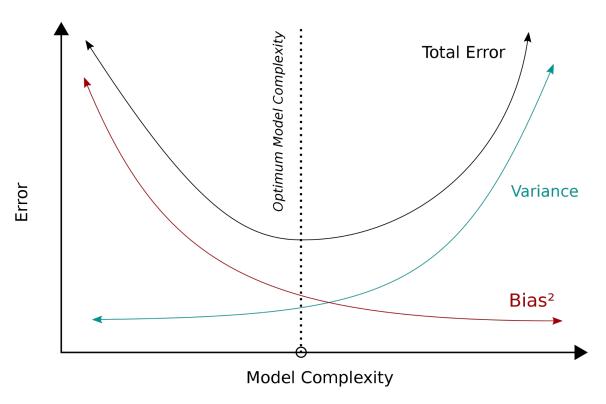
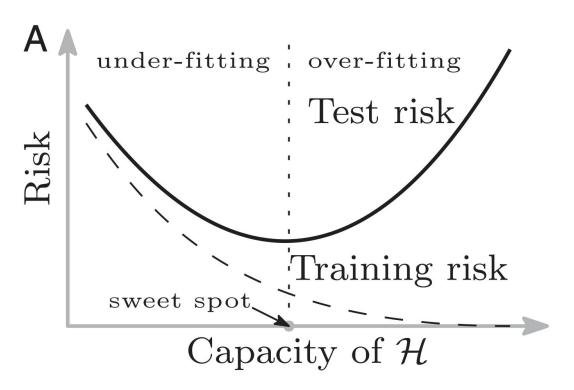
# Modern ML / DL vs Classical Bias-Variance Tradeoff

### Classical Bias vs Variance Tradeoff

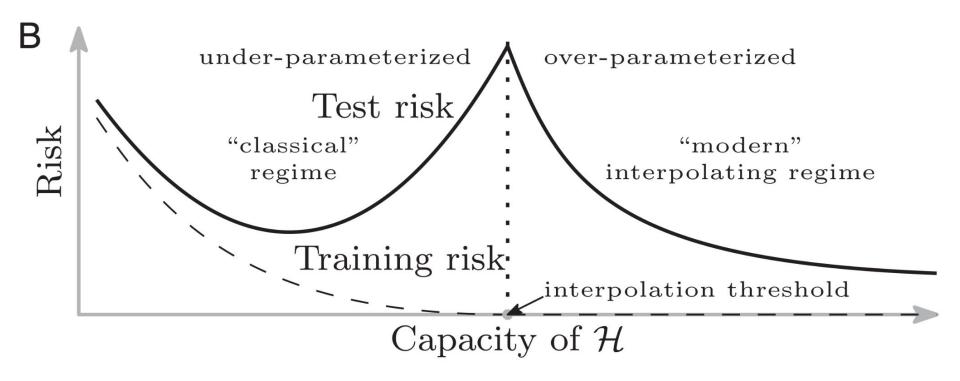


# Classical: Under-fitting vs Over-fitting



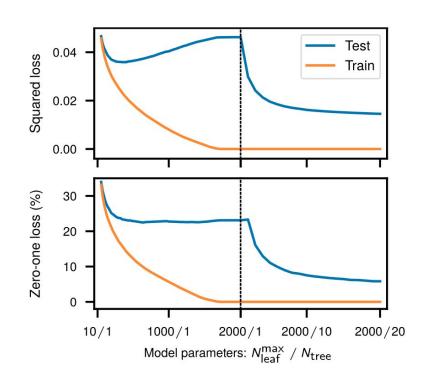
Belkin, M., Hsu, D., Ma, S., & Mandal, S. (2019). Reconciling modern machine-learning practice and the classical bias–variance trade-off. *Proceedings of the National Academy of Sciences*, *116*(32), 15849-15854.

## Modern: Under-parameterized vs Over-parameterized



Belkin, M., Hsu, D., Ma, S., & Mandal, S. (2019). Reconciling modern machine-learning practice and the classical bias–variance trade-off. *Proceedings of the National Academy of Sciences*, 116(32), 15849-15854.

### Double Descent - Random Forest

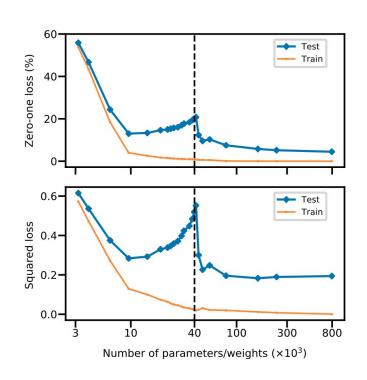


The double-descent risk curve is observed for random forests with increasing model complexity trained on a subset of MNIST (n = 104, 10 classes).

Its complexity is controlled by the number of trees (N *tree*) and the maximum number of leaves allowed for each tree (N max leaf)

Belkin, M., Hsu, D., Ma, S., & Mandal, S. (2019). Reconciling modern machine-learning practice and the classical bias-variance trade-off. *Proceedings of the National Academy of Sciences*, 116(32), 15849-15854.

### Double Descent - Fully Connected Neural Network



Double-descent risk curve for a fully connected neural network on MNIST. Shown are training and test risks of a network with a single layer of H hidden units, learned on a subset of MNIST ( $n = 4 \times 10^3$ , d = 784, K=10 classes).

The number of parameters is  $(d+1)\cdot H+(H+1)\cdot K$ .

The interpolation threshold (black dashed line) is observed at n · K.

Belkin, M., Hsu, D., Ma, S., & Mandal, S. (2019). Reconciling modern machine-learning practice and the classical bias-variance trade-off. *Proceedings of the National Academy of Sciences*, 116(32), 15849-15854.