EKN-812 Lecture 2

Welfare Measurement; Restrictions on Preferences

Jesse Naidoo

University of Pretoria

• a direct proof of Shephard's Lemma: consider

$$e(p, u) = p \cdot x^{H}(p, u)$$

• differentiate with respect to p_i:

$$\frac{\partial e}{\partial p_i} = x_i^H + \sum_{j=1}^n p_j \frac{\partial x_j^H}{\partial p_i}$$

- but, we can ignore all the indirect effects:
 - use the utility constraint $u \equiv u(x''(p, u))$
 - then, notice that by the first-order conditions,

$$p_j = \lambda \frac{\partial u}{\partial x_i}$$

$$\frac{\partial \mathcal{L}}{\partial p_i} = \frac{\partial e}{\partial p_i}$$

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 - but, we can still find the sign of, e.g. price and income effects
 - · we do this by implicitly differentiating the system of first-order conditions
- e.g. the first-order conditions give us a system

$$u_{\mathsf{X}}(\mathsf{X},\mathsf{Y}) - \lambda p_{\mathsf{X}} \equiv 0 \tag{1}$$

$$\mu_y(x,y) - \lambda p_y \equiv 0 \tag{2}$$

$$n - p_{\mathsf{x}} x - p_{\mathsf{y}} y \equiv 0 \tag{3}$$

- if we differentiate with respect to (say) y we get a linear system for the income effects
 - can solve element-by-element using Cramer's rule
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- With two goods, a measure of the curvature of indifference curves
 - Does not generalize well to higher dimensions though
 - Morishima elasticities are more appropriate then, although non-symmetric
- A different way of defining substitutability: whether the elasticity of substitution σ_{ij} is greater or smaller than 1
 - i.e. do changes in the relative price p_i/p_j lead to more than proportional changes in relative quantities?
 - ullet Can show that σ_{ii} is related to Hicksian elasticities via the formula

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- the demands generated by u(x) are the same as those generated by f(u(x)), where f'>0
 - marginal rates of substitution are the same
 - but diminishing marginal utility can be overturned if f'' > 0
- certain types of restrictions are preserved by increasing transformations
 - we call those "ordinal" restrictions (depend only on ranking of bundles)
 - e.g. quasiconcavity, elasticity of substitution, price elasticities
 - concavity is not preserved by monotone transformations
- this sensitivity to how preferences are represented means we are usually skeptical of conclusions that depend on interpersonal comparisons of utility
 - Pareto efficiency does not have this weakness
 - nevertheless, there are important areas (e.g. optimal taxation) which make use
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- first, suppose u(x) is homogenous of degree 1
 - e.g. Cobb-Douglas preferences $u(x_1, x_2) = x_1^{\alpha} x_2^{1-\alpha}$
- then all income elasticities are 1:
 - consider $x^{M}(p, ty)$ for some t > 0
 - what is the indirect utility when you scale up income by t?
 - is called do some than $tr(p,y) = tr(x^{m}(p,y))$. If strictly batter, $x^{m}(p,y)$ wasn't optimal to begin with
 - thus, $x^M(p, ty) \equiv tx^M(p, y)$ for all t > 0
- to complete the proof: differentiate wrt t and evaluate at t = 1.
- now, because utility is ordinal, only need that there is some increasing function f such that f(u(x)) is homogenous of degree 1

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- you may be wondering if rational choice has any other implications besides the NSD Slutsky matrix
 - the answer is no
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- so far we have been talking about the positive implications of utility theory
- however, consumer theory also has normative uses:
 - tracking changes in the cost of living over time
 - measuring the gains from innovation (new goods)
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- consider a change in prices from p to p'
- the equivalent variation is the change in income that is equivalent to the price change, starting at the original prices
 - EV implicitly defined by v(p, y + EV) = v(p', y)
 - can show this is equivalent to EV = e(p, u') y where u' = v(p', y)
 - the price a consumer is willing to pay to avoid a price increase
- the compensating variation is similar but evaluated at the new prices
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- recall the Hicksian demands are the derivatives of the expenditure function
 - this means we can interpret EV and CV as areas under a Hicksian demand curve
 - but, which ones?
- consumer surplus is the area under a Marshallian demand curve
 - in the case of a normal good

$$EV \leq \Delta CS \leq CV$$

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$$\pi_{t+1,t} = \frac{e(p(t+1),u) - e(p(t),u)}{e(p(t),u)}$$

- problems:
 - RHS depends on u, unless preferences are homothetic
 - we don't know preferences (and hence e(p, u))
- obviously, heterogeneity in preferences makes this more complicated
- two common types of price indices:
 - Laspeyres indices use initial bundle as weights for later prices
 - Paasche indices use current quantities as weights for earlier prices
 - chained indices: break up long periods into accumulation of short-term changes
- an important practical issue is how often to update the weights
 - trade off accuracy vs cost of data collection
- dealing with new goods (and exit of old goods) is another important issue
 - one strategy: compare new goods to "appropriate" average of existing ones
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- suppose we have three goods, x_1, x_2 and x_3
 - initial prices are p⁰
 - however, (p_2, p_3) always move "in parallel"
 - we will see that we can define an artificial "composite commodity" and proceed as if there are only two goods
- let $e^*(p_1, \theta, u) = e(p_1, \theta p_2^0, \theta p_3^0, u)$
 - here e(p, u) is the usual expenditure function
 - we are suppressing (p_2, p_3) as an argument of e^*
- notice that e^* has all the usual properties of a cost function
 - increasing in (p, θ) and in u
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 - high and low quality wine, apples, etc
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- Can show that if y is large enough Marshallian elasticity is exactly ε . (If y is too small, spend entire budget on q, so $c^M(p, y) = 0$.)
 - What are the income elasticities of c and q?
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- These preferences are very useful for studying the demand for one good in isolation; c is a "composite commodity" consisting of "all other goods"
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• suppose you can group goods e.g.

$$u = u(v, w)$$

$$v = f(x_1, x_2)$$

$$w = g(y_1, y_2)$$

- we say (x_1, x_2) is weakly separable from (y_1, y_2)
 - immediate implication: can mechanically solve consumer's problem in two stages

$$\begin{array}{lcl} \pi_{v}^{*}(p_{x,1},p_{x,2},v) & = & \min p_{x,1}x_{1} + p_{x,2}x_{2} \text{ s.t. } f(x_{1},x_{2}) \geq v \\ \pi_{w}^{*}(p_{y,1},p_{y,2},v) & = & \min p_{y,1}y_{1} + p_{y,2}y_{2} \text{ s.t. } g(y_{1},y_{2}) \geq w \end{array}$$

then, solve "upper-level" consumer's problem

min
$$\pi_{\scriptscriptstyle V}(v) + \pi_{\scriptscriptstyle W}(w)$$
 s.t. $\mathit{u}(v,w) \geq \mathit{u}$

• suppose you can group goods e.g.

$$u = u(v, w)$$

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$$\min \pi_v(v) + \pi_w(w)$$
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- more subtly, MRS between x-goods does not depend on y-goods
 - this restricts substitution patterns and cross-price effects
- in particular, the cross-price elasticities for goods in different groups
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 - intuition: marginal rates of substitution only depend on own-group prices
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$$u(x) = \sum_{i=1}^{n} v_i(x_i)$$

- examples:
 - $u(x_1, x_2) = 1 + x_1 + x_2 + x_1x_2$ is additively separable
 - $u(x_1, x_2) = x_1 + x_2 + x_1 x_2^2$ is **not** why?
- if all the v_i are increasing and concave:
 - all goods are normal
 - no (net) complements
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obviously this is restrictive

- the other side to restrictiveness is that you need less data
- e.g. Deaton and Muellbauer (1980) shows that the Marshallian price elasticities satisfy

$$egin{array}{lll} arepsilon_{ii}^M &=& \phi \eta_i - \eta_i s_i (1 + \phi \eta_i) \ arepsilon_{ij}^M &=& - \eta_i s_j (1 + \phi \eta_j) \end{array}$$

- here ϕ is some constant that depends on preferences and prices
- important point is that you only need
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References

Deaton, Angus, and John Muellbauer. 1980. *Economics and Consumer Behavior*. Cambridge, UK: Cambridge University Press.

Vives, Xavier. 1987. "Small Income Effects: A Marshallian Theory of Consumer Surplus and Downward Sloping Demand." *Review of Economic Studies* 54 (1): 87. https://doi.org/10.2307/2297448.

Table of Contents

Loose Ends

Implications of Rational Choice

Welfare Measurement

Composite Commodity Theorem

Quasilinear Approximations

Separable Preferences