

KSFUPRO1K1U – Functional Programming

Lecture 6: Modules

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The original slides has been used at a course in functional programming at DTU.

Overview



- Modular program design including
 - encapsulation
 - abstraction and
 - reuse of software components.
- A module is characterized by:
 - a signature an interface specifications and
 - a matching implementation containing declarations of the interface specifications.
- Example based (incomplete) presentation to give the flavor.

Sources:

• Chapter 7: Modules.

An example: Search trees



Consider the following implementation of search trees:

```
type Tree = Lf
            | Br of Tree*int*Tree;;
let rec insert i = function
 | Lf
                   -> Br(Lf,i,Lf)
 \mid Br(t1,j,t2) as tr ->
     match compare i j with
     1 0
        -> tr
     \mid n when n<0 -> Br(insert i t1 , j, t2)
             -> Br(t1, j, insert i t2);;
let rec memberOf i = function
 | Lf -> false
 | Br(t1,j,t2) -> match compare i j with
                 | 0 -> true
                 In when n<0 -> memberOf i t1
                 -> memberOf i t2;;
```

Example cont'd



Is this implementation adequate?

No. Search tree property can be violated by a programmer:

```
toList(insert 2 (Br(Br(Lf,3,Lf), 1, Br(Lf,0,Lf))));;
> val it = [3;1;0;2]: int list
```

Problem: The tree argument to toList is not balanced.

Solution: Hide the internal structure of search trees.

Module



A module is a combination of a

- signature, which is a specification of an interface to the module (the user's view), and an
- implementation, which provides declarations for the specifications in the signature.

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Geometric vectors: Signature



The signature specifies one type and eight values:

```
// Vector signature
module VectorSimple
type vector
val ( ~-. ) : vector -> vector
                                  // Vector sign change
                                        // Vector sum
val (+.): vector -> vector -> vector
val ( -. ) : vector -> vector -> vector
                                        // Vector difference
val ( *. ) : float -> vector -> vector
                                        // Product with number
val ( &. ) : vector -> vector -> float
                                        // Dot product
val norm : vector -> float
                                        // Length of vector
val make : float * float -> vector
                                        // Make vector
val coord : vector -> float * float
                                        // Get coordinates
```

The specification 'vector' does not reveal the implementation

• Why is make and coord introduced?

Geometric vectors (2): Simple implementation



An implementation must declare each specification of the signature:

```
// Vector implementation module VectorSimple type vector = V of float * float let (~-.) (V(x,y)) = V(-x,-y) let (+.) (V(x1,y1)) (V(x2,y2)) = V(x1+x2,y1+y2) let (-.) v1 v2 = v1 +. -. v2 let (*.) a (V(x1,y1)) = V(a*x1,a*y1) let (&.) (V(x1,y1)) (V(x2,y2)) = x1*x2 + y1*y2 let norm (V(x1,y1)) = sqrt(x1*x1+y1*y1) let make (x,y) = V(x,y) let coord (V(x,y)) = (x,y)
```

 Since the representation of 'vector' is hidden in the signature, the type must be implemented by either a tagged value or a record.

Geometric vectors (3): Compilation



Suppose

- the signature is in a file 'VectorSimple.fsi'
- the implementation is in a file 'VectorSimple.fs'

A library file 'VectorSimple.dll' is constructed by the following command:

```
fsc -a VectorSimple.fsi VectorSimple.fs
```

On my MacBook installation I have to use fsharpc instead of fsc.

The library 'Vector' can now be used just like other libraries, such as 'Set' or 'Map'.

Geometric vectors (4): Use of library



A library must be referenced before it can be used.

```
#r @"/Users/.../VectorSimple.dll";;
--> Referenced '/Users/.../VectorSimple.dll'
open Vector ::
let a = make(1.0, -2.0);
val a : vector
let b = make(3.0, 4.0);;
val b : vector
let c = 2.0 *. a -. b;
val c : vector
coord c ::
val it : float * float = (-1.0, -8.0)
let d = c \& a::
val d : float = 15.0
let e = norm b;;
val e : float = 5.0
```

Notice: the implementation of vector is not visible and it cannot be exploited.

Type augmentation

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A type augmentation

- adds declarations to the definition of a tagged type or a record type
- allows declaration of (overloaded) operators.

In the 'Vector' module we would like to

- overload +, and * to also denote vector operations.
- overload * is even overloaded to denote two different operations on vectors.

Type augmentation - signature (Vector.fsi)



```
module Vector
```

```
[<Sealed>]
type vector =
  static member ( ~- ) : vector -> vector
  static member ( + ) : vector * vector -> vector
  static member ( - ) : vector * vector -> vector
  static member ( * ) : float * vector -> vector
  static member ( * ) : vector * vector -> float
val make : float * float -> vector
val coord: vector -> float * float
val norm : vector -> float
```

- The attribute [<Sealed>] is mandatory when a type augmentation is used.
- The "member" specification and declaration of an infix operator (e.g. +) correspond to a type of form type₁ * type₂ -> type₃
- The operators can still be used on numbers.

Type augmentation – implementation and use (Vector.fs)



The operators +, -, * are available on vectors even without opening:

```
let a = Vector.make(1.0,-2.0);;
val a : Vector.vector

let b = Vector.make(3.0,4.0);;
val b : Vector.vector

let c = 2.0 * a - b;;
val c : Vector.vector
```

Type Extension



You can insert function declarations between the type defintion and member declarations using *type extension*

A library file 'VectorTypeExtension.dll' is constructed by the following command:

```
fsc -a Vector.fsi VectorTypeExtension.fs
```

On my MacBook installation I have to use fsharpc instead of fsc.

Customizing the string function



- The default ToString function that do not reveal a meaningful value is overridden to give a string for the pair of coordinates.
- A type extension is used.

Example:

```
let a = Vector.make(1.0,2.0);;
val a : Vector.vector = (1, 2)
string(a+a);;
val it : string = "(2, 4)"
```

Classes and objects

Class Definition



F# has OO capabilities which is heavily used when integrating to the .NET library.

A class can be defined as follows:

Notice the syntactic resemblance with *Type Augmentation*.

Classes and objects





The use of a class is straight forward:

```
let a = ObjVector(1.0, -2.0)
> val a : ObjVector
let b = ObjVector(Y=4.0, X=3.0)
> val b : ObjVector
b.coord()
> val it : float * float = (3.0, 4.0)
let c = 2.0 * a - b
> val c : ObjVector
c.coord()
> val it : float * float = (-1.0, -8.0)
h.x
> val it : float = 3.0
let d = c * a
> val d : float = 15.0
let e = b.norm()
> val e : float = 5.0
let \alpha = (+) a b
> val q : ObjVector
a.coord()
> val it : float * float = (4.0, 2.0)
```

Notice the use of Named Arguments.

Parametrized modules (QueueSimple.fsi)



Type variables in signatures

Example to make a Queue class where objects in the queue can be of any type τ as long as they are all of the same type τ .

```
module Queue
type Queue<'a>
val empty : Queue<'a>
val put : 'a -> Queue<'a> -> Queue<'a>
val get : Queue<'a> -> 'a * Queue<'a>
exception EmptyQueue</a>
```

Notice you can write

type 'a Queue

instead of

type Queue< 'a>

Parametrized modules (QueueSimple.fs)

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Queue Implementation

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The Queue is implemented using a front list and a rear list supporting either constant time or linear time get functionality.

The "hope" is that in many cases it will be constant time.

If the front list is empty, then the rear list is reversed and used as front list.

Parametrized modules

Queue Example



Notice the most generic type for ${\tt q0}$ and then afterwards a non polymorphic int queue.

```
\#r @"/Users/.../OueueSimple.dll"
let q0 = Oueue.empty
> val q0 : Oueue.Oueue<'a>
let q0 = Oueue.empty : Oueue.Oueue<int>
> val q0 : Oueue.Oueue<int>
let q1 = Oueue.put 1 q0
> val q1 : Queue.Queue<int>
let q2 = Oueue.put 2 q1
> val g2 : Oueue.Oueue<int>
let (x,q3) = Queue.qet q2
> val x : int = 1
 val q3 : Oueue.Oueue<int>
let q4 = Oueue.put 4 q3
> val x2 : int = 2
 val q5 : Oueue.Oueue<int>
let (x2.q5) = Oueue.qet q4
> val x2 : int = 2
  val q5 : Oueue.Oueue<int>
```

Customizing Equality



Structural Equality does not work for the data representation chosen for Queue:

```
> let qnew = Queue.put 2 q0 ;;
val qnew : Queue.Queue<int>

> qnew = q3 ;;
val it : bool = false
```

The representation of

```
qnew, {front=[]; rear=[2]} and q3, {front=[2]; rear=[]}
is different.
```

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Customizing Equality



We can override the default equality function with type augmentation. An equality constraint is added to the element type in the signature:

```
type Queue<'a when 'a : equality>
```

You cannot override in a separate type extension.

You also have to re-define the hash function.

Below we also override ToString at the same time.

```
module Oueue
exception EmptyQueue
[<CustomEquality; NoComparison>]
type Queue<'a when 'a : equality> =
     {front: 'a list; rear: 'a list}
     member q.list() = q.front @ (List.rev q.rear)
     override q1.Equals gobi =
         match gobj with
         | :? Queue<'a> as q2 -> q1.list() = q2.list()
         | _ -> false
     override q.GetHashCode() = hash (q.list())
     override q.ToString() = string (q.list())
anew = a3
> val it : bool = true
```

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Customizing Ordering

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You can also change the ordering and indexing on values on a defined type.

```
module Oueue
exception EmptyQueue
[<CustomEquality;CustomComparison>]
type Queue<'a when 'a : comparison> =
     {front: 'a list; rear: 'a list}
     member q.list() = q.front @ (List.rev q.rear)
. . .
     interface System. I Comparable with
       member gl.CompareTo gob; =
         match gobj with
         | :? Queue < 'a > as q2 -> compare (q1.list()) (q2.list())
           invalidArg "gobj"
                       "cannot compare values of different types"
     member q.Item
       with qet n = (q.list()).[n]
. . .
```

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Summary



Modular program development

- program libraries using signatures and structures
- type augmentation, overloaded operators, customizing string (and other) functions
- Encapsulation, abstraction, reuse of components, division of concerns, ...

• ...