

Lab 3

Recap: random variable

In this lab:

- Random Process
 - Bernoulli Process
- Poisson distribution vs Binomial distribution

Random Process

Def

A sequence of random variables

e.g.

Bernoulli process

$X_1, X_2, X_3, X_4, \dots$
 $\diagdown \quad \diagup \quad | \quad /$
 Bernoulli(p)

Characterize a Bernoulli Process

0 1 0 0 0 1 1 0 1 0 0 0 1 0 1 0

X:

L: 2 5 1 2 4 2

S: 2 7 8 10 14 16

C: 0 1 1 1 1 2 3 3 4 4 4 4 5 5 6 6

Poisson distribution.

$$X \sim \text{Poi}(\lambda)$$

$$P(X=k) = \frac{\lambda^k}{k!} e^{-\lambda}, \quad k \geq 0.$$

Binomial distribution

$$Y \sim \text{Binom}(n, p)$$

$$P(Y=k) = \binom{n}{k} p^k (1-p)^{n-k}, \quad 0 \leq k \leq n.$$

if • n is large

• p is small

$$\bullet \lambda \approx np$$

$$\Rightarrow X \approx Y$$