CSE 7350 – Test 2
April 12, 2023

Name: _____

ID_____

- This exam is **closed book** and **closed notes**.

- No cell phones, or other electronics.

- Pencil and/or pen and TI-30Xa calculator only are permitted. No sharing of calculators.

- It is **3 hours** in duration.

- You should have 12 problems. Pay attention to the point value of each problem and dedicate time as appropriate.

On my honor, I have neither given nor received unauthorized aid on this exam.

SIGNED:_____

DATE:_____

CSE 7350 – Exam #2
April 12, 2023

Name: _____

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[+5 pts for CS-5350 students]

1. [10 pts] An implementation requires 3 days to run for an input size of 64. How long would the implementation take to run for an input size of 128 if:

    (i)   The implementation is $\Theta(n^3)$?

    (ii)   The implementation is $\Theta(n)$?

    (iii)   The implementation is $\Theta(n^2)$?

    (iv)   The implementation is $\Theta(n!)$?

    (v)   The implementation is $\Theta(2^n)$?

2. [6 pts] Set up the table and show the Extended Euclidean Algorithm for computing 1/23 modulo 15717. Give the answer as well:

3. [10 pts] Consider an RSA encryption system that has a public key of 294947 for the value e and 812909 for the value of the modulus N. You also saw a message that had been encrypted by the public key. The value of this encrypted message is 3.

      (i)   You are able to factor N=561233 into the product of two prime numbers 853 * 953. What is the value of the private key? Show your work including the table for computing the Extended Euclidean Algorithm.

      (ii)   What was the message before it was encrypted (Give an integer)

4. [10 pts] Set up the table to find the longest increasing sub-sequence of the following sequence: 5, 6, -3, 9, -1, 10, 4, 7, 8, -2, 6, 9, 7, 5, 2

5. [10 pts] Consider the Levensthein Edit Distance for two strings A and B.

    (i)   Write the equation describing what you would put in the table for location $T[i,j]$.

    (ii)   Fill in the following table for finding the "Levensthein Edit Distance" for two strings, M and N

$$M = A \; B \; X \; B \; Y \; C \qquad N = A \; Z \; X \; B \; C \; Y$$

6. [6 pts] Using n_0 equal to 10, find the tightest C_1 and C_2 possible to show that
$$f(n) = 5n^3 + 6n^2 + 2n + 18 \text{ is } \Theta(n^3).$$

7. [10 pts] Consider the Longest Common Subsequence for two strings A and B.

(iii)   Write the equation describing what you would put in the table for location T[i,j].

(iv)   Fill in the following table for finding the "Longest Common Subsequence" for two strings, M and N

M = A B X B Y C   N = A Z X B C Y

8. [10 pts] You are interested in purchasing the items listed below. You have 12 points you can use to purchase items and you plan to pay cash for the rest. Setup and fill in the entire dynamic programming table for the problem and indicate which items you would use points for.

Item 1: 3 points, $5
Item 2   5 points, $8
Item 3: 7 points, $9
Item 4: 4 points, $5
Item 5: 2 points, $4

9. [10 pts] You have 3 different dice that are not evenly weighted:
  - Dice 1 has sides {1,2,3} and a 20% chance of rolling a 1, a 30% chance of rolling a 2 and a 50% chance of rolling a 3.
  - Dice 2 has sides {2,2,3,3,3,4,4} with a 20% chance for each 2, a 10% chance for each 3 and a 15% chance for each 4.
  - Dice 3 has sides {1,1,2,2} with a 20% chance for each 1, a 30% chance for each 2
  - Set up the table for the dynamic programming algorithm (using percentages instead of counts) and fill in the complete column for Dice 1 and Dice 2 and Dice 3.
  - What is the probability of rolling a 6 with these dice?

10. [6 pts] Argue that the Problem I of finding the longest increasing subsequence is just as hard or possibly harder (with in $\Theta(n)$ extra work) than the Problem D of finding the longest decreasing subsequence

11. [6 pts] You have a tree with the following in-order and pre-order traversals. Draw the tree:

IN ORDER: T M P X R A S L
POST_ORDER: M T X A R S P L

12. [6 pts] Give an in-order and pre-order traversal that cannot form a tree:

Scratch Paper