EKN-812 Lecture 1

Methodology; Basic Theory of Demand

Jesse Naidoo

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- Lionel Robbins (1932): "Economics is the science which studies human behaviour as a relationship between ends and scarce means which have alternative uses."
- Gary Becker (1976): economics is defined by its method, not its subject matter.
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 - stable preferences
 - equilibrium (in either implicit or explicit "markets")
- economists study many types of "non-market" behavior:
 - crime
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 - fertility
 - health
 - time use

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- understanding mechanisms
- generating predictions for new circumstances
- obviously, theories have to be tested against evidence
 - so, we will avoid theories that are unfalsifiable (no empirical content
 - compare: astrology, Tarot reading
- what do we have that journalists don't?
 - coherent body of theory
 - the concept of "equilibrium": different people's actions have to be mutually consistent
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- preferences: axiomatic foundations
- Hicksian and Marshallian demand
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- "choice" is meaningless if there is no scarcity
- a simple situation in which resources are limited
 - two goods x_1 , x_2 available in any nonnegative amounts
 - constant prices $p_1, p_2 > 0$ and a given budget y
 - then $p_1 x_1 + p_2 x_2 \le y$
- consumer choices give us the functions $x_1^*(p, y), x_2^*(p, y)$
 - here $p = (p_1, p_2)$ is the vector of prices
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- Say we are choosing quantities of n goods with prices p_i (i = 1, ... n)
- the i-th budget share is

$$s_i = \frac{p_i x_i^*}{y}$$

• the income elasticity of the *i*-th good is

$$\eta_i = \frac{y}{x_i^*} \frac{\partial x_i^*}{\partial y}$$

• the elasticity of demand for good *i* with respect to the *j* pprice is

$$\varepsilon_{ij} = \frac{p_j}{x_i^*} \frac{\partial x_i^*}{\partial p_j}$$

- obviously these quantities are all "local"
 - might vary with the particular (p, y) facing the consumer
- shares and elasticities are unitless
 - why is this good?

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- budget constraint holds as an identity in (p, y), so we can differentiate it
- differentiate wrt y to get "Engel aggregation"
 - in elasticity form:

$$\sum_{i=1}^n s_i \eta_i \equiv 1$$

- budget-share weighted average of income elasticities is always:
- differentiate wrt p_j to get "Cournot aggregation"
 - in elasticity form:

$$s_j + \sum_{i=1}^n s_i \varepsilon_{ij} \equiv 0$$

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- · price changes have two effects on the budget set
 - change the relative price of goods
 - change aggregate "purchasing power"
- it is often useful to distinguish between these two mechanism for how prices affect choices
 - substitution effects due to changes in relative prices
 - income effects due to changes in overall purchasing power
- as a simple example of why this distinction might matter, consider two policies:
 - levy a general consumption tax to fund highway maintainence
 - collect tolls on drivers
- Slutsky compensation: alter income after a price change such that the original bundle is feasible
 - \bullet with two goods, suppose p_1 rises to $p_1'>p_1$; what is the Slutsky compensation?

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- price changes have two effects on the budget set
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- main result in consumer theory: compensated own-price effects are negative
 - "demand curves slope down"
 - we will see a more precise statement of this later
- however, a lot of the positive content of consumer theory comes from the budget constraint alone
 - not from particular assumptions about rationality
- suppose prices are p_1, p_2 and all consumers have the same income y
- suppose consumers are passive: half buy only x_1 and half buy only x_2
 - what is the market demand?
- ullet now, suppose p_1 rises to p_1' and we compensate everyone
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- suppose the set of bundles you can choose from is a subset of \mathbb{R}^n_+ (n-tuples of nonnegative reals)
- what do we mean by "preferences"?
 - a "relation"

 describing a person's evaluation of the statement "is at least as good as"
 - a "binary relation" in the sense that you need two bundles x, y in order to evaluate "x ≻ y"
- if this relation satisfies certain properties then:
 - we can construct a utility function u(x) that "represents" this person's preferences
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- We can construct a continuous utility function u that represents the preference relation

 if the preferences relation is
 - reflexive: for all x, $x \succeq x$
 - complete: for all x, y either $x \succeq y$ or $y \succeq x$
 - transative: if $x' \succeq x$ and $x'' \succeq x'$, then also $x'' \succeq x$
 - continuous: for any x, the sets $\{y: y \succeq x\}$ and $\{y: y \preceq x\}$ are closed
- often it's convenient to add:
 - convexity: if $x' \succeq x$, then for any $\alpha \in [0,1]$, $\alpha x' + (1-\alpha)x \succeq x$
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- two ways to think of the consumer's problem
- maximize utility subject to a budget constraint
 - $x^M(p,y) = \arg\max u(x)$ s.t. $px \le y$ are the Marshallian demands • $v(p,y) = \max u(x)$ s.t. $px \le y$ is the indirect utility function
- minimize the cost of obtaining a target level of utility
 - $x^H(p,u)= ext{arg min } px ext{ s.t. } u(x) \geq u ext{ are the } Hicksian \ demands$
 - \bullet $e(p,u)=\min px$ s.t. $u(x)\geq u$ is the expenditure function (or cost function
- "obviously":

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• x^M(p, e(p, u)) \equiv x^H(p, u) for all (p, u)
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- what are the analogous relationships between the expenditure and indirect utility functions?

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- easier to work with for welfare analysis (why?
- harder to use, because we don't get to observe utility levels
- let's notice some useful properties of e(p, u):
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 - differentiate the identity $x^{M}(p, e(p, u)) \equiv x_{i}^{H}(p, u)$ wrt p
- the result is called the "Slutsky equation":

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- we can translate the properties of Hicksian demand into elasticity form:
 - homogeneity: for all goods i,

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Marshallian Elasticities

- we've already seen some restrictions on Marshallian demand
 - Cournot aggregation

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 of course, we can exploit the relationship to the compensated elasticities to derive other implications

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- similarly, let's call i and j complements if an increase in the price of j leads to
 a decrease in the compensated demand for i
 - i.e. if $\varepsilon_{ij}^H < 0$
- what might go wrong if we defined things in terms of Marshallian demand?
- with a two-good demand system, you can only have substitutes (prove this!)

- so far we have only imposed the budget constraint on consumers
- suppose the quantities of some goods were fixed, e.g. because of rationing
 - say the quantity of good 1 is fixed at z, and x₋₁ is the vector of all the other goods
 - the consumer's expenditure-minimization problem becomes:

$$\overline{e}(p, u, z) = \min_{\substack{x = 1 \ x = 1}} p_1 z + p_{-1} x_{-1} \text{ s.t. } u(z, x_{-1}) \ge u$$

- let $\overline{x}^H(p_{-1}, u, z)$ be the constrained Hicksian demands
- notice how the price of the rationed good does not directly affect the constrained demands

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- let $\Delta(p, u, z) = \overline{e}(p, u, z) e(p, u)$ be the "excess" expenditure due to rationing
 - clearly $\Delta(p, u, z) \geq 0$ with a minumum where $z = x_1^H(p, u)$ why?
 - and, the constrained Hicksian demands satisf

$$\overline{x}_{i}^{H}(p_{-1}, u, x_{1}^{H}(p_{1}, p_{-1}, u)) \equiv x_{i}^{H}(p_{1}, p_{-1}, u)$$

• if we differentiate wrt the price of the rationed good (p_1) ,

$$\frac{\partial \overline{x}_i}{\partial z} = \frac{\sigma_{i1}}{\sigma_{11}}$$

- what does this tell us about the effects of rationing on the demand for other goods?
- and, if we differentiate with respect to p_i , we get

$$\frac{\partial \overline{x}_i^H}{\partial p_i} = \sigma_{ii} - \frac{\sigma_{i1}^2}{\sigma_{11}}$$

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