Does Size Matter? (Estimation of Banana Weight with a regression modeling appraoch)

Scott Graham, Kaisa Roggeveen February 13, 2018

Summary

Introduction

The purpose of this study was to determine the most effective regression model to predict the weight of a banana using external measurements. This study also demonstrated multiple techniques for developing regression models. These models were then examined to demonstrate their effectiveness at creating regression models.

Data Collection

First a small sample set bananas were purchased from the Real Canadian Superstore. The weight, length, diameter and circumference were then calculated using a scale and a ruler.

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.003 0.418 0.621 0.572 0.757 0.979
```

In order to determine the minimum sample size needed, random sample sizes of 10 were generated using radius and length as the predictors. The correlation of the random sample sizes were calculated and a matrix of the correlations were generated. The value of the squared population multiple correlation coefficients with two predictor variables was then calculated and determined to be approximately 0.5718. From this the minimum sample size required was then determined from the table from Gregory T. Knofcznski's Sample Size When Using Multiple Linear Regression for Prediction, the minimum sample size was determined to be between 15 and 35, therefore the minimum number of bananas required was finalized at 24 bananas.

Analysis

To begin analysis a model using all predictor variables was created. In this case the density of the banana is assumed to be a constant.

Let:

$$W = \text{Weight (g)}, L = \text{Length (mm)}, R = \text{Radius (mm)}$$

Then:

$$\log(W) = \log(L) + \log(R) + \log(C)$$

In the second model the predictor variable, circumference, was removed.

$$\log(W) = \log(L) + \log(R)$$

The third model considered only one predictor, radius.

$$\log(W) = \log(R)$$

The fourth model considered the predictor, length.

```
\log(W) = \log(L)
```

```
##
## Call:
## lm(formula = Weight_log ~ Length_log + Radius_log + Circumference_log,
       data = .)
##
##
## Residuals:
##
        Min
                  1Q
                      Median
                                    3Q
                                            Max
## -0.24351 -0.06228 0.02400 0.06062
                                        0.11528
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      10.0594
                                 26.3199
                                           0.382
## Length_log
                       0.1230
                                  0.1275
                                           0.965
                                                    0.346
## Radius log
                       7.5264
                                 14.0928
                                           0.534
                                                    0.599
## Circumference_log -5.7885
                                 14.1601
                                         -0.409
                                                    0.687
## Residual standard error: 0.09248 on 20 degrees of freedom
## Multiple R-squared: 0.3318, Adjusted R-squared: 0.2316
## F-statistic: 3.31 on 3 and 20 DF, p-value: 0.04104
##
## Call:
## lm(formula = Weight_log ~ Radius_log + Length_log, data = .)
## Residuals:
        Min
                  1Q
                      Median
                                    3Q
## -0.24861 -0.05259 0.02164 0.05202 0.11544
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
               -0.6702
                            1.9132
                                   -0.350 0.72961
## Radius_log
                 1.7702
                            0.5596
                                     3.163 0.00468 **
## Length_log
                 0.1223
                            0.1249
                                     0.979 0.33888
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.09062 on 21 degrees of freedom
## Multiple R-squared: 0.3262, Adjusted R-squared: 0.2621
## F-statistic: 5.084 on 2 and 21 DF, p-value: 0.01583
##
## Call:
## lm(formula = Weight_log ~ Radius_log, data = .)
## Residuals:
##
                  1Q
                      Median
                                    3Q
        Min
                                            Max
## -0.25201 -0.05851 0.02530 0.05814 0.12150
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                 0.3046
                            1.6319
                                     0.187 0.85363
## (Intercept)
                                     3.038 0.00604 **
## Radius_log
                 1.6689
                            0.5494
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.09054 on 22 degrees of freedom
## Multiple R-squared: 0.2955, Adjusted R-squared: 0.2635
## F-statistic: 9.227 on 1 and 22 DF, p-value: 0.006043
##
## Call:
## lm(formula = Weight_log ~ Length_log, data = .)
##
## Residuals:
        Min
                   1Q
                         Median
                                      3Q
## -0.204865 -0.072290 -0.000595 0.055375 0.177835
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                          0.80371
                                    6.209
## (Intercept) 4.99043
                                             3e-06 ***
## Length_log
              0.04917
                          0.14574
                                    0.337
                                            0.739
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1076 on 22 degrees of freedom
## Multiple R-squared: 0.005146,
                                  Adjusted R-squared: -0.04007
## F-statistic: 0.1138 on 1 and 22 DF, p-value: 0.739
```

Res.Df	RSS	Df	Sum of Sq	\mathbf{F}	$\Pr(>F)$
21	0.1724705	NA	NA	NA	NA
20	0.1710414	1	0.0014291	0.1671057	0.687041
Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
22	0.1803370	NA	NA	NA	NA
20	0.1710414	2	0.0092956	0.5434713	0.5890658
Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)

NA

NA

NA

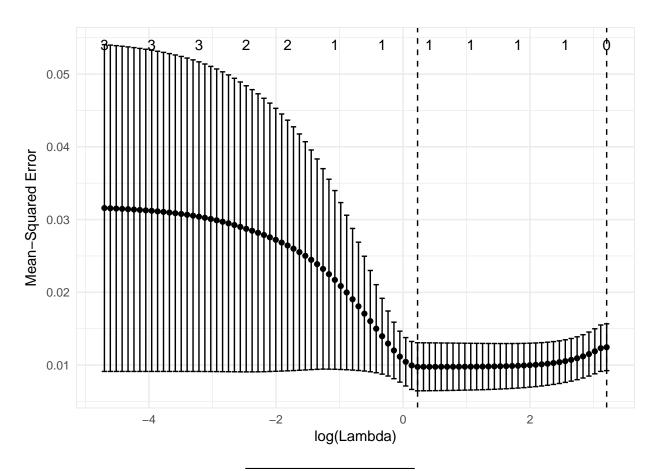
NA

22

per fold

0.1803370

 $\mbox{\tt \#\#}$ Warning: Option grouped=FALSE enforced in cv.glmnet, since < 3 observations $\mbox{\tt \#\#}$ per fold

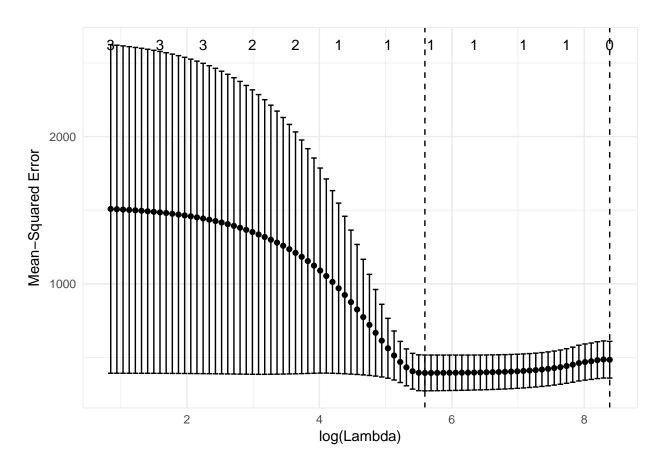


	1
(Intercept)	0.55713
Length	0.00000
Radius	0.00000
Circumference	0.00000
Length_log	0.00000
Radius_log	1.58392
$Circumference_log$	0.00000

	1
(Intercept)	5.261471
Length	0.000000
Radius	0.000000
Circumference	0.000000
Length_log	0.000000
Radius_log	0.000000
$Circumference_log$	0.000000

 $\mbox{\tt \#\#}$ Warning: Option grouped=FALSE enforced in cv.glmnet, since < 3 observations $\mbox{\tt \#\#}$ per fold

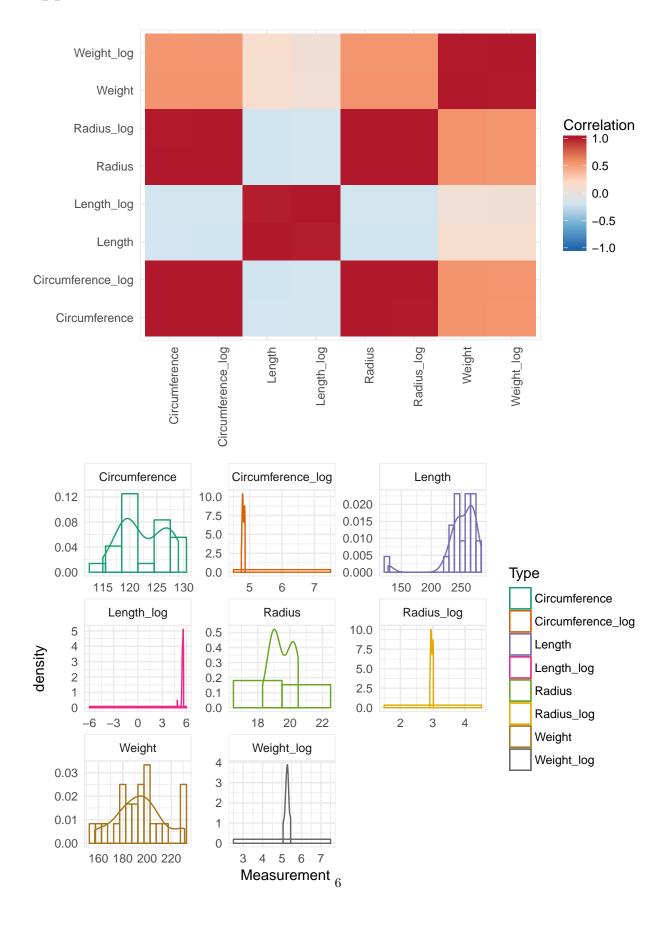
 $\mbox{\tt \#\#}$ Warning: Option grouped=FALSE enforced in cv.glmnet, since < 3 observations $\mbox{\tt \#\#}$ per fold

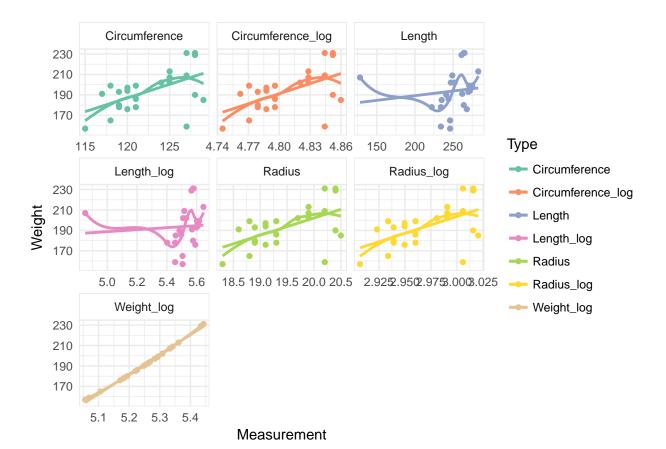


	1
(Intercept)	-725.4831
Length	0.0000
Radius	0.0000
Circumference	0.0000
Length_log	0.0000
Radius_log	309.5136
${\bf Circumference_log}$	0.0000

	1
(Intercept)	193.7917
Length	0.0000
Radius	0.0000
Circumference	0.0000
Length_log	0.0000
Radius_log	0.0000
$Circumference_log$	0.0000

Appendix





Cross Validation

```
## Analysis of Variance Table
##
## Response: Weight_log
             Df Sum Sq Mean Sq F value Pr(>F)
## Length_log 1 0.0013 0.0013
                                  0.16 0.6928
## Radius_log 1 0.0822 0.0822
                                  10.01 0.0047 **
## Residuals 21 0.1725 0.0082
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
## fold 1
## Observations in test set: 8
##
                 [,1]
                        [,2]
                               [,3]
                                       [,4]
                                              [,5]
                                                      [,6]
                                                             [,7]
              5.2368 5.2368 5.196
                                   5.1998 5.3143 5.2304
## Predicted
                                                           5.344
                                                                  5.215
## cvpred
              5.2428 5.2428
                             5.207
                                    5.2131 5.3184 5.2464
                                                           5.358
## Weight_log 5.2832 5.2679 5.106 5.1818 5.3613 5.1818 5.220 5.193
## CV residual 0.0404 0.0251 -0.101 -0.0314 0.0429 -0.0646 -0.137 -0.029
##
## Sum of squares = 0.04
                           Mean square = 0
##
## fold 2
```

```
## Observations in test set: 8
                                      [,4] [,5]
##
                   [,1] [,2] [,3]
                                                     [,6]
                                                            [,7]
                                                                 [.8]
               5.24195 5.348 5.333 5.2350 5.2548 5.3386 5.1853 5.3251
               5.23389 5.324 5.310 5.2248 5.2417 5.3184 5.1822 5.3056
## cvpred
              5.22575 5.434 5.442 5.1705 5.2933 5.2470 5.2523 5.3423
## Weight log
## CV residual -0.00814 0.109 0.132 -0.0543 0.0516 -0.0714 0.0701 0.0367
                           Mean square = 0.01
                                                 n = 8
## Sum of squares = 0.05
##
## fold 3
## Observations in test set: 8
               [,1]
                    [,2]
                             [,3]
                                                         [,7]
                                    [,4]
                                          [,5]
                                                  [,6]
              5.22 5.318 5.1488 5.3497 5.2822 5.2976 5.2173 5.2101
## Predicted
## cvpred
              4.78 5.267 5.1137 5.3771 5.2744 5.2788 5.2464 5.2500
## Weight_log 5.33 5.069 5.0562 5.4424 5.3083 5.3083 5.2627 5.2933
## CV residual 0.55 -0.198 -0.0574 0.0654 0.0339 0.0295 0.0163 0.0433
##
## Sum of squares = 0.35
                           Mean square = 0.04
                                                 n = 8
## Overall (Sum over all 8 folds)
##
      ms
## 0.0183
## # A tibble: 24 x 13
##
         ID Weight Radius Length Circumference Weight_log Radius_log
      <int> <int> <dbl> <int>
##
                                        <int>
                                                   <dbl>
                                                              <dbl>
## 1
         1
              197
                    19.1
                            272
                                          120
                                                    5.28
                                                               2.95
   2
          2
               194
                    19.1
                            272
                                          120
                                                    5.27
                                                               2.95
##
## 3
          3
              165
                    18.8
                            246
                                          118
                                                    5.11
                                                               2.93
##
  4
          4
              186
                    19.3
                            244
                                          121
                                                    5.23
                                                               2.96
## 5
              178
                    18.9
                                          119
                                                    5.18
         5
                            234
                                                               2.94
##
   6
         6
              207
                    19.9
                            128
                                          125
                                                    5.33
                                                               2.99
##
  7
         7
              213
                    19.9
                            283
                                          125
                                                    5.36
                                                               2.99
##
  8
              178
                    19.3
                            222
                                          121
                                                    5.18
                                                               2.96
         8
## 9
         9
              229
                    20.4
                            261
                                          128
                                                    5.43
                                                               3.02
## 10
         10
              231
                    20.2
                            265
                                          127
                                                    5.44
                                                               3.01
## # ... with 14 more rows, and 6 more variables: Length_log <dbl>,
      Circumference_log <dbl>, Predicted <dbl>, cvpred <dbl>, `CV Residual`
## # <dbl>, Residual <dbl>
MAE
## # A tibble: 1 x 2
```

```
## # A tibble: 1 x 2
## MAE MPAE
## <dbl> <dbl>
## 1 13.7 0.0722
```