Feedback — Problem Set #5

Help Center

You submitted this quiz on **Mon 27 Apr 2015 9:44 AM IST**. You got a score of **5.00** out of **5.00**.

Question 1

Your Answer	Score	Explanation
There is an NP-complete problem that is polynomial-time solvable.		
Some NP-complete problems are polynomial-time solvable, and some NP-complete problems are not polynomial-time solvable.	✓ 1.00	A polynomial-time algorithm for a single NP-complete automatically yields polynomial-time algorithms for all NP-complete algorithms (i.e., implies that P=NP).
There is an NP-complete problem that can be solved in $O(n^{\log n})$ time, where n is the size of the input.		
There is no NP-complete problem that can be solved in $O(n^{\log n})$ time, where n is the size of the input.		
Total	1.00 / 1.00	

Question 2

Your Answer	Score	Explanation
If the minimum-size vertex cover problem can be solved in time $O(T(n))$ in bipartite graphs, then the maximum-size independent set problem can be solved in time $O(T(n))$ in bipartite graphs.		
If the minimum-size vertex cover problem can be solved in time $O(T(n))$ in general graphs, then the maximum-size independent set problem can be solved in time $O(T(n))$ in general graphs.		
If the maximum-size independent set problem can be solved in time $O(T(n))$ in general graphs, then the minimum-size vertex cover problem can be solved in time $O(T(n))$ in general graphs.		
All three of the other assertions are true.	1.00	Vertex covers and independent sets are complements (take the complement of one and you get the other). Thus solving one problem allows you to solve the other with $\Theta(n)$ postprocessing, where n is the number of vertices.
Total	1.00 /	

Question 3 Which of the following statements is true? **Your Answer** Score **Explanation** Consider a TSP instance in which every edge cost is negative. Deleting a vertex and all of its incident edges cannot increase the cost of the optimal (i.e., minimum sum of edge lengths) tour. Consider a TSP 1.00 Take the optimal tour in the original instance. Now, instead of visiting the deleted vertex v, skip straight from instance in which v's predecessor to its successor on the tour. Because every edge cost is the Euclidean distance Euclidean distance satisfies the "Triangle Inequality", this shortcut only decreases the overall distance between two points in traveled. The best tour can of course only be better. the place (just like in Programming Assignment #5). Deleting a vertex and all of its incident edges cannot increase the cost of the optimal (i.e., minimum sum of edge lengths) tour. Consider a TSP instance in which every edge cost is either 1 or 2. Then an optimal tour can be computed in polynomial time. Consider a TSP instance in which every edge cost is

negative. The dynamic programming algorithm covered in the video lectures might not correctly compute the optimal (i.e., minimum sum of edge lengths) tour of this instance.

Total 1.00 / 1.00

Question 4

Let TSP1 denote the following problem: given a TSP instance in which all edge costs are positive integers, compute the value of an optimal TSP tour. Let TSP2 denote: given a TSP instance in which all edge costs are positive integers, and a positive integer T, decide whether or not there is a TSP tour with total length at most T. Let HAM1 denote: given an undirected graph, either return the edges of a Hamiltonian cycle (a cycle that visits every vertex exactly once), or correctly decide that the graph has no such cycle. Let HAM2 denote: given an undirected graph, decide whether or not the graph contains at least one Hamiltonian cycle.

Your Answer	Score	Explanation
0		
Polynomial-time		
solvability of TSP2		
does not		
necessarily imply		
polynomial-time		
solvability of TSP1.		
Polynomial-time		
solvability of HAM2		
does not		
necessarily imply		
polynomial-time		
solvability of		
HAM1.		

Polynomial-time solvability of TSP2 does not necessarily imply polynomial-time solvability of TSP1. But, if HAM2 is polynomial-time solvable, then so is HAM1.

polynomial-time solvable, then so is TSP1. If HAM2 is polynomial-time solvable, then so is HAM1.

Given a polynomial-time algorithm for TSP2, use it repeatedly while binary searching over the choice of T to solve TSP1 (the number of iterations necessary is logarithmic in the sizes of the input numbers, which is polynomial in the input size). Use a polynomial-time algorithm for HAM2 to solve HAM1 as follows. First, run HAM2 on the graph. If it says "no", report "no". Otherwise, delete some edge (in effect, guessing that there is also a Hamiltonian cycle without it) and run HAM2 again. If it says "yes", iterate on the new smaller graph. If it says "no", restore the edge (it lies on every Hamiltonian cycle, do you see why?) and move on to the next edge. If HAM2 originally said "yes", you will identify (in O(m) iterations) a sequence of successful edge deletions, and the remaining edges will constitute a Hamiltonian cycle of the original graph.

polynomial-time solvable, then so is TSP1. But, polynomial-time solvability of HAM2 does not necessarily imply polynomial-time solvability of HAM1.

Total

1.00 /

1.00

1.00

Question 5

Assume that $P \neq NP$. Consider undirected graphs with nonnegative edge lengths. Which of the following problems can be solved in polynomial time?

Hint: The Hamiltonian path problem is: given an undirected graph with n vertices, decide whether or not there is a (cycle-free) path with n-1 edges that visits every vertex exactly once. You can use the fact that the Hamiltonian path problem is NP-complete. There are relatively simple reductions from the Hamiltonian path problem to 3 of the 4 problems below.

Your Answer	Score	Explanation
Amongst all spanning trees of the graph, compute one with the smallest-possible number of leaves.		
For a given source s and destination t , compute the length of a shortest s - t path that has exactly $n-1$ edges (or $+\infty$, if no such path exists). The path is not allowed to contain cycles.		
For a given source s and destination t , compute the length of a shortest s - t path that has exactly $n-1$ edges (or $+\infty$, if no such path exists). The path is allowed to contain cycles.	✔ 1.00	Use a Bellman-Ford-type recurrence.
Amongst all spanning trees of the graph, compute one with the minimum-possible maximum degree. (Recall the degree of a vertex is the number of incident edges.)		
Total	1.00 / 1.00	

https://class.	001170070	ora/olao	~ 100	1117/f00	lhaa
1111105:7701455.	coursera.	.ora/arao	12-00 4 /0	uiz/ieeu	mac