

Assignment 1

Name | Yubin Hu

ID | 11712121

Date | 2020.09.23

Required Exercises

Exercise 1

When a C compiler compiles the following statement, how many tokens will it generate? [5 points]

```
1 | int a3 = a * 3;
```

There are 7 tokens will be generated.

- <keyword, int>
- <id, a3>
- <id, a>
- <assign, =>
- <assign, *>
- <assign, ;>
- <number, 3>

Exercise 2

In a string of length n ($n > 0$), how many of the following are there?

1. Prefixes [5 points]
2. Proper prefixes [5 points]
3. Prefixes of length m ($0 < m \leq n$) [5 points]
4. Suffixes of length m ($0 < m \leq n$) [5 points]
5. Proper prefixes of length m ($0 < m \leq n$) [10 points]
6. Substrings [10 points]
7. Subsequences [10 points]

1. $n + 1$
2. $n - 1$
3. 1
4. 1
5. $res = \begin{cases} 0 & m=n \\ 1 & \text{otherwise} \end{cases}$
6. $1 + \frac{(1+n)n}{2}$
7. 2^n

Exercise 3

Describe the languages denoted by the following regular expressions:

1. $((\epsilon|a)^*b^*)^*$ [5 points]
2. $(a|b)^*a(a|b)(a|b)$ [5 points]
3. $a^*ba^*ba^*ba^*$ [5 points]

1. A string consisting of a and b
2. A string consisting of a and b whose third-to-last digit is a
3. A string consisting of a and b with only three

Exercise 4

Write regular definitions or regular expressions for the following languages.

1. All strings representing valid telephone numbers in Shenzhen. A valid telephone number contains the country code (86), a hyphen, the area code 0755, another hyphen, and eight digits where the first one cannot be zero (e.g., 86-0755-88015159). [10 points]
2. All strings of a's and b's that start with a and end with b. [10 points]
3. All strings of lowercase letters that contain the five vowels in order. [10 points]

```
1 | 86-0755-[1-9][0-9]{7}
```

```
1 | a(a|b)*b
```

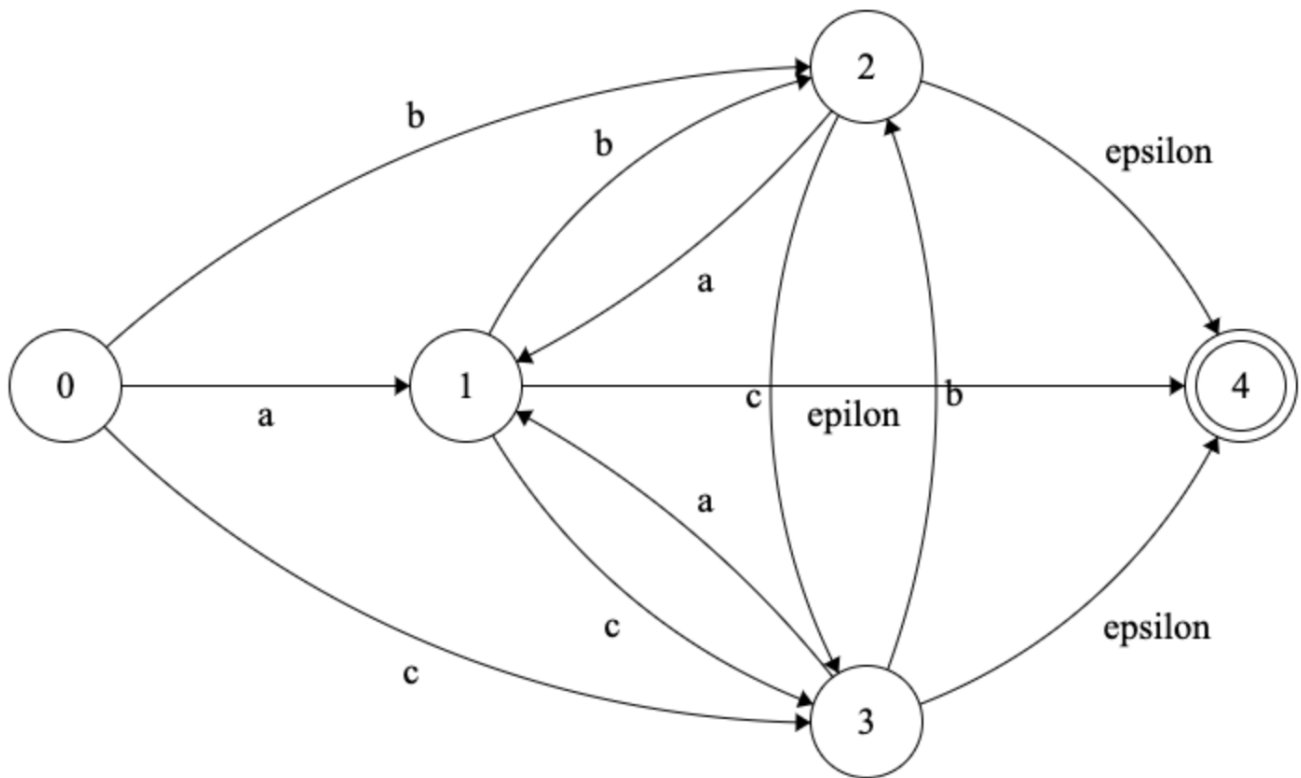
```
1 | pattern = [b-df-hj-np-tv-z]
2 | {pattern}*a{pattern}*e{pattern}*i{pattern}*o{pattern}*u{pattern}*
```

Optional Exercises

Exercise 1

Suppose we have a alphabet $\Sigma = \{a, b, c\}$, write regular definitions to describe all strings over Σ without repeated letters. [Hint: You may draw an NFA for the language and convert the NFA to regular definitions.]

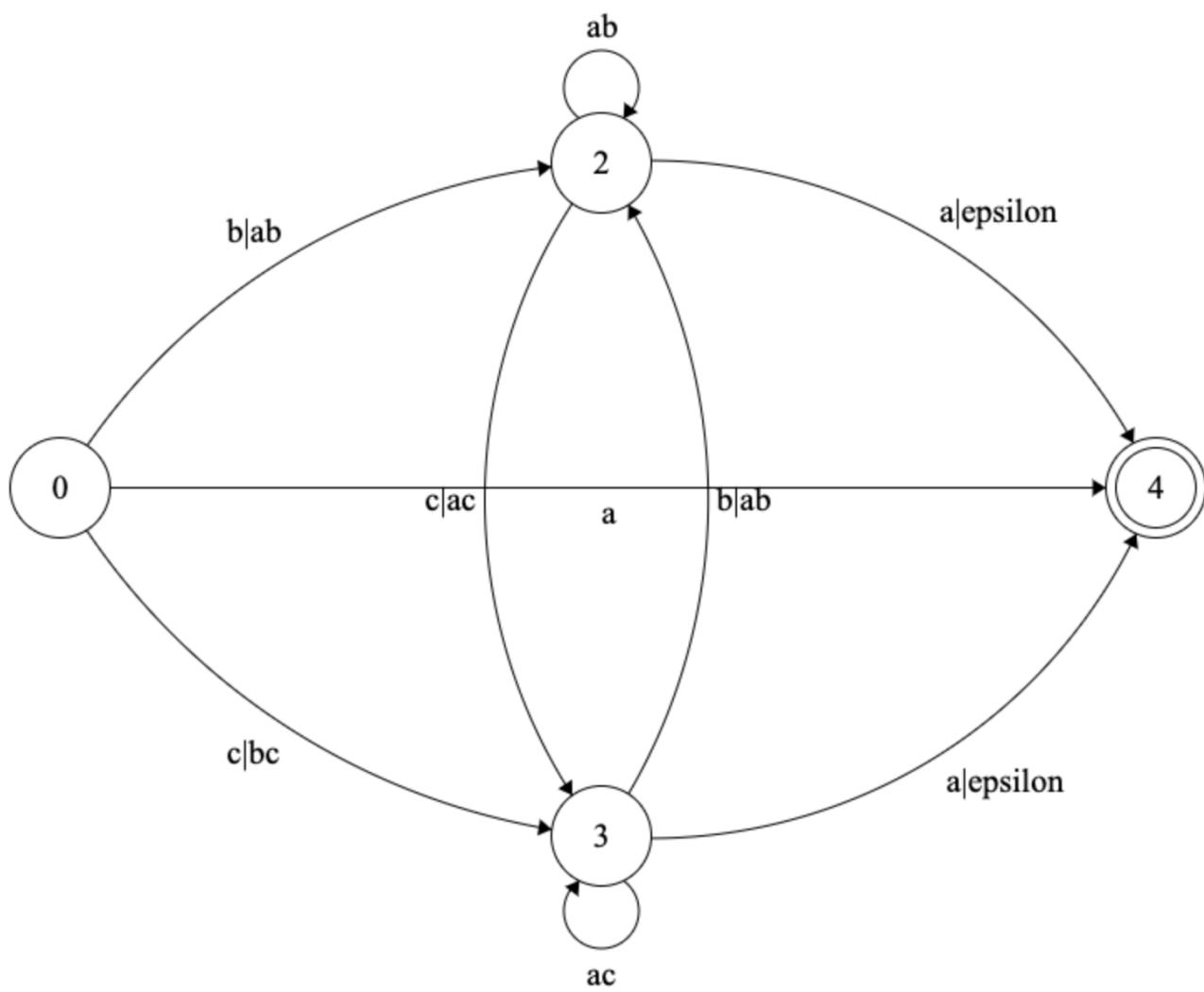
The origin NFA figure

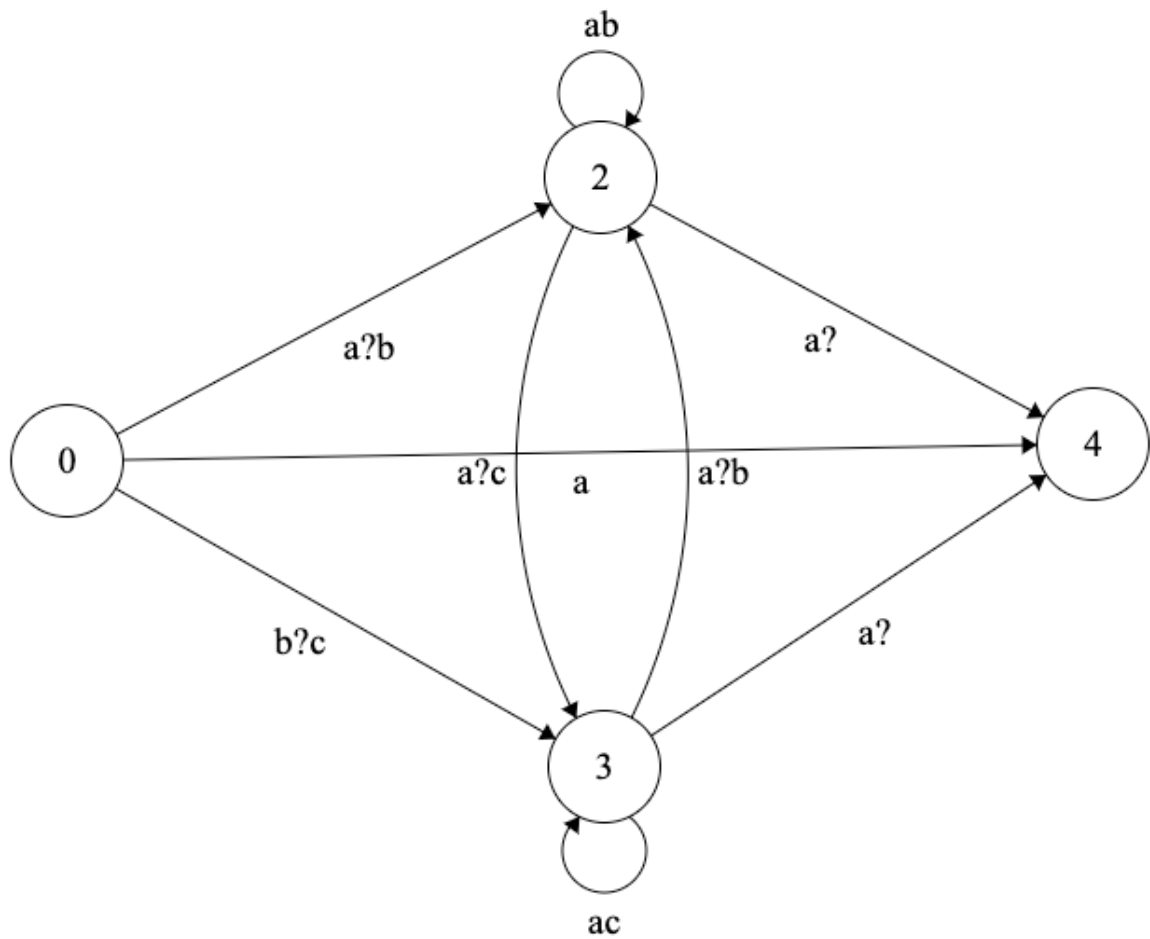


Then, we should simplify the figure by removing the state 1, 2, 3 to get the regular definitions.

Remove state 1

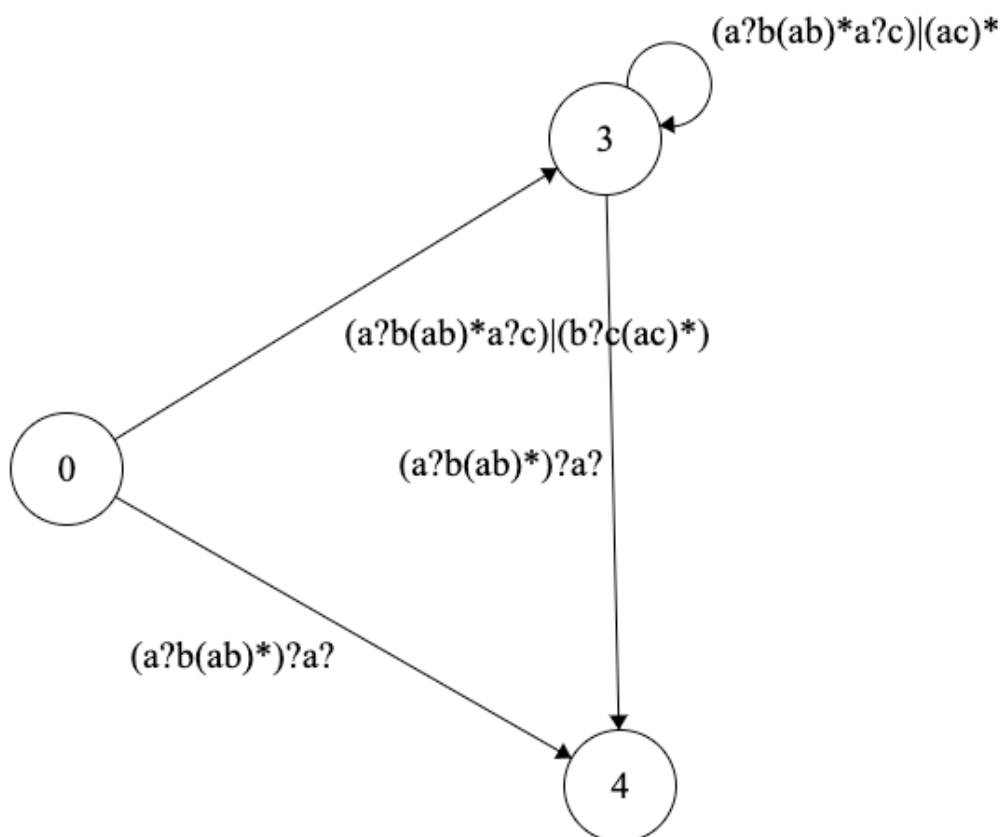
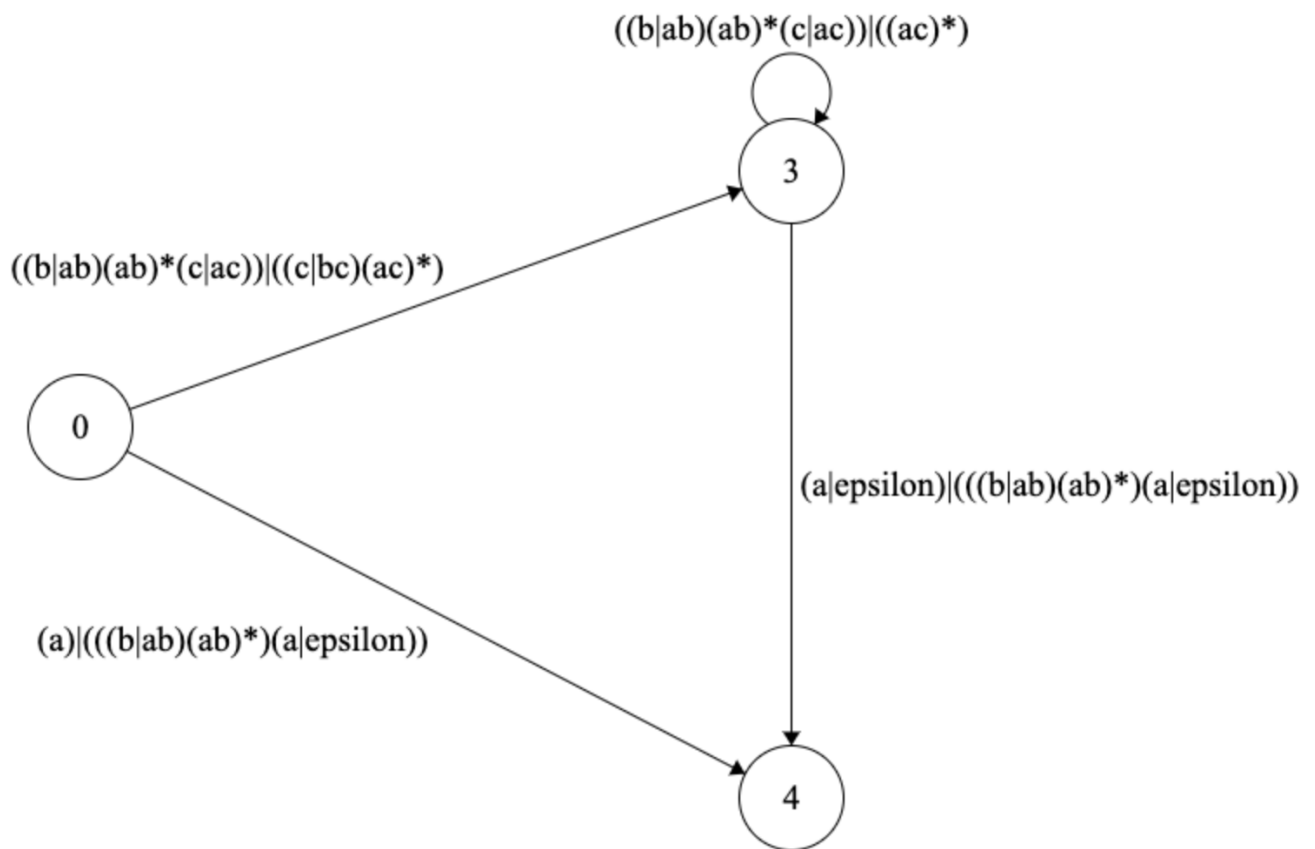
edge	Regular expression
0 -> 2	$b ab$
0 -> 3	$c bc$
0 -> 4	a
2 -> 2	ab
2 -> 3	$c ac$
2 -> 4	$a \epsilon$
3 -> 2	$b ab$
3 -> 3	ac
3 -> 4	$a \epsilon$





Remove state 2

edge	Regular expression
0 -> 3	$((b ab)(ab)^*(c ac)) ((c bc)(ac)^*)$
0 -> 4	$(a) (((b ab)(ab)^*)(a \epsilon))$
3 -> 3	$((b ab)(ab)^*(c ac)) ((ac)^*)$
3 -> 4	$(a \epsilon) (((b ab)(ab)^*)(a \epsilon))$



Remove state 3

edge	Regular expression
0 -> 4	$((a) (((b ab)(ab)^*(a \epsilon)))) (((b ab)(ab)^*(c ac)) ((c bc)(ac)^*)((b ab)(ab)^*(c ac)) ((ac)^*) * ((a \epsilon) (((b ab)(ab)^*(a \epsilon)))))$

So, from NFA to regular expression, the result is

$((a)|(((b|ab)(ab)^*(a|\epsilon))))|(((b|ab)(ab)^*(c|ac))|((c|bc)(ac)^*)((b|ab)(ab)^*(c|ac))|((ac)^*) * ((a|\epsilon)|(((b|ab)(ab)^*(a|\epsilon)))))$
 .

if we can use symbol `?`, the regular expression is

$((a?b(ab)^*a?c)|(b?c(ac)^*)((a?b(ab)^*a?c)|(ac)^*)^*)?(a?b(ab)^*)?a?$

regex101

REGULAR EXPRESSION

7 matches, 359 steps (~1ms)

/

^(((a?b(ab)*a?c)|(b?c(ac)*))((a?b(ab)*a?c)|(ac)*)*)?(a?b(ab)*a?c)b(ab)*a?\$

/gm

TEST STRING

a

b

c

ab

ba

abababab

abcbca

aaa

abba

abccba

cabcc