CS323 Compilation Principle

Assignment 1

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Required Exercises

Exercise 1

> When a C compiler compiles the following statement, how many tokens will it generate? [5 points]
>
> ```
> int a3 = a * 3;
> ```

There are 7 tokens will be generated.

- <keyword, int>
- <id, a3>
- <id, a>
- <assign, =>
- <assign, *>
- <assign, ;>
- <number, 3>

Exercise 2

> In a string of length n (n > 0), how many of the following are there?
>
> 1. Prefixes [5 points]
> 2. Proper prefixes [5 points]
> 3. Prefixes of length m (0 < m ≤ n) [5 points]
> 4. Suffixes of length m (0 < m ≤ n) [5 points]
> 5. Proper prefixes of length m (0 < m ≤ n) [10 points]
> 6. Substrings [10 points]
> 7. Subsequences [10 points]

1. $n+1$
2. $n-1$
3. 1
4. 1

5. $res = \begin{cases} 0 & \text{m=n} \\ 1 & \text{otherwise} \end{cases}$
6. $1 + \frac{(1+n)n}{2}$
7. 2^n

Exercise 3

> Describe the languages denoted by the following regular expressions:
>
> 1. ((ε|a)*b*)* [5 points]
> 2. (a|b)*a(a|b)(a|b) [5 points]
> 3. a*ba*ba*ba* [5 points]

1. A string consisting of a and b
2. A string consisting of a and b whose third-to-last digit is a
3. A string consisting of a and b with only three

Exercise 4

> Write regular definitions or regular expressions for the following languages.
>
> 1. All strings representing valid telephone numbers in Shenzhen. A valid telephone number contains the country code (86), a hyphen, the area code 0755, another hyphen, and eight digits where the first one cannot be zero (e.g., 86-0755-88015159). [10 points]
> 2. All strings of a's and b's that start with a and end with b. [10 points]
> 3. All strings of lowercase letters that contain the five vowels in order. [10 points]

```
86-0755-[1-9][0-9]{7}
```

```
a(a|b)*b
```

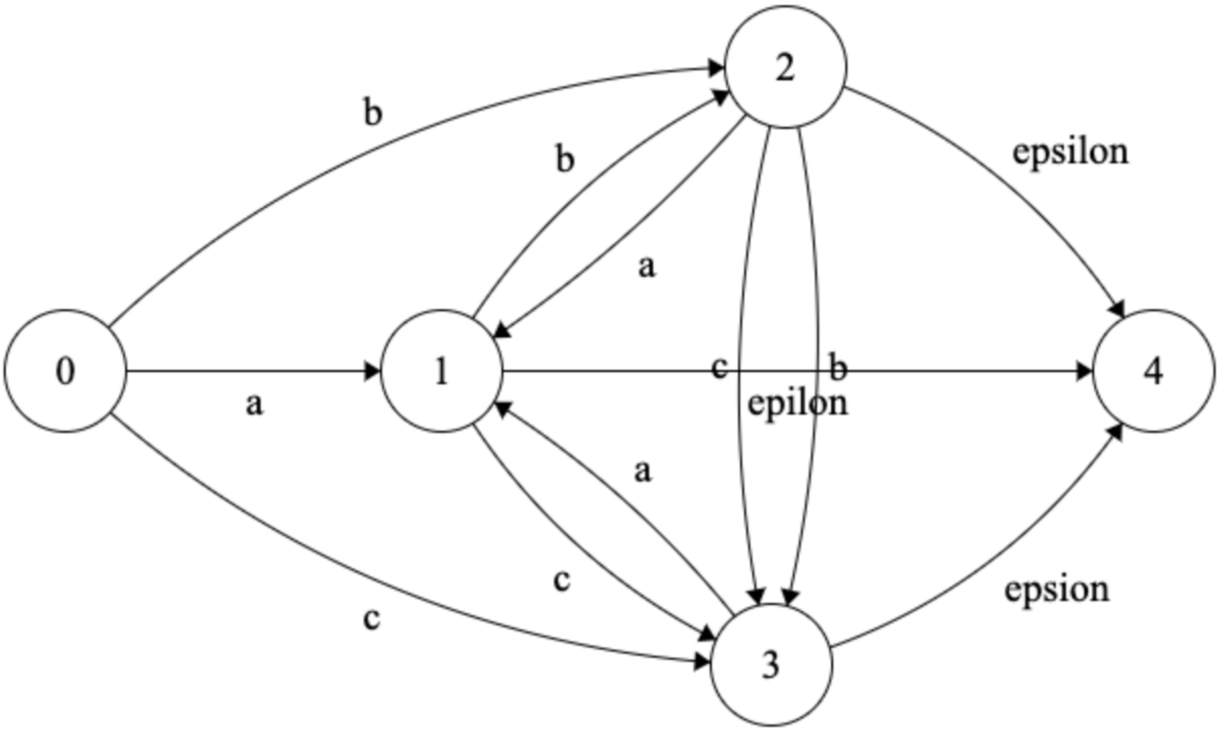
```
[a-z^aeiou]*a[a-z^aeiou]*e[a-z^aeiou]*i[a-z^aeiou]*o[a-z^aeiou]*u[a-z^aeiou]*
```

Optional Exercises

Exercise 1

> Suppose we have a alphabet Σ = {a, b, c}, write regular definitions to describe all strings over Σ without repeated letters. [Hint: You may draw an NFA for the language and convert the NFA to regular definitions.]

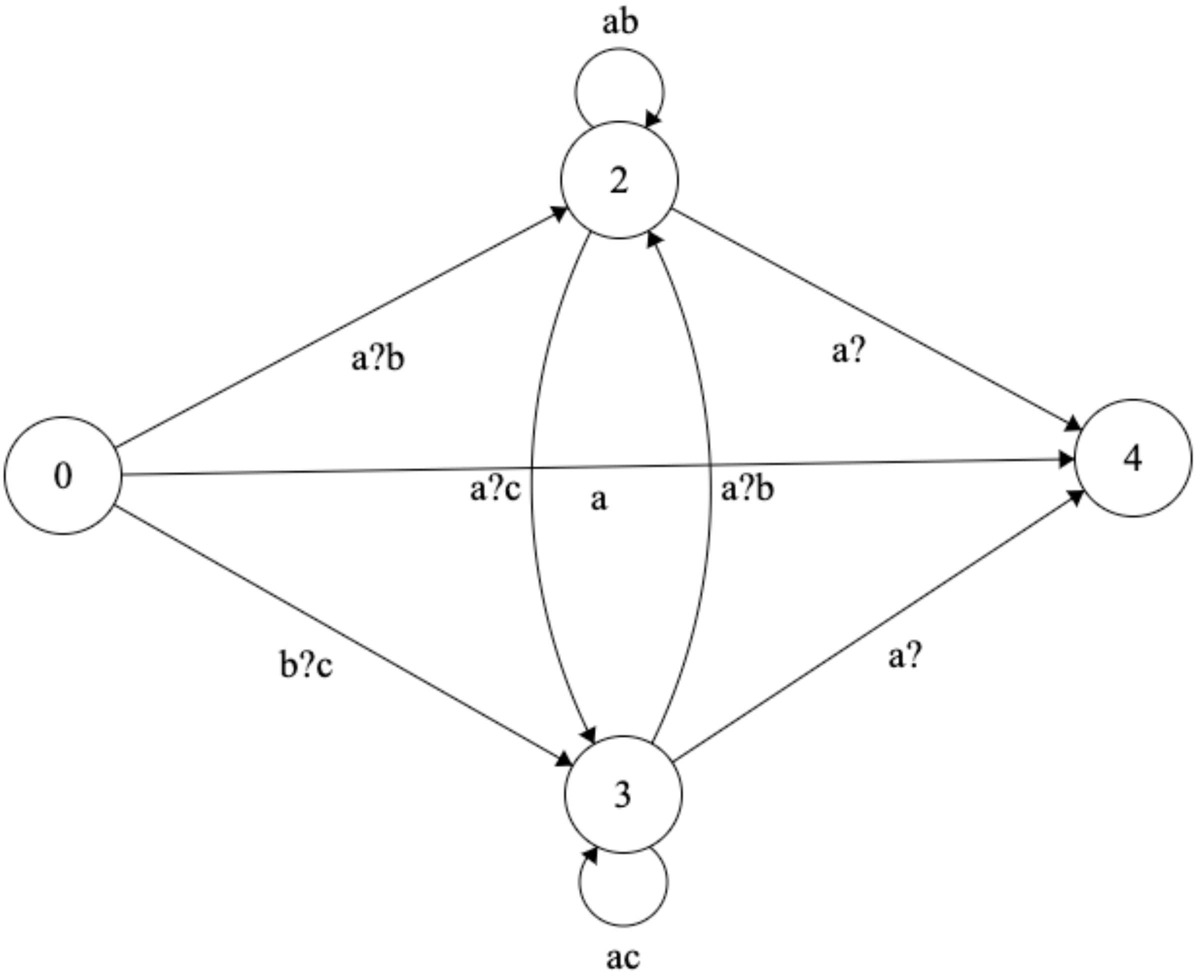
The origin NFA figure



Then, we should simplify the figure by removing the state 1, 2 , 3 to get the regular definitions.

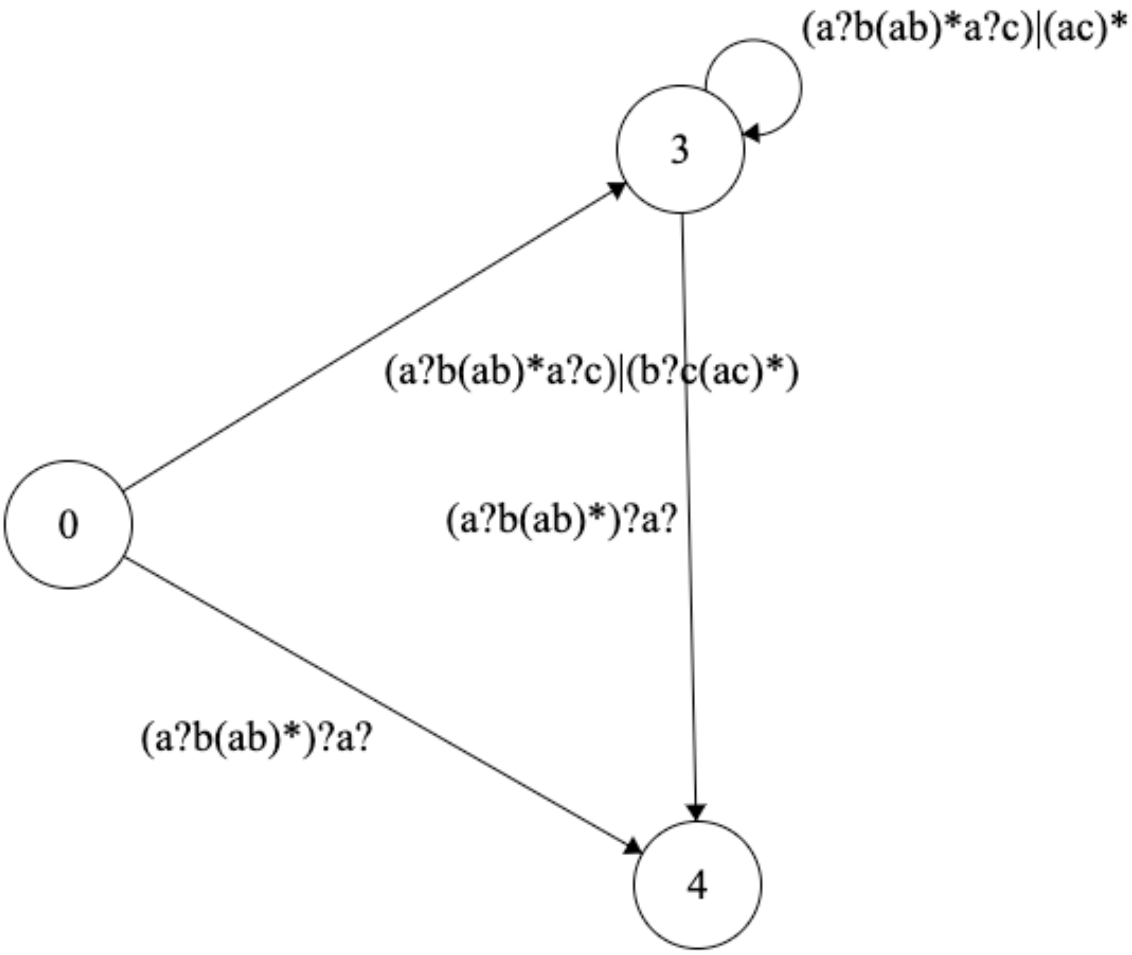
Remove state 1

edge	Regular expression
0 -> 2	a?b
0 -> 3	b?c
0 -> 4	a
2 -> 2	ab
2 -> 3	a?c
2 -> 4	a?
3 -> 2	a?b
3 -> 3	ac
3 -> 4	a?



Remove state 2

edge	Regular expression
0 -> 3	(a?b(ab)*a?c)|(b?c(ac)*)
0 -> 4	(a?b(ab)*)?a?
3 -> 3	(a?b(ab)*a?c)|(ac)*
3 -> 4	(a?b(ab)*)?a?



Remove state 3

edge	Regular expression
0 -> 4	(((a?b(ab)*a?c)|(b?c(ac)*))((a?b(ab)*a?c)|(ac)*)*)?(a?b(ab)*)?a?

So, from NFA to regular expression, the result is $(((a?b(ab)\ast a?c)|(b?c(ac)\ast))((a?b(ab)\ast a?c)|(ac)\ast)\ast)?(a?b(ab)\ast)?a?$