

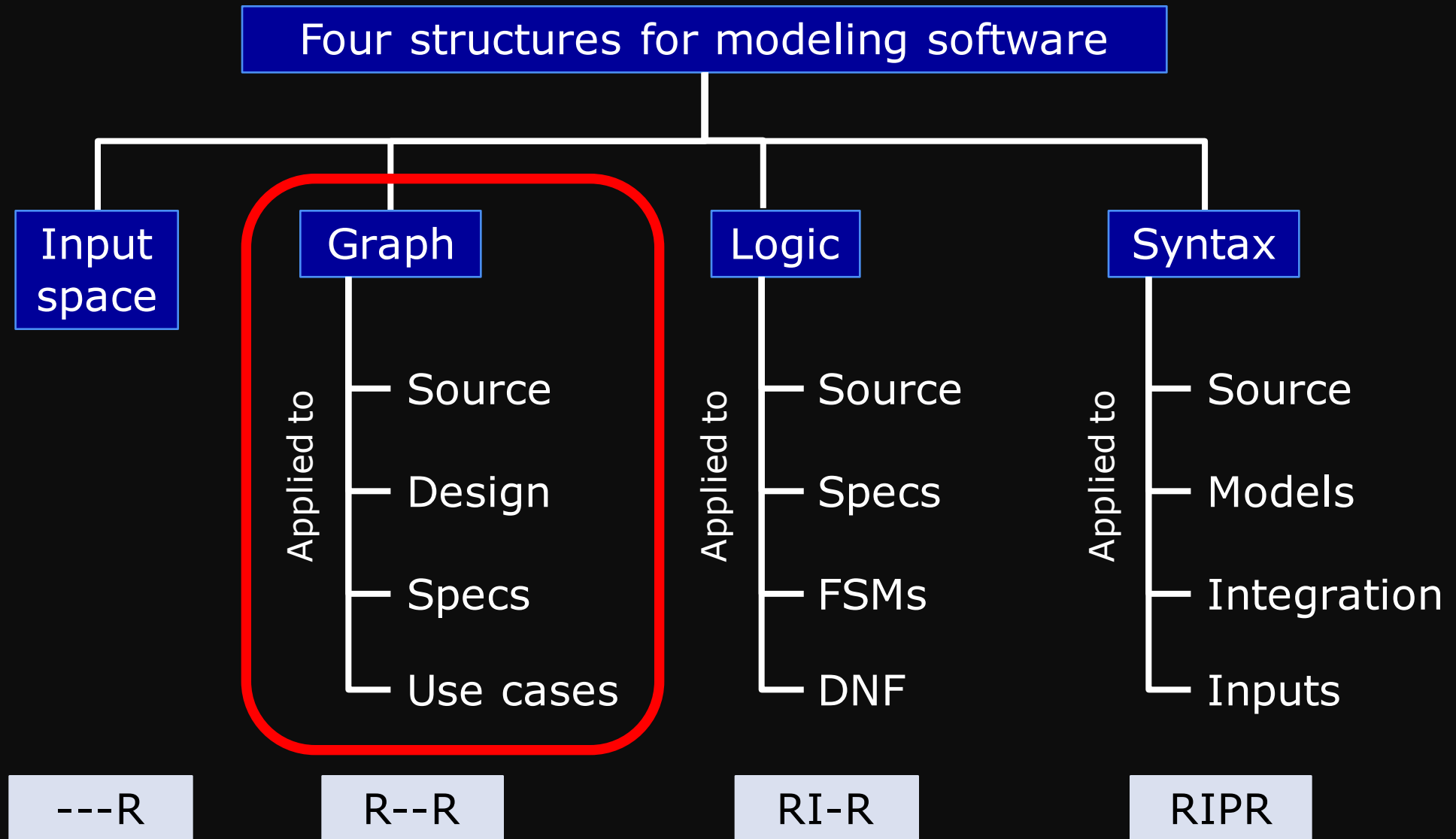
# Graph: Data Flow Coverage Criteria

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## CS 3250 Software Testing

[Ammann and Offutt, “Introduction to Software Testing,” Ch. 7]

# Structures for Criteria-Based Testing



# Graph Coverage Criteria

## Satisfaction

- *Given a set  $TR$  of test requirements for a criterion  $C$ , a set of tests  $T$  satisfies  $C$  on a graph if and only if for every test requirement in  $TR$ , there is a test path in  $path(T)$  that meets the test requirement  $tr$*

## Two types

### 1. Structural coverage criteria

- Define a graph just in terms of nodes and edges

### 2. Data flow coverage criteria

- Requires a graph to be annotated with references to variables

# Today's Objectives

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- Analyze data flow of software artifacts
- Understand how to integrate data flow into a graph model of the program under test
- Focusing on the flow of data, understand how to define criteria and design tests
  - All-Defs Coverage (ADC)
  - All-Uses Coverage (AUC)
  - All-DU-Paths Coverage (ADUPC)

# Data Flow Criteria

- Goal: Ensure that the values are created and used correctly
- How: Focus on definitions and uses of values
- **Definition (def)**: A location where a value for a variable is stored in a memory
- **Use**: A location where a variable's value is accessed

Values are carried from defs to uses, refer to as  
***"du-pairs"***

- Also known *definition-use, def-use, du associations*

# Data Flow Criteria

Data flow coverage criteria define test requirements TR in terms of the flows of data values in a graph G

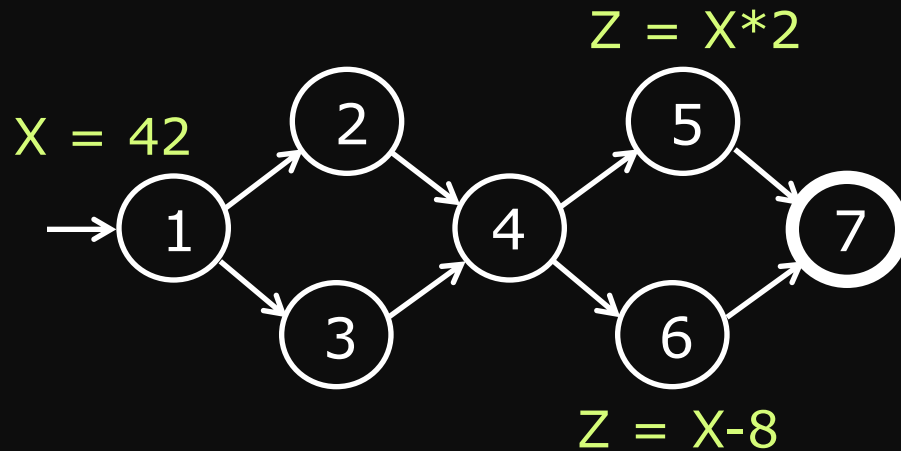
Steps:

1. Develop a model of the software as a graph
2. **Integrate data flow into the graph**
3. A test requirement is met by visiting a particular node or edge or by touring a particular path

# Def, Use, and DU Pairs

- **def( $n$ ) or def( $e$ )**: The set of variables defined by node  $n$  or edge  $e$
- **use( $n$ ) or use( $e$ )**: The set of variables used by node  $n$  or edge  $e$
- **DU-pair**: A pair of locations  $(l_i, l_j)$  such that a variable  $v$  is defined at  $l_i$  and used at  $l_j$

# Example: Defs, Uses, DU-Pairs



defs:

- $\text{def}(1) = \{ X \}$
- $\text{def}(5) = \{ Z \}$
- $\text{def}(6) = \{ Z \}$

uses:

- $\text{use}(5) = \{ X \}$
- $\text{use}(6) = \{ X \}$

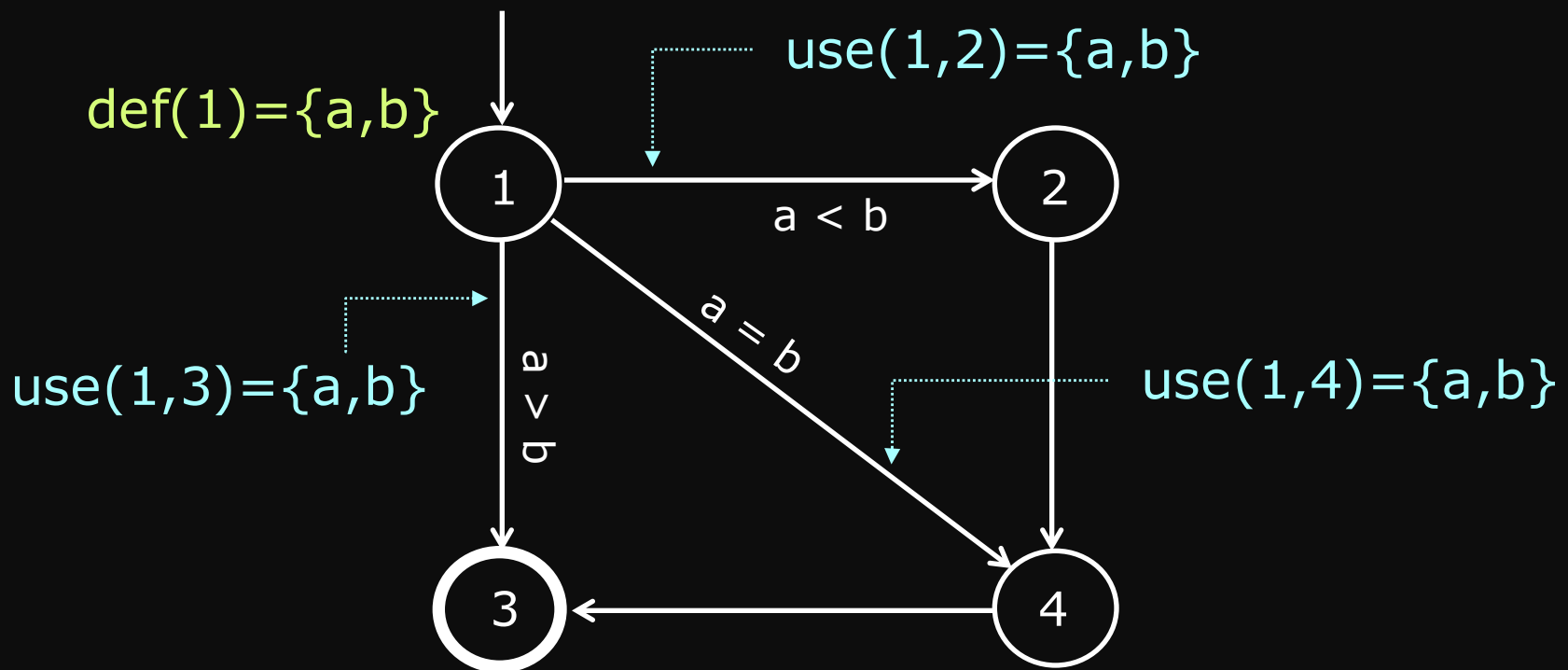
du-pairs: for variable X

- (1, 5)
- (1, 6)



# Example (2)

All variables involved in a decision are assumed to be used on the associated edges



# Your Turn: POTD 5 (1)

$N = \{ 1, 2, 3, 4, 5, 6 \}$

$N_0 = \{ 1 \}$

$N_f = \{ 6 \}$

$E = \{ (1,2), (2,3), (2,6), (3,4), (3,5), (4,5), (5,2) \}$

$\text{def}(1) = \text{def}(3) = \text{use}(3) = \text{use}(6) = \{ x \}$

// Assume the use of  $x$  in node 3 precedes the def

1. Draw the graph. Be sure to annotate all information

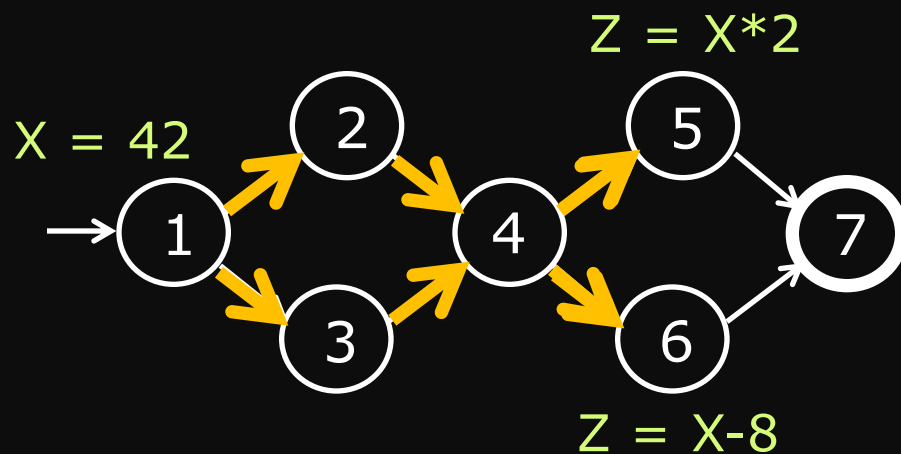
# Def-clear and Reach

- **Def-clear**: A path from  $l_i$  to  $l_j$  is *def-clear* with respect to variable  $v$  if  $v$  is not given another value on any of the nodes or edges in the path
- The values given in **defs** should reach at least one, some, or all possible **uses**. However, a def of a variable may or may not reach a particular use
- Why?
  - No path goes from a location where a variable is defined to a location where the variable is used
  - A variable's value may be changed by another def before it reaches the use
- **Reach**: If there is a def-clear path from  $l_i$  to  $l_j$  with respect to  $v$ , the def of  $v$  at  $l_i$  reaches the use at  $l_j$

# DU-Paths

- **du-path**: A simple subpath that is def-clear with respect to a variable  $v$  from a def of  $v$  to a use of  $v$
- **$\text{du}(n_i, n_j, v)$** : the set of du-paths from  $n_i$  to  $n_j$
- **$\text{du}(n_i, v)$** : the set of du-paths that start at  $n_i$
- Keep the path simple to ensure a reasonably small number of paths

# Example: DU-Paths



**du-paths:** for variable X

- $\text{du}(1, 5, X) = \{[1, 2, 4, 5], [1, 3, 4, 5]\}$
- $\text{du}(1, 6, X) = \{[1, 2, 4, 6], [1, 3, 4, 6]\}$

**defs:**

- $\text{def}(1) = \{X\}$
- $\text{def}(5) = \{Z\}$
- $\text{def}(6) = \{Z\}$

**uses:**

- $\text{use}(5) = \{X\}$
- $\text{use}(6) = \{X\}$

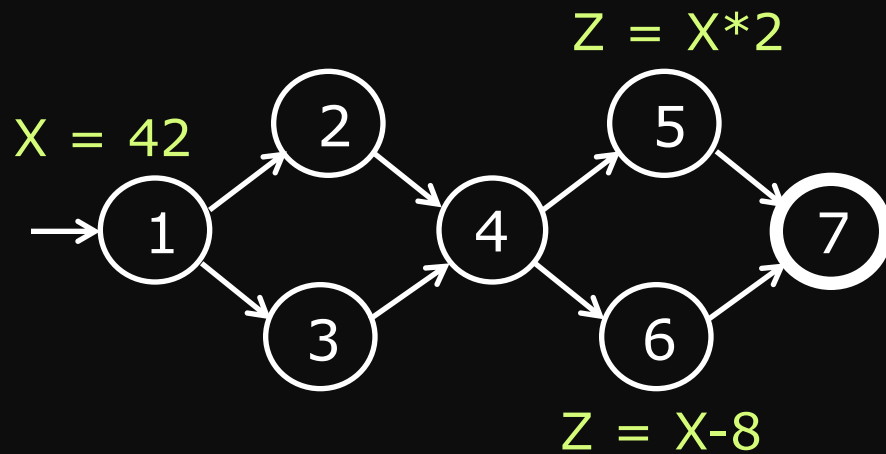
**du-pairs:** for variable X

- (1, 5)
- (1, 6)

# Categorizing DU-Paths

- The core of data flow testing – allowing definitions to flow to uses
- The test criteria for data flow will be defined as sets of du-paths. Thus, we first categorize the du-paths according to:
- **def-path set**
  - $du(n_i, v)$ : All simple paths w.r.t. a given variable  $v$  defined in a given node
- **def-pair set**
  - $du(n_i, n_j, v)$ : All simple paths w.r.t. a given variable  $v$  from a given definition ( $n_i$ ) to a given use ( $n_j$ )

# Example: Def-Path and Def-Pair



## du-path sets

- $\text{du}(1, X) = \{[1,2,4,5], [1,3,4,5], [1,2,4,6], [1,3,4,6]\}$

## du-pair sets

- $\text{du}(1, 5, X) = \{[1,2,4,5], [1,3,4,5]\}$
- $\text{du}(1, 6, X) = \{[1,2,4,6], [1,3,4,6]\}$

# Your Turn: POTD 5 (2)

$N = \{ 1, 2, 3, 4, 5, 6 \}$

$N_0 = \{ 1 \}$

$N_f = \{ 6 \}$

$E = \{ (1,2), (2,3), (2,6), (3,4), (3,5), (4,5), (5,2) \}$

$\text{def}(1) = \text{def}(3) = \text{use}(3) = \text{use}(6) = \{ x \}$

// Assume the use of  $x$  in node 3 precedes the def

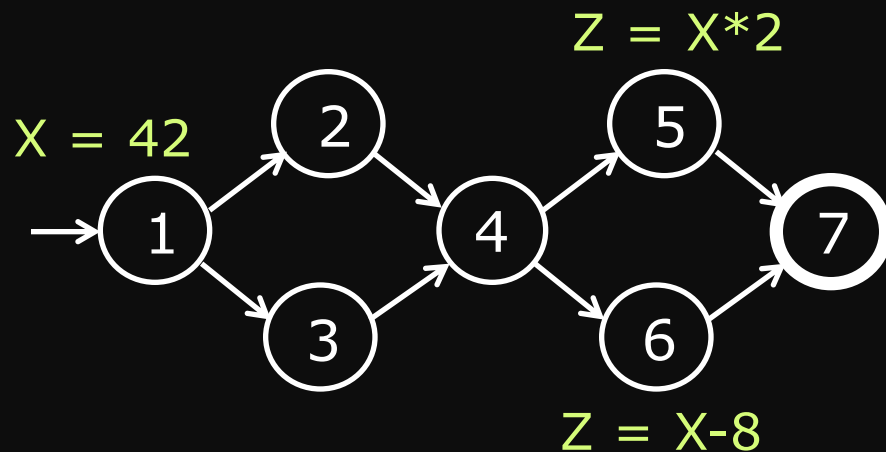
2. List all of the du-paths with respect to  $x$



# Touring DU-Paths

A test path  $p$  **du-tours** subpath  $d$  with respect to  $v$  if  $p$  tours  $d$  and the subpath taken is **def-clear** with respect to  $v$

**Sidetrips** can be used, just as with previous touring



Test path  $[1,2,4,5,7]$  du-tours  
du-path  $[1,2,4,5]$

## du-path sets

- $\text{du}(1, X) = \{[1,2,4,5], [1,3,4,5], [1,2,4,6], [1,3,4,6]\}$

## du-pair sets

- $\text{du}(1, 5, X) = \{[1,2,4,5], [1,3,4,5]\}$
- $\text{du}(1, 6, X) = \{[1,2,4,6], [1,3,4,6]\}$

# Your Turn: POTD 5 (3)

```
N    = { 1, 2, 3, 4, 5, 6 }
N0   = { 1 }
Nf   = { 6 }
E    = { (1,2), (2,3), (2,6), (3,4), (3,5), (4,5), (5,2) }
def(1) = def(3) = use(3) = use(6) = { x }
// Assume the use of x in node 3 precedes the def
```

Test paths

```
t1 = [1, 2, 6]
t2 = [1, 2, 3, 4, 5, 2, 3, 5, 2, 6]
t3 = [1, 2, 3, 5, 2, 3, 4, 5, 2, 6]
t4 = [1, 2, 3, 5, 2, 6]
```

3. Determine which du-paths each test path tours.

# Data Flow Coverage Criteria

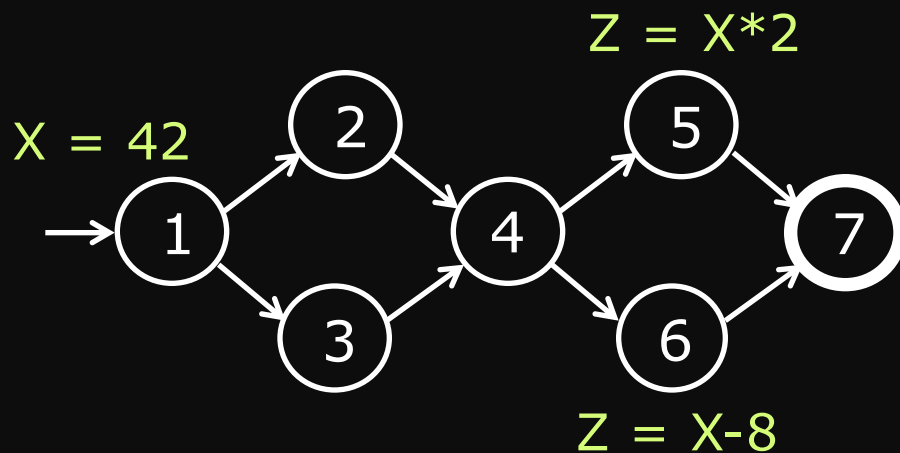
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- All-Defs Coverage (ADC)
  - Use every def
- All-Uses Coverage (AUC)
  - Get to every use
- All-du-Paths Coverage (ADUPC)
  - Follow all du-paths

# All-Defs Coverage (ADC)

For each set of du-paths  $S = \text{du}(n, v)$ , TR contains at least one path  $d$  in  $S$

- For each def, **at least one use** must be reached



## du-path sets

- $\text{du}(1, X) = \{[1, 2, 4, 5], [1, 3, 4, 5], [1, 2, 4, 6], [1, 3, 4, 6]\}$

TR for  $X = \{[1, 2, 4, 5]\}$

Test paths =  $\{[1, 2, 4, 5, 7]\}$

# Your Turn: POTD 5 (4)

```
N    = { 1, 2, 3, 4, 5, 6 }
N0   = { 1 }
Nf   = { 6 }
E    = { (1,2), (2,3), (2,6), (3,4), (3,5), (4,5), (5,2) }
def(1) = def(3) = use(3) = use(6) = { x }
// Assume the use of x in node 3 precedes the def
```

Test paths

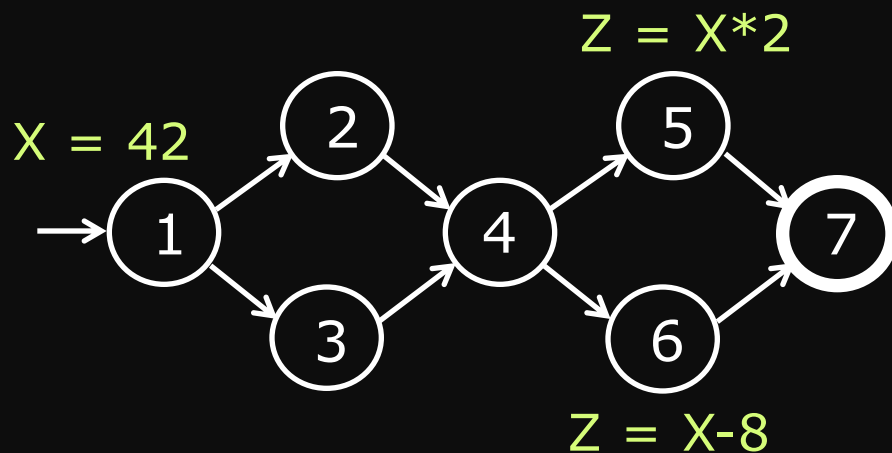
```
t1 = [1, 2, 6]
t2 = [1, 2, 3, 4, 5, 2, 3, 5, 2, 6]
t3 = [1, 2, 3, 5, 2, 3, 4, 5, 2, 6]
t4 = [1, 2, 3, 5, 2, 6]
```

4. List a minimal test set that satisfies **all defs** coverage with respect to x (direct tours only).

# All-Uses Coverage (AUC)

For each set of du-paths  $S = \text{du}(n_i, n_j, v)$ , TR contains at least one path  $d$  in  $S$

- For each def, **all uses** must be reached



## du-pair sets

- $\text{du}(1, 5, X) = \{[1, 2, 4, 5], [1, 3, 4, 5]\}$
- $\text{du}(1, 6, X) = \{[1, 2, 4, 6], [1, 3, 4, 6]\}$

TR for  $X = \{[1, 2, 4, 5], [1, 2, 4, 6]\}$

Test paths =  $\{[1, 2, 4, 5, 7], [1, 2, 4, 6, 7]\}$

# Your Turn: POTD 5 (5)

```
N    = { 1, 2, 3, 4, 5, 6 }
N0   = { 1 }
Nf   = { 6 }
E    = { (1,2), (2,3), (2,6), (3,4), (3,5), (4,5), (5,2) }
def(1) = def(3) = use(3) = use(6) = { x }
// Assume the use of x in node 3 precedes the def
```

Test paths

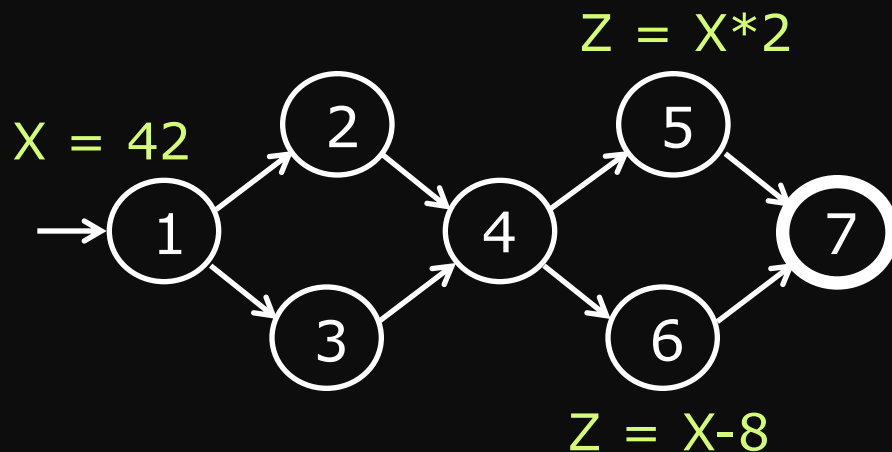
```
t1 = [1, 2, 6]
t2 = [1, 2, 3, 4, 5, 2, 3, 5, 2, 6]
t3 = [1, 2, 3, 5, 2, 3, 4, 5, 2, 6]
t4 = [1, 2, 3, 5, 2, 6]
```

5. List a minimal test set that satisfies **all uses** coverage with respect to x (direct tours only).

# All-DU-Paths Coverage (ADUPC)

For each set of du-paths  $S = \text{du}(n_i, n_j, v)$ , TR contains every path  $d$  in  $S$

- For each def-use pair, **all paths** between defs and uses must be covered



## du-pair sets

- $\text{du}(1, 5, X) = \{[1,2,4,5], [1,3,4,5]\}$
- $\text{du}(1, 6, X) = \{[1,2,4,6], [1,3,4,6]\}$

TR for  $X = \{[1,2,4,5], [1,3,4,5], [1,2,4,6], [1,3,4,6]\}$

Test paths =  $\{[1,2,4,5,7], [1,3,4,5,7], [1,2,4,6,7], [1,3,4,6,7]\}$



# Your Turn: POTD 5 (6)

```
N    = { 1, 2, 3, 4, 5, 6 }
N0   = { 1 }
Nf   = { 6 }
E    = { (1,2), (2,3), (2,6), (3,4), (3,5), (4,5), (5,2) }
def(1) = def(3) = use(3) = use(6) = { x }
// Assume the use of x in node 3 precedes the def
```

Test paths

```
t1 = [1, 2, 6]
t2 = [1, 2, 3, 4, 5, 2, 3, 5, 2, 6]
t3 = [1, 2, 3, 5, 2, 3, 4, 5, 2, 6]
t4 = [1, 2, 3, 5, 2, 6]
```

6. List a minimal test set that satisfies **all du-paths** coverage with respect to x (direct tours only).

# Summary

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- Graphs are very powerful abstraction for designing tests
- Graphs appear in many situations in software
- Each criterion has its own cost/benefit tradeoffs
  - No silver bullet
  - When possible, choose the criterion that yields the smallest number of test requirements while maintaining fault detection capability

# Graph Coverage Criteria Subsumption

