
profiles_extrapolation

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1 Extrapolation of a standard plasma profiles in tokamaks

This notebook allows the extrapolation of electron density and temperature profiles

$$n_e = n_e(\rho), \quad T_e = T_e(\rho)$$

where $\rho = \sqrt{\psi}$ and ψ is the normalized poloidal flux. Generally, the profiles are given as an arrays

$$n_{e,i} = n_e(\rho_i), \quad T_{e,j} = T_e(\rho_j),$$

over (possibly different uniform grid $\rho_i = \rho_{\text{off},n} + ih$ for $i \in \{0, \dots, N\}$, $h > 0$, and $\rho_j = \rho_{\text{off},T} + jk$ for $j \in \{0, \dots, M\}$, $k > 0$, with possible offsets $\rho_{\text{off},n}, \rho_{\text{off},T} \geq 0$).

Such profiles are extended from the point with indices $i_{\text{start}} \leq N$ and $j_{\text{start}} \leq M$ up to the given common value ρ_{max} of the poloidal flux coordinate. This implies that the profiles are replated by model functions in the range $\rho > \rho_{i_{\text{start}}}$ and $\rho > \rho_{j_{\text{start}}}$, respectively, and thus the indices i_{start} and j_{start} must be large enough for the data in the plasma core to be unchanged.

Usage:

The user should change the input file name and the parameters below as appropriate and run the whole notebook. Plots are meant to give an indication about the quality of the result.

2 Read data and preliminary definitions

First the density profile is read from the file 'ne.dat' and the temperature profile from 'Te.dat'. The data format for the density is the standard format used by the TORBEAM code, namely, an ASCII file with

N

$\rho_0 \ n_{e,0}$

$\rho_1 \ n_{e,1}$

...

$\rho_{N-1} \ n_{e,N-1}$

and analogously for the electron temperature. The first line is skipped when data are loaded by the numpy function `loadtxt`.

```

In [1]: # Working directory (must contain the original data files)
        working_dir = '/home/omaj/Codes/WKBeam/WKBEAM/StandardCases/AUG30907_0_72/input/origin

In [2]: # Import statements
        from pylab import *
        import math
        from scipy.optimize import curve_fit

        %matplotlib inline

In [3]: # Load density data
        data_ne = loadtxt(working_dir + '/ne.dat', skiprows=1)
        rho_ne = data_ne[:,0]
        Ne = data_ne[:,1]
        # Load temperature data
        data_Te = loadtxt(working_dir + '/Te.dat', skiprows=1)
        rho_Te = data_Te[:,0]
        Te = data_Te[:,1]

```

It is expected that ρ_i is given in strictly increasing order, i.e., $\rho_i < \rho_j$ for indices $i < j$. It may happen that this is not the case. Then the data are flipped.

```

In [4]: # Check the order of the radial coordinate and flip the data if needed.
        # ... general function ...
        def flip_data(rho, data):
            """ Check if the order of the data is ok, and, if not, flip the data
                appropriately. """
            if rho[0] > rho[1]:
                flipped_rho = flipud(rho)
                flipped_data = flipud(data)
                return flipped_rho, flipped_data
            else:
                return rho, data
        # ... density data ...
        rho_ne, Ne = flip_data(rho_ne, Ne)
        # ... temperature data ...
        rho_Te, Te = flip_data(rho_Te, Te)

```

3 Fitting function

For both density and temperature profiles the data on the outer part of profiles are fitted to the model

$$F_{a,b,c,d}(\rho) = a \left(\frac{1}{2} - \frac{1}{\pi} \arctan\left(\frac{\rho - c}{b}\right) \right) \begin{cases} \exp\left(-(\rho - c)^2/d^2\right), & \text{for } \rho > c, \\ 1, & \text{for } \rho \leq c, \end{cases}$$

where $a, b, c, d \in \mathbb{R}$ are parameters of the fit, for which `curve_fit` from `scipy.interpolate` is used.

```

In [5]: # Fit function
        def func(x,a,b,c,d):
            result = empty([x.size])
            for i in range(0,x.size):
                if x[i] > c:
                    result[i] = (0.5 - math.atan((x[i]-c)/b) / math.pi)*a*\
                                math.exp(-(x[i]-c)**2 / d**2)
                else:
                    result[i] = (0.5 - math.atan((x[i]-c)/b) / math.pi)*a
            return result

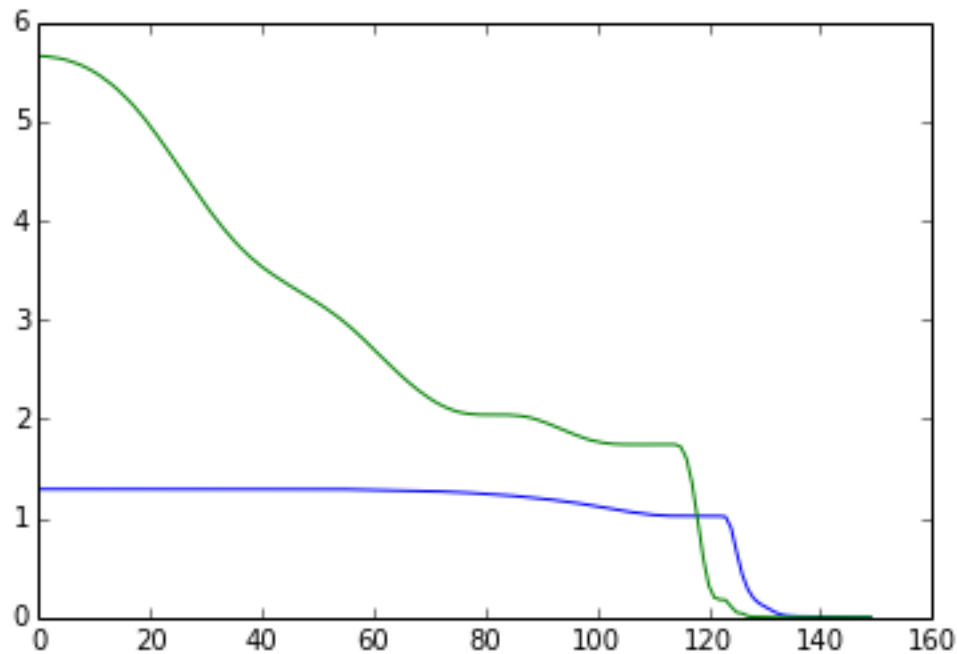
```

3.1 Set parameters

In this section, the parameter for the extrapolation should be defined. Before setting the parameters, one should check the data array.

```
In [6]: # Plot data arrays vs their index, not the physical coordinate
figure(0)
# ... density ...
plot(Ne)
plot(Te)
[<matplotlib.lines.Line2D at 0x7f3a53abe198>]
```

Out [6]:



```
In [7]: # Parameters for the density profile
IndexIstart = 125
IndexIstop = rho_ne.size
fit_parameter_seed_ne = [10., 0.03, 1., 0.2]
# Parameters for the temperature profile
IndexJstart = 115
IndexJstop = rho_Te.size
fit_parameter_seed_Te = [10., 0.03, 1., 0.2]
# Common parameters
rho_max = 1.9
nmbrAdditionalPoints = 200
```

4 Perform the calculations

For both the density and temperature profiles the following operations are performed:

1. Fit the model $F_{a,b,c,d}(\rho)$ to the desired slice of data. This gives the values of the fit parameters a, b, c, d .
2. Extend the data by appending additional point after the start indices i_{start} and j_{start} .

```
In [8]: # --- Extend Denisty ---
# Best fit for the density
p_ne, info = curve_fit(func,
```

```

        rho_ne[IndexIstart:IndexIstop],
        Ne[IndexIstart:IndexIstop],
        fit_parameter_seed_ne)

# Extrapolated points for the density
rho_ne_cut = rho_ne[0:IndexIstart-1]
Ne_cut = Ne[0:IndexIstart-1]
rho_ne_new = linspace(rho_ne[IndexIstart], rho_max, nmbrAdditionalPoints)
Ne_new = func(rho_ne_new, p_ne[0], p_ne[1], p_ne[2], p_ne[3])

# Combine unchanged data with the extrapolated profile
rho_ne_extended = append(rho_ne_cut, rho_ne_new, axis=0)
Ne_extended = append(Ne_cut, Ne_new, axis=0)

# --- Extend Temperature ---

# Best fit for the density
p_Te, info = curve_fit(func,
                        rho_Te[IndexJstart:IndexJstop],
                        Te[IndexJstart:IndexJstop],
                        fit_parameter_seed_Te)

# Extrapolated points for the density
rho_Te_cut = rho_Te[0:IndexJstart-1]
Te_cut = Te[0:IndexJstart-1]
rho_Te_new = linspace(rho_Te[IndexJstart], rho_max, nmbrAdditionalPoints)
Te_new = func(rho_Te_new, p_Te[0], p_Te[1], p_Te[2], p_Te[3])

# Combine unchanged data with the extrapolated profile
rho_Te_extended = append(rho_Te_cut, rho_Te_new, axis=0)
Te_extended = append(Te_cut, Te_new, axis=0)

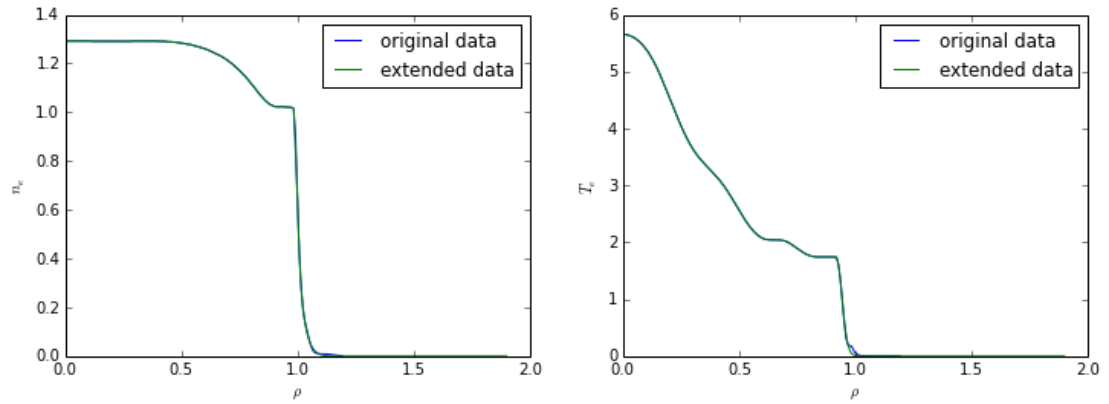
```

Plots of the original and extrapolated profiles

```

In [9]: figure(1, figsize=(12,4))
# Density
subplot(121)
plot(rho_ne, Ne);
plot(rho_ne_extended, Ne_extended);
xlabel(r'$\rho$')
ylabel(r'$n_e$')
legend(('original data', 'extended data'));
# Temperature
subplot(122)
plot(rho_Te, Te);
plot(rho_Te_extended, Te_extended);
xlabel(r'$\rho$')
ylabel(r'$T_e$')
legend(('original data', 'extended data'));

```



Save data in the appropriate format

When the user is satisfied with the quality of the extrapolation, here the extrapolated data can be saved in the TORBEAM format described above.

```
In [10]: # Output files
Ne_filename = working_dir + '/ne.dat.extended'
Te_filename = working_dir + '/Te.dat.extended'

# Open output files
Ne_file = open(Ne_filename, 'ab')
Te_file = open(Te_filename, 'ab')

# Export the data
data = array([rho_ne_extended, Ne_extended])
savetxt(Ne_file, array([rho_ne_extended.size, dtype=int]))
savetxt(Ne_file, data.T)
#
data = array([rho_Te_extended, Te_extended])
savetxt(Te_file, array([rho_Te_extended.size, dtype=int]))
savetxt(Te_file, data.T)

# Close files
Ne_file.close()
Te_file.close()
```

End of notebook.