Software Quality Engineering:

Testing, Quality Assurance, and Quantifiable Improvement

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Chapter 9. Boundary Testing

- Input Domain Partitioning
- Simple Domain Analysis and Testing
- Important Boundary Testing Strategies
- Extensions and Perspectives

Non-Uniform Partition Testing

- Extensions to basic partition testing ideas:
 Non-uniform partitioned testing.
 - > Testing based on related problems

 - ▷ Boundary problems ⇒ What to do?
- Usage-related problems:

 - - ⇒ (Musa's) operational profiles (OPs)
- Boundary problems (This Chapter):
 - \Rightarrow input domain boundary testing (BT).

Boundary Testing: Overview

What is it?

- Classifying/partitioning of input space:
 - case-like processing model.
- Cover input space and related boundary conditions.
- Also called (input) domain testing.

• Characteristics and applications?

- Functional/black-box view(I/O mapping for multiple sub-domains)
- Well-defined input data:
 - numerical processing and decisions.
- ▶ Implementation information may be used.

I/O Variables and Values

• Input:

- \triangleright Input variables: x_1, x_2, \dots, x_n .
- ▶ Input space: n-dimensional.
- \triangleright Input vector: $X = [x_1, x_2, \dots, x_n]$.
- \triangleright Test point: X with specific x_i values.
- Domains and sub-domains: specific types of processing are defined.
- > Focus on input domain partitions.
- Output (assumed, not the focus)
 - Output variables/vectors/space/range similarly defined.
 - ▶ Mapped from input by a function.

Domain Partitioning and Sub-domains

- Input domain partitioning
 - ▷ Divide into sets of sub-domains.
 - "domain", "sub-domain", and "region" often used interchangeably
- A sub-domain is typically defined by a set of conditions in the form of:

$$f(x_1, x_2, \dots, x_n) < K$$

where "<" can also be substituted by ">", "=", " \neq ", " \leq ", or " \geq ".

Domain Partitioning and Sub-domains

- Domain (sub-domain) boundaries:
 - Distinguishes/defines different sub-domains.
 - \triangleright Each defined by it boundary condition, e.g., $f(x_1, x_2, \dots, x_n) = K$
 - Adjacent domains: those share common boundary(ies)
- Boundary properties and related points:

$$a_1x_1 + a_2x_2 + \ldots + a_nx_n = K$$

(Otherwise, it is a nonlinear boundary.)

- ⊳ Boundary point: on the boundary.
- Other properties w.r.t. domains later.

Boundary and Domain Properties

- Boundary properties w.r.t domains:
 - \triangleright Closed boundary: inclusive (\leq , \geq)
 - \triangleright Open boundary: exclusive (<, >)
- Domain properties and related points:

 - Den domain: all boundaries open
 - Linear/nonlinear domain: all linear boundary conditions?
 - ▶ Interior point: in domain and not on boundary.
 - Exterior point: not in domain and not on boundary.

Input Domain Partition Testing

• General steps:

- ▶ Identify input variable/vector/domain.
- ▶ Partition the input domain into sub-domains.
- ▶ Perform domain/sub-domain analysis.
- Define test points based on the analysis.
- > Perform test and followup activities.
- Boundary testing: Above with focus on boundaries.
- Domain analysis:
 - Domain limits in each dimension.
 - ▷ Domain boundaries (more meaningful).

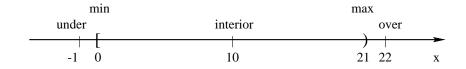
 - \triangleright Plotting for 1D/2D, algebraic for 3D+.

Problems in Partitioning

- Domain partitioning problems:
 - > Ambiguity: under-defined/incomplete.
 - ▷ Contradictions: over-defined/overlap.
 - ▶ Most likely to happen at boundaries.
- Related boundary problems:
 - > Closure problem.
 - \triangleright Boundary shift: $f(x_1, x_2, \dots, x_n) = K + \delta$
 - ▷ Boundary tilt: parameter change(s).

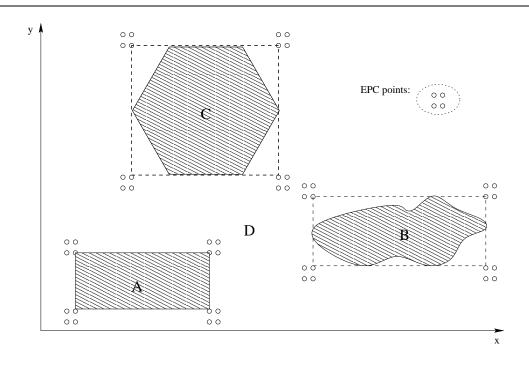
Simple Domain Analysis and EPC

- Simple domain analysis:
 - identify domain limits in each dimensionmin, max values
 - push "over" max, "under" min
 - ⇒ 4 values for each variable or dimension: under, min, max, over
- 1D example: Fig 9.1 (p.133)



- Extreme point combinations (EPC)
 - Combine above to derive test points.
 - \triangleright Combine variables (\times , cross-product).
 - \triangleright # testcases: $4^n + 1$.

Simple Domain Analysis and EPC



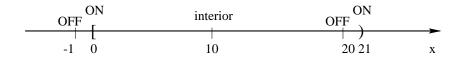
- 2D examples: 9.2 (p.134)
- Problems/shortcomings with EPC:
 - Missing boundary points: 2D example.
 (unless boundaries perfectly aligned)
 - \triangleright Exponential # testcases: $4^n + 1$.
 - \Rightarrow Need more effective strategies.

Boundary Testing Ideas

- Using points to detect boundary problems:
 - A set of points selected on or near a boundary: ON and OFF points.
 - ▷ Able to detect movement, tilt, etc.
 - Motivational examples for boundary shift.
- ullet neighborhood and ON/OFF points
 - \triangleright Region of radius ϵ around a point
 - > Theoretical: could be infinitesimal
 - > Practical: numerical precision
 - ▷ ON point: On the boundary
 - ▷ OFF point:
 - opposite to ON processing
 - off boundary, within ϵ distance
 - closed boundary, outside
 - open boundary, inside

Weak N x 1 Strategy

- N x 1 strategy (N-dimensional space)
 - N ON points (linearly independent): confirm (n-1)-D hyper-plane boundary.
 - ▷ 1 OFF point: centroid of ON points.
 - ▷ 1D: 1 ON, 1 OFF



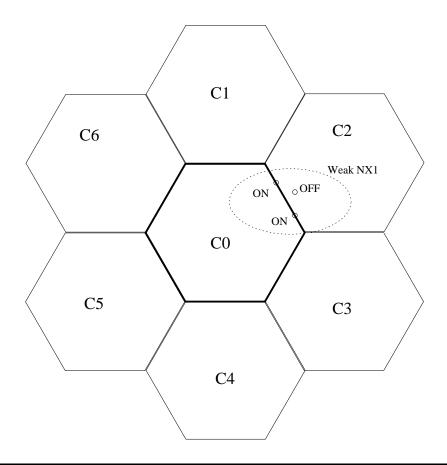
- Typical errors detected:
 - Closure bug

 - ⊳ Boundary tilt (later)

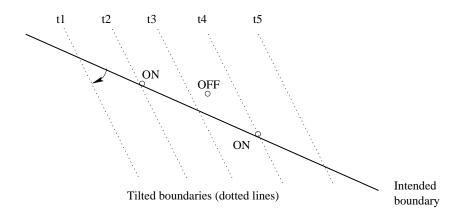
 - Missing boundary

Weak N x 1 Strategy

- N x 1: N ON and 1 OFF points
 - Weak: set of tests per boundary instead of per boundary segment.
 - \triangleright #test points: $(n+1) \times b + 1$
 - - advantages over EPC!



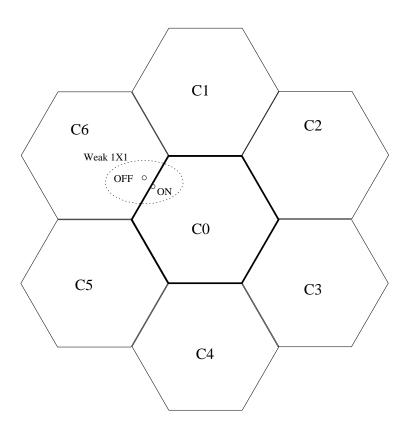
Weak N x 1 Strategy



- Boundary tilt: Fig 9.5 (p.138) above
 - ⊳ series of tilting points
 - some ON/OFF points combination will detect each tilt
- ullet Other problems detected pprox 1D example

Weak 1 x 1

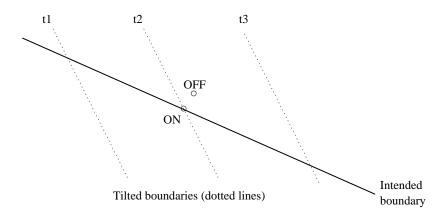
- Motivation: #test-points\u00ed without losing much of the problem detection capability.
 - \triangleright boundary defined by 1 ON 1 OFF (n ON points in weak $N \times 1$ form an equivalent class \Rightarrow sampling 1)
 - ▷ 2D example: Fig 9.6 (p.139) below.



Weak 1 x 1

- Typical errors detected:

 - ⊳ Boundary tilt (not always!)
 - Missing boundary
 - Extra boundary (sometimes)
- Tilting in Fig 9.7, p.140, below
 (miss tilting at ON point, vs Weak N×1)



Other BT Strategies

- Strong vs. weak testing strategies:
 - ▶ Weak: 1 set of tests for each boundary
 - ▷ Strong: 1 set of tests for each segment
- Why use strong BT strategies?

 - Coincidental correctness:particularly stepwise implementation

 - Use in safety-critical applications
- Nonlinear boundaries: Approximate (e.g., piecewise) strategies often useful.

BT Extensions

- Direct extensions
 - Data structure boundaries.
 - ▷ Capacity testing.
- Other extensions
 - - problem with boundary combinations
 - follow after boundary test (1X1 etc.)
 - test effective concerns
 - Output domain in special cases
 - similar to backward chaining
 - safety analysis, etc.
- Queuing testing example below.

BT and Queuing

- Queuing description: priority, buffer, etc.
- Priority: time vs. other:
 - b time: FIFO/FCFS, LIFO/stack, etc.
 - other/explicit: SJF, priority#, etc.
 - > purely random: rare
- Buffer: bounded or unbounded?
- Other information:
 - ▶ Pre-emption allowed?
 - Mixture/combination of queues
 - ▶ Batch and synchronization

Testing a Single Queue

- Test case design/selection:
 - ▷ Conformance to queuing priority.
 - ▶ Boundary test
 - ▶ Test cases: input + expected output.
 - Combined cases of the above.
- Testing specific boundary conditions:
 - b lower bound: 0, 1, 2 (always)
 - ⊳ server busy/idle at lower bound
 - \triangleright upper bounds: B, B \pm 1 (bounded Q) for bounded queue with bound B
- Other test cases:
 - > Typical case: usage-based testing idea.
 - ▷ Q unbounded: some capacity testing.

BT Limitations

- Simple processing/defect models:
 - ▷ Processing: case-like, general enough?
 - ▷ Specification: ambiguous/contradictory.
 - ▷ Boundary: likely defect.

Limitations

- ▶ Processing model: no loops.
- ▷ Coincidental correctness: common.
- \triangleright ϵ -limits, particularly problematic for multiplication products.
- OFF point selection for closed domain
 - possible undefined territory,
 - may cause crash or similar problems.
- Detailed analysis required.