

#### 1. Training RNNs

big corpus of text -> feed into RNN-LM; for every step t -> Loss function/cross entropy -> Average of overall loss

$$J^{(t)}(\theta) = CE(\boldsymbol{y}^{(t)}, \hat{\boldsymbol{y}}^{(t)}) = -\sum_{w \in V} \boldsymbol{y}_w^{(t)} \log \hat{\boldsymbol{y}}_w^{(t)} = -\log \hat{\boldsymbol{y}}_{x_{t+1}}^{(t)}$$

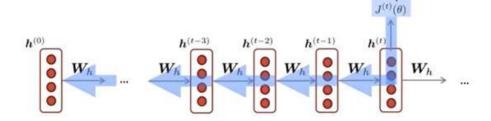
$$J(\theta) = \frac{1}{T} \sum_{t=1}^T J^{(t)}(\theta) = \frac{1}{T} \sum_{t=1}^T -\log \hat{\boldsymbol{y}}_{x_{t+1}}^{(t)}$$

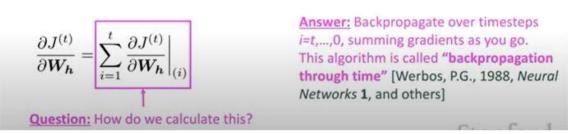
$$\downarrow^{\text{Coss}} \xrightarrow{J^{(1)}(\theta)} \stackrel{J^{(2)}(\theta)}{\uparrow} \stackrel{J^{(3)}(\theta)}{\uparrow} \stackrel{J^{(4)}(\theta)}{\uparrow} \stackrel{\text{Corpus}}{\downarrow} \stackrel{\text{$$

#### 2. Uses of RNNs

# **Backpropagation for RNNs**







- => gernerating text with RNN(repeated sampling) eg. Harry Potter, recipes,
- Evaluating
- · The standard evaluation metric for Language Models is perplexity.

$$\text{perplexity} = \prod_{t=1}^{T} \left( \frac{1}{P_{\text{LM}}(\boldsymbol{x}^{(t+1)}|\ \boldsymbol{x}^{(t)},\dots,\boldsymbol{x}^{(1)})} \right)^{1/T} \\ \text{Normalized by number of words}$$
 Inverse probability of corpus, according to Language Model

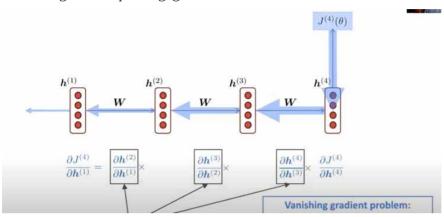
• This is equal to the exponential of the cross-entropy loss  $J(\theta)$ :

$$= \prod_{t=1}^{T} \left( \frac{1}{\hat{y}_{x_{t+1}}^{(t)}} \right)^{1/T} = \exp \left( \frac{1}{T} \sum_{t=1}^{T} -\log \hat{y}_{x_{t+1}}^{(t)} \right) = \exp(J(\theta))$$

sequence tagging, sentiment classification, language encoder module, generating text ...

#### 3. Problems with RNNs

Vanishing and exploding gradients



Vanishing gradient proof sketch

• Recall: 
$$\boldsymbol{h}^{(t)} = \sigma \left( \boldsymbol{W}_h \boldsymbol{h}^{(t-1)} + \boldsymbol{W}_x \boldsymbol{x}^{(t)} + \boldsymbol{b}_1 \right)$$

• What if  $\sigma$  were the identity function,  $\sigma(x)=x$  ?

$$rac{\partial m{h}^{(t)}}{\partial m{h}^{(t-1)}} = \mathrm{diag}\left(\sigma'\left(m{W}_hm{h}^{(t-1)} + m{W}_xm{x}^{(t)} + m{b}_1
ight)\right)m{W}_h \qquad ext{(chain rule)}$$
 $= m{I} \ m{W}_h = m{W}_h$ 

• Consider the gradient of the loss  $J^{(i)}(\theta)$  on step i, with respect to the hidden state  ${m h}^{(j)}$  on some previous step j. Let  $\ell=i-j$ 

$$\begin{split} \frac{\partial J^{(i)}(\theta)}{\partial \boldsymbol{h}^{(j)}} &= \frac{\partial J^{(i)}(\theta)}{\partial \boldsymbol{h}^{(i)}} \prod_{j < t \leq i} \frac{\partial \boldsymbol{h}^{(t)}}{\partial \boldsymbol{h}^{(t-1)}} & \text{(chain rule)} \\ &= \frac{\partial J^{(i)}(\theta)}{\partial \boldsymbol{h}^{(i)}} \prod_{j < t \leq i} \boldsymbol{W}_h = \frac{\partial J^{(i)}(\theta)}{\partial \boldsymbol{h}^{(i)}} \boldsymbol{W}_h^{\ell} & \text{(value of } \frac{\partial \boldsymbol{h}^{(i)}}{\partial \boldsymbol{h}^{(t-1)}} \text{)} \\ & \text{If } \boldsymbol{W}_h \text{ is "small", then this term gets} \\ & \text{exponentially problematic as } \ell \text{ becomes large.} \end{split}$$





Gradient signal from far away is lost because it's much smaller than gradient signal from close-by.

So, model weights are updated only with respect to near effects, not long-term effects.

#### 4. LSTMs

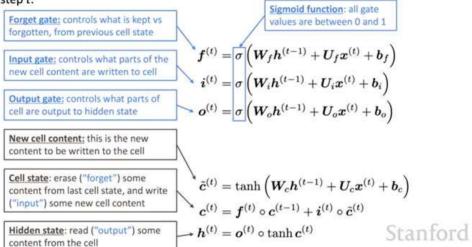
A type of RNN propsed as a solution to the vanishing gradients problem

- On step t, there is a hidden state  $oldsymbol{h}^{(t)}$  and a cell state  $oldsymbol{c}^{(t)}$ 
  - · Both are vectors length n
  - · The cell stores long-term information
  - . The LSTM can read, erase, and write information from the cell
    - . The cell becomes conceptually rather like RAM in a computer

### Long Short-Term Memory (LSTM)



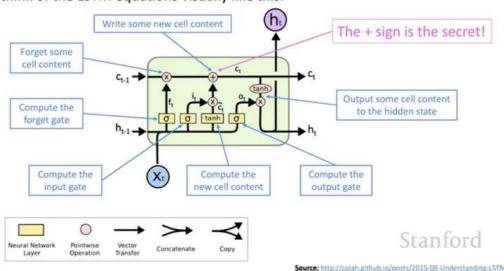
We have a sequence of inputs  $x^{(t)}$ , and we will compute a sequence of hidden states  $h^{(t)}$  and cell states  $c^{(t)}$ . On timestep t:



## Long Short-Term Memory (LSTM)



You can think of the LSTM equations visually like this:



45

5. bidirectional RNNs and multi-layer RNNs

### Task: Sentiment Classification

