

ECE374 Assignment 4

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Problem 4

4. Suppose we are given an array $A[1..n]$ of n distinct integers, which could be positive, negative, or zero, sorted in increasing order so that $A[1] \leq A[2] \leq \dots \leq A[n]$. Suppose we wanted to count the number of times some integer value x occurs in A . Describe an algorithm (as fast as possible) which returns the number of elements containing value x .

Solution:

Intuition: as the array is sorted, all occurrences of a number x must be consecutive. Therefore, we could solve this problem by using a binary search for the left bound of the consecutive x s and then use another binary search for the right bound of the consecutive x s. A subtraction of the indices would give us the number of x s.

Algorithm:

NUMBER_OF_X (A, x):

```
# binary search for the left most x
l = 0
r = length(A) - 1
left_most = None
while (l <= r):
    m = floor ((l + r) / 2)      # use floor to avoid the case of
                                # can't reach 0 (l=0, r=1, m=0.5→1)
    if (A[m]>=x):
        left_most=m
        r = m - 1
    else:
        l = m + 1

# binary search for the left most x
```

```
l = 0
r = length(A) - 1
right_most = None
while (l <= r):
    m = ceil ((l + r) / 2)      # use ceil to avoid the case of can't
                                # reach n-1 (l=n-2,r=n-1,m=n-1.5→n-2)

    if (A[m] <= x):
        right_most = m
        l = m + 1
    else:
        r = m + 1

if (left_most != None and right_most != None)
    return right_most - left_most + 1
else:
    return 0
```

With two binary searches, the running time of this algorithm is $O(\log n) + O(\log n) + O(1) = O(\log n)$.