

## **Abstract Data Types (ADTs)**

- Definition: An ADT is a data type whose properties (domain and operations) are specified independently of any particular implementation
  - Separation of specification from implementation
  - An ADT is an abstraction of a data structure
- ADT: An ADT that holds other objects.
   Typically we are interested in inserting, removing, and iterating through the contents of a collection.
- A collection ADT specifies:
  - Data stored
  - Operations on the data
  - Error conditions associated with operations

Stacks

#### The Stack ADT

- A Stack is an ordered collection of homogeneous elements, in which all insertions and deletions are made at one end of the list called the "\_\_\_\_\_" of the stack
- □ A stack has a \_\_\_\_\_ ""last in, first out"" structure
- Think of a spring-loaded plate dispenser

© 2010 Goodrich, Tamassia

**Stacks** 

13

## Stack ADT (cont.)

- Main stack operations:
  - push(object): inserts an element
  - object pop(): removes and returns the last inserted element
- Auxiliary stack operations:
  - object top(): returns the last inserted element without removing it
  - integer size(): returns the number of elements stored
  - boolean isEmpty(): indicates whether no elements are stored

#### **Example**

Method	Return Value	Stack Contents
push(5)	-	(5)
push(3)	_	(5, 3)
size()	2	(5, 3)
pop()	3	(5)
isEmpty()	false	(5)
pop()	5	()
isEmpty()	true	()
pop()	null	()
push(7)	_	(7)
push(9)	-	(7, 9)
top()	9	(7, 9)
push(4)	1-1	(7, 9, 4)
size()	3	(7, 9, 4)
pop()	4	(7, 9)
push(6)	1-	(7, 9, 6)
push(8)	1-	(7, 9, 6, 8)
pop()	8	(7, 9, 6)

c

# **Applications of Stacks**

- Direct applications
  - Page-visited history in a Web browser
  - Undo sequence in a text editor
  - Chain of method calls in the Java Virtual Machine
- Indirect applications
  - Auxiliary data structure for algorithms
  - Component of other data structures

#### Method Stack in the JVM

- The Java Virtual Machine (JVM) keeps track of the chain of active methods with a stack
- When a method is called, the
   JVM pushes on the stack a
   stack frame (or activation record) for the called method
- When a method ends, its frame is popped from the stack and control is passed to the method on top of the stack
- Allows for recursion

```
main() {
    int i = 5;
    foo(i);
    }
    m = 6

foo(int j) {
    int k;
    k = j+1;
    bar(k);
    }

bar(int m) {
    i = 5
}
```

```
Separate ADTs for each type that a collection can hold?
```

```
interface StackOfDouble {
interface StackOfInt {
    void push(int x) {...}
                                       void push(double x) {...}
                                       double pop() {...}
    int pop() {...}
                                       double top() {...}
    int top() {...}
    boolean isEmpty() {...}
                                       boolean isEmpty() {...}
}
                                  }
interface StackOfApple {
    void push(Apple x) {...}
    Apple pop() {...}
                                    interface StackOfAnything {
    Apple top() {...}
                                        void push(Anything x) {...}
    boolean isEmpty() {...}
                                        Anything pop() {...}
}
                                        Anything top() {...}
                                        boolean isEmpty() {...}
                                    }
```

We need a single, reusable definition for every types.

#### Solution in Java (I)

Use java.lang. \_\_\_\_ class as an element type

```
Object

String Number BankAccount

Integer
```

```
interface Stack {
    void push(Object x) {...}
    Object pop() {...}
    Object top() {...}
    boolean isEmpty() {...}
}
```

- When an element is removed from the collection it can only be referenced as an **Object**. If you intend to use it as something else you must \_\_\_\_\_ it into the type that you intend to use.
- For example:

```
s.push("CSE210 Data Structures"); // push string on a stack
String course = (String) s.top(); // cast top to String
System.out.println(course.toLowerCase()); // use the string
```

9

## Solution in Java (II)

- Drawbacks of using java.lang.Object
  - Program is cluttered with ugly casts
  - More importantly, it is not
- Use \_\_\_\_\_\_ types introduced as of Java 5
- In generic types (generic class or generic interface),
   commonalities are defined with the help of \_\_\_\_\_ parameters.
  - Guarantees element homogeneity at compile time
  - Type-safety is guaranteed if used properly

```
interface Stack<E> { ... } // See next slide
class ArrayStack<E> implements Stack<E> { ... }
Stack<Integer> s = new ArrayStack<Integer>(100);
s.push(1234);
s.push("Hello"); // compile-time error
int val = s.pop(); // No cast is necessary
```

#### Stack Interface in Java

- Java interface corresponding to our Stack ADT
- Requires the definition of class
   EmptyStackException
- Different from the built-in Java class java.util.Stack

```
public interface Stack<E> {
   public int size();
   public boolean isEmpty();
   public E top()
        throws EmptyStackException;
   public void push(E element);
   public E pop()
        throws EmptyStackException;
}
```

11

#### **Exceptions**

- Attempting the execution of an operation of ADT may sometimes cause an error condition, called an exception
- Exceptions are said to be "thrown" by an operation that cannot be executed
- In the Stack ADT,
   operations pop and top
   cannot be performed if
   the stack is empty
- Attempting the execution of pop or top on an empty stack throws an EmptyStackException



- A simple way of implementing the Stack ADT uses an array
- We add elements from left to right
- A variable keeps track of the index of the top element

Algorithm *size()* return *t* + 1

Algorithm pop()
if isEmpty() then
throw EmptyStackException
else

13

 $t \leftarrow t - 1$ return S[t + 1]



# Array-based Stack (cont.)

- The array storing the stack elements may become full
- A push operation will then throw a FullStackException
  - Limitation of the arraybased implementation
  - Not intrinsic to the Stack ADT

Algorithm *push*(o)

if t = S.length - 1 then
throw FullStackException
else

 $t \leftarrow t + 1$  $S[t] \leftarrow o$ 



#### Performance and Limitations

- Performance
  - Let n be the number of elements in the stack
  - The space used is O(n)
  - Each operation runs in time O(1)
- Limitations
  - The maximum size of the stack must be defined a priori and cannot be changed
  - Trying to push a new element into a full stack causes an implementation-specific exception

15

## Array-based Stack in Java

```
public class ArrayStack<E>
    implements Stack<E> {

    // holds the stack elements
    private E S[];

    // index to top element
    private int top = -1;

    // constructor
    public ArrayStack(int capacity) {
        S = (E[]) new Object[capacity]);
    }
}
```

```
public E pop()
    throws EmptyStackException {
    if isEmpty()
        throw new EmptyStackException
            ("Empty stack: cannot pop");
        E temp = S[top];
            // facilitate garbage collection:
            S[top] = null;
            top = top - 1;
            return temp;
        }
... (other methods of Stack interface)
```

#### Example use in Java

```
public class Tester {
    // ... other methods
    public intReverse(Integer a[]) {
        Stack<Integer> s;
        s = new ArrayStack<Integer>();
        ... (code to reverse array a) ...
    }
```

```
public floatReverse(Float f[]) {
    Stack<Float> s;
    s = new ArrayStack<Float>();
    ... (code to reverse array f) ...
}
```

17

#### Linked-Based Implmentation

- In this section we study a link-based implementation of the Stack ADT.
- To support this we first define a LLObjectNode class
- After discussing the link-based approach we compare our stack implementation approaches.

### The LLObjectNode class

Our stacks hold elements of class Object.

#### LLObjectNode

- -LLObjectNode:link
- -Object:info
- +LLObjectNode(Object info)
- +setInfo(Object info):void
- +getInfo():Object
- +setLink(LLObjectNode link):void
- +getLink():LLObjectNode

19

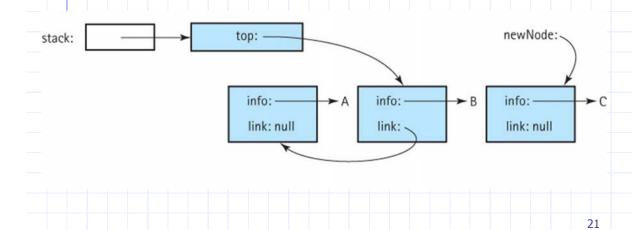
#### The LinkedStack Class

```
public class LinkedStack implements Stack
{
   // reference to the top of this stack
   protected LLObjectNode top;

public LinkedStack()
{
   top = null;
}
. . .
```

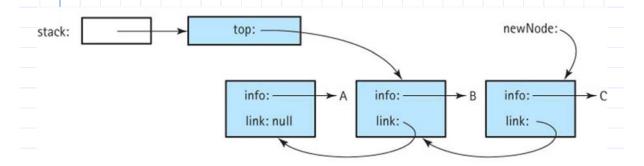


- Allocate space for the next stack node and set the node info to element
- Set the node link to the previous top of stack
- Set the top of stack to the new stack node



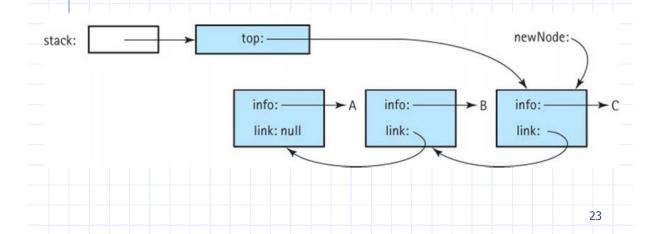


- Allocate space for the next stack node and set the node info to element
  - Set the node link to the previous top of stack
  - Set the top of stack to the new stack node



#### The push(C) operation (step 3)

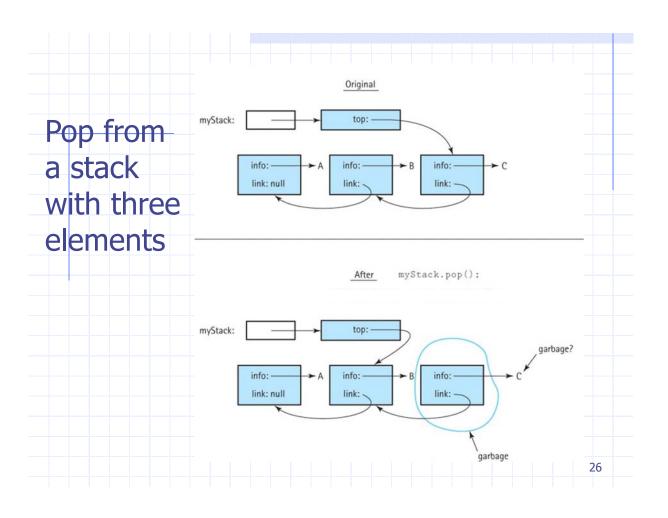
- Allocate space for the next stack node
   and set the node info to element
- Set the node link to the previous top of stack
  - Set the top of stack to the new stack node



## Code for the push method

```
public void push(Object element)
// Places element at the top of this stack.
{
   LLObjectNode newNode = new LLObjectNode(element);
   newNode.setLink(top);
   top = newNode;
}
```

### Code for the pop method



#### The remaining operations

#### **Comparing Stack Implementations**

- Storage Size
  - Array-based: takes the same amount of memory, no matter how many array slots are actually used, proportional to maximum size
  - Link-based: takes space proportional to actual size of the stack (but each element requires more space than with array approach)
- Operation efficiency
  - All operations, for each approach, are \_
  - Except for the Constructors:
    - Array-based: O(N)
    - Link-based: O(1)

#### Parentheses Matching

- Each "(", "{", or "[" must be paired with a matching ")", "}", or "["
  - correct: ( )(( )){([( )])}
  - correct: ((( )(( )){([( )])}
  - incorrect: )(( )){([( )])}
  - incorrect: ({[])}
  - incorrect: (

29

#### Parentheses Matching Algorithm

**Algorithm** ParenMatch(*X*,*n*):

*Input:* An array *X* of *n* tokens, each of which is either a grouping symbol, a variable, an arithmetic operator, or a number

Output: true if and only if all the grouping symbols in X match

Let S be an empty stack

for *i*=0 to *n*-1 do

if X[i] is an opening grouping symbol then
 S.push(X[i])

else if X[i] is a closing grouping symbol then

if S.isEmpty() then

return false {nothing to match with}

if S.pop() does not match the type of X[i] then

return false {wrong type}

if S.isEmpty() then

return true {every symbol matched}

else return false {some symbols were never matched}

#### Parenthesis Matching (Java)

```
public static boolean isMatched(String expression) {
 final String opening = "({["; // opening delimiters
 final String closing = ")}]"; // respective closing delimiters
 Stack<Character> buffer = new LinkedStack<>( );
 for (char c : expression.toCharArray( )) {
  if (opening.indexOf(c) !=-1) // this is a left delimiter
    buffer.push(c);
  else if (closing.indexOf(c) !=-1) { // this is a right delimiter
   if (buffer.isEmpty()) // nothing to match with
    return false;
   if (closing.indexOf(c) != opening.indexOf(buffer.pop()))
    return false; // mismatched delimiter
   }
 return buffer.isEmpty(); // were all opening delimiters matched?
                                                                    31
```

# **HTML Tag Matching**

☐ For fully-correct HTML, each <name> should pair with a matching </name>

#### <body>

<center>

<h1> The Little Boat </h1>

</center>

The storm tossed the little boat like a cheap sneaker in an old washing machine. The three drunken fishermen were used to such treatment, of course, but not the tree salesman, who even as a stowaway now felt that he had overpaid for the voyage.

Vill the salesman die?

What color is the boat?

And what about Naomi?

</body>

#### The Little Boat

The storm tossed the little boat like a cheap sneaker in an old washing machine. The three drunken fishermen were used to such treatment, of course, but not the tree salesman, who even as a stowaway now felt that he had overpaid for the voyage.

- 1. Will the salesman die?
- 2. What color is the boat?
- 3. And what about Naomi?

## HTML Tag Matching (Java)

```
public static boolean isHTMLMatched(String html) {
 Stack<String> buffer = new LinkedStack<>( );
 int j = html.indexOf('<'); // find first '<' character (if any)
 while (j != -1) {
  int k = html.indexOf('>', j+1); // find next '>' character
  if (k == -1)
    return false; // invalid tag
  String tag = html.substring(j+1, k); // strip away < >
  if (!tag.startsWith("/")) // this is an opening tag
    buffer.push(tag);
  else { // this is a closing tag
    if (buffer.isEmpty( ))
     return false; // no tag to match
    if (!tag.substring(1).equals(buffer.pop( )))
     return false; // mismatched tag
  j = html.indexOf('<', k+1); // find next '<' character (if any)
 return buffer.isEmpty(); // were all opening tags matched?
```

#### Evaluating Arithmetic Expressions

14 - 3 \* 2 + 7 = (14 - (3 \* 2)) + 7

Operator precedence

\* has precedence over +/-

#### **Associativity**

operators of the same precedence group evaluated from left to right

Example: (x - y) + z rather than x - (y + z)

Idea: push each operator on the stack, but first pop and perform higher and *equal* precedence operations.

#### Algorithm for Evaluating Expressions

# Two stacks: opStk holds operators valStk holds values

Use \$ as special "end of input" token with lowest precedence

#### Algorithm doOp()

 $x \leftarrow valStk.pop();$   $y \leftarrow valStk.pop();$   $op \leftarrow opStk.pop();$ valStk.push( y op x )

Algorithm repeatOps( refOp ):

while (valStk.size() > 1 ∧

prec(refOp) ≤

prec(opStk.top())

doOp()

#### Algorithm EvalExp()

Input: a stream of tokens representing an arithmetic expression (with numbers)

Output: the value of the expression

while there's another token z

if isNumber(z) then
 valStk.push(z)

else

repeatOps(z);
 opStk.push(z)
repeatOps(\$);
return valStk.top()

