

1 极限篇

- (1) $\cos\alpha$ (2) e^3 (3) $\frac{1}{2}$ (4) $\frac{1}{2}$ (5) $(abc)^{\frac{1}{3}}$ (6)-50 (7)1 (8) $-\frac{1}{6}$
 (9) $-\frac{e}{2}$ (10) $\ln 2$ (11) $\frac{1}{2}$ (12)3 (13)2 (14)e (15) $-\frac{1}{2x}$ (16) $\frac{3}{2}$
 (17) $\frac{1}{6}$ (18)24 (19)1 (20)0 (21)1 (22) $-\frac{e}{2}$

2 积分篇

- (1) $\frac{(\ln \tan x)^2}{2} + C$ (2) $-\frac{1}{24} \sin 2x + \frac{1}{4} \sin 2x + C$ (3) $\frac{1}{3} \ln \left| \frac{x-2}{x+1} \right| + C$ (4) $\frac{a^2}{2} \arcsin \frac{x}{a} - \frac{x\sqrt{a^2-x^2}}{2} + C$
 (5) $x \in (-\infty, -1)$ 或 $(1, +\infty)$ 时, 原式为 $-\arcsin \frac{1}{|x|} + C$ (6) $\sqrt{x^2-9} - 3 \arccos \frac{3}{|x|} + C$ (7) $\arcsin x - \frac{x}{1+\sqrt{1-x^2}} + C$
 (8) $\frac{1}{2}(\arcsin x + \ln|x+\sqrt{1-x^2}|) + C$ (9) $\frac{1}{2} \ln(x^2+2x+3) - \sqrt{2} \arctan \frac{x+1}{\sqrt{2}} + C$
 (10) $\frac{1+x}{2(1+x^2)} + \frac{1}{2} \ln(1+x^2) + \frac{1}{2} \arctan x + C$ (11) $\frac{1}{6}x^3 + \frac{1}{2}x^2 \sin x + x \cos x - \sin x + C$
 (12) $\frac{1}{2}(x^2-1) \ln(x-1) - \frac{1}{4}x^2 - \frac{1}{2} + C$ (13) $-\frac{\ln^3 x + 3 \ln^2 x + 6 \ln x + 6}{x} + C$
 (14) $\frac{x(\cos \ln x + \sin \ln x)}{2} + C$ (15) $x(\arcsin x)^2 + 2\sqrt{1-x^2} \arcsin x - 2x + C$
 (16) $\frac{1}{2}e^x - \frac{1}{5}e^x \sin 2x - \frac{1}{10}e^x \cos 2x + C$ (17) $\frac{1}{4} \tan^2 \frac{x}{2} + \tan \frac{x}{2} + \frac{1}{2} \ln \left| \tan \frac{x}{2} \right| + C$
 (18) $-\frac{x+1}{x^2+x+1} - \frac{4}{\sqrt{3}} \arctan \frac{2x+1}{\sqrt{3}} + C$ (19) $\frac{2}{\sqrt{3}} \arctan \frac{2 \tan \frac{x}{2} + 1}{\sqrt{3}} + C$
 (20) $\frac{1}{\sqrt{5}} \arctan \frac{3 \tan \frac{x}{2}}{\sqrt{5}} + C$ (21) $x - 4\sqrt{x+1} + 4 \ln(\sqrt{x+1} + 1) + C$ (22) $-\frac{3}{2} \sqrt[3]{\frac{x+1}{x-1}} + C$
 (23) $\ln|2x+1+2\sqrt{x(1+x)}| + C$ (24) $-\frac{1}{3} \sqrt{1-x^2}(2+x^2) \arccos x - \frac{1}{9}x(1+x^2) + C$
 (25) $\frac{1}{2}(\sin x - \cos x) - \frac{1}{2\sqrt{2}} \ln \left| \frac{\tan \frac{x}{2} - 1 + \sqrt{2}}{\frac{x}{2} - 1 - \sqrt{2}} \right| + C$
 (26) $\frac{1}{8} \sec^2 \frac{x}{2} + \frac{1}{4} \ln |\csc x - \cot x| + C$ (27) $e^{2x} \tan x + C$
 (28) $2\sqrt{x}(\arcsin \sqrt{x} + \ln x) + 2\sqrt{1-x} - 4\sqrt{x} + C$ (29) $x^2 - x + \frac{1}{3} \ln|x-1| - \frac{1}{6} \ln(x^2+x+1) + \frac{1}{\sqrt{3}} \arctan \frac{2x+1}{\sqrt{3}} + C$
 (30) $\frac{x}{2} - \frac{1}{2} \ln |\sin x + \cos x| + C$