Programming Languages CSCI-GA.2110.001 Fall 2021

Homework 2 Due Sunday, December 19 at 11:55pm

You should write the answers using word, latex, etc., and upload them as a PDF document. Important: You <u>must</u> turn this in by 11:55pm on December 19. I will be posting the solutions shortly after.

- 1. (a) In ML, why do all lists have to be homogeneous (i.e. all elements of a list must be of the same type)?
 - (b) Write a function in ML whose type is:

(c) What is the type of the following function (try to answer without running the ML system)?

```
fun foo (op <) f g (x,y) z = if f(x,y) < g x then z + 1 else z - 1
```

- (d) Provide an intuitive explanation of how the ML type inferencer would infer the type that you gave as the answer to the previous question.
- 2. (a) In the λ -calculus, give an example of an expression which would reduce to normal form under normal-order evaluation, but not under applicative-order evaluation.
 - (b) Write the definition of a recursive function (other than factorial, which I did in class) using the Y combinator. Show a series of reductions of an expression involving that function which illustrates how it is, in fact, recursive (as I did in class for factorial).
 - (c) Write the actual expression in the λ -calculus representing the Y combinator, and show that it satisfies the property $Y(f) \Leftrightarrow f(Y(f))$.
 - (d) Summarize, in your own words, what the two Church-Rosser theorems state.
- 3. (a) As discussed in class, what are the three features that a language must have in order to considered object oriented?
 - (b) What is the "subset interpretation of suptyping"?
 - (c) Provide an intuitive answer, and give an example, showing why class derivation in Java satisfies the subset interpretation of subtyping.
 - (d) Provide an intuitive answer, and give an example (in code), showing why subtyping of functions, in languages (such as Scala) that allow it, satisfies the subset interpretation of subtyping.
- 4. In Java generics, subtyping on instances of generic classes is invariant. That is, two different instances C<A> and C of a generic class C have no subtyping relationship, regardless of a subtyping relationship between A and B (unless, of course, A and B are the same class).
 - (a) Write a function (method) in Java that illustrates why, even if B is a subtype of A, C should not be a subtype of C<A>. That is, write some Java code that, if the compiler allowed such covariant subtyping among instances of a generic class, would result in a run-time type error.

- (b) Modify the code you wrote for the above question that illustrates how Java allows a form of polymorphism among instances of generic classes, without allowing subtyping. That is, make the function you wrote above be able to be called with many different instances of a generic class.
- 5. (a) Consider the following Scala definition of a tree type, where each node contains a value.

```
abstract class Tree[T <: Ordered[T]]
case class Node[T <: Ordered[T]](v:T, 1:Tree[T], r:Tree[T]) extends Tree[T]
case class Leaf[T <: Ordered[T]](v:T) extends Tree[T]</pre>
```

Ordered is a built-in trait in Scala (see

http://www.scala-lang.org/api/current/index.html#scala.math.Ordered). Write a Scala function minTree that takes a Tree[T], for any ordered T, and returns the minimum value in the tree. Be sure to use good Scala programming style.

- (b) i. In Scala, write a generic class definition that supports covariant subtyping among instances of the class. For example, define a generic class C[E] such that if class B is a subtype of class A, then C[B] is a subtype of C[A].
 - ii. Give an example of the use of your generic class.
- (c) i. In Scala, write a generic class definition that supports contravariant subtyping among instances of the class. For example, define a generic class C[E] such that if class B is a subtype of class A, then C[A] is a subtype of C[B].
 - ii. Give an example of the use of your generic class.
- 6. (a) What is the advantage of a mark-and-sweep garbage collector over a reference counting collector?
 - (b) What is the advantage of a copying garbage collector over a mark and sweep garbage collector?
 - (c) Write a brief description of generational copying garbage collection.
 - (d) Write, in the language of your choice, the procedure delete(x) in a reference counting GC system, where x is a pointer to a structure (e.g. object, struct, etc.) and delete(x) reclaims the structure that x points to. Assume that there is a free list of available blocks and addToFreeList(x) puts the structure that x points to onto the free list.