

Does Size Matter? (Estimation of Banana Weight with a regression modeling approach)

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Summary

Introduction

The purpose of this study was to determine the most effective regression model to predict the weight of a banana using external measurements. This study also demonstrated multiple techniques for developing regression models. These models were then examined to demonstrate their effectiveness at creating regression models.

Data Collection

First a small sample set bananas were purchased from the Real Canadian Superstore. The weight, length, diameter and circumference were then calculated using a scale and a ruler.

##	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
##	0.003	0.418	0.621	0.572	0.757	0.979

In order to determine the minimum sample size needed, random sample sizes of 10 were generated using radius and length as the predictors. The correlation of the random sample sizes were calculated and a matrix of the correlations were generated. The value of the squared population multiple correlation coefficients with two predictor variables was then calculated and determined to be approximately 0.5718. From this the minimum sample size required was then determined from the table from Gregory T. Knofczynski's Sample Size When Using Multiple Linear Regression for Prediction, the minimum sample size was determined to be between 15 and 35, therefore the minimum number of bananas required was finalized at 24 bananas.

Analysis

To begin analysis a model using all predictor variables was created. In this case the density of the banana is assumed to be a constant.

Let:

$$W = \text{Weight (g)}, L = \text{Length (mm)}, R = \text{Radius (mm)}$$

Then:

$$\log(W) = \beta_0 + \beta_1 \log(L) + \beta_2 \log(R) + \beta_3 \log(C) \implies W = e^{\beta_0} \times L^{\beta_1} \times R^{\beta_2} \times C^{\beta_3}$$

In the second model the predictor variable, circumference, was removed. This is because $C = 2\pi R$.

$$\log(W) = \beta_0 + \beta_1 \log(L) + \beta_2 \log(R)$$

The third model considered the predictor, length.

$$\log(W) = \beta_0 + \beta_1 \log(L)$$

The fourth model considered only one predictor, radius.

$$\log(W) = \beta_0 + \beta_2 \log(R)$$

```
##
## Call:
## lm(formula = Weight_log ~ Length_log + Radius_log + Circumference_log,
##     data = .)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.24351 -0.06228  0.02400  0.06062  0.11528
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    10.0594     26.3199   0.382   0.706
## Length_log      0.1230      0.1275   0.965   0.346
## Radius_log      7.5264     14.0928   0.534   0.599
## Circumference_log -5.7885     14.1601  -0.409   0.687
##
## Residual standard error: 0.09248 on 20 degrees of freedom
## Multiple R-squared:  0.3318, Adjusted R-squared:  0.2316
## F-statistic:  3.31 on 3 and 20 DF,  p-value: 0.04104
##
## Call:
## lm(formula = Weight_log ~ Radius_log + Length_log, data = .)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.24861 -0.05259  0.02164  0.05202  0.11544
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -0.6702      1.9132  -0.350  0.72961
## Radius_log    1.7702      0.5596   3.163  0.00468 **
## Length_log    0.1223      0.1249   0.979  0.33888
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.09062 on 21 degrees of freedom
## Multiple R-squared:  0.3262, Adjusted R-squared:  0.2621
## F-statistic: 5.084 on 2 and 21 DF,  p-value: 0.01583
##
## Call:
## lm(formula = Weight_log ~ Radius_log, data = .)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.25201 -0.05851  0.02530  0.05814  0.12150
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    0.3046      1.6319   0.187  0.85363
## Radius_log     1.6689      0.5494   3.038  0.00604 **
```

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.09054 on 22 degrees of freedom
## Multiple R-squared:  0.2955, Adjusted R-squared:  0.2635
## F-statistic: 9.227 on 1 and 22 DF,  p-value: 0.006043
##
## Call:
## lm(formula = Weight_log ~ Length_log, data = .)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.204865 -0.072290 -0.000595  0.055375  0.177835
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  4.99043     0.80371   6.209   3e-06 ***
## Length_log   0.04917     0.14574   0.337   0.739
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1076 on 22 degrees of freedom
## Multiple R-squared:  0.005146, Adjusted R-squared:  -0.04007
## F-statistic: 0.1138 on 1 and 22 DF,  p-value: 0.739
```

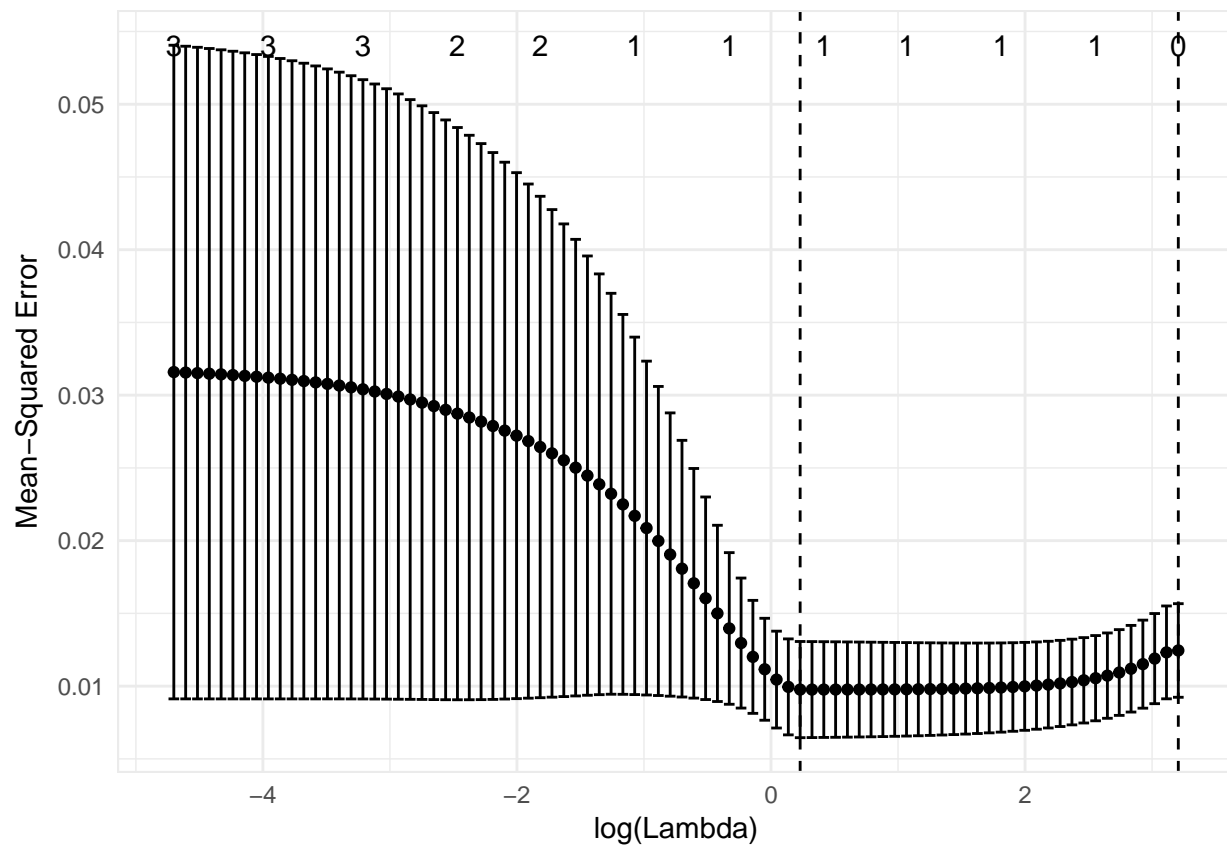
Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
21	0.1724705	NA	NA	NA	NA
20	0.1710414	1	0.0014291	0.1671057	0.687041

Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
22	0.1803370	NA	NA	NA	NA
20	0.1710414	2	0.0092956	0.5434713	0.5890658

Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
22	0.1803370	NA	NA	NA	NA
21	0.1724705	1	0.0078665	0.9578258	0.3388762

```
## Warning: Option grouped=FALSE enforced in cv.glmnet, since < 3 observations
## per fold
```

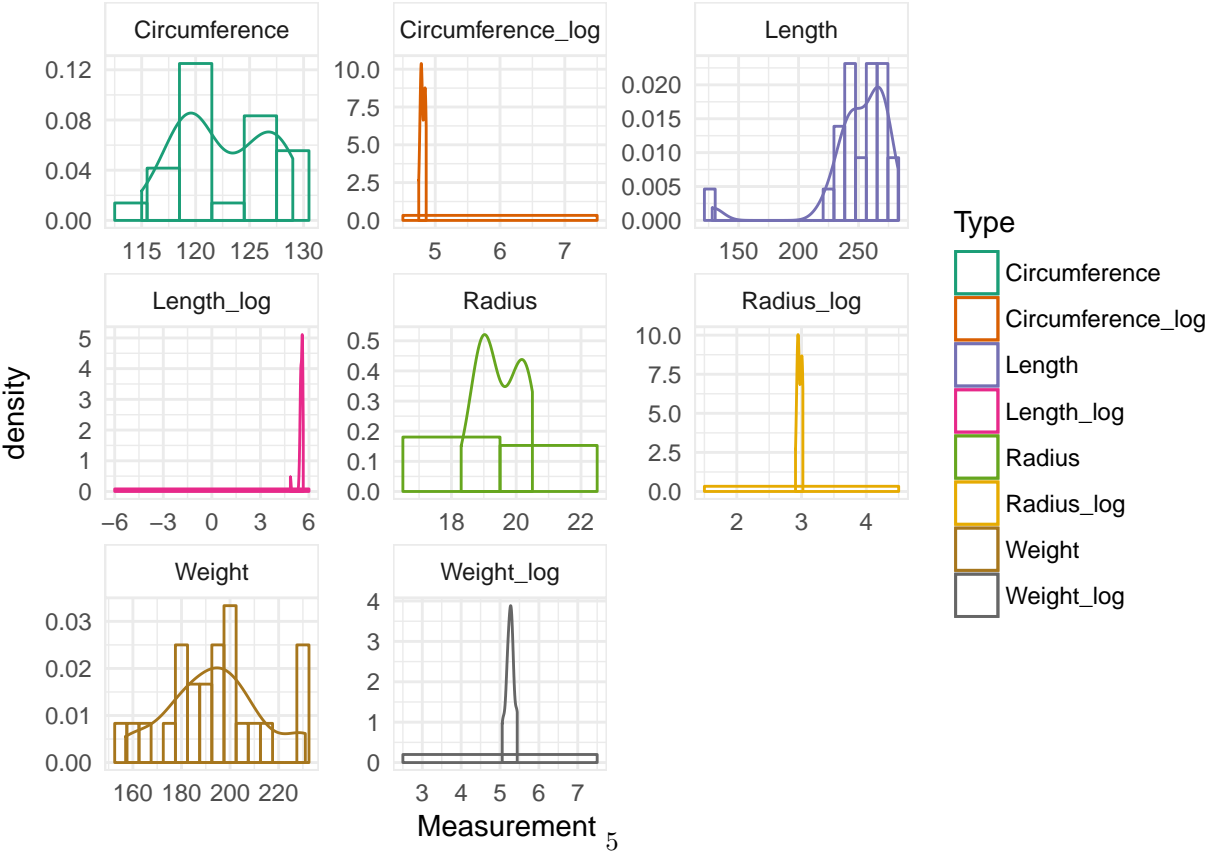
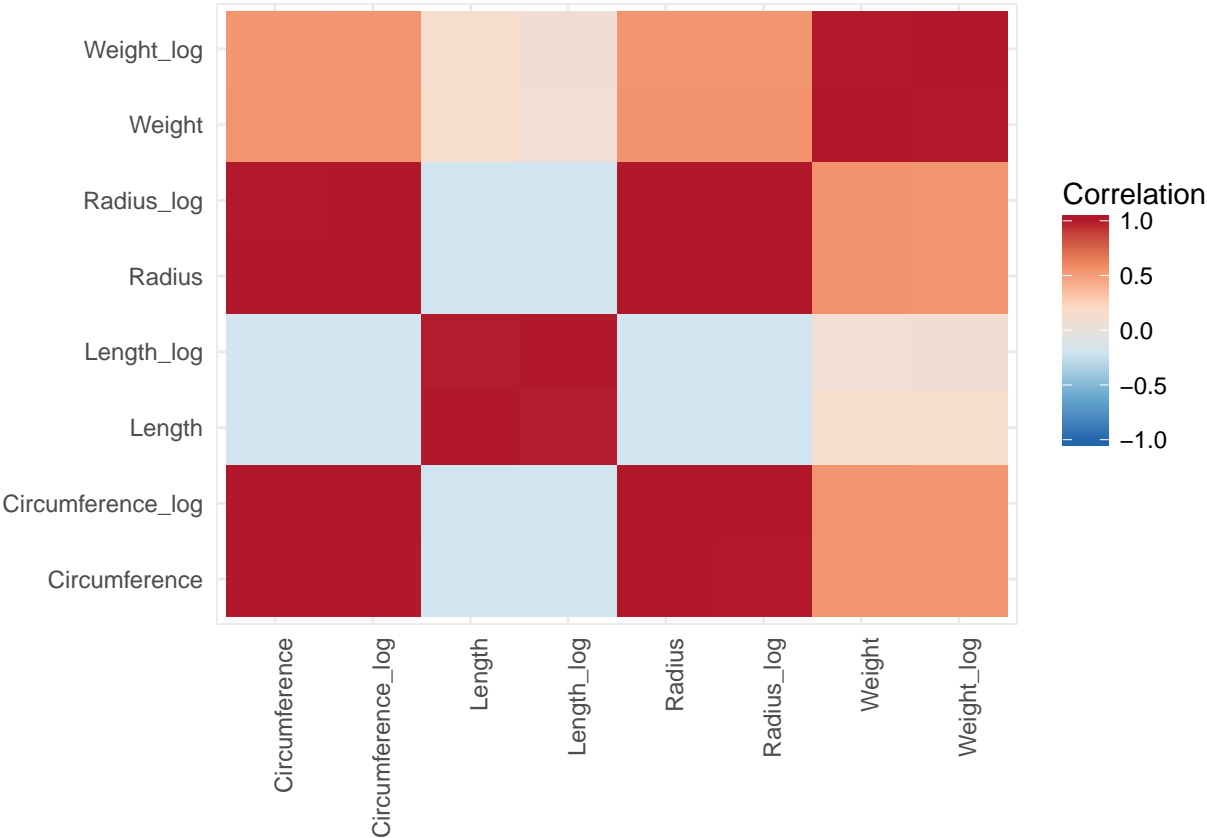
```
## Warning: Option grouped=FALSE enforced in cv.glmnet, since < 3 observations
## per fold
```

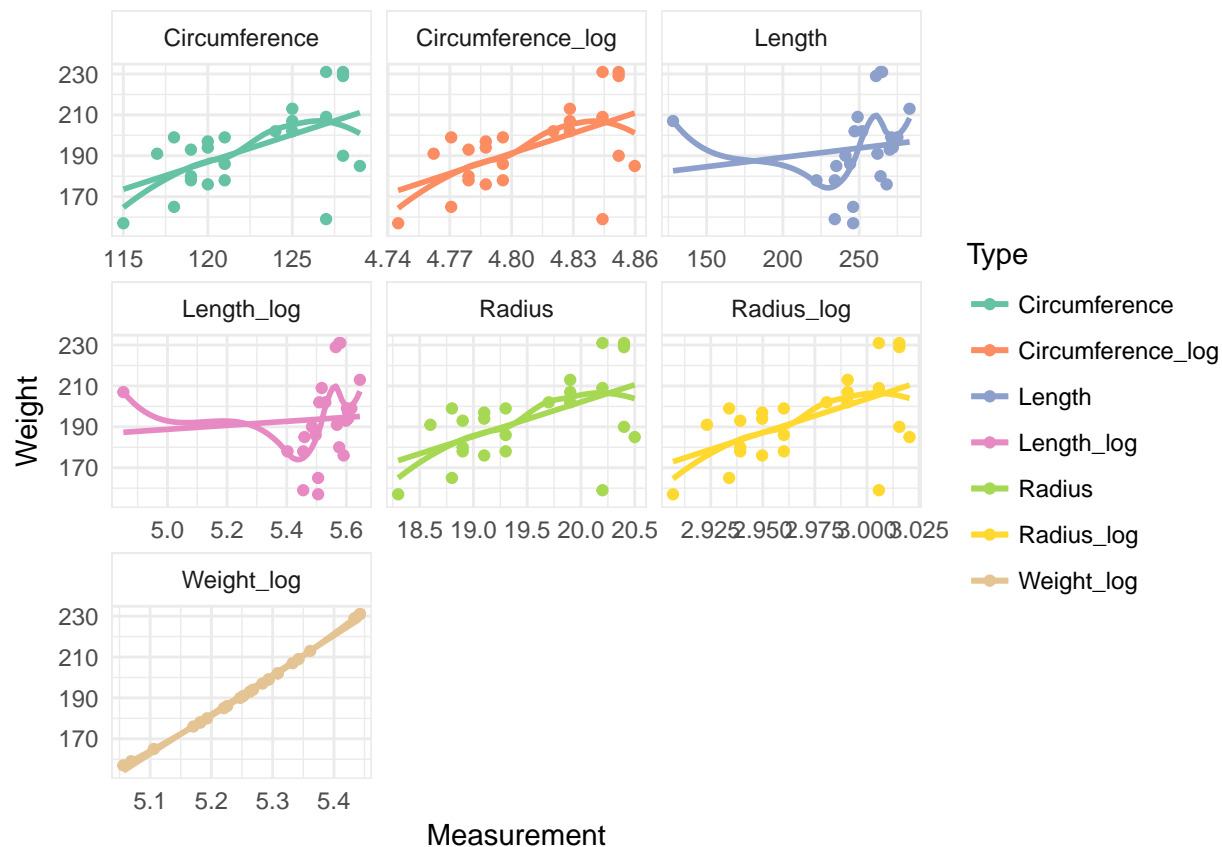


1	
(Intercept)	0.55713
Length	0.00000
Radius	0.00000
Circumference	0.00000
Length_log	0.00000
Radius_log	1.58392
Circumference_log	0.00000

1	
(Intercept)	5.261471
Length	0.000000
Radius	0.000000
Circumference	0.000000
Length_log	0.000000
Radius_log	0.000000
Circumference_log	0.000000

Appendix





Cross Validation

```
## Analysis of Variance Table
##
## Response: Weight_log
##           Df Sum Sq Mean Sq F value Pr(>F)
## Length_log  1  0.0013   0.0013    0.16 0.6928
## Radius_log   1  0.0822   0.0822   10.01 0.0047 **
## Residuals  21  0.1725   0.0082
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
## fold 1
## Observations in test set: 8
##           [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
## Predicted  5.2368 5.2368 5.196 5.1998 5.3143 5.2304 5.344 5.215
## cvpred     5.2428 5.2428 5.207 5.2131 5.3184 5.2464 5.358 5.222
## Weight_log 5.2832 5.2679 5.106 5.1818 5.3613 5.1818 5.220 5.193
## CV residual 0.0404 0.0251 -0.101 -0.0314 0.0429 -0.0646 -0.137 -0.029
##
## Sum of squares = 0.04    Mean square = 0    n = 8
##
## fold 2
```

```

## Observations in test set: 8
##      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
## Predicted  5.24195 5.348 5.333 5.2350 5.2548 5.3386 5.1853 5.3251
## cvpred     5.23389 5.324 5.310 5.2248 5.2417 5.3184 5.1822 5.3056
## Weight_log  5.22575 5.434 5.442 5.1705 5.2933 5.2470 5.2523 5.3423
## CV residual -0.00814 0.109 0.132 -0.0543 0.0516 -0.0714 0.0701 0.0367
##
## Sum of squares = 0.05      Mean square = 0.01      n = 8
##
## fold 3
## Observations in test set: 8
##      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
## Predicted  5.22 5.318 5.1488 5.3497 5.2822 5.2976 5.2173 5.2101
## cvpred     4.78 5.267 5.1137 5.3771 5.2744 5.2788 5.2464 5.2500
## Weight_log  5.33 5.069 5.0562 5.4424 5.3083 5.3083 5.2627 5.2933
## CV residual 0.55 -0.198 -0.0574 0.0654 0.0339 0.0295 0.0163 0.0433
##
## Sum of squares = 0.35      Mean square = 0.04      n = 8
##
## Overall (Sum over all 8 folds)
##      ms
## 0.0183

## # A tibble: 24 x 13
##      ID Weight Radius Length Circumference Weight_log Radius_log
##      <int> <int> <dbl> <int>          <int>          <dbl>      <dbl>
## 1      1      197  19.1    272           120           5.28       2.95
## 2      2      194  19.1    272           120           5.27       2.95
## 3      3      165  18.8    246           118           5.11       2.93
## 4      4      186  19.3    244           121           5.23       2.96
## 5      5      178  18.9    234           119           5.18       2.94
## 6      6      207  19.9    128           125           5.33       2.99
## 7      7      213  19.9    283           125           5.36       2.99
## 8      8      178  19.3    222           121           5.18       2.96
## 9      9      229  20.4    261           128           5.43       3.02
## 10     10     231  20.2    265           127           5.44       3.01
## # ... with 14 more rows, and 6 more variables: Length_log <dbl>,
## #   Circumference_log <dbl>, Predicted <dbl>, cvpred <dbl>, `CV Residual`
## #   <dbl>, Residual <dbl>

```

MAE

```

## # A tibble: 1 x 2
##      MAE  MPAE
##      <dbl> <dbl>
## 1  13.7 0.0722

```