Does Size Matter? (Estimation of Banana Weight with a Regression Modeling Approach)

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Summary

Introduction

The purpose of this study was to determine the most effective regression model to predict the weight of a banana using external measurements. This study also demonstrated multiple techniques for developing regression models. These models were then examined to demonstrate their effectiveness at creating regression models.

Data Collection

First a small sample set bananas were purchased from the Real Canadian Superstore. The weight, length, diameter and circumference were then calculated using a scale and a ruler.

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
0.0004513	0.4005	0.6352	0.5719	0.7617	0.9812

In order to determine the minimum sample size needed, random sample sizes of 10 were generated using radius and length as the predictors. The correlation of the random sample sizes were calculated and a matrix of the correlations were generated. The value of the squared population multiple correlation coefficients with two predictor variables was then calculated and determined to be approximately 0.5719. From this the minimum sample size required was then determined from the table from Gregory T. Knofcznski's Sample Size When Using Multiple Linear Regression for Prediction, the minimum sample size was determined to be between 15 and 35, therefore the minimum number of bananas required was finalized at 24 bananas.

Analysis

To begin analysis a model using all predictor variables was created. In this case the density of the banana is assumed to be a constant.

Let:

$$W = \text{Weight (g)}, L = \text{Length (mm)}, R = \text{Radius (mm)}$$

Then:

$$\log(W) = \beta_0 + \beta_1 \log(L) + \beta_2 \log(R) + \beta_3 \log(C) \implies W = e^{\beta_0} \times L^{\beta_1} \times R^{\beta_2} \times C^{\beta_3}$$

	Estimate	Std. Error	t value	$\Pr(> t)$
(Intercept)	10.06	26.32	0.3822	0.7063
${\bf Length_log}$	0.123	0.1275	0.9652	0.346

	Estimate	Std. Error	t value	$\Pr(> t)$
Radius_log	7.526	14.09	0.5341	0.5992
${f Circumference_log}$	-5.788	14.16	-0.4088	0.687

Table 3: Fitting linear model: Weight_log \sim Length_log + Radius_log + Circumference_log This returned values with insignificant p-values

Observations	Residual Std. Error	R^2	Adjusted \mathbb{R}^2
24	0.09248	0.3318	0.2316

In the second model the predictor variable, circumference, was removed. This is because $C = 2\pi R$.

$$\log(W) = \beta_0 + \beta_1 \log(L) + \beta_2 \log(R)$$

	Estimate	Std. Error	t value	$\Pr(> t)$
(Intercept)	-0.6702	1.913	-0.3503	0.7296
${ m Length_log}$	0.1223	0.1249	0.9787	0.3389
Radius_log	1.77	0.5596	3.163	0.004684

Table 5: Fitting linear model: Weight_log ~ Length_log + Radius_log

Observations	Residual Std. Error	R^2	Adjusted \mathbb{R}^2
24	0.09062	0.3262	0.2621

The third model considered the predictor, length.

$$\log(W) = \beta_0 + \beta_1 \log(L)$$

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	4.99	0.8037	6.209	3e-06
${f Length_log}$	0.04917	0.1457	0.3374	0.739

Table 7: Fitting linear model: Weight_log \sim Length_log

Observations	Residual Std. Error	R^2	Adjusted \mathbb{R}^2
24	0.1076	0.005146	-0.04007

The fourth model considered only one predictor, radius.

$$\log(W) = \beta_0 + \beta_2 \log(R)$$

	Estimate	Std. Error	t value	$\Pr(> t)$
(Intercept)	0.3046	1.632	0.1867	0.8536
Radius_log	1.669	0.5494	3.038	0.006043

Table 9: Fitting linear model: Weight_log \sim Radius_log

Observations	Residual Std. Error	R^2	Adjusted R^2
24	0.09054	0.2955	0.2635

Table 10: foo

Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
21	0.1725	NA	NA	NA	NA
20	0.171	1	0.001429	0.1671	0.687

Table 11: Analysis of Variance Table

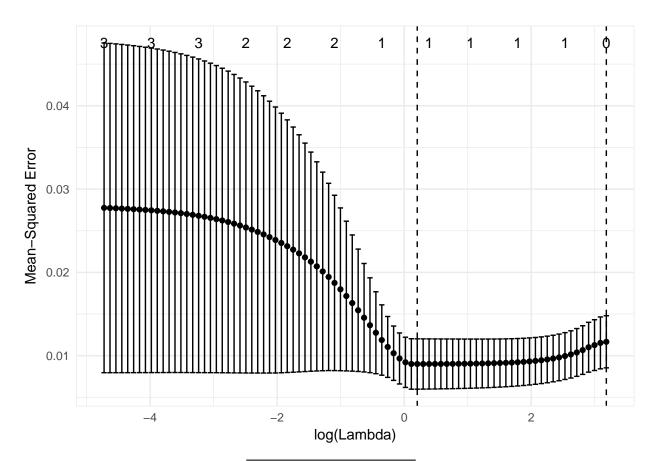
Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
22	0.2547	NA	NA	NA	NA
20	0.171	2	0.08362	4.889	0.01868

Table 12: Analysis of Variance Table

Res.Df	RSS	Df	Sum of Sq	F	$\Pr(>F)$
22	0.2547 0.1725	NA 1	NA 0.08219	NA 10.01	NA 0.004684
21	0.1725	1	0.08219	10.01	0.004084

 $\mbox{\tt \#\#}$ Warning: Option grouped=FALSE enforced in cv.glmnet, since < 3 observations $\mbox{\tt \#\#}$ per fold

 $\mbox{\tt \#\#}$ Warning: Option grouped=FALSE enforced in cv.glmnet, since < 3 observations $\mbox{\tt \#\#}$ per fold



	1
(Intercept)	0.55713
Length	0.00000
Radius	0.00000
Circumference	0.00000
Length_log	0.00000
Radius_log	1.58392
$\underline{\text{Circumference}_\text{log}}$	0.00000

	1
(Intercept)	5.261471
Length	0.000000
Radius	0.000000
Circumference	0.000000
Length_log	0.000000
Radius_log	0.000000
$Circumference_log$	0.000000

Recommendations

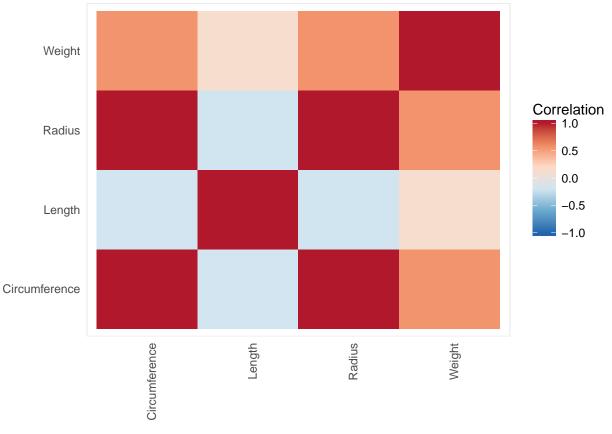
It can be determiend that the best way to predict the weight of a banana is by measuring the radius of the banana. The model that is then used for banana weight prediction is the following:

$$\log(W) = \beta_0 + \beta_1 \log(R)$$

$$\log(W) = 0.3046 + 1.669 \log(R)$$

The predictor variable radius, was more significantly correlated to the weight in comparison to circumference and length.

Appendix

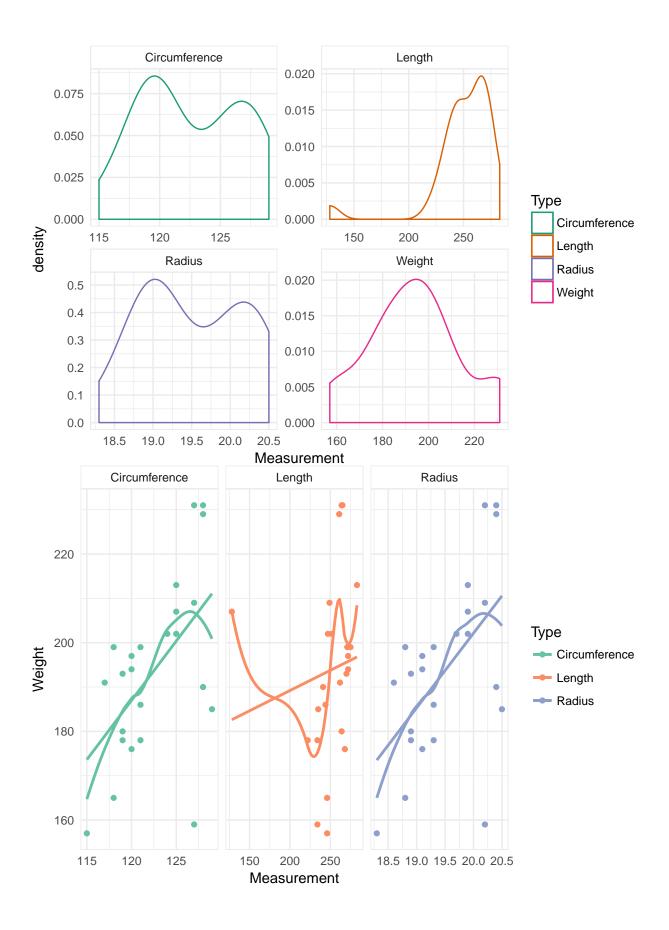


```
## Warning: Computation failed in `stat_bin()`:
## is.numeric(width) is not TRUE

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```



Cross Validation

```
## Analysis of Variance Table
## Response: Weight_log
             Df Sum Sq Mean Sq F value Pr(>F)
## Length_log 1 0.0013 0.0013
                                  0.16 0.6928
## Radius log 1 0.0822 0.0822
                                 10.01 0.0047 **
## Residuals 21 0.1725 0.0082
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## fold 1
## Observations in test set: 8
                 [,1]
                        [,2]
                               [,3]
                                       [,4]
                                              [,5]
                                                      [,6]
                                                             [,7]
                                                                    [8,]
              5.2368 5.2368 5.196 5.1998 5.3143 5.2304
## Predicted
                                                            5.344
              5.2428 5.2428 5.207 5.2131 5.3184 5.2464 5.358 5.222
## cvpred
## Weight_log 5.2832 5.2679 5.106 5.1818 5.3613 5.1818 5.220 5.193
## CV residual 0.0404 0.0251 -0.101 -0.0314 0.0429 -0.0646 -0.137 -0.029
##
## Sum of squares = 0.04
                           Mean square = 0
                                              n = 8
##
## fold 2
## Observations in test set: 8
##
                   [,1] [,2] [,3]
                                       [,4]
                                              [,5]
                                                      [,6]
                                                             [,7]
                                                                    [.8]
               5.24195 5.348 5.333 5.2350 5.2548 5.3386 5.1853 5.3251
## Predicted
               5.23389 5.324 5.310 5.2248 5.2417 5.3184 5.1822 5.3056
## cvpred
               5.22575 5.434 5.442 5.1705 5.2933 5.2470 5.2523 5.3423
## Weight_log
## CV residual -0.00814 0.109 0.132 -0.0543 0.0516 -0.0714 0.0701 0.0367
## Sum of squares = 0.05
                           Mean square = 0.01
                                                  n = 8
##
## fold 3
## Observations in test set: 8
               [,1]
                      [,2]
                              [,3]
                                     [,4]
                                            [,5]
                                                   [,6]
## Predicted
              5.22 5.318 5.1488 5.3497 5.2822 5.2976 5.2173 5.2101
              4.78 5.267 5.1137 5.3771 5.2744 5.2788 5.2464 5.2500
## Weight_log 5.33 5.069 5.0562 5.4424 5.3083 5.3083 5.2627 5.2933
## CV residual 0.55 -0.198 -0.0574 0.0654 0.0339 0.0295 0.0163 0.0433
##
## Sum of squares = 0.35
                           Mean square = 0.04
##
## Overall (Sum over all 8 folds)
##
      ms
## 0.0183
## # A tibble: 24 x 13
##
         ID Weight Radius Length Circumference Weight_log Radius_log
##
      <int>
            <int>
                   <dbl> <int>
                                         <int>
                                                    dbl>
##
   1
          1
               197
                     19.1
                            272
                                           120
                                                     5.28
                                                                2.95
##
          2
               194
                     19.1
                             272
                                           120
                                                     5.27
   2
                                                                2.95
## 3
          3
               165
                     18.8
                             246
                                                     5.11
                                                                2.93
                                           118
##
          4
              186
                     19.3
                             244
                                           121
                                                     5.23
                                                                2.96
```

```
## 5
         5
              178
                     18.9
                             234
                                           119
                                                     5.18
                                                                2.94
## 6
              207
                     19.9
                            128
                                           125
                                                     5.33
                                                                2.99
         6
                             283
                                                     5.36
                                                                2.99
##
   7
         7
              213
                     19.9
                                           125
## 8
         8
               178
                     19.3
                             222
                                           121
                                                     5.18
                                                                2.96
## 9
         9
               229
                     20.4
                             261
                                           128
                                                     5.43
                                                                3.02
              231
                     20.2
                             265
                                           127
                                                                3.01
## 10
         10
                                                     5.44
```

... with 14 more rows, and 6 more variables: Length_log <dbl>,

Circumference_log <dbl>, Predicted <dbl>, cvpred <dbl>, `CV

Residual` <dbl>, Residual <dbl>

MAE

A tibble: 1 x 2 ## MAE MPAE ## <dbl> <dbl> ## 1 13.7 0.0722