

Social fluidity mobilizes infectious disease in human and animal populations: supplementary information

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Contents

S1 Measuring social fluidity	1
S1.1 Mathematical model of social behavior	1
S1.2 Choosing ϵ	2
S1.3 Degree distribution	2
S1.4 Estimating ϕ in empirical data	2
S2 Modelling the spread of disease	3
S2.1 The number of secondary infections	3
S2.2 Calibration of time-scales	4
S2.3 Limit of R_0 as $N \rightarrow \infty$	4
S2.4 Simulating the spread of disease	4
S3 Sources of empirical data	5
S3.1 Human face-to-face interaction	5
S3.2 Ant trophallaxis	5
S3.3 Ant antennal Contact	5
S3.4 Bat food-sharing	5
S3.5 Vole territory sharing	5
S3.6 Mouse territory sharing	5
S3.7 Association by group membership	6
S3.8 Grooming	6
S3.9 Aggression and dominance	6

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S1 Measuring social fluidity

Our analysis concerns a closed system containing a set \mathcal{N} of N individuals who can interact with each other in some way. The model has only one tunable parameter which we call “social fluidity” and can be interpreted as both the heterogeneity of relationship strengths, and the level of mixing in the population. From the description of the model we derive, analytically, the expected value of the the observed number of interaction partners of an individual, d_i , as a function of the number of times they been observed in an interaction, s_i . By using maximum likelihood methods we are able to measure and compare social fluidity quantity across a wide range of data.

S1.1 Mathematical model of social behavior

We start by considering one focal individual i and its relationship to another individual j . Suppose that i is observed interacting with one other individual. We use $x_{j|i}$, for all $j \in \mathcal{N} \setminus \{i\}$, to denote the probability that the interaction will be with j .

If at least one interaction has been observed between i and j then we say that an edge exists between them. The probability that this is the case after i has been observed s_i times is

$$P(i \rightarrow j | s_i) = 1 - (1 - x_{j|i})^{s_i}. \quad (1)$$

We now introduce heterogeneity into the distribution of relationship strengths. We make no assumptions about the relationship between i and j other than that $x_{j|i}$ is drawn from some distribution $\rho(x)$. The probability that an edge exists between i and any node in the network after

s interactions is

$$\Psi(s) = 1 - \int \rho(x)(1-x)^s dx. \quad (2)$$

Letting d_i be the degree of i , the expectation is simply $\mathbb{E}(d_i) = (N-1)\psi(s_i)$. For a given distribution (ρ) of relationship strengths in a population we now have a formula that connects the number of interactions to the degree.

Our goal is to choose the distribution ρ that produces an accurate recreation of the behavior seen in real social systems. We therefore choose the truncated power law,

$$\rho(x) = \frac{\phi \epsilon^\phi}{1 - \epsilon^\phi} x^{-(1+\phi)} \text{ for } \epsilon < x < 1. \quad (3)$$

The reason for choosing a power law is that it allows the heterogeneity of the relationship strengths to be controlled by a single parameter ϕ making it adaptable to a wide variety of social systems. The distribution is truncated at ϵ so as not to include an asymptote at $x = 0$. It is truncated 1 to ensure that all values of $x_{j|i}$, which are probabilities, are less than 1.

S1.2 Choosing ϵ

The value of ϵ is determined by the choice of ϕ . To find ϵ , consider that interactions are pairwise; when i interacts, exactly one other individual is involved. Hence, the expectation of the sum of the $x_{j|i}$ ’s over all $j \in \mathcal{N} \setminus \{i\}$ is equal to 1. Another way to express this is

$$(N-1)\langle x \rangle = 1 \quad (4)$$

where $\langle x \rangle$ denotes the mean of the distribution $\rho(x)$, and is

$$\langle x \rangle = \frac{\phi \epsilon^\phi (1 - \epsilon^{1-\phi})}{(1 - \phi)(1 - \epsilon^\phi)}. \quad (5)$$

Combining Eq.(4) and Eq.(5) we find that the only possible choice of ϵ is the solution of

$$(A + 1)\epsilon^\phi - \epsilon - A = 0 \quad (6)$$

where $A = (1 - \phi)/(N - 1)\phi$.

S1.3 Degree distribution

Substituting Eq.(3) into Eq.(2) we have, for an individual that has had s interactions, that

$$\Psi(s) = 1 - \frac{\phi\epsilon^\phi}{1 - \epsilon^\phi} \int_\epsilon^1 x^{-(1+\phi)} (1 - x)^s dx. \quad (7)$$

This simplifies to

$$\Psi(s) = 1 - \frac{\phi\epsilon^\phi(1 - \epsilon)^{s+1}}{(1 - \epsilon^\phi)(s + 1)} {}_2F_1(s + 1, 1 + \phi, s + 2, 1 - \epsilon) \quad (8)$$

The notation ${}_2F_1$ refers to the Gauss hypergeometric function [1]. Recall that $\Psi(s_i)$ is the probability that an edge exists from i to j , for any $j \in \mathcal{N} \setminus \{i\}$, after i has been involved in s_i interactions. The existence of any edge is therefore determined by a Bernoulli trial independent of the existence of any other. After s interactions the degree of any node should therefore follow a binomial distribution $d(s) \sim B(N - 1, \Psi(s))$, however, this gives non-zero probabilities for cases where $d > s$. This only occurs for $0 < s < N$ so we replace the formula in this region with a binomial distribution with the same mean, $(N - 1)\Psi(s)$, but bounded by s . Thus

$$d_i(s) \sim \begin{cases} B\left(s, \frac{(N - 1)\Psi(s)}{s}\right) & \text{if } 0 < s < N \\ B(N - 1, \Psi(s)) & \text{if } s \geq N \end{cases} \quad (9)$$

S1.4 Estimating ϕ in empirical data

The model we have described is based on the assumption that the system is closed; over some sampling period the N individuals only interact with others from the same population. For each node i we need to know the number of time they interacted, s_i , and the number of others they interacted with, d_i . We write this as two vectors $\mathbf{d} = \{d_1, d_2, \dots, d_N\}$ and $\mathbf{s} = \{s_1, s_2, \dots, s_N\}$.

The family of distributions in Eq.(9) allow us to calculate $P(d|s)$, the probability that an individual will have degree d given that they have interacted s times, for any value of the global parameter ϕ . The log-likelihood function is

$$\log \mathcal{L}(\phi|\mathbf{d}, \mathbf{s}) = \sum_{i=1}^N \log[P(d_i|s_i)]. \quad (10)$$

We then compute the maximum likely estimate of ϕ , $\hat{\phi} = \text{argmax}_\phi \log \mathcal{L}(\phi|\mathbf{d}, \mathbf{s})$. Standard error SE_ϕ is calculated at 95% confidence intervals using $SE_\phi = 1.96/\sqrt{-N(\log \mathcal{L})''}$ where the derivatives of $\log \mathcal{L}$ are computed numerically. The standard error is a measure of confidence that our chosen ϕ is in fact the best choice. It does not tell us how well the model fits the data in the first place. To quantify this we introduce a measure of model fidelity.

To measure model fidelity we compare the likelihood of the proposed model it to a null model that represents the most random, i.e. uniformly distributed, possible degree distribution for each given t . The null model equivalent of Eq.(9) is

$$d(s) \sim \begin{cases} U(0, s) & \text{if } 0 < s < N \\ U(0, N - 1) & \text{if } s \geq N. \end{cases} \quad (11)$$

Model fidelity, f_ϕ , quantifies the amount to which the proposed model fits the data when compared to an equivalent

null model. We define it as

$$f_\phi = (1/N)[\log \mathcal{L}(\phi|\mathbf{d}, \mathbf{s}) - \log \mathcal{L}(\text{null}|\mathbf{d}, \mathbf{s})]. \quad (12)$$

Because we are using observed values of s_i this approach controls for fact activity levels may vary between data sets.

Finally, to find a benchmark to compare the model fidelity we measured f_ϕ for several synthetically generated data sets. These data were generated by first selecting 100 values of s between 1 and 100 uniformly at random, then, for each one we select a value of d either from the model distribution given by Eq.(9) or from the noise distribution given by Eq.(11) ($N = 100$ and $\phi = 0.6$). When less than 8% of the synthetic values of d come from the noise distribution, f_ϕ is positive. We conclude that positive values of f_ϕ found in any data-set implies that the model is a good fit to the data.

S2 Modelling the spread of disease

The disease model is described as follows: We consider a fully susceptible population of N individuals. At a randomly selected point in time, one individual, i , becomes infectious. They remain infectious for a duration of length τ , where τ is a random variable drawn from an exponential distribution $P(\tau) = \gamma \exp(-\gamma\tau)$. This is equivalent to i being able to recover at any point in time and γ being the probability that recovery occurs at any point during an interval of length 1. The times for which infected individual, i , engages in interaction follows a Poisson process with rate parameter a_i . Given that i is engaged in an interaction, the probability that the interaction is with individual j is $x_{j|i}$. Once contact is established, the probability that the disease will transmit is β .

S2.1 The number of secondary infections

We are interested in $r(a_i)$, the expected number of other individuals infected by i , given that the rate of interaction of i is a_i .

The transmission probability, the probability that i infects j during an infectious period of length τ , is equal to the probability that at i makes infectious contact with j at least once during that time. Since the rate of infectious contact between i and j follows a Poisson process with rate $a_i x_{j|i} \beta$, the transmission probability for an infectious period of length τ is derived from the Poisson distribution and is

$$T_{i \rightarrow j}(\tau, a_i, x_{j|i}) = 1 - \exp(-a_i x_{j|i} \beta \tau). \quad (13)$$

As in Section S1.1 we make no assumptions about the relationship between i and j other than that $x_{j|i}$ is drawn from the distribution given by Eq.(3). The probability that transmission occurs from i to any other node in the network is

$$\begin{aligned} T(\tau, a_i) &= \int_0^\infty \rho(x) T_{i \rightarrow j}(\tau, a_i, x) dx \\ &= 1 - \frac{\phi \epsilon^\phi}{1 - \epsilon^\phi} \int_\epsilon^1 x^{-(1+\phi)} \exp(a_i x_{j|i} \beta \tau) dx \quad (14) \\ &= 1 - \phi \sum_{k=0}^\infty \frac{(-a_i \beta \tau)^k}{(k - \phi) k!} \frac{\epsilon^\phi - \epsilon^k}{1 - \epsilon^\phi}. \end{aligned}$$

The probability that i was infectious for a period of duration τ is $\gamma \exp(-\gamma\tau)$. Integrating Eq.(14) across all possible values of τ we get

$$\begin{aligned} T(a_i) &= \int_0^\infty \gamma e^{-\gamma\tau} T_i(\tau, a_i) d\tau \\ &= 1 - \phi \sum_{k=0}^\infty \frac{(-a_i \beta / \gamma)^k}{k - \phi} \frac{\epsilon^\phi - \epsilon^k}{1 - \epsilon^\phi}. \end{aligned} \quad (15)$$

The quantity T is the probability that i will infect j for

Table S1: Summary of parameters and variables

Social behavior		Disease transmission	
N	Number of nodes	β	The probability of transmission given that contact has occurred
$\sum s_i/2$	The total number of interactions of all nodes	γ	Recovery rate of the disease model. Chosen so that the mean number of infectious contacts is the same across all data-sets Eq.(24)
ϕ	The mixing parameter. The optimal value calculated from the process described in Section S1.1	r_i	Mean individual reproduction number based on either Eq.(21) or disease simulation.
ϵ	The lower cut-off for the relationship strength distribution, Eq.(3)	SE_r	Standard error of the reproduction number based on disease simulation
SE_ϕ	The standard error of the estimate of ϕ	$ e $	Absolute error. Sum of the differences between r_i predicted by Eq.(21) and r_i simulated
f_ϕ	Model fidelity. Given by Eq.(12)		

any $j \in \mathcal{N} \setminus \{i\}$. To get the expected number of secondary infections that come from i we simply have to multiply by the number of susceptibles. We therefore have that

$$r(a_i) = (N - 1)T(a_i). \quad (16)$$

It is not possible to express $T_i(a_i)$ in terms of N so we instead express it in terms of ϵ . By substituting $N - 1 = 1/\langle x \rangle$ and Eq.(5) into Eq.(16) we get

$$\begin{aligned} r(a_i) &= \frac{T_i(a_i)}{\langle x \rangle} \\ &= \frac{1 - \phi}{\phi(\epsilon^\phi - \epsilon)} \left[1 - \epsilon^\phi - \phi \sum_{k=0}^{k=\infty} \frac{(-a_i\beta/\gamma)^k}{k - \phi} (\epsilon^\phi - \epsilon^k) \right] \end{aligned} \quad (17)$$

which can also be expressed using hypergeometric functions

$$\begin{aligned} r(a_i) &= \frac{1 - \phi}{\phi(\epsilon^\phi - \epsilon)} \left[1 - \epsilon^\phi + \epsilon^\phi {}_2F_1(-\phi, 1, 1 - \phi; -a_i\beta/\gamma) \right. \\ &\quad \left. - {}_2F_1(-\phi, 1, 1 - \phi; -\epsilon a_i\beta/\gamma) \right] \end{aligned} \quad (18)$$

S2.2 Calibration of time-scales

The collection of data-sets we compare is diverse and social activity happens on different time-scales. Addition-

ally, the type of diseases that affect one species is unlikely to affect another. Instead of choosing parameter values that relate to some specific disease, it is more informative to select parameter values for each system separately in a way that exposes the effects of population size and social fluidity. To achieve this the two temporal variables, γ and the mean activity rate, $\langle a_i \rangle$, are calibrated to each other in such a way that R_0 would always be the same value if, hypothetically, the effects of social fluidity and population size were not present.

We define R^* to be the value of R_0 in a large population with homogenous mixing. In this case, the infectious individual, i , will never repeat an interaction with an individual whom they previously infected. In other words, every interaction during the infectious period will, with probability β , cause a new infection, and so R^* can be found by multiplying the mean infectious period by β and the mean rate interactions,

$$R^* = \frac{\beta \langle a_i \rangle}{\gamma}. \quad (19)$$

By estimating the rate parameter a_i from the number of observed interactions s_i as $a_i = \frac{s_i}{\Delta_t}$ where Δ_t is the dura-

tion of the time-frame of the data, Eq.(19) becomes

$$\gamma = \frac{\beta \langle s \rangle}{\Delta_t R^*}, \quad (20)$$

where $\langle s \rangle$ is the mean of s_i over all individuals. Additionally, by substituting this value of gamma into Eq.(18) we get

$$r(s) = \frac{1 - \phi}{\phi(\epsilon^\phi - \epsilon)} \left[1 - \epsilon^\phi + \epsilon^\phi {}_2F_1(-\phi, 1, 1 - \phi; -R^*s/\langle s \rangle) - {}_2F_1(-\phi, 1, 1 - \phi; -\epsilon R^*s/\langle s \rangle) \right]. \quad (21)$$

Note that no temporal information appears in this equation. In all the analysis presented we have arbitrarily chosen $R^* = 2$.

S2.3 Limit of R_0 as $N \rightarrow \infty$

Noting that the taking the limit in Eq.(17) as $\epsilon \rightarrow 0$ is equivalent to $N \rightarrow \infty$ we can also say

$$\lim_{N \rightarrow \infty} r_i(a_i) = \frac{1 - \phi}{\phi} [-1 + {}_2F_1(-\phi, 1, 1 - \phi; -a_i\beta/\gamma)] \quad (22)$$

if $\phi < 1$ and

$$\lim_{N \rightarrow \infty} r_i(a_i) = a_i\beta/\gamma \quad (23)$$

if $\phi > 1$ (at $\phi = 1$, $\rho(x)$ is not defined). Arriving at this solution requires the use of L'Hopital's Rule.

S2.4 Simulating the spread of disease

Because the fidelity of the social behavior model, i.e. the extent to which it agrees with the data, varies across the different social settings, we expect that the predictions made in Section S2.1 are only applicable to a some of our data-sets. To test how accurate the prediction of Eq.(18) is, we simulated the effects of transmission on the real

contact data.

The collection of data-sets we are comparing is diverse, and social activity happens on dramatically different time-scales. To control for this variability the recovery rate γ is adjusted. We choose γ to be

$$\gamma = \frac{2\beta \sum t_i}{N\Delta_t s} \quad (24)$$

where Δ_t is the duration of the time-frame of the data. Eq.(24) is equivalent to choosing γ such that, if the system is well-mixed, then an individual with the mean rate of activity is expected to directly infect s others. In all the results presented we set $s = 2$.

For every individual, i , the simulated reproduction number r_i^{sim} is found by averaging the number of successful infections caused by i over 10^3 simulation trials. Each trial followed the following procedure:

1. A time τ is chosen randomly and uniformly between the beginning and end of the time-frame of the data
2. The length of infectious period Δ_I is generated from an exponential distribution with rate parameter γ
3. A list L of interactions that involved i between time τ and $\tau + \Delta_I$ is generated. If $\tau + \Delta_I$ is beyond the time-frame of the data then interactions from the beginning of the sampling time-frame are used in place of the missing data.
4. Each interaction in the set L is removed with probability $1 - \beta$ and r_i is the number of remaining individuals $j \in \mathcal{N} \setminus \{i\}$ that have interactions in L

This gives a reproduction number for every individual in the system. In Table S2 we provide the mean \bar{r} and standard error SE_r over the population.

Finally, to measure the accuracy of Eq.(18) we calculate the mean absolute error $|e|$. We first calculate the rate of activity $a_i = t_i/\Delta_t$ which, along with the associated values of N , phi , and ϵ , is used in Eq.(18) to compute r_i . The error is given by

$$|e| = \frac{1}{N} \sum_{i \in \mathcal{N}} |r_i - r_i^{\text{sim}}| \quad (25)$$

S3 Sources of empirical data

S3.1 Human face-to-face interaction

We use human contact data from the Sociopatterns project (sociopatterns.org). Participants wore radiofrequency identification sensors that detect face-to-face proximity of other participants within 1-1.5 meters in 20-second intervals. Each dataset lists the identities of the people in contact, as well as the 20-second interval of detection. The timing and duration of contacts are known with a resolution of 20-seconds. To exclude contacts detected while participants momentarily walked past one another, only contacts detected in at least two consecutive intervals are considered interactions.

The data we use comes from two studies: an academic conference which occurred over the course of 3 days [2], a primary school for which there are 2 days of data [3], a high school which spanned 5 days [4], and a hospital which spanned 4 full days [5]. In each case the data were divided into 24 hour subsets beginning at midnight.

S3.2 Ant trophallaxis

We collected data from three carpenter ant colonies (*Camponotus Pennsylvanicus*). In nature, carpenter ant foragers consume liquid food and, upon returning to the nest, regurgitate it into the mouths of their nest-mates, a pro-

cess known as trophallaxis. Typically, foragers will only give food to a small number of other ants; to feed the entire colony it gets passed through a complex network of feeding interactions [6]. Trophallaxis is also an important form of communication and a way that information about the state of the colony can be shared by all of its members [7, 8].

We placed colonies of approximately 80 ants in a nest designed to replicate the conditions found in nature. The colony was first given a restrictive area of $65 \times 42\text{mm}$ to live (high density) the ants were given several days to adjust before 4 hours of trophallaxis activity was recorded. The nest was then expanded by a factor of 4 (low density) and after another adjustment period another 4 hours were recorded. The process was repeated for 3 unrelated colonies.

S3.3 Ant antennal Contact

The antennae of ants contain highly sensitive olfactory cells. By touching the cuticle of another ant they are able to perceive information (primarily the status of the other ant) which is expressed through hydrocarbons secreted on their cuticle. We use data from [9] which was collected by constant human observation of video footage of ant colonies over a period of approximately 30 minutes. The experiment was performed on 3 unrelated *Temnothorax rugatulus* colonies, each of which was recorded in two sessions separated by a two week period.

S3.4 Bat food-sharing

Vampire bats share food with each other through regurgitation. In order to initiate such an event a hungry bat will lick the mouth of another bat from whom they hope to receive food. The data we use is a record of mouth-licking

observations originally collected to address questions of altruism and reciprocity in bat communities [10,11].

A population of vampire bats (*Desmodus rotundus*) were kept captive in an enclosure. Out of the 25 bats, 20 were subjected to experimental treatment. In each case, the subject was removed from the enclosure and starved for 24 hours. The observation period of 2 hours began when the starved bat was let back into the enclosure and during this time the usual sources of food were not available. Thus, for the subject bat to feed, interaction with others was necessary. The starvation treatment and observations occurred on a different day for each bat. Some bats were tested more than once so to avoid biasing our results we select only the first day they were tested.

S3.5 Vole territory sharing

Data were collected from a population of wild voles (*Microtus agrestis*) to assess the role of space in determining the structure of social networks [12]. [Sentence about vole behavior and what an interaction is].

In each of four field sites 100 traps were placed in a square grid covering 0.3 hectares. Bait was put into the traps and then three days later observers would check the traps for voles, those who were found were tagged so that they could be recognized should they be caught again. During each trapping session the traps were checked on several consecutive days. If a vole is observed in a trap at any point during a trapping session then we say that they interacted with any other vole that was observed in the same trap at any point during the same trapping session. The time of the interaction is the day that the trapping session began.

We then discard any voles that had 10 or less interactions and all interactions in which they participated. Since

the voles have a very short lifespan and cyclic fluctuations in population size we use only a sub-sample of each dataset. We chose periods of 130 days selected at times of high activity for each of the four experiment sites.

S3.6 Mouse territory sharing

Mice *Mastomys natalensis* [13] were kept in a large enclosed space that contained nine evenly spaced feeding stations. Four of nine feeding stations had sensors that recorded the moment when a mouse passed through its door.

If two mice pass through within 30 minutes of each other then we regard this as a territory sharing interaction comparable to the Vole data (in the source paper the authors used a 30 second threshold). The experiment was repeated with varying densities of mice, at low densities the very little interaction occurs so we use only the highest density treatments (enclosure C and enclosure D during the last 5 days).

S3.7 Association by group membership

Since foraging groups and social groups can change from one day to the next, a commonly way to measure the strength of a pairwise relationship is to consider the number of times that the pair were observed in the same group. In most studies of this kind the data is processed in a way that attempts to correct for observation bias and group size heterogeneity, which makes it incompatible for our method of analysis. We were, however, able to use 3 experiments from which the raw data is available. These are kangaroos *Macropus giganteus* [14], barn swallow *Hirundo rustica erythrogaster* [15], and howler monkeys *Alouatta palliata* [16]. The data from each of these papers were collected through intermittent, rather than continuous, ob-

servation. We define an interaction as belonging to the same group during one round of observation.

S3.8 Grooming

Grooming in monkeys, and other primates, is used to build and social bonds, avoid conflict, and maintain social structures including the dominance hierarchy. We used grooming data from two studies of macaques *Macaca mulatta* [17, 18] and one of stumptailed macaques *Macaca arctoides* [19]. Data were collected intermittently rather than through continuous observation. If one animal was grooming another during one round of observations then this would be recorded as a directed interaction. For our analysis we neglect the direction of the interaction (it is unclear whether the direction would have consequences relevant to the spread of disease).

S3.9 Aggression and dominance

Aggression between animals can be in the form of a physical fight or a display of dominance that causes one individual to concede. From the literature we obtained aggression data from macaques *Macaca fuscata fuscata* [20], female bighorn sheep *Ovis canadensis* [21], bison *Bison bison* [22], cattle [23], and parakeets *Myiopsitta monachus* [24]. The data from each of these papers were collected during intermittent observation periods. When an animal was determined to be the winner of a dominance encounter then this would be recorded as a directed interaction between the winner and the loser. For our analysis we neglect the direction of the interaction (it is unclear whether the direction would have consequences relevant to the spread of disease).

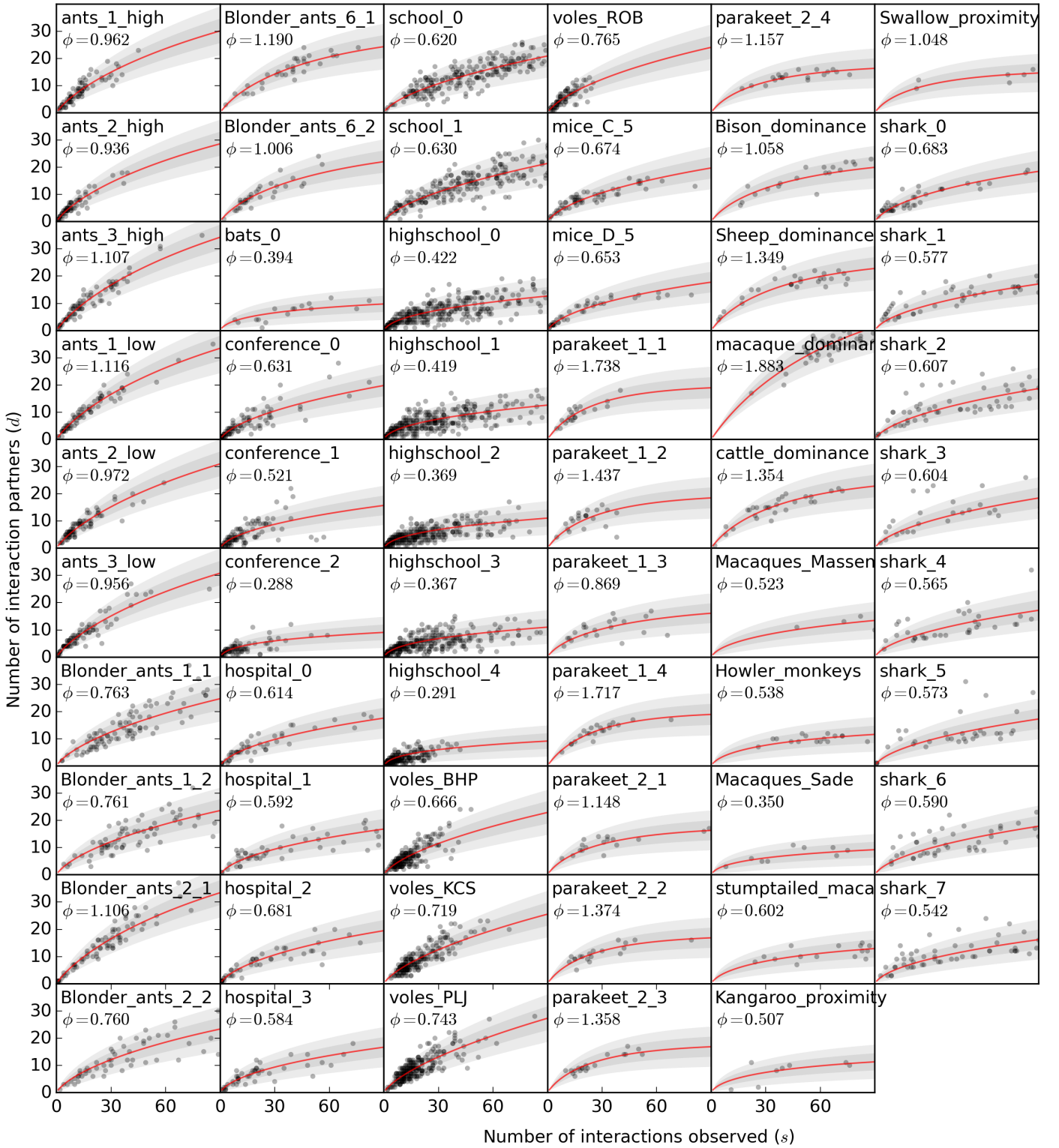


Figure S1: Every data-set used in our analysis as detailed in Section S3. Each point represents one individual in the system. In each case, the mixing parameter ϕ has been tuned to maximize the likelihood of the model using the process described in Section S1.4. The optimal ϕ is given and the curve shows the mean degree of an individual as a function of the number of interactions. The shaded area and the lighter shaded area represent intervals that are one and two standard deviations from the mean respectively. Data points for which the number of interactions is more than 90 are excluded from the figure but not from the inference of ϕ . [Reference the formulas that are in the text].

Table S2: A description of each row header is given in Table S1

Data set	System	Interaction	N	$\sum s_i/2$	$\sum d_i/2$	σ_w^2/\bar{w}	ϕ	$\epsilon \times 10^3$	f_ϕ	R_0 (Pre.)	$\gamma \times 10^4$	R_0 (Sim.)	Error
conference_0	Conference	Face-to-face	93	663	262	5.946	0.631	0.356	0.221	1.254	0.206	1.178	0.192
conference_1	Conference	Face-to-face	92	650	239	6.306	0.521	0.150	0.016	1.234	0.204	1.149	0.258
conference_2	Conference	Face-to-face	84	477	134	9.790	0.288	0.005	0.424	1.054	0.164	0.879	0.215
hospital_0	Hospital	Face-to-face	51	778	213	12.225	0.614	0.878	0.769	1.223	0.441	1.142	0.130
hospital_1	Hospital	Face-to-face	49	1075	250	12.201	0.592	0.825	0.845	1.239	0.635	1.142	0.165
hospital_2	Hospital	Face-to-face	51	855	242	8.849	0.681	1.244	0.803	1.279	0.485	1.253	0.123
hospital_3	Hospital	Face-to-face	50	743	198	12.585	0.584	0.759	0.713	1.213	0.430	1.141	0.136
school_0	Primary school	Face-to-face	237	6420	1744	9.267	0.620	0.070	1.245	1.378	0.784	1.299	0.142
school_1	Primary school	Face-to-face	238	6514	1769	9.367	0.630	0.076	1.148	1.368	0.792	1.288	0.146
highschool_0	High school	Face-to-face	312	4919	1058	15.620	0.422	0.003	0.830	1.175	0.456	0.990	0.228
highschool_1	High school	Face-to-face	311	4419	997	14.894	0.419	0.002	0.685	1.167	0.411	0.982	0.228
highschool_2	High school	Face-to-face	299	3415	746	13.011	0.369	0.001	0.765	1.129	0.330	0.953	0.222
highschool_3	High school	Face-to-face	294	3331	732	13.483	0.367	0.001	0.669	1.130	0.328	0.954	0.229
highschool_4	High school	Face-to-face	233	1084	316	7.154	0.291	0.000	0.345	1.073	0.135	0.833	0.252
ants_1_high	Ant	Food sharing	74	496	293	2.401	0.962	2.030	0.450	1.556	1.164	1.506	0.138
ants_2_high	Ant	Food sharing	68	318	196	2.282	0.936	2.105	0.427	1.506	0.812	1.325	0.187
ants_3_high	Ant	Food sharing	76	674	399	2.351	1.107	2.752	0.655	1.615	1.540	1.599	0.123
ants_1_low	Ant	Food sharing	70	606	356	2.277	1.116	3.075	0.782	1.606	1.503	1.611	0.100
ants_2_low	Ant	Food sharing	79	547	324	2.731	0.972	1.926	0.626	1.561	1.202	1.494	0.115
ants_3_low	Ant	Food sharing	82	610	342	2.695	0.956	1.763	0.548	1.525	1.291	1.492	0.117
Blonder_ants_1_1	Ant	Antennal contact	89	1834	649	4.756	0.763	0.794	0.806	1.461	35.825	1.539	0.157
Blonder_ants_1_2	Ant	Antennal contact	72	1721	556	5.516	0.761	1.065	0.763	1.450	34.166	1.538	0.135
Blonder_ants_2_1	Ant	Antennal contact	71	943	505	2.391	1.106	2.970	0.825	1.631	23.091	1.700	0.107
Blonder_ants_2_2	Ant	Antennal contact	69	1880	549	5.644	0.760	1.124	0.810	1.416	37.926	1.534	0.174
Blonder_ants_6_1	Ant	Antennal contact	33	647	258	2.467	1.190	8.320	1.105	1.604	25.555	1.716	0.117
Blonder_ants_6_2	Ant	Antennal contact	32	362	162	2.458	1.006	6.407	0.751	1.516	16.115	1.602	0.122
bats_0	Bat	Food sharing	16	290	54	9.236	0.427	3.105	0.640	1.228	6.380	1.077	0.344
voles_BHP	Vole	Territorial	195	1339	640	3.332	0.666	0.141	0.368	1.412	132.051	1.374	0.166
voles_KCS	Vole	Territorial	193	1874	865	3.236	0.719	0.206	0.632	1.459	186.728	1.498	0.148
voles_PLJ	Vole	Territorial	233	2126	1048	2.991	0.743	0.183	0.448	1.476	175.470	1.519	0.145
voles ROB	Vole	Territorial	77	381	214	2.613	0.765	0.982	0.243	1.454	95.155	1.291	0.179
mice_C_5	Mouse	Territorial	57	665	242	4.075	0.674	1.008	0.957	1.354	0.125	1.219	0.188
mice_D_5	Mouse	Territorial	41	404	138	4.587	0.653	1.550	0.800	1.251	0.105	1.336	0.136
parakeet_1_1	Parakeet	Aggression	21	175	98	0.742	1.738	22.574	0.738	1.671	nan	nan	nan
parakeet_1_2	Parakeet	Aggression	21	222	110	2.826	1.437	18.361	0.061	1.619	nan	nan	nan
parakeet_1_3	Parakeet	Aggression	21	325	107	5.518	0.869	8.568	0.268	1.446	nan	nan	nan
parakeet_1_4	Parakeet	Aggression	21	291	131	1.573	1.717	22.304	1.151	1.675	nan	nan	nan
parakeet_2_1	Parakeet	Aggression	19	399	113	7.737	1.148	15.418	0.878	1.532	nan	nan	nan
parakeet_2_2	Parakeet	Aggression	19	273	105	1.931	1.374	19.537	0.957	1.593	nan	nan	nan
parakeet_2_3	Parakeet	Aggression	19	247	99	1.552	1.358	19.266	1.032	1.588	nan	nan	nan
parakeet_2_4	Parakeet	Aggression	19	441	126	2.267	1.157	15.592	1.204	1.551	nan	nan	nan
Bison_dominance	Bison	Aggression	26	897	222	2.467	1.058	9.130	0.884	1.546	nan	nan	nan
Sheep_dominance	Sheep	Aggression	28	658	235	1.806	1.349	12.166	0.940	1.649	nan	nan	nan
cattle_dominance	Cattle	Aggression	28	498	205	1.544	1.354	12.230	0.946	1.647	nan	nan	nan
macaque_dominance	Monkey	Aggression	62	2435	1167	0.908	1.883	7.795	1.442	1.860	nan	nan	nan
Macaques_Massen	Monkey	Grooming	28	2025	228	15.949	0.523	1.573	1.913	1.320	nan	nan	nan
Macaques_Sade	Monkey	Grooming	16	647	69	10.074	0.350	1.917	0.912	1.208	nan	nan	nan
stumptailed_macaque	Monkey	Grooming	19	742	113	5.351	0.602	4.776	0.958	1.344	nan	nan	nan
Howler_monkeys	Monkey	Association	17	502	85	2.135	0.538	4.605	1.009	1.321	nan	nan	nan
Kangaroo_proximity	Kangaroo	Association	17	1161	91	12.532	0.507	4.030	1.247	1.245	nan	nan	nan
Swallow_proximity	Swallow	Association	17	886	122	6.808	1.048	15.619	1.578	1.505	nan	nan	nan

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