Leafs

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Introduction

Background information about pear and cherry tree leaves. Midrib is the central vein of a leaf.

Data

Measurement Process

The first step taken in the measurement of the leaves was to give each leaf an identification number based on the species. The method used to measure the dimensions was to create a box with the minimum length and width in which the entire leaf would be encompassed in the box.

To begin creating the sides of the box, a ruler was aligned parallel to the midrib, which is the central vein in the leaf and moved towards the left and the right of the picture until only one point on the leaf remained [reference]. From the single point on the side of the leaf, a line was drawn parallel to the midrib of the leaf.

Next, the base and point of the leaf were measured, a ruler was placed perpendicular to the midrib and the ruler was moved towards to tip of the leaf until a single point remained, a line was draw perpendicular to the midrib at this point. At the base of the leaves the length of the leaf was set as the point where the leaf ends and the stem begins, at this point a line was drawn perpendicular to the midrib.

After all the boxes were created, the width (lines parallel to midrib) and the length (lines perpendicular to midrib) were measured and the results were recorded in a spread sheet.

Data Creation

| Type | Length | Width |
|--------|--------|-------|
| Cherry | 11.5 | 5.9 |
| Cherry | 16.7 | 9.1 |
| Cherry | 10.4 | 4.9 |
| Cherry | 18.1 | 8.4 |
| Cherry | 19.3 | 6.5 |
| Cherry | 12.2 | 8.0 |
| Cherry | 10.3 | 5.3 |
| Cherry | 9.9 | 4.3 |
| Cherry | 9.6 | 6.8 |
| Cherry | 19.2 | 10.4 |
| Cherry | 12.8 | 6.2 |
| Cherry | 12.1 | 8.3 |
| Cherry | 12.5 | 6.2 |
| Cherry | 8.3 | 4.3 |

| Type | Length | Width |
|--------|--------|-------|
| Cherry | 6.9 | 4.5 |
| Cherry | 9.2 | 5.5 |
| Pear | 5.3 | 3.1 |
| Pear | 6.9 | 6.2 |
| Pear | 9.2 | 8.9 |
| Pear | 8.5 | 7.5 |
| Pear | 8.2 | 4.1 |
| Pear | 5.7 | 4.0 |
| Pear | 5.8 | 5.1 |
| Pear | 16.8 | 9.9 |
| Pear | 6.1 | 5.9 |
| Pear | 8.9 | 4.1 |
| Pear | 6.4 | 4.4 |
| Pear | 18.8 | 15.2 |

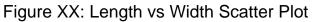
| Type | Length | Width |
|-----------|----------------|----------------|
| Cherry:16 | Min.: 5.300 | Min.: 3.100 |
| Pear :12 | 1st Qu.: 7.875 | 1st Qu.: 4.475 |
| NA | Median: 9.750 | Median: 6.050 |
| NA | Mean $:10.914$ | Mean: 6.536 |
| NA | 3rd Qu.:12.575 | 3rd Qu.: 8.075 |
| NA | Max. :19.300 | Max. :15.200 |

Classification Procedure

Training Data

New Data

Observation Space



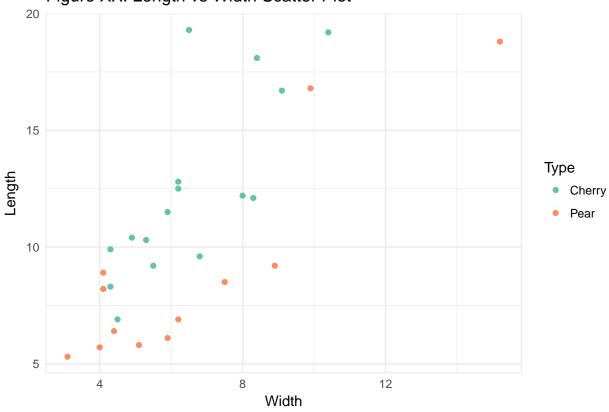


Figure XX: Length vs Width Scatter Plot

Overlayed with the Contour Plot

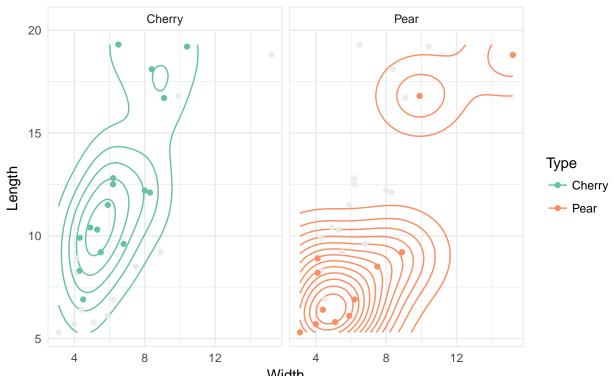


Figure XX: Length vs Width Scatter Plot

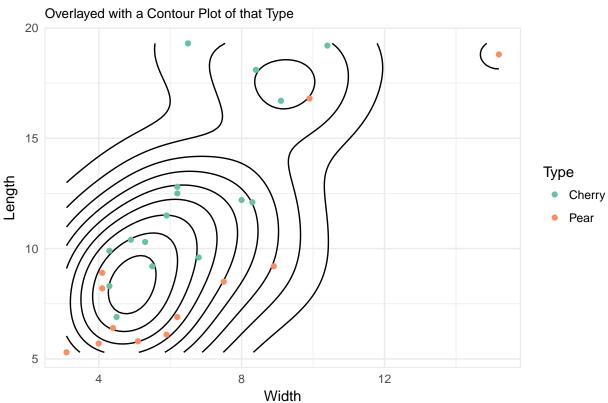
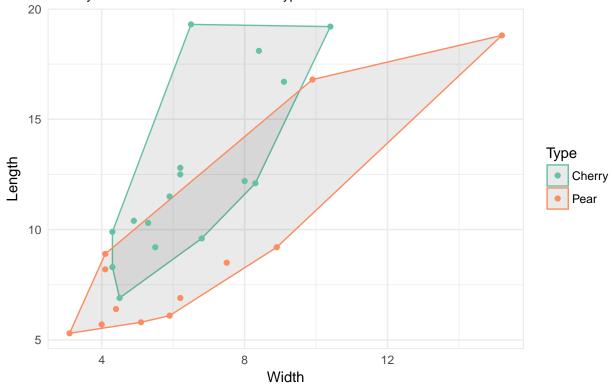


Figure XX: Length vs Width Scatter Plot

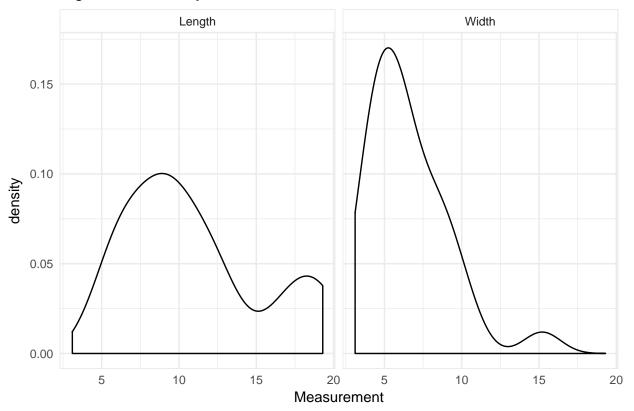
Overlayed with the Convex Hull of that Type



```
## Warning: Computation failed in `stat_bin()`:
## is.numeric(width) is not TRUE

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## is.numeric(width) is not TRUE
```

Figure XX: Density Plot



```
## Warning: Computation failed in `stat_bin()`:
## is.numeric(width) is not TRUE

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## is.numeric(width) is not TRUE

## Warning: Computation failed in `stat_bin()`:
## is.numeric(width) is not TRUE
```

Cherry Pear 0.20 0.15 Length 0.10 0.05 Type density 0.00 0.20 Cherry Pear 0.15 Width 0.10 0.05 0.00 5 10 15 20 5 10 15 20

Figure XX: Density Plot by Type

Covariance Matrix

Table 3: Shared Covariance Matrix

Measurement

| | Length | Width |
|--------|-----------|----------|
| Length | 19.422011 | 8.476508 |
| Width | 8.476508 | 6.685344 |

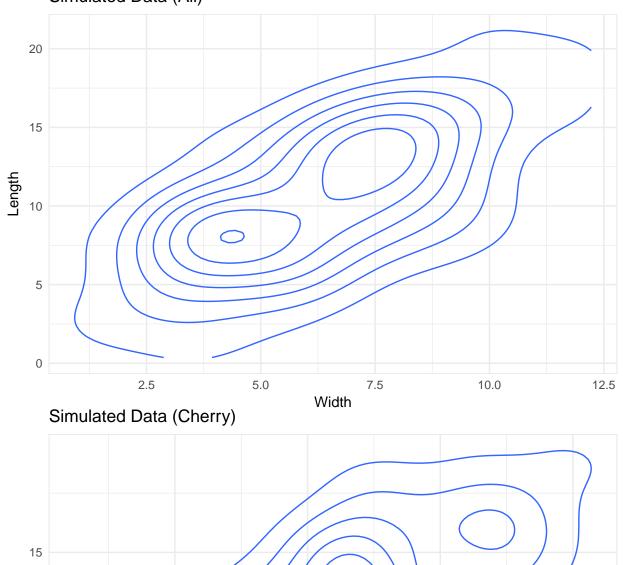
Table 4: Cherry Covariance Matrix

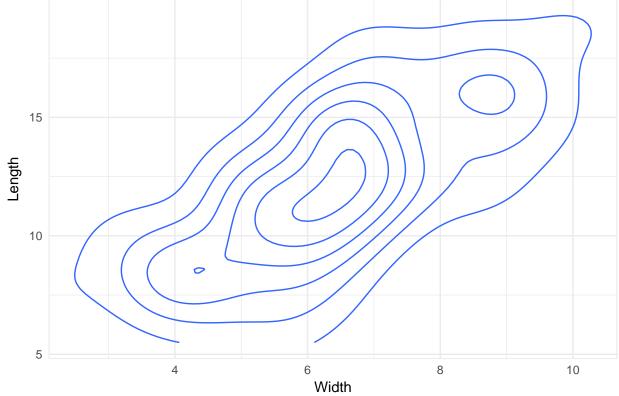
| | Length | Width |
|--------|-----------|----------|
| Length | 15.047833 | 5.443833 |
| Width | 5.443833 | 3.357167 |

Table 5: Pear Covariance Matrix

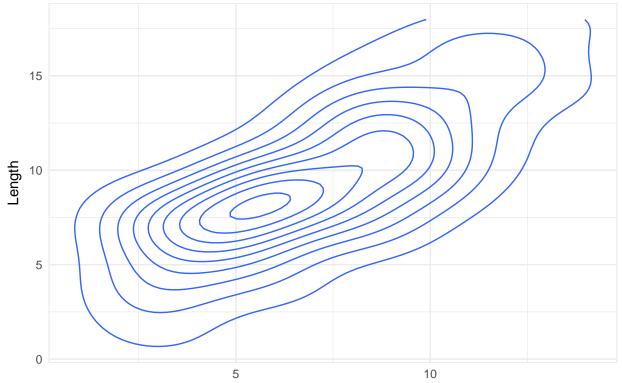
| | Length | Width |
|--------|----------|----------|
| Length | 19.27788 | 13.37333 |
| Width | 13.37333 | 11.83152 |







Simulated Data (Pear)



Width

| Number | Length | Width |
|--------|--------|-------|
| 1 | 8.2 | 3.2 |
| 2 | 5.2 | 3.8 |
| 3 | 7.6 | 4.0 |

| Length | Width | Density |
|--------|-------|---------|
| 6.9000 | 4.3 | 0.0124 |
| 7.6592 | 4.3 | 0.0163 |
| 8.1653 | 4.3 | 0.0186 |

| Length | Width | Density |
|--------|--------|---------|
| 5.3000 | 3.1000 | 0.0179 |
| 7.5041 | 3.1000 | 0.0168 |
| 8.3306 | 3.1000 | 0.0135 |
| 5.3000 | 3.8408 | 0.0216 |
| 7.5041 | 3.8408 | 0.0213 |
| 8.3306 | 3.8408 | 0.0169 |
| 5.3000 | 4.0878 | 0.0223 |
| 7.5041 | 4.0878 | 0.0224 |
| 8.3306 | 4.0878 | 0.0177 |

Conclusion