & u + \tau_{passive} \\ & + K_{fb}(ref_{fb} - sensors + w_s(q, \dot{q})) + w_M(u) \\ & + K_{ff}(ref_{ff} - sensors + w_s(q, \dot{q}))\end{aligned}$$

$$\min \quad \tau^2 + \dot{\tau}^2 + T + \text{landing variability} + K^2 + \dot{K}^2$$

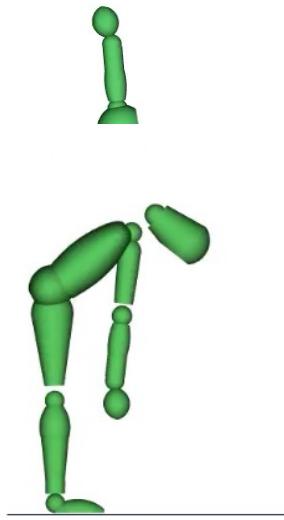
$$s.t. \quad x_{k+1} = F(x_k, \tau_k)$$

*Feet on the ground at the end*

*Center of mass over toes at the end*

$$ref_{fb,ff} = \overline{sensors}$$

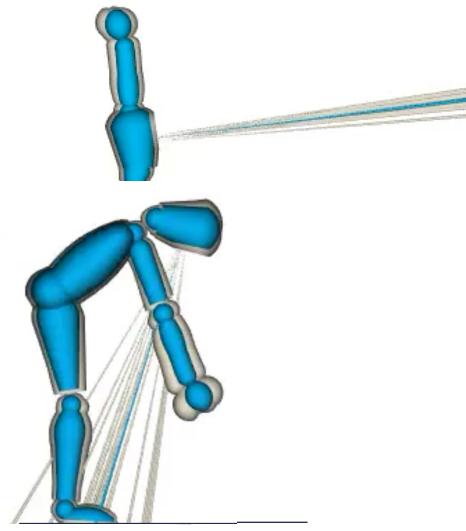
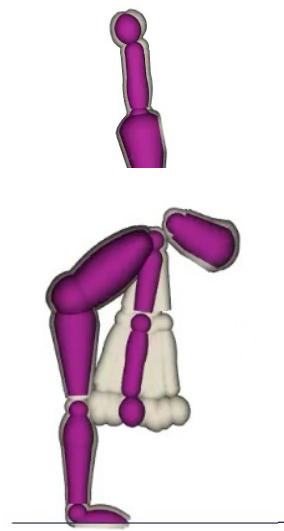
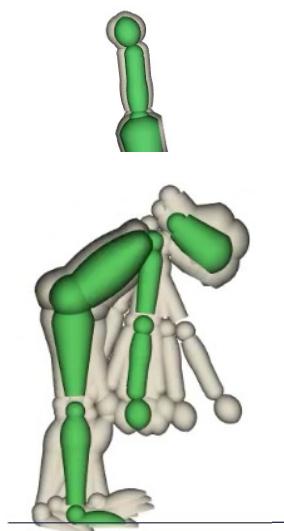
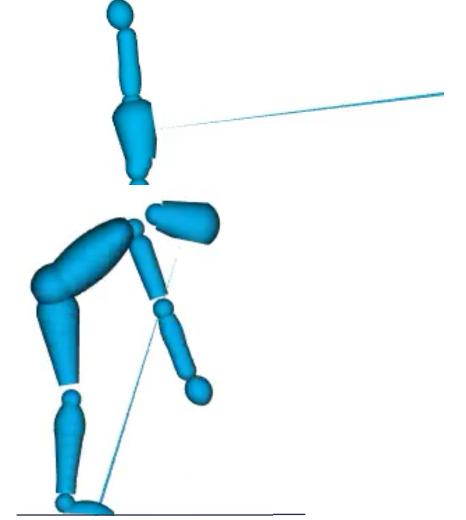
OCP



SOCP



SOCP+

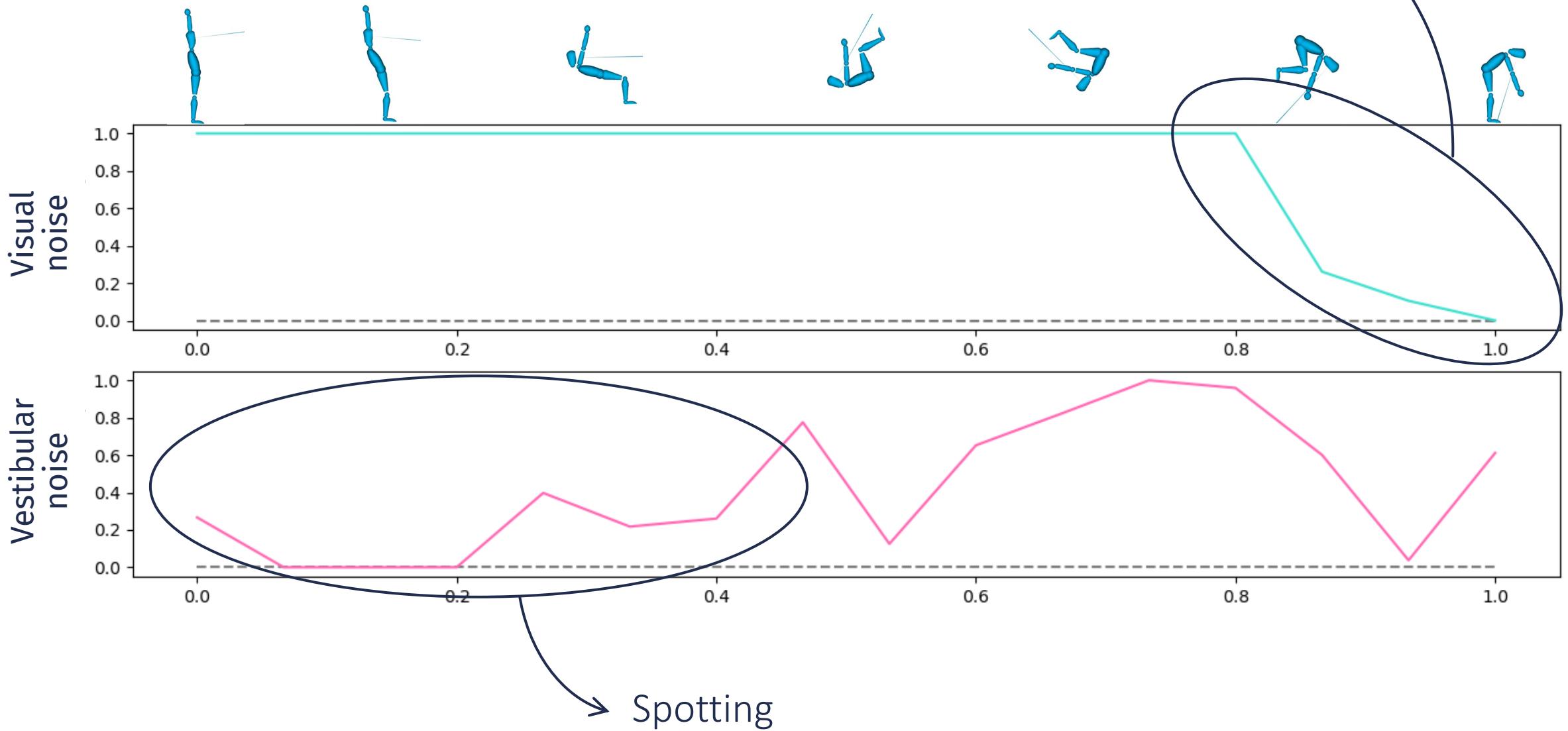


Resolution time: Few seconds

Few days

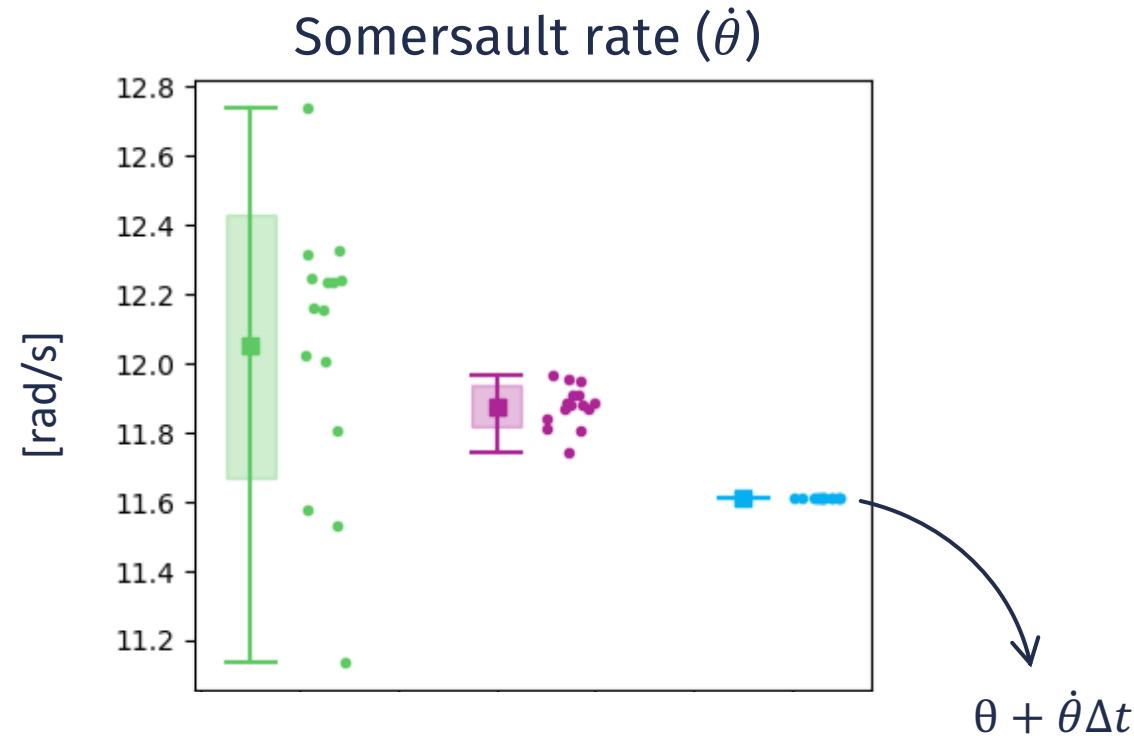
Few days

Fixation on the floor



# Results

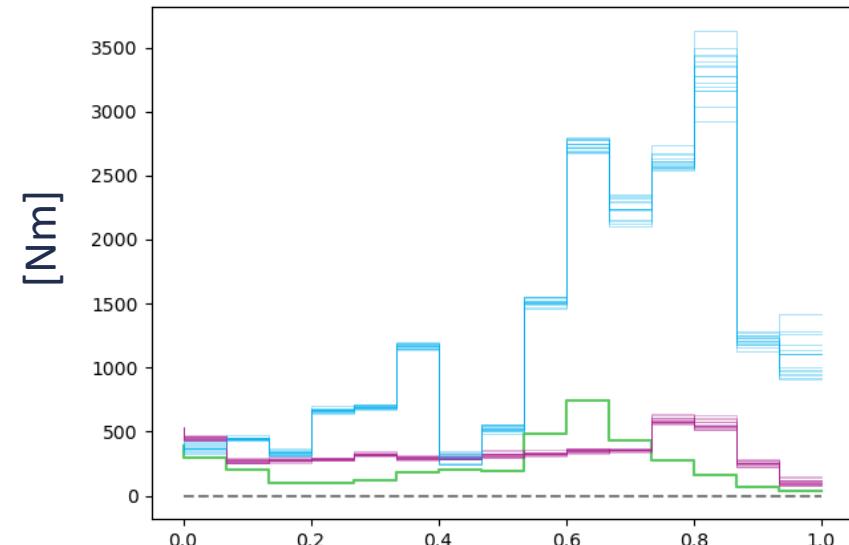
Objective:  $\tau^2 + \dot{\tau}^2 + T + \text{landing variability} + K^2 + \dot{K}^2$



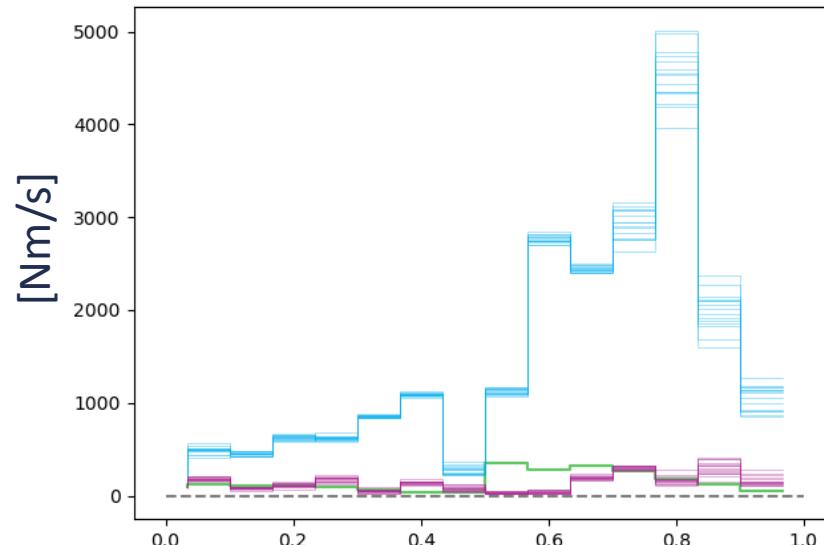
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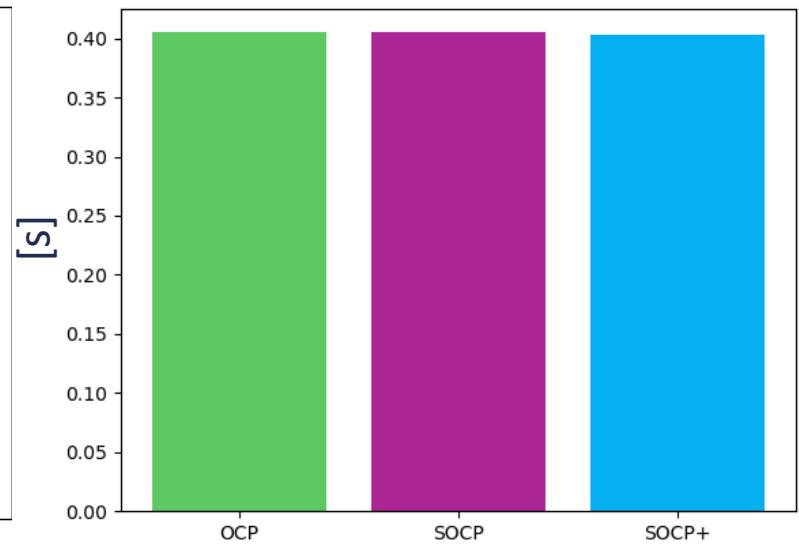
$\|\tau\|$



$\|\dot{\tau}\|$



$T$



— OCP

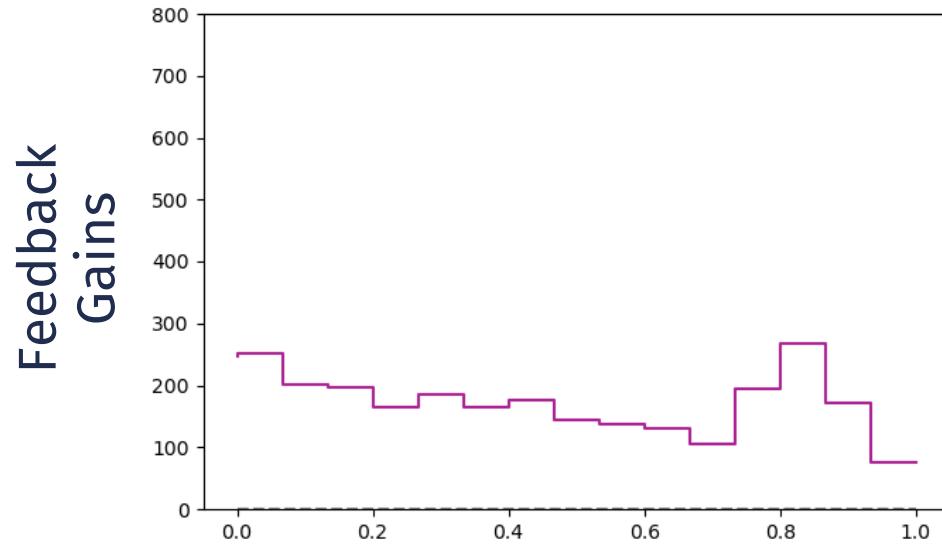
— SOCP

— SOCP+

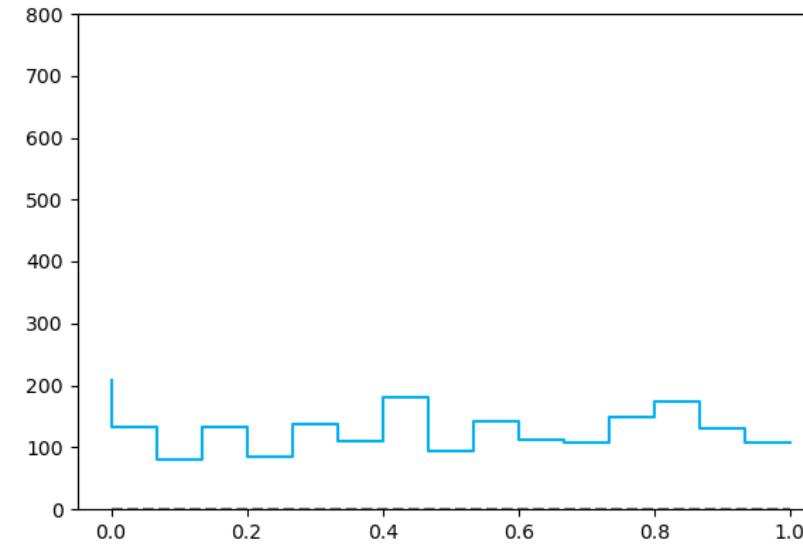
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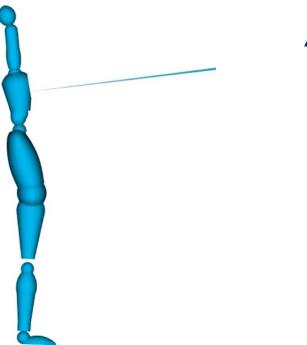
SOCP



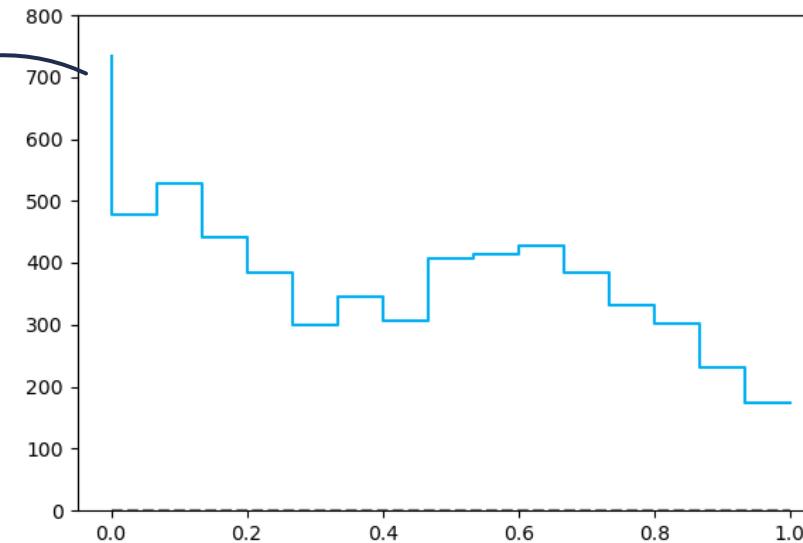
SOCP+



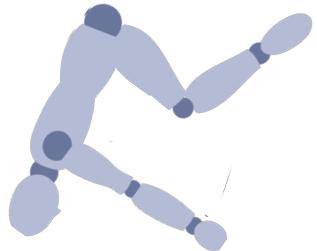
Feedforward Gains



Largest gains: knee & shoulder

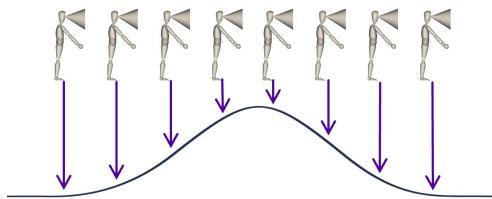


# Limitations



Movement simplifications

- ↳ Only aerial phase (no take-off & landing)
- ↳ No hand-leg contact (constrained end-effector variability)

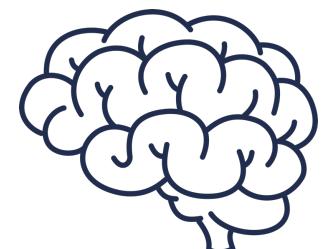
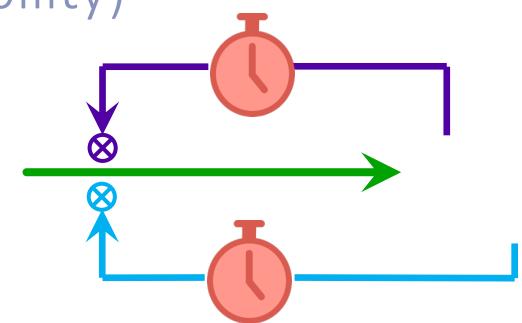


Sampling instead of considering the distribution

- ↳ More precise with a larger number of models
- ↳ Heavy computationally

Expertise is assumed (perception-action)

- ↳ Idealized motor command
- ↳ Task-specific gains





# Take home message

- Confirmation of the relevance of this **numerical method**
- The use of stochastic optimal control can increase the **robustness** of control policies
- The addition of **feedforward** term and **variable noise** can increase the realism of control policies
- There is still room for **realism** improvements, but still a promising start!

# References

- [1] Chow, C. K., & Jacobson, D. H. (1971). Studies of human locomotion via optimal programming. *Mathematical Biosciences*, 10(3-4), 239-306.
- [2] Ghosh, T. K., & Boykin Jr, W. H. (1976). Analytic determination of an optimal human motion. *Journal of Optimization Theory and Applications*, 19(2), 327-346.
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- [4] Todorov, E., & Jordan, M. I. (2002). Optimal feedback control as a theory of motor coordination. *Nature neuroscience*, 5(11), 1226-1235.
- [5] Gibson, J. J. (1979). *The ecological approach to visual perception*. Houghton, Mifflin and Company.
- [6] Van Wouwe, T., Ting, L. H., & De Groot, F. (2022). An approximate stochastic optimal control framework to simulate nonlinear neuro-musculoskeletal models in the presence of noise. *PLOS Computational Biology*, 18(6), e1009338.
- [7] Harris, C. M., & Wolpert, D. M. (1998). Signal-dependent noise determines motor planning. *Nature*, 394(6695), 780-784.
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- [10] Bardy, B. G., & Laurent, M. (1998). How is body orientation controlled during somersaulting?. *Journal of Experimental Psychology: Human Perception and Performance*, 24(3), 963.

# Questions ?

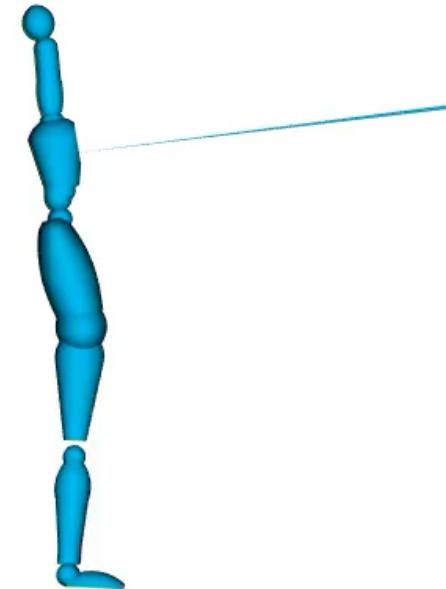
Open source code:



EveCharbie/Stochastic\_standingBack



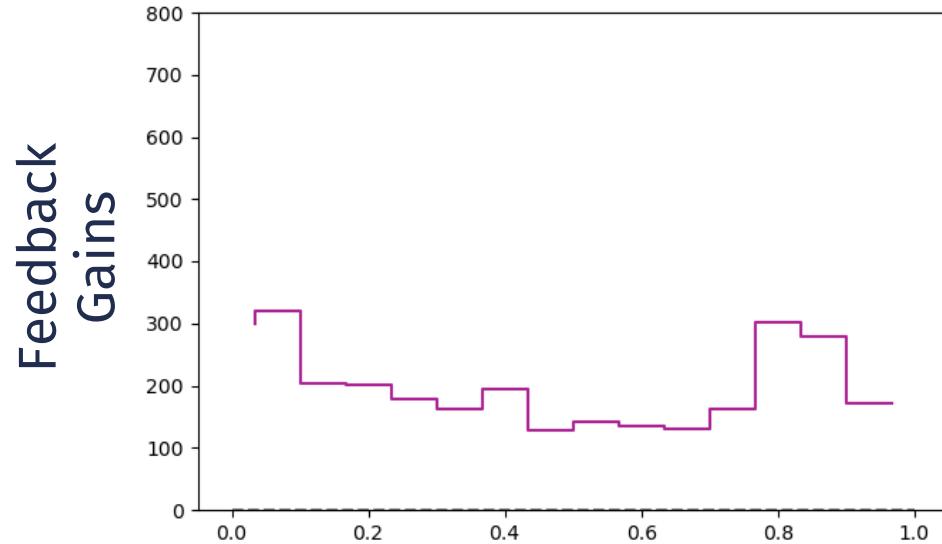
**Bioptim**  
Biomechanical optimal control



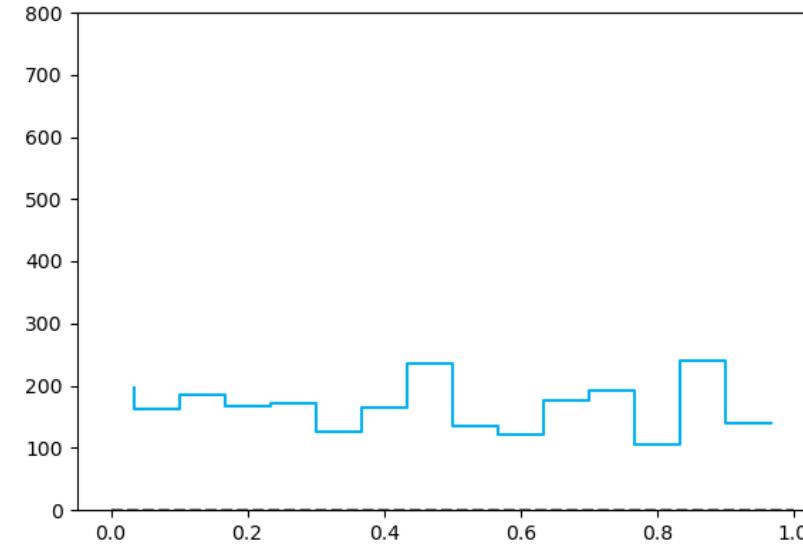
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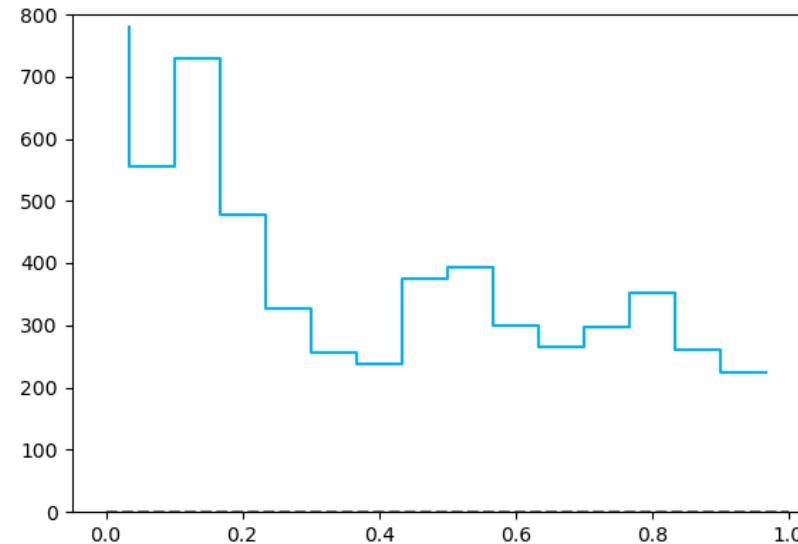
SOCP



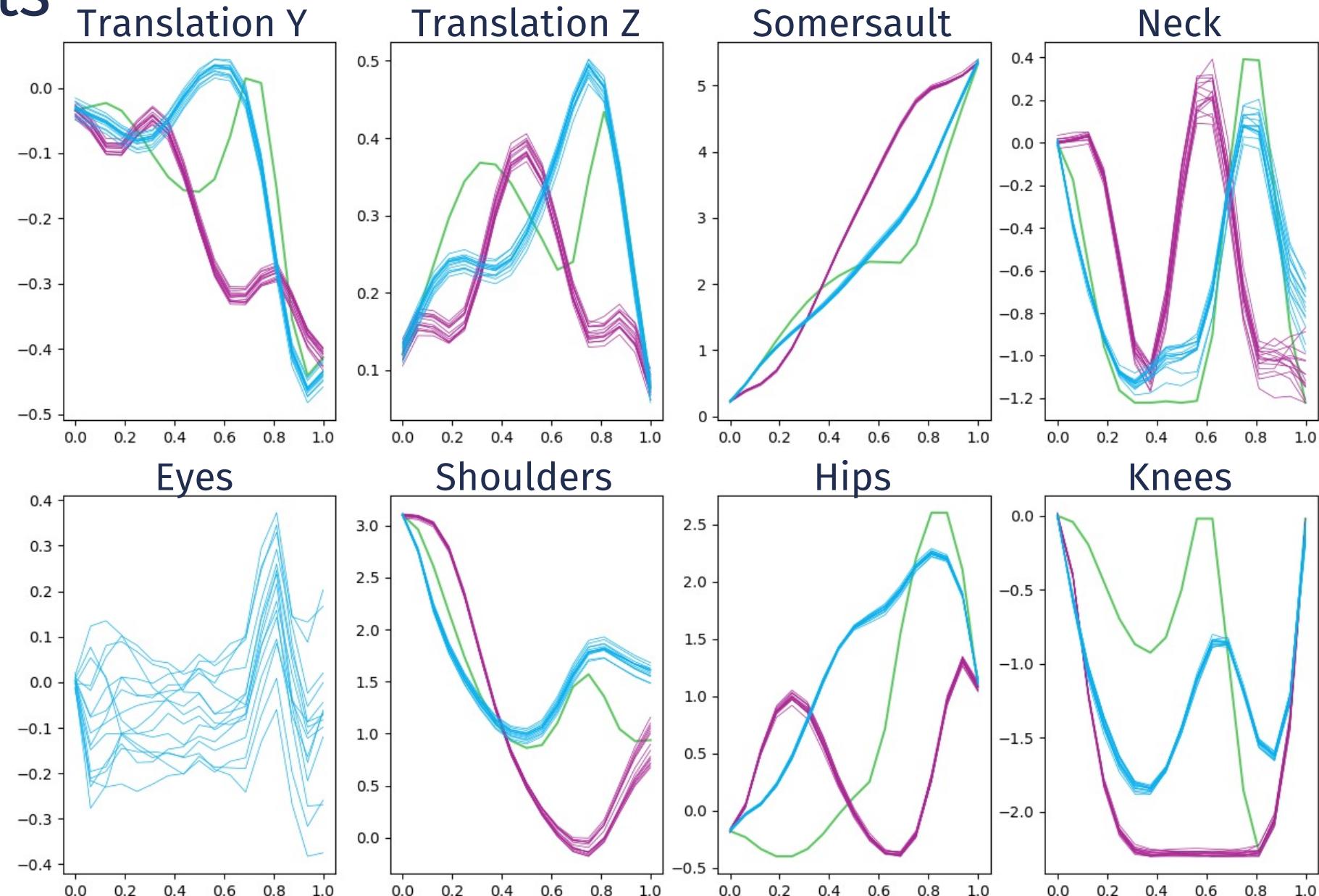
SOCP+



Feedforward  
Gains

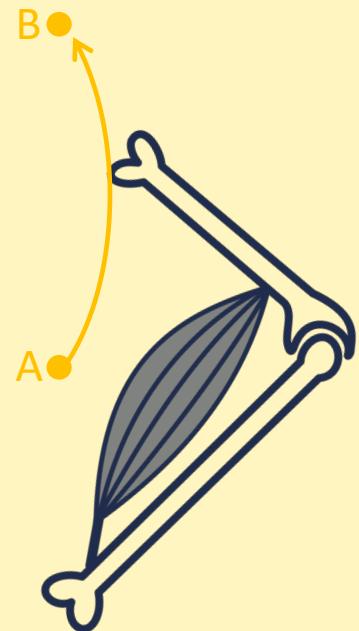


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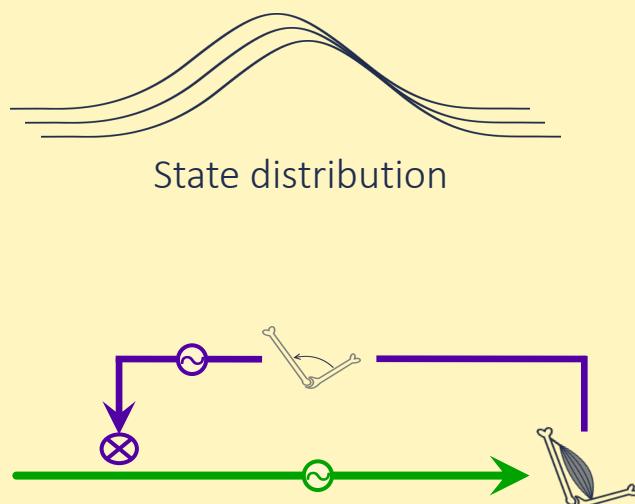
### Complex musculoskeletal model

- 6 muscles
- 2 joints



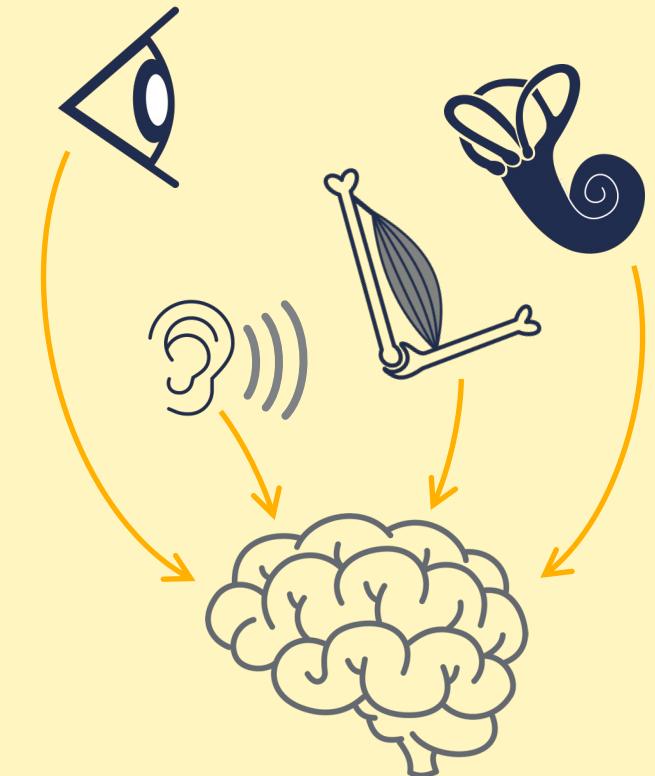
### Robust control strategy

- Proprioceptive feedbacks
- Motor & sensory noises



### Simple pointing task

- Only one feedback
  - Only two joints
- No perception-action interaction



- 16+1 nodes
- Motor noise STD: 0.5
- Position proprioception noise STD: 0.005
- Velocity proprioception STD: 0.015
- Vestibular and visual noise STD: 0.015

$$\begin{aligned}\tau_{total} = & u + \tau_{passive} \\ & + K_{fb}(ref_{fb} - sensors + w_s(q, \dot{q})) + w_M(u) \\ & + K_{ff}(ref_{ff} - sensors + w_s(q, \dot{q}))\end{aligned}$$

$$\ddot{q}_k = M(q_k)^{-1}(\tau_k - N(q_k, \dot{q}_k) - G(q_k))$$

M = mass matrix

N = non-linear effects (Coriolis and centrifugal effect)

G = gravity effects

$[q_{k+1}, \dot{q}_{k+1}]$  are obtained by integrating with 5 steps of a 4<sup>th</sup> order Runge-Kutta