

CS 5/7350 – Test 2
April 21, 2021

Name: _____

- This exam is **closed book** and **closed notes**.
- You MAY have a calculator and 1 page of notes that is 8.5 x 11 inches
- No cell phones, or other electronics except as required for zoom and only used for zoom or other proctoring.
- Pencil and/or pen are permitted.
- It is **3 hours** in duration plus time for scanning and uploading, etc.
- You should have 10 problems. Pay attention to the point value of each problem and dedicate time as appropriate.

On my honor, I have neither given nor received unauthorized aid on this exam.

SIGNED: _____

DATE: _____

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Name: _____

ID: _____

1. [8 pts] Consider the following NP completeness questions. Answer them with “some” “all” “none” or “unknown”
 - (i) Which Problems in NP are also in P? (“some” “all” “none” or “unknown”)
 - (ii) Which problems in NP are also in NP-Hard? (“some” “all” “none” or “unknown”)
 - (iii) If someone can solve the Circuit Sat problem in Polynomial Time, then all NP and all NP complete problems can be solved in Polynomial Time? (True or False)
 - (iv) NP means Non-Polynomial? (True or False)
 - (v) Some NP problems can be solved in polynomial time? (True or False)
 - (vi) Which NP-Hard Problems are also NP-Complete? (“some” “all” “none” or “unknown”)

2. [8 pts] Argue that the Hamiltonian Cycle is NP-Complete given that the Hamiltonian Path is NP-Complete

3. [7 pts] Compute the value for Z given that $((161 * Z) + 5729) \bmod 11609 = 11169$

4. [8 pts] How many colors are needed to color the following special graphs:

(i) A complete graph with $|V|$ vertices.

(ii) A cycle with an odd number of vertices

(iii) A tree.

(iv) A bipartite graph with 8 vertices in one partition and 9 vertices in the other partition.

- sides $\{-2, -2, 0, 0\}$ Die #3 has sides $\{1, 1, 1, 1\}$ and Die #4 has sides $\{0, 0, 0, 2, 2, 2\}$

(i) Fill in the table below

(ii) How many ways can you roll a 0 with these 4 dice?

(iii) What is the probability of rolling a 0 with these 4 dice?

(iv) How many ways can you roll a 4 with these 4 dice?

(v) What is the probability of rolling a 4 with these 4 dice?

[illegible]

- As an example, if the original sequence is 6,2,3,4,7 a regular longest increasing subsequence would be 2,3,4,7 but a longest 2-increasing subsequence would be 2,4,7.

3, 9, 6, 7, 14, 8, 11, 17, 12, 13, 20, 16, 17, 18, 23, 20, 24

[illegible]

The longest 2-increasing subsequence is:

- 67 65 68 65 257 256 69 258 260

- [illegible]

8. [12 pts] Consider an RSA encryption system that has a public key of 7433 for the value of e and 21353 for the value of the modulus n . With a quantum computer, you are able to factor the 21353 into the product of two primes: 131×163 .

Using this information, set up the table for the GCD (Extended Euclidian Algorithm)

What is the private key?

If you wanted to sign a message of value 3, what is the cipher text? (Compute the number)

9. [12 pts] You are interested in purchasing the items listed below. You have 14 points you can use to purchase items and you plan to pay cash for the rest. Setup and fill in the entire dynamic programming table for the problem and indicate which items you would purchase with points to minimize the cash you would have to spend for the rest.

Item 1: 3 points, \$12

Item 2: 4 points, \$14

Item 3: 7 points, \$18

Item 4: 4 points, \$10

Item 5: 2 points, \$7

Which items would you take:

10. [9 pts] The Levensthein Edit Distance determines the edit distance between two strings when Addition, Deletion and Substitution are allowed. Consider a different edit distance where only Addition and Deletion are allowed and Substitution is not.

Assume you have two strings: A and B. The i^{th} character of A is A_i and the j^{th} character of B is B_j .

- (i) When considering the i^{th} character of A and the j^{th} character of B, what is the “formula” for you would use for determining the value placed in the table at location i,j when finding the standard Levensthein Edit Distance

- (ii) When considering the i^{th} character of A and the j^{th} character of B, what is the “formula” for you would use for determining the value placed in the table at location i,j when finding the modified Levensthein Edit Distance without substitution

- (iii) When considering the i^{th} character of A and the j^{th} character of B, what is the “formula” for you would use for determining the value placed in the table at location i,j when finding the Longest Common Subsequence