

# Assignment3functions.R

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#####
## dependencies
require(stats)

#####
## some useful functions
# discrete uniform distribution of 0~k
rdunif <- function(n, k) floor(runif(n) * (k + 1))
# discrete exponential distribution, bound specifies minimum value
rdexp <- function(n, rate = 0.1, bound = 0) floor(rexp(n, rate)+bound)
# discrete normal distribution
rdnorm <- function(n, mean = 0, sd = 1) round(rnorm(n, mean, sd))

#####
## simulate x ~ f(x), f is continuous
# interval: 01          x > 0 && x < 1
#             real_positive  x > 0
#             real          x is arbitrary real number
# method:      "inverse"    FUN = F-1(x)
#             "acceptance"  FUN = f
# parameter if known distribution is exponential, this parameter specifies lambda
# 1.instead of searching, we use optimization method to acquire c this time
# 2.if we want to use this function frequently on one single distribution, c can be preprocessed
rcont <- function(n,FUN,interval = c("01","real_positive","real"),
                  method = c("inverse","acceptance"),
                  c = NULL, parameter = NULL)
{
  if(n < 1 | !(is.function(FUN))) {
    stop("invalid input argument")
  }
  interval = match.arg(interval)
  method = match.arg(method)
  if(is.null(c))
    c = optimize(f = {if(interval == "01")FUN
                      else if(interval == "real_positive")function(x) FUN(x)/dexp(x)
                      else if(interval == "real")function(x) FUN(x)/dnorm(x)
                      },
                 maximum = T,
                 interval = {if(interval == "01")c(0,1)
                             else if(interval == "real_positive")c(0,100)
                             else if(interval == "real")c(-100,100)}}$objective
  if(is.null(parameter))
    parameter = 1
  result <- if (method == "acceptance") {
    sapply(1:n,function(y){
      if (interval == "01"){
        repeat{
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    u = runif(1);v = runif(1,parameter)
    if(u < (FUN(v)/c)){return(v)}
  }
}
else if (interval == "real_positive"){
  repeat{
    u = runif(1);v = rexp(1)
    if(u < (FUN(v)/c/dexp(v))){return(v)}
  }
}
else if (interval == "real"){
  repeat{
    u = runif(1);v = rnorm(1)
    if(u < (FUN(v)/c/dnorm(v))){return(v)}
  }
}
})
}
else if(method == "inverse"){
  sapply(runif(n),FUN)
}
result
}

#####
## simulate  $x \sim f(x)$ ,  $x$  is discrete
# interval:  finite           $x \in [0, \dots, bound]$ 
#           positive         $x \geq bound$ 
#           integer          $x$  is arbitrary integer
# method:    "inverse"       $FUN = F^{-1}(x)$ 
#           "acceptance"     $FUN = f$ 
# note:
# 1.if necessary we can use more accurate maximization algorithms to calculate  $c$ 
# 2.if we want to use this function frequently on one single distribution,  $c$  can be preprocessed
rdisc <- function(n, FUN, interval = c("finite","positive","integer"), bound = 0,
                 method = c("inverse","acceptance"), C = NULL){
  if(n < 1 | !(is.function(FUN))) {
    stop("invalid input argument")
  }
  interval = match.arg(interval)
  method = match.arg(method)
  if(is.null(C))
    C = if (interval == "finite"){max(sapply(0:bound,FUN))*(bound+1)}
          else if (interval == "positive"){max(sapply(bound:100,FUN)/dexp(bound:100),na.rm = T)}
          else if (interval == "integer"){max(sapply(-100:100,FUN)/dnorm(-1000:100),na.rm = T)}
  result <- if (method == "acceptance") {
    sapply(1:n,function(y){
      if (interval == "finite"){
        repeat{
          u = runif(1);v = rdunif(1,(bound+1))
          if(u < (FUN(v)/C*bound)){return(v)}
        }
      }
    })
  }
}

```

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else if (interval == "positive"){
  repeat{
    u = runif(1);v = rdexp(1,bound = bound)
    if(u < (FUN(v)/C/dexp(v))){return(v)}
  }
}
else if (interval == "integer"){
  repeat{
    u = runif(1);v = rdnorm(1)
    if(u < (FUN(v)/C/dnorm(v))){return(v)}
  }
}
})
}
else if(method == "inverse"){
  floor(sapply(runif(n),FUN))
}
result
}

```