# **Instruction Manual**

# EEMS: a method to visualize patterns of non-stationary isolation by distance

Version 0.0.0.9000

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# **Contents**

1	Inst	allation	3
2	Inp	ut data	3
3	Input parameters		5
	3.1	Population grid	6
4	Rur	nning the EEMS program	8
5	Plotting the EEMS results		9
	5.1	Required arguments	9
	5.2	Optional arguments about the graphics format	10
	5.3	Optional arguments about the population grid	10
	5.4	Optional arguments about the cartographic projection	11
	5.5	Optional arguments about the geographic map	12
	5.6	Optional arguments about the color scheme	12
	5.7	A test function to generate Voronoi diagrams	13
6	Obs	served vs fitted distances	14
L	ist (	of Figures	
	1	The input data – an example	4
	2	The triangular grid – an example	7
	3	EEMS graphics with default options	16
	4	EEMS graphics with flipped axes	17
	5	EEMS graphics with population grid	18
	6	EEMS graphics in the Mercator projection	18
	7	EEMS graphics with geographic map	19
	8	EEMS graphics with alternative divergent colors	19
	9	Voronoi diagrams drawn from the posterior	20
	10	Observed vs fitted genetic dissimilarities	21

EEMS is a program to analyze and visualize spatial population structure from geo-referenced genetic samples. EEMS uses the concept of *effective migration* to model the relationship between genetics and geography, and it outputs an *estimated effective migration surface* (hence, EEMS) – a visual representation of population structure that highlights potential regions of higher-than-average and lower-than-average historic gene flow.

## 1 Installation

This EEMS implementation uses Eigen for linear algebra computations and Boost for random number generation and the habitat geometry. The Eigen template library can be downloaded from http://eigen.tuxfamily.org, and the Boost libraries can be downloaded from http://www.boost.org. EEMS has been tested with Eigen 3.2.2 and Boost 1\_57.

After downloading Eigen (which does not need installation) and installing Boost, update the variables EIGEN\_INC, BOOST\_LIB in the Makefile. The dynamic Boost libraries are linked to slightly differently on a Mac and a Linux machine, so run 'make darwin' on a Mac or 'make linux' on a Linux machine.

There are two versions of EEMS: runeems\_snps for SNP data and runeems\_sats for microsatellite data. The data input format and the EEMS model are somewhat different for SNPs and microsatellites, hence the two versions. The source code can be found in runeems\_snps/src and runeems\_sats/src, respectively. The directories runeems\_snps/data and runeems\_sats/data contain data, simulated with ms [Hudson, 2002], to illustrate the input file format and how EEMS is run.

# 2 Input data

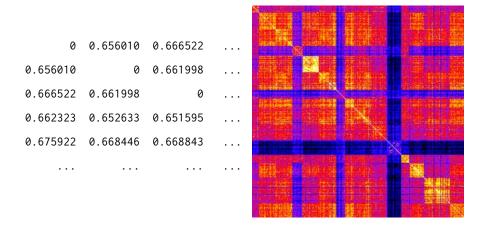
There are three data input files as well as a parameter input file. The data input files should be in the same directory, and the description below assumes that datapath is the full path + the file name (but without the extension).

For SNP data on *n* individuals, the input files are:

- datapath.diffs: the matrix of average pairwise genetic dissimilarities. This can be computed with the small program bed2diffs if the dataset is already in plink binary format. See Figure 1(a).
- datapath.coord: the sample coordinates, two coordinates per sample, one sample per line. See Figure 1(b).
- datapath.outer: the habitat coordinates, as a sequence of vertices that form a closed polygon. See Figure 1(c).

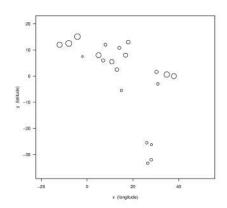
For microsatellite data on *n* individuals at *L* loci, the input files are:

- datapath.sites: the matrix of allele copies (This matrix is  $n \times L$  for L haploid markers and  $n \times 2L$  for L diploid markers; missing alleles are specified by any negative number.)
- datapath.coord, datapath.outer: as described above for SNP data.



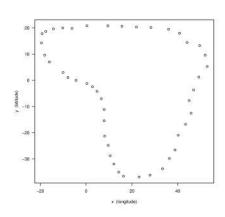
(a) The observed genetic dissimilarity matrix: the top left corner of datapath.diffs on the left and the entire matrix as a heatmap on the right.

30.9 -3.0 30.9 -3.0 30.9 -3.0 30.9 -3.0 30.9 -3.0



(b) The sample coordinates: the top 5 lines in datapath.coord on the left and the complete sampling scheme on the right. A bigger circle means that more samples are taken from that location.

-18.1 9.6 -16.0 7.0 -10.0 3.0 ... -19.2 17.8 -19.5 14.3 -18.1 9.6



(c) The habitat polygon: the top and bottom lines in datapath.outer on the left and the entire habitat outline on the right.

Figure 1 EEMS requires three data input files. (a) datapath.diffs is the observed genetic dissimilarity matrix. There is a lot of population structure in this example and the rows and columns can be ordered to emphasize the pattern further. This ordering, however, is irrelevant to EEMS. (b) The sampling locations in datapath.coord should be given in the same order as the rows and columns of the dissimilarity matrix. (c) The habitat vertices in datapath.outer should be listed *counterclockwise* and the first vertex should also be the last vertex, so that the outline is a *closed ring*. Otherwise, EEMS attempts to "correct" the polygon and prints a warning message.

# 3 Input parameters

There are a number of program parameters that can be set by the user. First, there are several parameters that have to be specified (there are no default values for those):

- datapath: path to the input data. For SNP data, EEMS expects three files: a matrix of average pairwise differences, datapath.diffs; a list of sample coordinates, datapath.coord; a list of habitat boundary points, datapath.outer. For microsatellite data, EEMS also expects three files: a matrix of allele copies, datapath.sites; a list of sample coordinates, datapath.coord; a list of habitat boundary points, datapath.outer.
- mcmcpath: path to the output directory. EEMS creates this directory and saves all results there. (There is an accompanying R package which parses the output files and generates several figures to visualize the EEMS results.)
- nIndiv and nSites: number of samples and number of markers.
- numMCMCIter, numBurnIter, numThinIter: number of MCMC iterations, number of burn-in iterations to discard at the start, and number of iterations to thin between two writing steps.
- nDemes: the (approximate) number of demes in the population graph. If the habitat is irregular, the actual number of demes in the grid might not be exactly equal to the specified number of demes. See Figure 2. Alternatively, instead of nDemes, specify gridpath where the file gridpath demes is a list of demes, the file gridpath edges is a list of edges and gridpath ipmap is a mapping which assigns samples to demes. See Section 3.1.

Further, there are several extra parameters that can be specified optionally (they have default values but modifying those values could improve convergence).

- Variances for the proposal distributions of migration parameters:
  - mEffctProposalS2: proposal variance for the migration cell effects,  $e_1, \ldots, e_{C_m}$
  - mSeedsProposalS2: proposal variance for the migration cell locations,  $s_1, \ldots, s_{C_m}$
  - mrateMuProposalS2: proposal variance for the overall migration rate  $\mu$  (on the  $\log_{10}$  scale)
- Variances for the proposal distributions of diversity parameters:
  - qEffctProposalS2: proposal variance for the diversity cell effects,  $f_1, \ldots, f_{C_a}$
  - qSeedsProposalS2: proposal variance for the diversity cell locations,  $t_1, \ldots, t_{C_q}$
- Hyperparameters:
  - mrateShape,mrateScale: (inverse gamma) hyperparameters for the variance  $\omega_m^2$  of the migration effects
  - qrateShape,qrateScale: (inverse gamma) hyperparameters for the variance  $\omega_q^2$  of the diversity effects

- s2locShape, s2locShape: (inverse gamma) hyperparameters for the scale parameters  $\sigma_1^2,\ldots,\sigma_p^2$
- negBiSize: number of failures for the Negative-Binomial prior on the number of Voronoi tiles
- negBiProb: success probability for the Negative-Binomial prior on the number of Voronoi tiles

## 3.1 Population grid

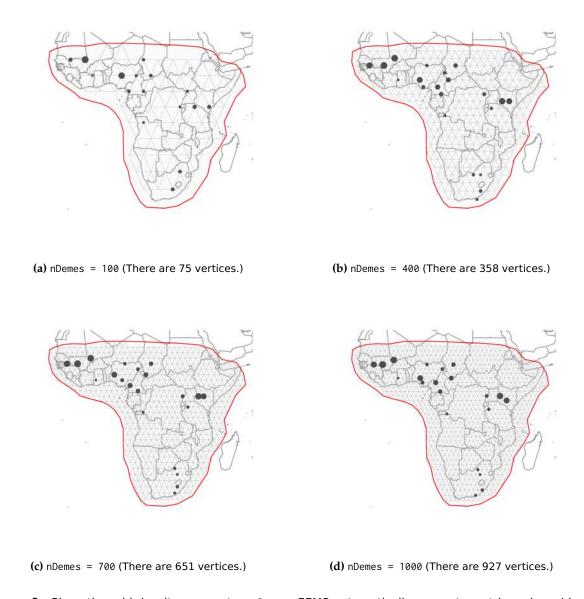
The population graph is a triangular grid contained entirely inside the habitat. The user specifies its density as a number of demes, nDemes, and EEMS constructs a grid with about the same number of demes which fills the habitat. This procedure is not necessarily optimal (i.e., it might not cover as much area as possible near the boundaries) and it might be helpful to iterate between refining the habitat specification and the density argument nDemes, to choose a satisfactory grid. [Or even better, since the assignment of samples to demes changes with the grid, run EEMS with slightly different grids to investigates how/whether this changes the results.] See Figure 2 for an illustration. Furthermore, there exists a convenient online tool to draw polygons with Google Maps API, available at http://www.birdtheme.org/useful/v3tool.html, that might be useful for outlining an irregularly shaped habitat.

Alternatively, EEMS can read in the population graph. In this case, there are three necessary files:

- gridpath.demes: list of demes, two coordinates per deme, one deme per row.
- gridpath.edges: list of connected pairs of demes, two indices per edge, one edge per row. Demes are indexed from 1 to *d* (where *d* is the number of demes in the grid), in the order implied by gridpath.demes, i.e., the deme with index 1 has the coordinates on the 1st row in gridpath.demes.
- gridpath.ipmap: list of deme indices which indicate the deme each sample is assigned to. There should be *n* rows (where *n* is the number of samples), with one row for each sample in datapath.coord, in the same order.

The sample and habitat coordinates can be specified either latitude first or longitude first as long as the files datapath.coord and datapath.outer use the same convention. However, the ordering of the coordinates must be specified when plotting the results; see Section 5.

Finally, the vertices of the population graph (the demes) fall inside the habitat by construction. However, EEMS does not check that the sampling locations fall inside the habitat – instead, each sample is assigned to the closest deme. Therefore, the user should specify a habitat that is sufficiently large to cover all sampling locations.



**Figure 2** Given the grid density parameter, nDemes, EEMS automatically generates a triangular grid, which is contained entirely inside the habitat. Then EEMS assigns each sample to its closest deme. Here the habitat is outlined in red. [The outline was created, as a "polyline", with a convenient online tool from Google, available at http://www.birdtheme.org/useful/v3tool.html.] A higher value for nDemes produces a denser grid, and a denser grid means a more flexible EEMS model because, with more vertices and edges, there are more rate parameters in the model. However, the computational cost of running EEMS increases as well.

# 4 Running the EEMS program

This example shows how to run EEMS on a small simulated dataset (one of the "barrier to migration" datasets used for Figure 2 in the EEMS paper.)

First, copy/create the three input parameter files. All parameters are the same, except for the output directory mcmcpath.

#### params-simno1.ini:

```
datapath = ../data/barrier-schemeX-nIndiv300-nSites3000

mcmcpath = ../data/barrier-schemeX-nIndiv300-nSites3000-EEMS-nDemes200-simno1

nIndiv = 300

nSites = 3000

nDemes = 200

diploid = false

numMCMCIter = 1500000

numBurnIter = 500000

numThinIter = 2999
```

#### params-simno2.ini:

```
datapath = ../data/barrier-schemeX-nIndiv300-nSites3000
mcmcpath = ../data/barrier-schemeX-nIndiv300-nSites3000-EEMS-nDemes200-simno2
nIndiv = 300
nSites = 3000
nDemes = 200
diploid = false
numMCMCIter = 1500000
numBurnIter = 500000
numThinIter = 2999
```

#### params-simno3.ini:

```
datapath = ../data/barrier-schemeX-nIndiv300-nSites3000
mcmcpath = ../data/barrier-schemeX-nIndiv300-nSites3000-EEMS-nDemes200-simno3
nIndiv = 300
nSites = 3000
nDemes = 200
diploid = false
numMCMCIter = 1500000
numBurnIter = 500000
numThinIter = 2999
```

Then run EEMS (on the command line) on the simulated dataset, with three different random seeds. The argument --seed is optional; it can be specified in the parameter file as well, and if not specified, the seed is randomly assigned.

```
./runeems_snps --params params-simno1.ini --seed 123

./runeems_snps --params params-simno2.ini --seed 456

./runeems_snps --params params-simno3.ini --seed 789
```

# 5 Plotting the EEMS results

First install the R package rEEMSplots which provides the function eems.plots. It is not on CRAN, so install it from source instead.

```
## Check that the current directory contains the rEEMSplots source directory (from GitHub)

if (file.exists("./rEEMSplots")) {
   install.packages("rEEMSplots", repos=NULL, type="source")

} else {
   stop("Move to the directory that contains the rEEMSplots source to install the package.")

6 }
```

rEEMSplots provides a single function, with a variety of options. I will use an example to demonstrate those options.

```
## Use the provided example or supply the path to your own EEMS run.

eems.results.to.plot = paste(path.package("rEEMSplots"),"/extdata/EEMS-example",sep="")

name.figures.to.save = "EEMS-example-rEEMSplots"

if (!file.exists(eems.results.to.plot)) {
    stop("Check that the rEEMSplots package is installed without errors.")
}
```

## 5.1 Required arguments

- mcmcpath is a list of EEMS output directories, for the same dataset. It can be a single directory but it is better to run EEMS several times, randomly initializing the MCMC chain each time. [In other words, it is a good idea to simulate several realizations of the Markov chain, each realization starting with a different value of the EEMS parameters.] Warning: There is minimal checking that all directories in the list are for the same dataset.
- 2. plotpath is the full path + the file name for the graphics to be generated. There are five output figures: plotpath-mrates01 (effective migration surface), plotpath-qrates01 (effective diversity surface), plotpath-rdist01 (between-demes component of genetic dissimilarity), plotpath-rdist02 (within-demes component of genetic dissimilarity), plotpath-pilogl01 (posterior probability trace). The three latter figures are helpful in checking that the MCMC sampler has converged (the trace plot) and that the EEMS model fits the data well (the scatter plots of genetic dissimilarities).
- 3. longlat specifies whether coordinates are given as pairs (longitude, latitude) or (latitude, longitude). In the former case, longlat = TRUE, and in the latter case, longlat = FALSE. [More generally, the coordinates are ordered pairs of numbers. Almost all plotting options are valid for general coordinates, except for the options to specify the projection and to add the geographic map.]

I will use the PoBI data to demonstrate how to visualize EEMS results. PoBI stands for "People of the British Isles" – see [Winney et al., 2012] for information on how the data was collected and an initial analysis, as well as [Leslie et al., 2015] for extensive population structure analysis using fineSTRUCTURE [Lawson et al., 2012].

Figure 3 shows the figures produced by eems.plots when only the three required arguments are specified.

```
## Produce the five EEMS figures, with default values for all optional parameters.

eems.plots(mcmcpath = eems.results.to.plot,

plotpath = paste(name.figures.to.save,"-default",sep=""),

longlat = TRUE)
```

Passing longlat = FALSE instead of longlat = TRUE has the effect of flipping the x-axis and the y-axis – compare Figures 3(a) and 3(b) to Figures 4(a) and 4(b). It is particularly important to specify this argument correctly if adding a geographic map to the migration and diversity contour plots. [That's why longlat is a required, not an optional argument.]

```
## Flip the x and y axis, i.e., assume that the x coordinate is the latitude and the y coordinate is the longitude.

eems.plots(mcmcpath = eems.results.to.plot,

plotpath = paste(name.figures.to.save,"-axes-flipped",sep=""),

longlat = FALSE)
```

#### 5.2 Optional arguments about the graphics format

eems.plots generates output graphics as either PNGs (the default) or PDFs.

- plot.height/plot.width: dimensions of the display region, in inches.
- out.png: TRUE or FALSE, specifies whether to generate PNGs or PDFs.
- res: resolution, in dots per inch, only relevant if the output is PNG graphics. The default is 600.

```
## Generate PNG figures with height 9 inches, width 8 inches and resolution 600 dots per inch.
   eems.plots(mcmcpath = eems.results.to.plot,
              plotpath = paste(name.figures.to.save,"-output-PNGs",sep=""),
              longlat = TRUE.
              plot.height = 8,
              plot.width = 7,
              res = 600,
              out.png = TRUE)
   ## Generate PDF figures with height 9 inches and width 8 inches. The resolution option, res, is ignored.
   eems.plots(mcmcpath = eems.results.to.plot,
              plotpath = paste(name.figures.to.save,"-output-PDFs",sep=""),
              longlat = TRUE,
              plot.height = 8,
14
              plot.width = 7,
15
              res = 600,
16
              out.png = FALSE)
```

#### 5.3 Optional arguments about the population grid

• add.grid: TRUE or FALSE, specifies whether to add the population grid or not.

- col.grid: the color of the grid (default is gray80)
- lwd.grid: the line width (default is 1)
- add.outline: TRUE or FALSE, specifies whether to add the habitat outline or not.
  - col.outline: the color of the outline (default is white)
  - lwd.outline: the line width (default is 2)
- add.demes: TRUE or FALSE, specifies whether to add the observed demes or not.
  - col.demes: the color of the demes (default is black)
  - pch. demes: the symbol/character used for plotting the demes (default is 19)
  - min.cex.demes: the minimum size of the deme symbol/character (default is 1)
  - ${\hspace{0.25cm}\text{--}\hspace{0.1cm}}$  max.cex.demes: the maximum size of the deme symbol/character (default is 3)

The unusual options are min.cex.demes and max.cex.demes. If max.cex.demes > min.cex.demes, then demes with more samples also have bigger size: the deme with the fewest samples has size min.cex.demes and the deme with the most samples has size max.cex.demes. So if the sampling is uneven, then max.cex.demes > min.cex.demes underlines this fact. See Figure 5 for an example.

```
## Choose somewhat impractical colors and shapes for the outline, the grid and the demes.
   eems.plots(mcmcpath = eems.results.to.plot,
              plotpath = paste(name.figures.to.save, "-demes-and-edges", sep=""),
              longlat = TRUE,
              add.grid = TRUE,
              col.grid = "gray90",
              lwd.grid = 2,
              add.outline = TRUE,
              col.outline = "blue",
              lwd.outline = 5,
10
              add.demes = TRUE,
              col.demes = "red",
              pch.demes = 5,
              min.cex.demes = 0.5,
              max.cex.demes = 1.5)
```

# 5.4 Optional arguments about the cartographic projection

If we know the projection of the input coordinates and the R package rgdal is installed, then we can plot the effective migration and diversity surfaces in another projection. See Figure 6 for an example.

- projection.in: input projection, as a valid PROJ.4 string.
- projection.out: output projection, as a valid PROJ.4 string.

```
library(rgdal)

## Produce contour plots in the Mercator projection (used by Google Maps)

eems.plots(mcmcpath = eems.results.to.plot,

plotpath = paste(name.figures.to.save,"-merc-projection",sep=""),

longlat = TRUE,

projection.in = "+proj=longlat +datum=WGS84",

projection.out = "+proj=merc +datum=WGS84")
```

## 5.5 Optional arguments about the geographic map

If we know the projection of the input coordinates and the R packages rgdal, rworldmap, rworldxtra are installed, then we can add a geographic map to the two contour plots. See Figure 7 for an example.

- add.map: TRUE or FALSE, specifies whether to add a geographic map or not.
- col.map: the color of the map (default is gray60)
- 1wd.map: the line width (default is 2)

#### 5.6 Optional arguments about the color scheme

Finally, we can also specify the color palette as a vector of colors, eems.plot, ordered from low to high. See Figure 8 for an example.

```
library(RColorBrewer)

## Use a divergent Red to Blue color scheme from 'RColorBrewer' instead of the default DarkOrange to Blue color scheme.

eems.plots(mcmcpath = eems.results.to.plot,

plotpath = paste(name.figures.to.save,"-new-eems-colors",sep=""),

longlat = TRUE,

projection.in = "+proj=longlat +datum=WGS84",

projection.out = "+proj=merc +datum=WGS84",

eems.colors = brewer.pal(11,"RdBu"))
```

## 5.7 A test function to generate Voronoi diagrams

Given one EEMS output directory, the function eems.voronoi, also available in the rEEMSplots package, produces Voronoi diagrams drawn from the posterior distribution of the rate parameters: there is one series of tessellations for the effective migration rates and another series for the effective diversity rates. Both series contain one figure for each saved MCMC iteration, after burn-in and thinning. Warning: eems.voronoi potentially generates a large number of figures. See Figure 9 for a small example.

```
library(deldir)

## Plot a series of Voronoi diagrams for the EEMS model parameters:

## the effective migration rates (m) and the effective diversity rates (q).

eems.voronoi(mcmcpath = eems.results.to.plot,

plotpath = paste(name.figures.to.save,"-default",sep=""),

longlat = TRUE,

plot.height = 7,

plot.width = 5)
```

### 6 Observed vs fitted distances

EEMS aims to model the genetic differentiation between individuals in space. To achieve this, EEMS constructs a triangular grid, assigns each sample to its closest vertex (deme) and estimates a migration rate for every edge and a diversity rate for every vertex in the grid.

To be specific, consider two different demes  $\alpha$  and  $\beta$ . Suppose that individual i is assigned to deme  $\alpha$ , which we denote by  $\delta(i) = \alpha$ . Similarly, suppose that  $\delta(i') = \alpha$  but i and i' are distinct individuals, that  $\delta(j) = \beta$  and  $\delta(j') = \beta$  but j and j' are distinct individuals. [Of course, i and j are distinct individuals because they come from two different demes.]

In EEMS, the observed genetic dissimilarity is the average squared genetic difference, across *p* markers:

$$D_{ij} = \frac{1}{p} \sum_{k=1}^{p} \left( Z_{ik} - Z_{jk} \right)^2, \tag{1}$$

where  $Z_{ik}$ ,  $Z_{ik}$  are the genotypes of i, j at marker k. There are various other ways to define genetic (dis)similarity – for example, fineSTRUCTURE uses a statistic called "coancestry" which is a measure of genetic similarity. Proportion of the genome shared identical by descent (IBD fraction) is another statistic informative about recent population structure.

EEMS assumes that individuals in the same deme are exchangeable. Since  $\delta(i) = \delta(i') = \alpha$  and  $\delta(j) = \delta(j') = \beta$ , exchangeability implies that:

$$E\{D_{ij}\} = \Delta_{\alpha\beta}, \qquad E\{D_{ii'}\} = \Delta_{\alpha\beta}, \qquad E\{D_{jj'}\} = \Delta_{\beta\beta}. \tag{2}$$

That is, the expected genetic dissimilarity between two distinct individuals depends only on their locations. [In other words, EEMS is a spatially explicit model.] In matrix notation, the observed data is the matrix of average squared genetic differences,  $D=(D_{ij})$ , which is modeled by a *block* matrix of expected genetic dissimilarities,  $\Delta=\left(\Delta_{\delta(i)\delta(j)}\right)=(\Delta_{\alpha\beta})$ . [Both matrices have a main diagonal of 0s because self-dissimilarity is 0.]

We might want a spatially explicit model to be consistent with the following ideas: We expect that (i, j) are more dissimilar than either (i, i') or (j, j') because i, j come from different locations. However, in general, we can't expect (i, i') to be as dissimilar as (j, j') – there might be some differences in local genetic diversity. And to model the genetic dissimilarity due to migration in space we need to take into account any differences in local diversity. For this reason, EEMS decomposes the genetic dissimilarity into two components: between demes and within demes:

$$\Delta_{\alpha\beta} = \underbrace{\Delta_{\alpha\beta} - \left(\Delta_{\alpha\alpha} + \Delta_{\beta\beta}\right)/2}_{\text{between demes}} + \underbrace{\left(\Delta_{\alpha\alpha} + \Delta_{\beta\beta}\right)/2}_{\text{within demes}}.$$
(3)

The within-demes component, *W*, characterizes the expected genetic dissimilarity between two distinct individuals from the same deme and is a function of the effective diversity rates:

$$W_{\alpha} = \Delta_{\alpha\alpha} = g(q)_{\alpha}. \tag{4}$$

[Here g(q) is a vector and  $g(q)_{\alpha}$  is the element that corresponds to deme  $\alpha$ .]

The between-demes component, *B*, characterizes the expected genetic dissimilarity between two individuals from distinct demes, *after* correcting for the local differences in genetic diversity, and is a function of the effective migration rates:

$$B_{\alpha\beta} = \Delta_{\alpha\beta} - \left(\Delta_{\alpha\alpha} + \Delta_{\beta\beta}\right)/2 = f(m)_{\alpha\beta}.$$
 (5)

[Here f(m) is a matrix and  $f(m)_{\alpha\beta}$  is the element that corresponds to the pair of demes  $(\alpha, \beta)$ .]

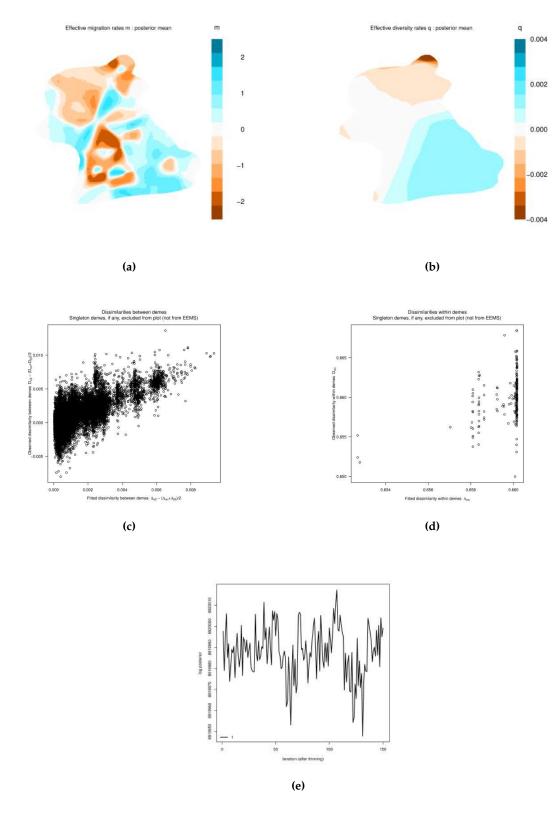
Therefore, EEMS models expected genetic dissimilarity as:

$$\Delta_{\alpha\beta} = \underbrace{\Delta_{\alpha\beta} - \left(\Delta_{\alpha\alpha} + \Delta_{\beta\beta}\right)/2}_{} + \underbrace{\left(\Delta_{\alpha\alpha} + \Delta_{\beta\beta}\right)/2}_{}$$
 (6)

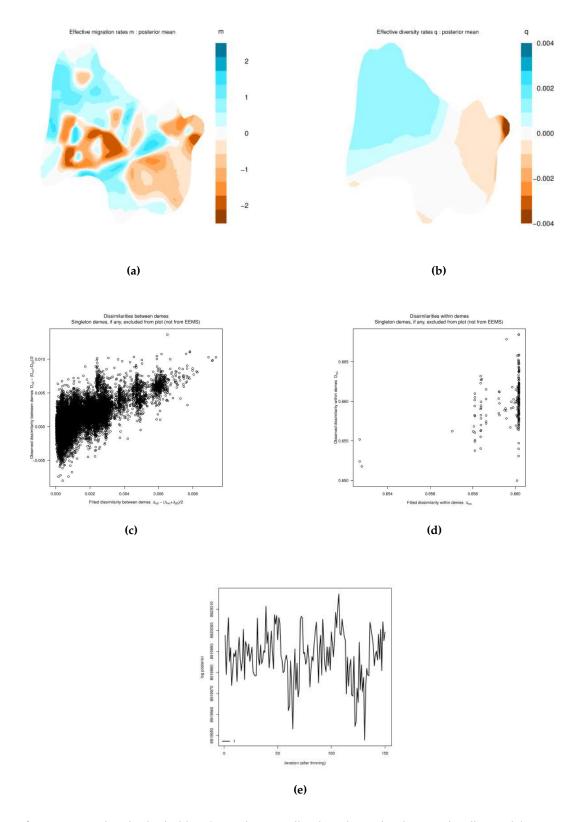
$$= B_{\alpha\beta} + (W_{\alpha} + W_{\beta})/2. \tag{7}$$

The between-demes component of the genetic dissimilarity is plotted in plotpath-rdist01, as a scatterplot of observed vs fitted values. The within-demes component of the genetic dissimilarity is plotted in plotpath-rdist02. See Figure 10 for an example. If the EEMS model fits the data well (after the MCMC chain has converged), we expect to see a strong linear relationship between the observed and fitted values in both scatterplots. Therefore, these scatterplots are useful for model-checking diagnostics.

However, once we are reasonably convinced that the EEMS model is appropriate for the data being analyzed, the parameters of the model are of greater interest than the expected dissimilarities: i.e., m and q are more interesting than f(m) and g(q). The rate parameters are visualized in the colored contour plots: the effective migration rates m are plotted in plotpath-mrates01, the effective diversity rates q are plotted in plotpath-qrates01, in both cases on the  $\log_{10}$  scale and after some normalization. [The function f, which takes the migration rates m and returns a matrix of expected between-demes dissimilarities, is the effective resistance distance in an undirected, connected graph. The function g, which takes the diversity rates and returns a vector of expected within-demes dissimilarities, is the identity.]



**Figure 3** The eems.plots function in the rEEMSplots package produces five figures. **(a)** Estimated effective migration surface. **(b)** Estimated effective diversity surface. **(c)** Observed vs fitted dissimilarities: between-demes component. See Section 6 for more details. **(d)** Observed vs fitted dissimilarities: within-demes component. See Section 6 for more details. **(e)** Posterior probability trace.



**Figure 4** In EEMS points in the habitat (e.g., the sampling locations, the demes, the tile seeds) are represented as ordered pairs (x, y). The x and y axes can be flipped with the longlat argument to eems.plots: use longlat = TRUE for the original ordering of the two coordinates and longlat = FALSE to flip them. This changes the migration and the diversity figures, **(a)** and **(b)**, but not the three diagnostic figures, **(c)**, **(d)** and **(e)**. In fact, all optional arguments to the plotting function modify only the migration and diversity contour plots.

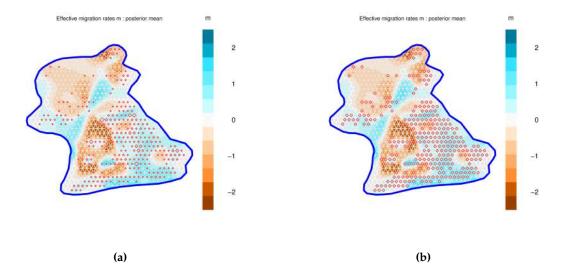
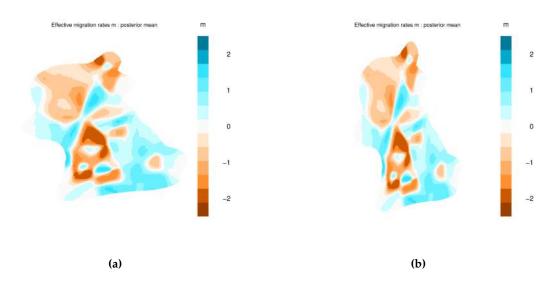
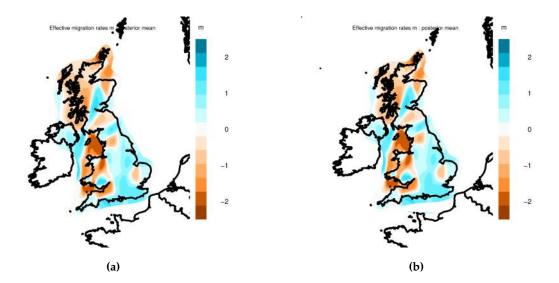


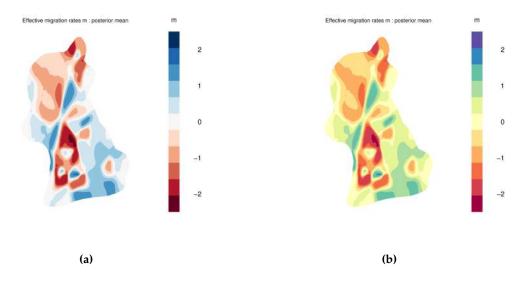
Figure 5 Use the options add.grid, add.demes, add.outline to add the population grid, the sampled demes and/or the habitat outline. The colors, line width and the symbol/character can all be specified. Most importantly, the arguments min.cex.demes and max.cex.demes can be used to underline the sampling scheme, so that a deme with more samples is indicated with a larger symbol/character. (a) min.cex.demes = 0.5, max.cex.demes = 1.5 (b) min.cex.demes = max.cex.demes = 1



**Figure 6** Use the arguments projection.in and projection.out to specify the input and output projection, as valid PROJ.4 strings. This requires the rgdal package. **(a)** The effective migration surface with longitude and latitude untransformed: projection.out = "+proj=longlat +datum=WGS84". **(b)** The same effective migration surface in the Mercator projection: projection.out = "+proj=merc +datum=WGS84".



**Figure 7** If we know the input projection (e.g., if we know that the input coordinates are given in longitude/latitude), then we can add a geographic map to the migration and diversity contour plots. This requires the rworldmap package (for the getMap function which provides access a world map derived from Natural Earth data) and the rworldxtra package (for the high-resolution version of the map). **(a)** In the Mercator (cylindrical) projection. **(b)** In the Lambert-93 (conic) projection, with PROJ.4 string "+proj=lcc +lat\_1=49 +lat\_2=44 +lat\_0=46.5 +lon\_0=3 +x\_0=700000 +y\_0=6600000 +ellps=GRS80 +towgs84=0,0,0,0,0,0 +units=m +no\_defs".



**Figure 8** By default, the plotting function eems.plots uses a DarkOrange to Blue color scheme, adapted from the dichromat package. [This scheme takes the dark oranges from the BluetoDarkOrange.12 theme and the blues the BrowntoBlue.12 theme.] To specify a different color scheme, we can supply a vector of colors with the eems.colors argument. These can be any colors but only a divergent scheme makes sense for a contour plot. **(a)** The effective migration surface in the RdBu palette from the RColorBrewer package. **(b)** The effective migration surface in the Spectral palette from the RColorBrewer package.

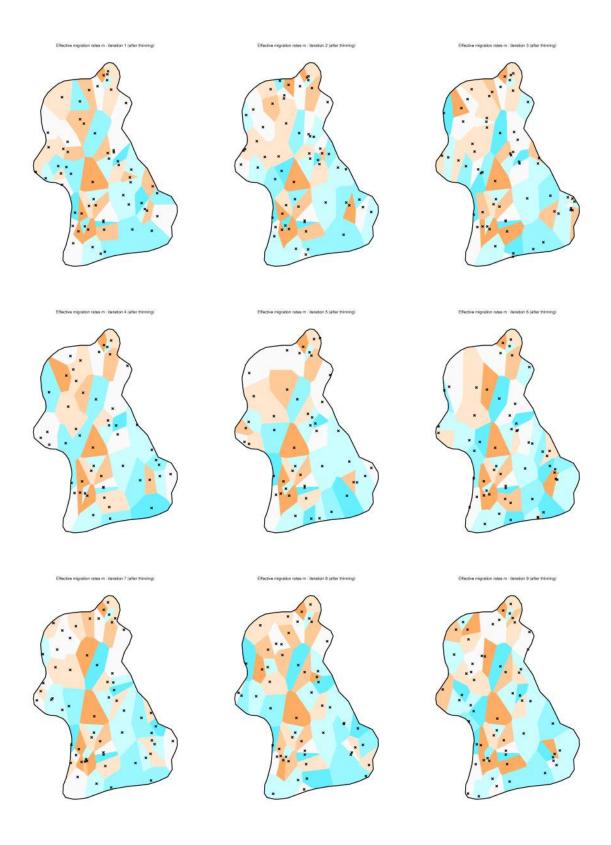
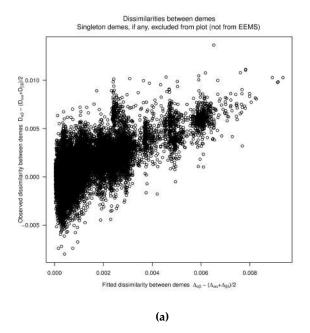


Figure 9 Voronoi diagrams drawn from the posterior distribution of the effective migration rates m, generated by eems.voronoi.



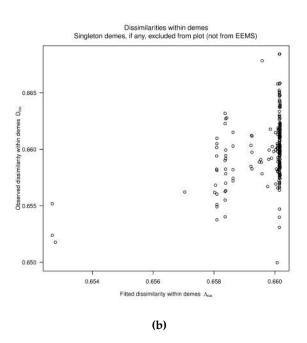


Figure 10 Observed vs fitted genetic dissimilarities, between and within demes. The observed genetic dissimilarities between individuals,  $D_{ij}$ , are averaged so that  $D_{\alpha\beta}=\frac{1}{n_{\alpha\beta}}\sum_{\delta(i)=\alpha,\delta(j)=\beta}D_{ij}$  where  $n_{\alpha\beta}$  is the number of pairs (i,j) such that  $\delta(i)=\alpha$ ,  $\delta(j)=\beta$ , i.e., sample i is assigned to deme  $\alpha$ , sample j is assigned to deme  $\beta$ , and i,j are distinct individuals. Singleton demes (those with a single sample) are excluded from both scatterplots. (a) Dissimilarities between demes: the fitted values  $B_{\alpha\beta}:=\Delta_{\alpha\beta}-(\Delta_{\alpha\alpha}+\Delta_{\beta\beta})/2$  comprise the between-demes component of the genetic dissimilarity, B, which is modeled by the effective migration rates: B=f(m). (b) Dissimilarities within demes: the fitted values  $W_{\alpha}:=\Delta_{\alpha\alpha}$  comprise the within-demes component of the genetic dissimilarity, W, which is modeled by the effective diversity rates: W=g(q). If the EEMS model fits the data well (after the MCMC chain has converged), we expect to see a strong linear relationship between the observed and fitted values in both scatterplots. See Section 6 for more details.

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