

Leading-order asymptotic for Legendre polynomials

16 июля 2016 г.

The generating function for Legendre polynomials is, as it's well-known,

$$\frac{1}{\sqrt{1-2t\cos\theta+t^2}} = \sum_{n=0}^{\infty} P_n(\cos\theta)t^n \quad (1)$$

That leads to the following expression for $P_n(\cos\theta)$:

$$P_n(\cos\theta) = \int \frac{dt}{t^{n+1}\sqrt{1-2t\cos\theta+t^2}} \quad (2)$$