CS 5/7350 – Test 3 May 11, 2022

Name:

• Th	nis exam is closed book and closed notes.
• No	o cell phones, or other electronics except for non-graphing calculator.
	encil and/or pen and non-graphing calculator only are permitted. No aring of calculators
• It	is 3 hours in duration plus time for scanning and uploading, etc.
	ou should have 14 problems. Pay attention to the point value of each oblem and dedicate time as appropriate.
On my honor, I h	have neither given nor received unauthorized aid on this exam.
	SIGNED:
	DATE:

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Name:			
ID:			

[+7 pts extra credit due to max quiz score for CS5350 Students]

- 1. [11 pts] Consider the following NP completeness questions. Answer them with the best answer of "some" "all" "none" or "unknown"
 - (i) Which Problems in NP are also in P? ("some" "all" "none" or "unknown")
 - (ii) Which Problems in P are also in NP? ("some" all") "none" or "unknown")
 - (iii) Which Problems in NP-Hard are also in NP? ("some" "all" "none")
 - (iv) Which Problems in NP-Complete are in NP-Hard ("some" "all" "none" or "unknown")
 - (v) If someone can solve an NP-Complete problem in Polynomial Time, then all NP and all NP-Hard problems can be solved in polynomial time. (true or false)
 - (vi) If someone can solve an NP-Complete problem in Polynomial Time, then all NP and all NP-Complete problems can be solved in polynomial time. (true or false)
 - (vii) At least 1 NP problem has a known solution to solve it in polynomial time? (True or False)
 - (viii) All NP-Complete problems are in P ("true" "false" or "unknown"
 - (ix) Which NP-Hard Problems are also NP-Complete? "some" all" "none" or "unknown")
 - (x) To show a problem, Q, is NP-Complete, you must show Problem Q is NP and that a solver for another NP-Hard problem can solve problem Q as well. (True or False)
 - (xi) To show a problem, Q, is NP-Complete, you must show Problem Q is NP and that a solver for problem Q can solve another NP-Hard problem (True or False)

- 2. [6 pts] Consider an LZW compression scenario with a dictionary that contained 1024 entries. In this dictionary, entries 0-255 were the standard ASCII values and entries 256-1023 were the dynamic part of the dictionary. This compression was able to compress a file of 1000kB to 750kB:
 - (i) What is one reason that a larger dictionary of size 2048 with dynamic entries from 256-2047 might cause the file to compress SMALLER than 750kB?

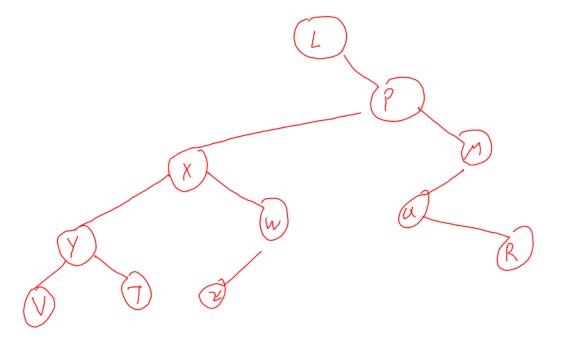
A larger dictionary can allow more patterns to be remembered and used without having to build them up again.

(ii) What is one reason that a larger dictionary of size 2048 with dynamic entries from 256-2047 might cause the file to compress LARGER than 750kB

A larger dictionary means that more bits are needed for each symbol in the compressed message.

3. [6 pts] You have a tree with the following in-order and pre-order traversals. Draw the tree:

IN ORDER: LVYTXZWPQRM PRE ORDER: LPXYVTWZMQR



- 4. [6 pts] You have 3 dice. Each one is different.
 - Die #1 has sides { 0, 1, 2 } with a
 - Die #2 has sides { 1, 2, 3 } with a
 - Die #3 has sides {0, 1} with a
 - (i) Fill in the table for the dynamic programming algorithm to solve the problem.
 - (ii) What is the probability of rolling a 0?
 - (iii) What is the probability of rolling a 3? 5/18
 - (iv) What is the probability of rolling a 6?

Vw	D ₁	11,12	D1.2.3	
O	1	6	<u>o</u>	
()	1	l	
2	1	2	3	
3	6	3	5	
Ч	0	2	5	
5	0		3	
6	0	0	1	

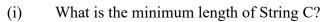
- 5. [6 pts] Answer the following questions.:
 - (i) A program requires 5s to attack an encryption key of 128 bits. If the running time is Θ (2ⁿ) about how many <u>vears</u> would it take to brute force attack an encryption key of 256 bits? (note there are about 32 million seconds in a year)

(ii) A program requires 5s to attack an encryption key of 128 bits. If you have access to a quantum computer where the running time is Θ (n²) about how many seconds would it take to brute force attack an encryption key of 256 bits?

6. [6 pts] Use the DGT algorithm discussed in class to determine how to represent the value 1023 using the number system $\beta=5$, $D=\{-2,-1,0,1,7\}$. Show your work.

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7.	[8 pts] You have two strings, A and B.
	• String A has a length of 11.
	• String B has a length of 8.
	• String C has an unknown length.
	• The Longest Common Subsequence between String A and C is 5.



5

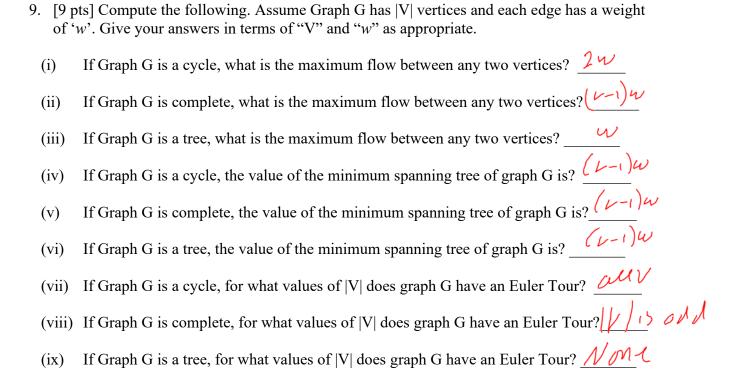
(ii) What is the maximum length of String C?

in finith

- (iii) What is the minimum length of the Levensthein Edit Distance of String A and String C?
- (iv) What is the maximum length of the Levensthein Edit Distance of String A and String B?
- 8. [6 pts] A program takes 10 seconds to process a data set of 1000 items using an algorithm that is Θ (n³). You want to process a data set of 10,000 items.
 - (i) How long would it take to process these 100,000 items on a computer that is 5 times faster using the algorithm that is Θ (n³)?

2,000,000 Sec

(ii) How long would it take to process these 100,000 items if the computer is the same speed, but the algorithm is Θ (n²) instead?



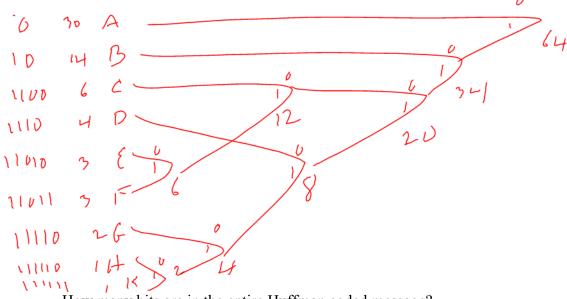
10.[5 pts] Argue that the problem, S, of sorting an unsorted array of integers of length greater than 100 elements is at least as hard - and maybe even harder - than the problem, L, of finding the median of the same array.

I can use a solver for S to solve L by sorting the array and returning the element it the middle index. since a solver for S can also solve L, s must be at least as hard or possibly harder than L.

11. [9 pts] A message contains the following number of each symbol:

30 A's, 14 B's, 6 C's, 4 D's, 3 E's, 3 F's, 2 G's, 1 H and 1 K.

Create a Huffman coding for each symbol:



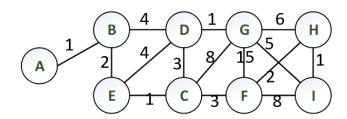
How many bits are in the entire Huffman coded message?

150

How much entropy does each "C" have?

3.45

12. [6 pts] Consider the following graph. When necessary for the algorithm, use vertex C as the starting vertex:



(i) Give a smallest last vertex ordering for the graph. Circle in your ordering the first vertex you wrote down for that ordering.

IHF6CDEBA

(ii) What is the edge you would choose 3rd when finding a minimum spanning tree with Kruskal's algorithm?

AnB

(iii) What is the edge you would choose 3rd when finding a minimum spanning tree with Prim's algorithm?

AOB

- 13. [4 pts] Two people need to establish a secret key for encrypting communications. They agree to use a Diffie-Hellman key exchange with a modulus of 11 and decide on 2 as the base. Person A chooses a random value performs the appropriate computations and sends the value 5 to person B. Person B chooses a random value of 3 and performs the appropriate computations:
 - a. What is the value Person B sends to Person A



b. What is the shared secret key between Person A and Person B

4

- 14. [8 pts] Consider an RSA encryption system that has a public key of 339251 for the value e and 748081 for the value of the modulus N. You also saw a message that had been encrypted by the public key. The value of this encrypted message is 2.
 - You are able to factor N=748081 into the product of two prime numbers 853 * (i) 877. What is the value of the private key? Show your work including the table for computing the Extended Euclidean Algorithm.
 - (ii) What was the original message before encryption? (Give an integer)

D=11 M=2048

15. [4 pts] Using n_0 equal to 10, show that $f(n) = 6n^3 + 2n^2 + 4n + 1$ is $\Theta(n^3)$.

b L Cir³ = 6n³ + 2n² + 4n + 1 & C₂n³ 0 C C C 6 2 + 4/2 + 1/2 = C₂ + 4/2 + 1/2 = C₂ Cr = 6.241

CS 5/7350 – Final Exam May 12, 2021

Name: _____

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```
LZW ENCODE:

set w = NIL
loop
  read a character k
  if wk exists in the dictionary
      w = wk
  else
      output the code for w
      add wk to the dictionary
      w = k
endloop
```

LZW DECODE:

```
read a character k
entry = dictionary entry for k
output entry
w = entry
loop
   read a character k
   entry = dictionary entry for k
   output entry
   add w + first char of entry to the dictionary
w = entry
endloop
```

Scratch Paper