

Fourth Monitoring Committee Meeting

Understanding the Information Content in Diverse Observations of Forest Carbon Stocks and
Fluxes for Data Assimilation and Ecological Modeling
NERC case partnership with Forest Research

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1 Introduction

Forest ecosystems play a large role in reducing the impact of anthropogenic CO₂ emissions and therefore understanding their response to climate change is important. Currently, in data assimilation, the optimal set of observations to add the most information to models of forest carbon balance is not known.

In our last monitoring committee the Data Assimilation Linked Ecosystem Carbon model (DALEC) [?] was introduced and we showed how this model could be implemented in a variational data assimilation (DA) framework in order to look at the information content of different forest carbon balance observations. In particular, Shannon Information Content [?] was used to investigate the level of information provided by single and successive observations of the Net Ecosystem Exchange (NEE) of CO₂ at flux tower sites and it was shown that observations of NEE taken in summer with warmer temperatures and higher daily irradiances had a higher information content than those taken in winter. This makes physical sense as observations of NEE in the summer are of greater magnitude and give more information about the fluxes of carbon throughout the forest. The error in our linearized version of DALEC was also considered. This is important as in four-dimensional variational data assimilation (4D-Var) the linearized model is used in the tangent linear hypothesis. The results from this experiment showed the linearized DALEC to perform poorly. However, I have now found that the linear DALEC was not derived correctly and repeating these experiments shows the tangent linear hypothesis to be a good approximation for DALEC.

Since our last meeting work has continued on the information content of forest carbon balance observations. The degrees of freedom for signal has been investigated as another measure for information content and I have written a first draft of a report on my findings (included alongside my monitoring report). DALEC was built into a 4D-Var scheme assimilating data from a young pine stand in Oregon in order to estimate the five carbon pools which make up the state vector. I have started visiting the Forest Research site at Alice Holt on a weekly basis and am helping with current measurement campaigns. A new version of the DALEC model has been released since our last meeting (DALECV2 [?]) which can be parameterized for both evergreen and deciduous forests, the previous DALEC only models evergreen forests. As Alice Holt is mainly deciduous I have started working with DALECV2. Currently, I have coded DALECV2 in Python and have started to build this into a 4D-Var scheme similar to that which I had written for the state estimation with DALEC but now also estimating the 17 model parameters. I hope this will allow me to parameterize DALECV2 for the Alice Holt research site. In this report we begin by showing some of the results from the information content experiments.

2 Information Content

In the last monitoring report the Shannon Information Content (SIC) was used as a measure of the reduction in entropy of a system given a set of observations [?]. The SIC can be derived as,

$$\text{SIC} = \frac{1}{2} \ln \frac{|\mathbf{B}|}{|\mathbf{A}|}, \quad (1)$$

where $|\mathbf{B}|$ is the determinant of the background error covariance matrix and $|\mathbf{A}|$ is the determinant of the analysis covariance matrix. The NEE of a forest in the DALEC model is expressed as the difference between the Gross Primary Production (GPP) of the forest and the respirations of the forest at time t ,

$$\text{NEE}(t) = -(1 - p_2)\text{GPP}(C_f(t), \phi) + p_8 C_l T(t) + p_9 C_s T(t), \quad (2)$$

where p_2, p_8, p_9 are model parameters, C_f, C_l, C_s are carbon pools, ϕ represents the meteorological driving data used by the GPP function and $T = \frac{1}{2} \exp(\Theta T_{\text{mean}}(t))$ is an exponential function of the mean daily temperature. Combining equations (1) and (2) and using the 4D-Var framework for DALEC we can derive the SIC for an observation of NEE at time t as,

$$\text{SIC for NEE}(t) = \frac{1}{2} \ln \frac{(p_2 - 1)^2 \text{GPP}'^2(C_f(t), \phi) \sigma_{cf,b}^2 + \sigma_{nee,o}^2 + T^2(t)(p_9^2 \sigma_{cs,b}^2 + p_8^2 \sigma_{cl,b}^2)}{\sigma_{nee,o}^2}. \quad (3)$$

where $\sigma_{cf,b}^2, \sigma_{cl,b}^2, \sigma_{cs,b}^2$ are the background variances for the carbon pools and $\sigma_{nee,o}^2$ is the variance of the error in an observation of NEE. If we assume that the variances and parameters here are fixed, we can see that the size of the SIC is dependent on the temperature term, $T(t)$, and the square of the first derivative of GPP. Generally, the value of GPP (and its first derivative) is highest in summer with higher temperatures and higher total daily irradiance. We therefore have that there will be more information content in observations that are taken when temperatures are higher. Physically this makes sense as more NEE takes place when temperatures are higher (to a point), so measurements are of greater magnitude and give us more information about carbon fluxes.

By plotting the SIC for a single observation of NEE, varying with three years of meteorological driving data, next to the temperature term ($T(t)$) for the same data we can see that both are closely linked, figure 1. This shows that observations of NEE made in the summer are much more

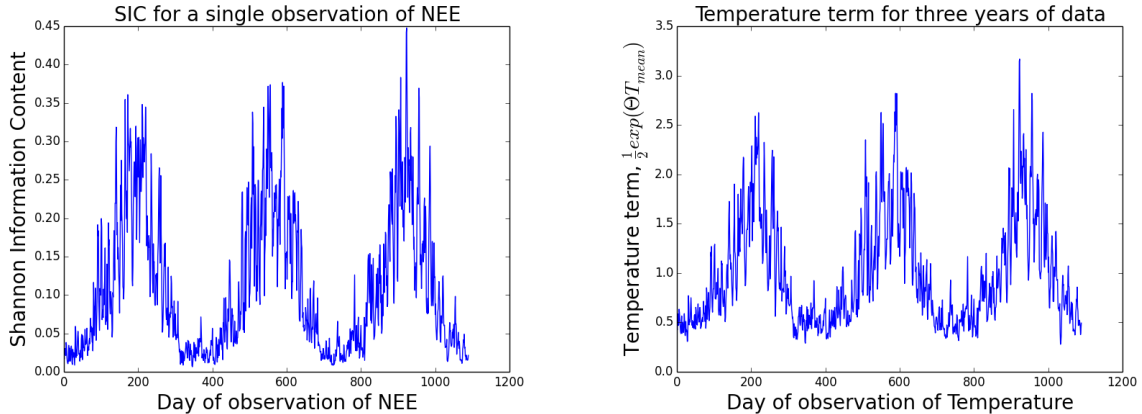


Figure 1: SIC and temperature varying over three years using driving data from Oregon pine forest.

valuable than those made in the winter assuming warmer temperatures, higher daily irradiance and a higher amount of foliar carbon in the summer.

In the report this idea is also explored for the degrees of freedom for signal (DFS) measure for information content. The DFS indicates the number of elements of the state that have been measured by the observations. If we consider a state vector \mathbf{x} with n elements (or n degrees of freedom) then the maximum value the DFS could attain would be n , in this case all elements of the state would have been measured. Conversely if $\text{DFS} = 0$ then no elements of the state would have been measured by our observations [?]. The DFS can be written as,

$$\text{DFS} = n - \text{trace}(\mathbf{B}^{-1}\mathbf{A}). \quad (4)$$

The result in figure 1 can be reproduced using the DFS showing that we measure more elements of our state with observations of NEE made in summer than observations made in winter. To understand how much more value the summer observations of NEE have compared to the winter observations we have plotted the increasing SIC and DFS for 50 observations made from December 21st onwards and also the the constant line of SIC and DFS for one observation of NEE made in summer at a mean daily temperature of 26°C on July 12th. This is shown in figure 2.

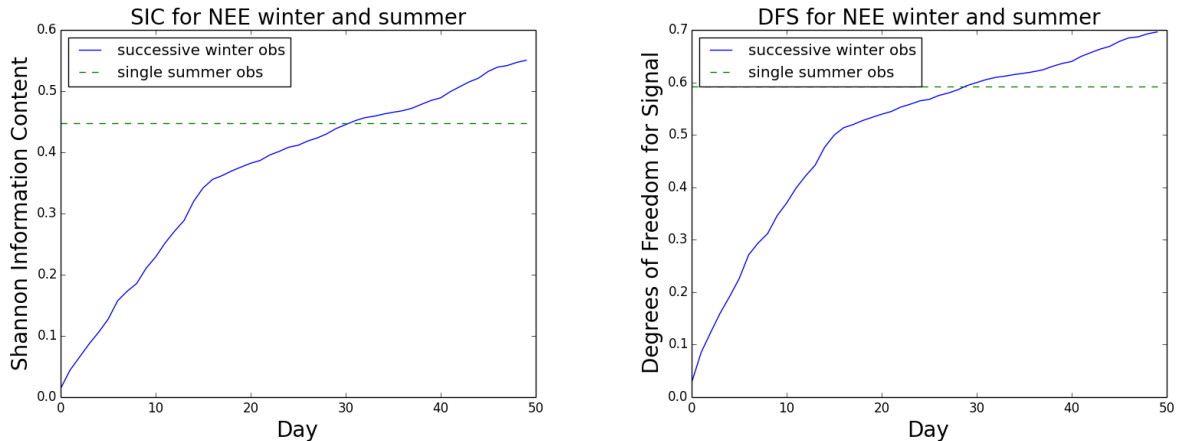


Figure 2: SIC (left) and DFS (right) for a single summer observation of NEE and successive winter observations of NEE using driving data from Oregon pine forest.

Figure 2 shows us that, for the driver data used in this experiment, we require 31 days of NEE observations to gain the same reduction in entropy for our analysis as 1 observation made in the summer and 30 days of NEE observations to achieve the same DFS as 1 observation made in the summer. For more detail on the information content experiments with DALEC please see the attached report [?].

3 4D-Var with DALEC

In 4D-Var we aim to maximise the probability of the initial state \mathbf{x}_0 given a set of observations \mathbf{y} , $P(\mathbf{x}_0|\mathbf{y})$, over some time window, N . $P(\mathbf{x}_0|\mathbf{y})$ is maximised by minimising a cost function $J(\mathbf{x})$ derived from Baye's Theorem [?]. The cost function is given as,

$$J(\mathbf{x}_0) = \frac{1}{2}(\mathbf{x}_0 - \mathbf{x}_b)^T \mathbf{B}^{-1}(\mathbf{x}_0 - \mathbf{x}_b) + \frac{1}{2} \sum_{i=0}^N (\mathbf{y}_i - h_i(\mathbf{x}_i))^T \mathbf{R}_i^{-1}(\mathbf{y}_i - h_i(\mathbf{x}_i)), \quad (5)$$

where \mathbf{x}_b is the background and acts as the initial guess of the state \mathbf{x}_0 , \mathbf{B} is the background error covariance matrix and quantifies the knowledge of the error in the background, h_i is the observation operator at time t_i and maps the state vector evolved by the nonlinear model ($m_{0 \rightarrow i}(\mathbf{x}_0) = \mathbf{x}_i$) to the observations at this time \mathbf{y}_i and \mathbf{R}_i is the observation error covariance matrix and represents the knowledge of the uncertainty in the observations. The state that minimises the cost function is called the analysis and is denoted as \mathbf{x}_a , this state is found using a minimisation routine that takes the cost function, the initial guess (\mathbf{x}_b) and also the gradient of the cost function defined as,

$$\nabla J(\mathbf{x}_0) = \mathbf{B}^{-1}(\mathbf{x}_0 - \mathbf{x}_b) - \sum_{i=0}^N \mathbf{M}_{i,0}^T \mathbf{H}_i^T \mathbf{R}_i^{-1}(\mathbf{y}_i - h_i(\mathbf{x}_i)), \quad (6)$$

where $\mathbf{H}_i = \frac{\delta h_i(\mathbf{x}_i)}{\delta \mathbf{x}_i}$ is the linearized observation operator and $\mathbf{M}_{i,0} = \mathbf{M}_{i-1} \mathbf{M}_{i-2} \cdots \mathbf{M}_0$ is the tangent linear model with $\mathbf{M}_i = \frac{\delta m_i(\mathbf{x}_i)}{\delta \mathbf{x}_i}$.

For DALEC the state \mathbf{x}_0 corresponds to the initial values of the five carbon pools, $\mathbf{x}_0 = (C_f(t_0), C_r(t_0), C_w(t_0), C_l(t_0), C_s(t_0))^T$. We can calculate the linearized model for DALEC as,

$$\mathbf{M}_i = \begin{pmatrix} (1 - p_5) + p_3(1 - p_2)\zeta_i & 0 & 0 & 0 & 0 \\ p_4(1 - p_3)(1 - p_2)\zeta_i & (1 - p_7) & 0 & 0 & 0 \\ (1 - p_4)(1 - p_3)(1 - p_2)\zeta_i & 0 & (1 - p_6) & 0 & 0 \\ p_5 & p_7 & 0 & (1 - (p_1 + p_8)T_i) & 0 \\ 0 & 0 & p_6 & p_1 T_i & (1 - p_9 T_i) \end{pmatrix}, \quad (7)$$

where $\zeta_i = \text{GPP}'(C_f(t_i), \phi)$ and $T_i = T(t_i)$. The cost function and gradient of the cost function were coded in Python along with the DALEC model. Meteorological driving data and observations for assimilation were initially taken from a young pine forest in Oregon. The analysis (\mathbf{x}_a) was found by passing the cost function and its gradient function along with \mathbf{x}_b to the Broyden-Fletcher-Goldfarb-Shanno minimization algorithm (BFGS) [?] found in the scipy.optimize package for Python. The results for the analysis when assimilating a years worth of NEE observations can be seen in figure 3.

In figure 3 we can see a better fit to the observations after assimilation of the NEE observations with the \mathbf{x}_a model trajectory. Assimilating the NEE data not only improves the fit of the model trajectory to the observations of NEE but also to the observations of GPP and total respiration (RT). This shows that by assimilating NEE observations we are also gaining information about GPP and RT. This is expected as NEE is a product of RT and GPP ($\text{NEE} = \text{RT} - \text{GPP}$) so improving the estimate of NEE should also improve the estimate of RT and GPP. We can also see how simple the DALEC model is in some areas by looking at its prediction of litter fall (LF) which is just modelled as a constant multiplied by C_f in this evergreen version of DALEC.

More experiments had been planned with DALEC in a 4D-Var scheme. However, with the release of DALECV2 [?] it was decided that it would be best to begin working with this new model. This new model DALECV2 can be parameterized for either deciduous or evergreen forests, whereas the DALEC being used for previous experiments only models evergreen forests. Parameterizing the model for a deciduous forest is important as the Forest Research site at Alice Holt forest is mainly deciduous and this is where I will be based for my field work.

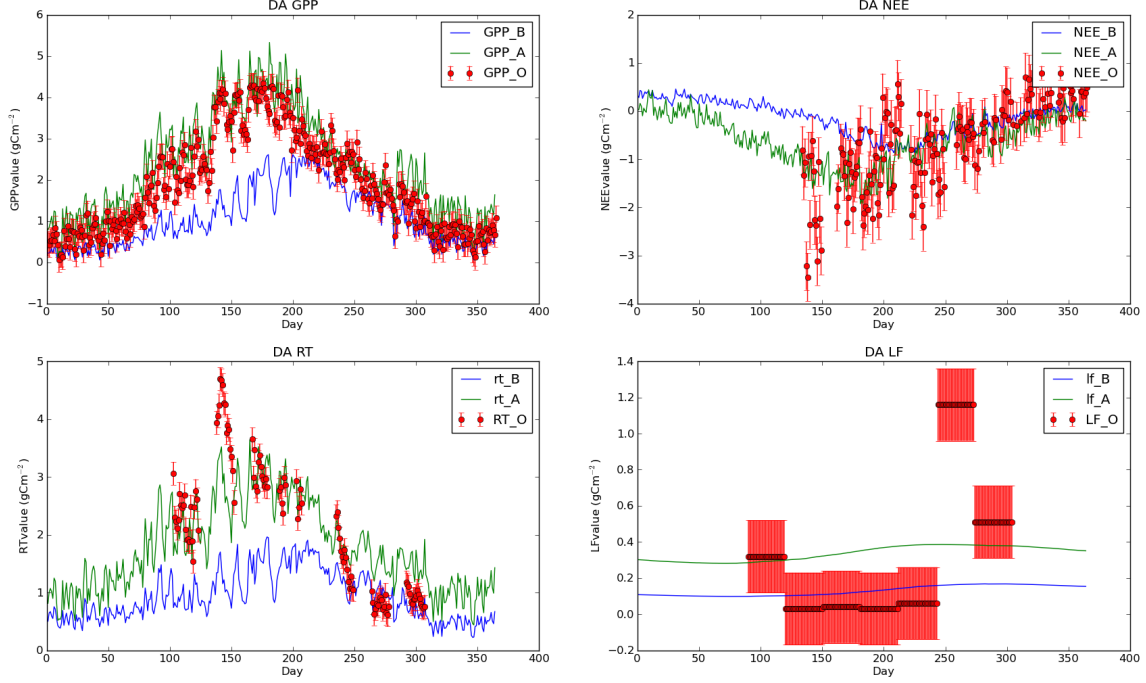


Figure 3: 4D-Var with DALEC assimilating observations of NEE over a year from Oregon pine stand. Here the blue line is the \mathbf{x}_b model trajectory, the green line is the \mathbf{x}_a model trajectory and the red dots are different forest carbon balance observations corresponding to GPP (top left), NEE (top right), total respiration (RT) (bottom left) and litter fall (LF) (bottom right).

4 Current Work

I am currently working on getting DALECV2 coded up with a 4D-Var scheme in Python, with a state made up of the initial carbon pool values and the 17 model parameters so that the model can be parameterized for the Alice Holt research site.

I have recently started working at Forest Research once a week on Tuesdays. I am currently helping out conducting stem and soil respiration measurements. The equipment used for the stem respiration measurements can be seen in figure 4. These measurements form part of an existing measurement campaign that Forest Research are conducting. The measurements of stem respiration may not be directly used in my own work. However, they are valuable for my understanding of conducting fieldwork measurements and learning my way around the Straits enclosure where the bulk of the carbon balance measurements are made at the Alice Holt site. I have received access to meteorological driving data and NEE observations from the Alice Holt flux tower and am converting this data into the correct format for use with DALECV2



Figure 4: Tree respiration chamber used at Alice Holt research site.

5 Future Plans

Parameterize DALECV2 for Alice Holt. Repeat information content experiments for DALECV2. Plan a measurement campaign based on information content experiments in order to better estimate poorly constrained DALECV2 parameters for Alice Holt research site.

6 Professional and Academic Development

6.1 Masters Courses

- MTMG49 (Boundary Layer) - 72%
- MTMD01 (Environmental Data Visualization) - 78%
- MTMD02 (Operational Data Assimilation) - 70%

6.2 Transferable Skills

During my PhD I have taken part in the following courses, workshops and activities:

- 28/01/2014 - Basic Statistics Refresher - RRDP
- 31/03/2014-01/04/2014 - Land Data Assimilation workshop at UCL - ESA
- 23/04/2014-25/03/2014 - Correlated Observation Errors in Data Assimilation Workshop - ESA
- 13/05/2014 - Social Media - Bloggs, Twitter and Your Online Presence - RRDP
- 29/05/2014 - How to Write a Paper - RRDP
- 25/06/2014-26/06/2014 - Software Carpentry Course - Git and Python
- 10/07/2014-11/07/2014 - Forest Research - Helped with field work LiDAR
- 21/07/2014-01/08/2014 - Fluxcourse Summer School - University of Colorado
- 29/09/2014-03/10/2014 - NERC course - Software Development for Environmental Scientists Level 1
- 08/10/2014-10/10/2014 - Environment YES - NERC "dragon's den" type competition at Syngenta, Jesops Hill
- 17/12/2014 - Presentation at Maths for Planet Earth Industry day
- 24/02/2015 - Reading Soil Centre Workshop - What can Land Surface Models do for you?
- 23/03/2015-27-03/2015 - NERC course - Software Development for Environmental Scientists Level 2

6.3 Demonstrating

During my PhD I have helped demonstrate on the following courses:

- 15/09/2014-19/09/2014 - NERC Data assimilation for environmental scientists training course
- 16/02/2015-20/02/2015 - NERC Software Development for Environmental Scientists Level 1
- 20/04/2015-23/04/2015 - MT26E Surface Energy Exchange Practicals

I have also demonstrated on the NERC 'Data assimilation and visualization for environmental sciences' training course held from 15/09/2014 to 19/09/2014 organised at the University of Reading.

On 17/12/14 I will be giving a presentation at the Mathematics for Planet Earth industry day at Imperial College about my project and working with a case partner.

6.4 Summer School

I attended the Fluxcourse summer school held at the University of Colorado from 21/07/2014 to 01/08/2014. During the course we stayed at the University's mountain research station near Boulder, Colorado. The course covered many different aspects of measuring and modelling the CO₂ flux of forests and plants. I found spending time with other early career scientists studying similar problems very helpful in the understanding of my own research topic. At the end of the course we had to present a piece of group work using a carbon balance model with a data assimilation scheme.