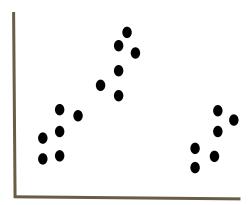
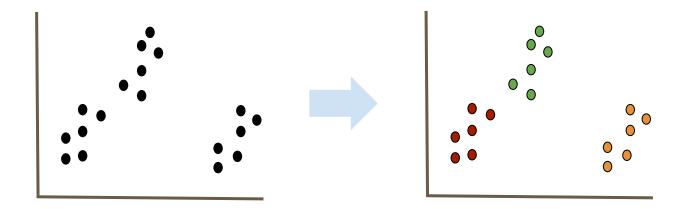
Clustering - Kmeans

Boston University CS 506 - Lance Galletti

What is a Clustering



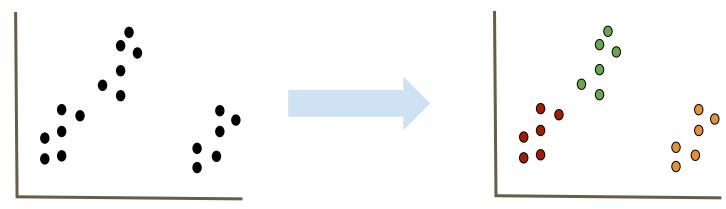
What is a Clustering



What is a Clustering

A clustering is a grouping / assignment of objects (data points) such that objects in the same group / cluster are:

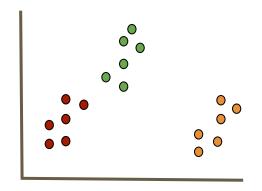
- similar to one another
- dissimilar to objects in other groups

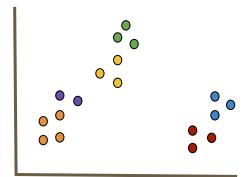


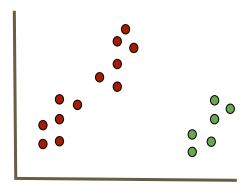
Applications

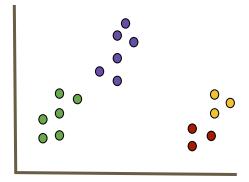
- Outlier detection / anomaly detection
 - Data Cleaning / Processing
 - Credit card fraud, spam filter etc.
- Feature Extraction
- Filling Gaps in your data
 - Using the same marketing strategy for similar people
 - Infer probable values for gaps in the data (similar users could have similar hobbies, likes / dislikes etc.)

Clusters can be Ambiguous









Types of Clusterings

Partitional

Each object belongs to exactly one cluster

Hierarchical

A set of nested clusters organized in a tree

Density-Based

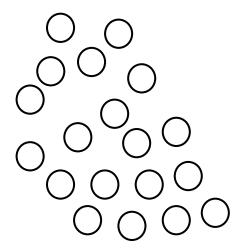
Defined based on the local density of points

Soft Clustering

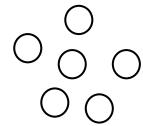
Each point is assigned to every cluster with a certain probability

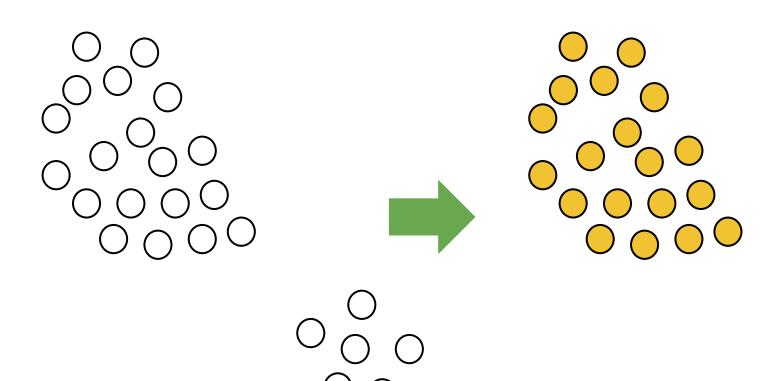
Partitional Clustering

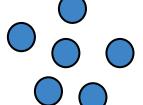
Partitional Clustering

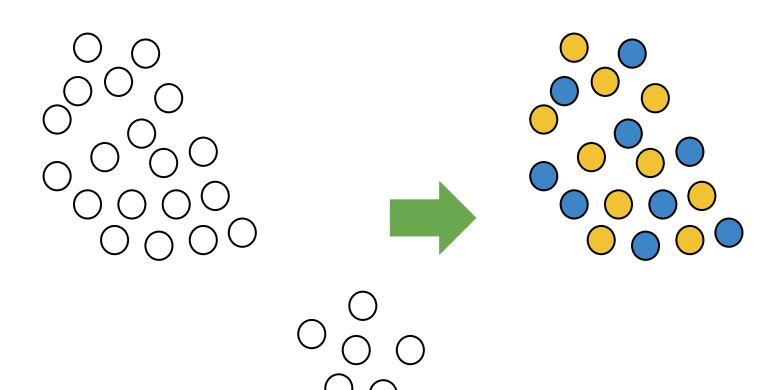


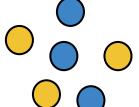
Goal: partition dataset into k partitions

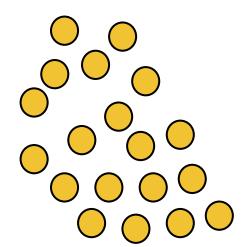


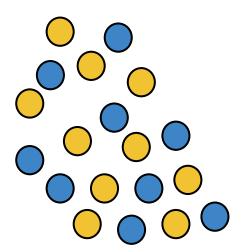


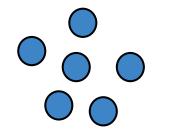


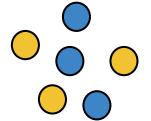


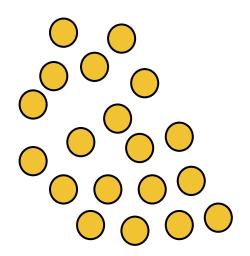


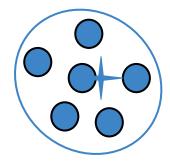


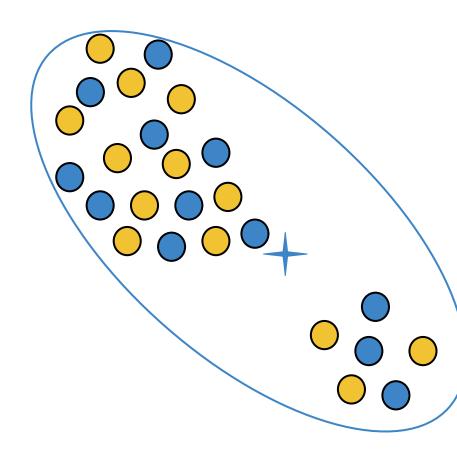


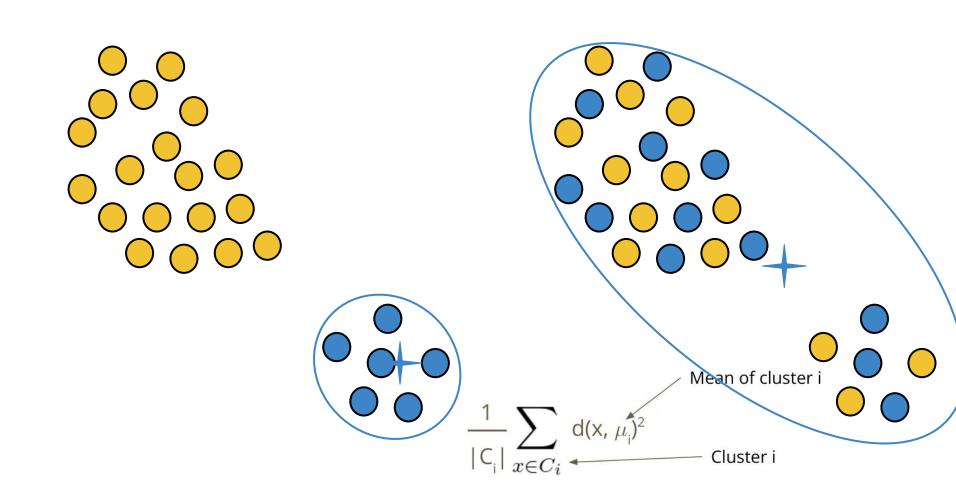












Cost Function

$$\sum_{i}^{k} \sum_{x \in C_i} d(x, \mu_i)^2$$

- Way to evaluate and compare solutions
- Hope: can find some algorithm that find solutions that make the cost small

K-means

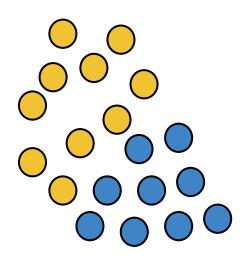
Given $X = \{x_1, ..., x_n\}$ our dataset, **d** the euclidean distance, and **k**

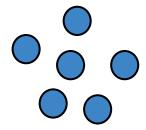
Find k centers $\{\mu_1, \dots, \mu_k\}$ that minimize the **cost function**:

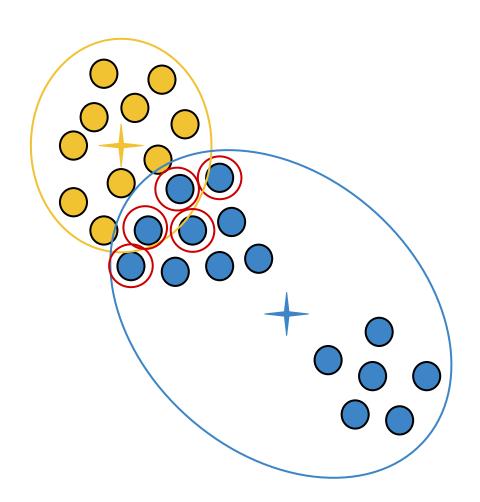
$$\sum_{i}^{k} \sum_{x \in C_{i}} d(x, \mu_{i})^{2}$$

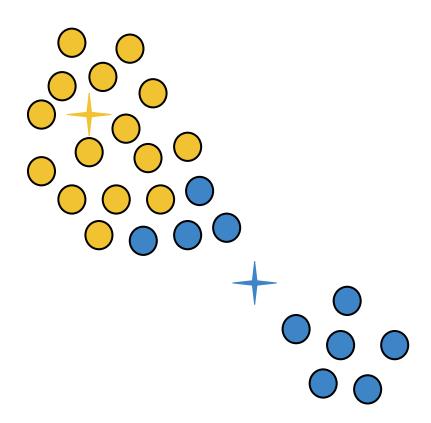
When **k=1** and **k=n** this is easy. Why?

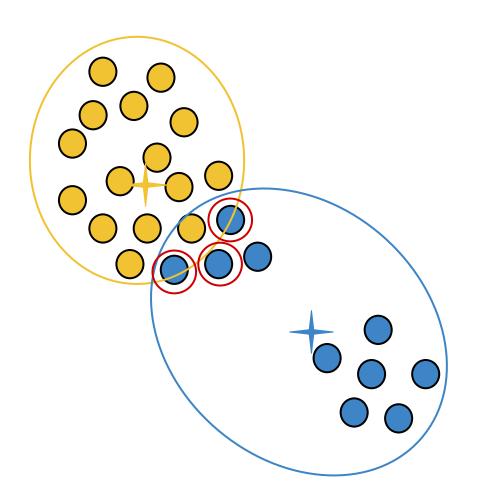
When $\mathbf{x_i}$ lives in more than 2 dimensions, this is a very difficult (**NP-hard**) problem

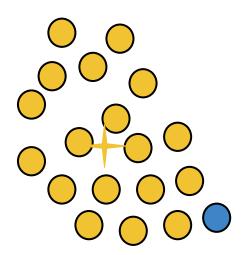


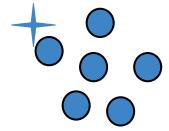


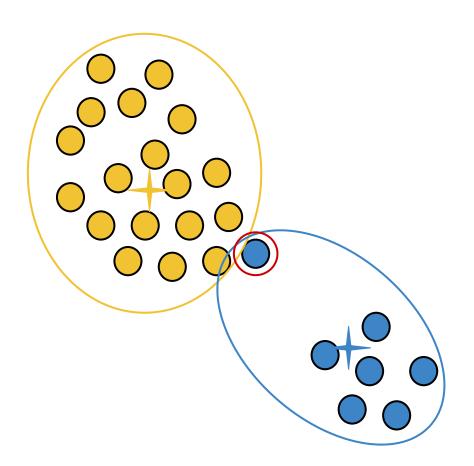


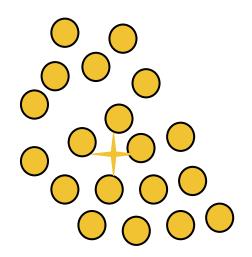


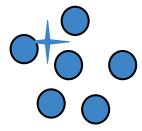






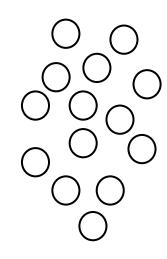


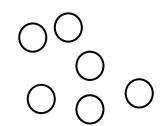


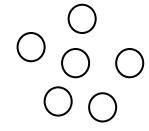


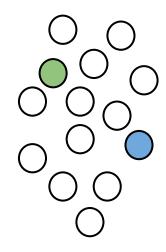
K-means - Lloyd's Algorithm

- 1. Randomly pick **k** centers {μ₁, ... , μ_k}
- 2. Assign each point in the dataset to its closest center
- 3. Compute the new centers as the means of each cluster
- 4. Repeat 2 & 3 until convergence

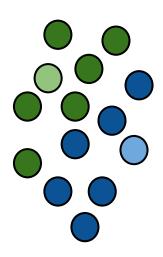




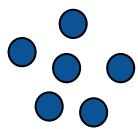


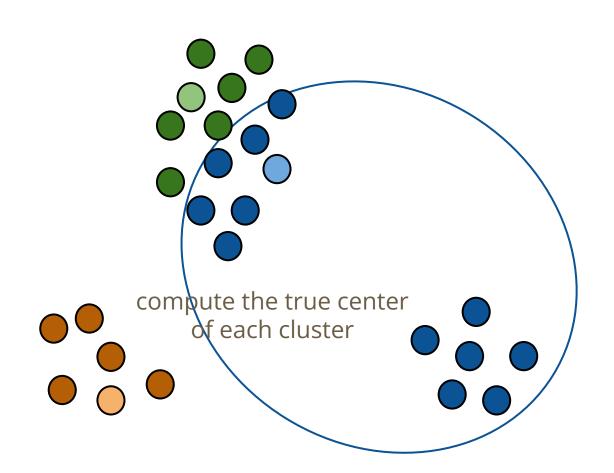


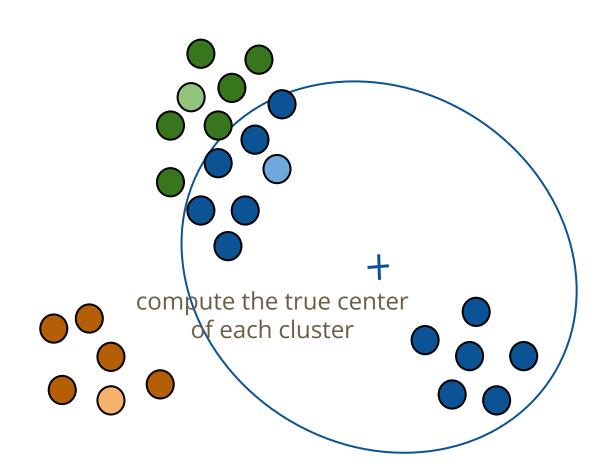


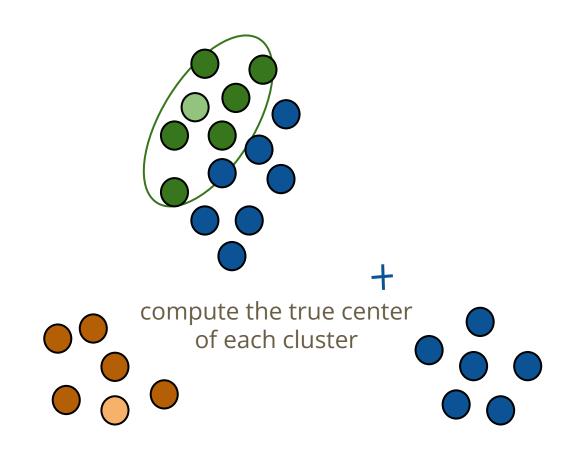


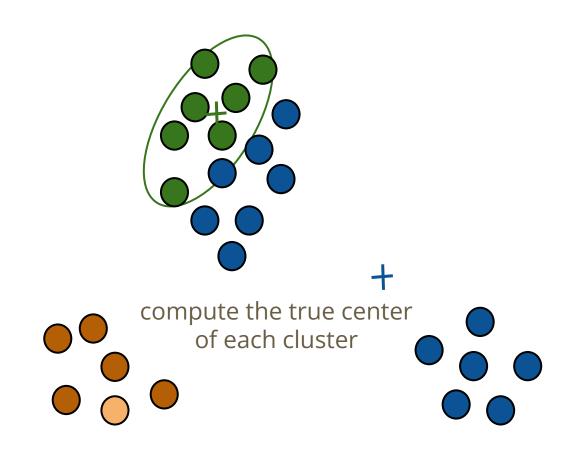


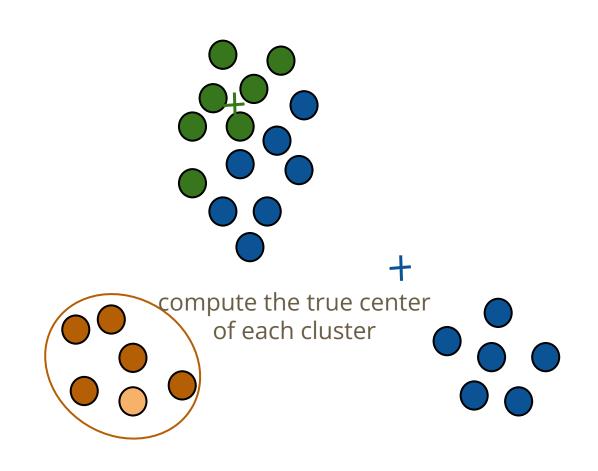


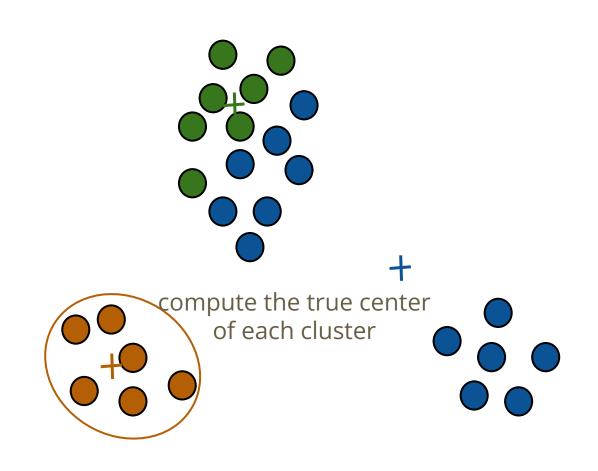


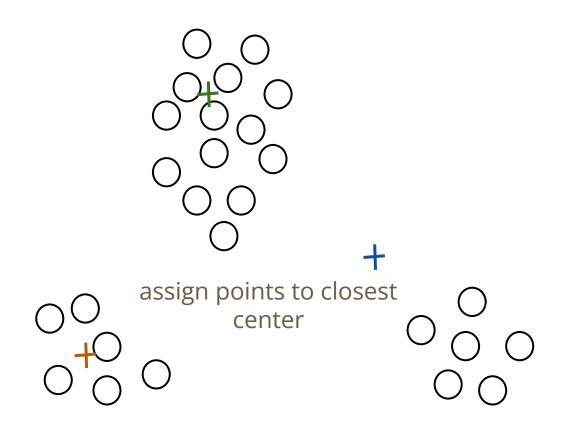


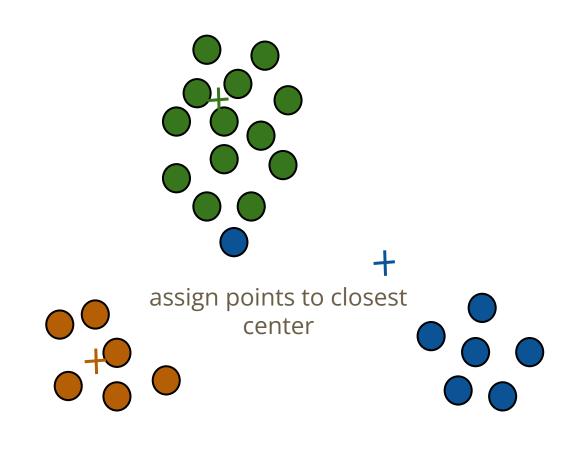


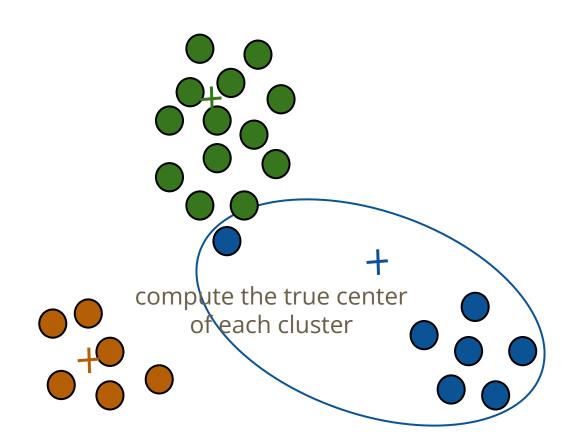


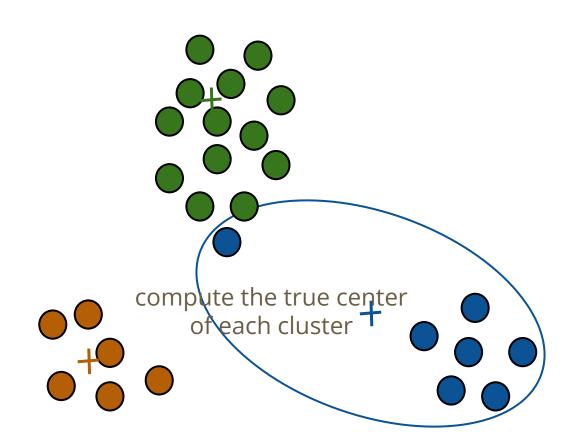


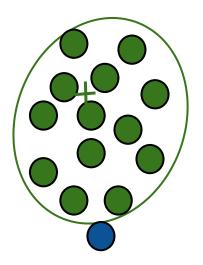


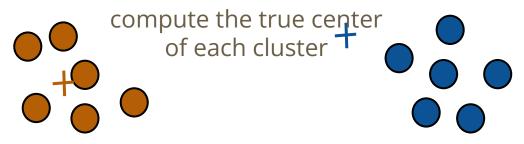


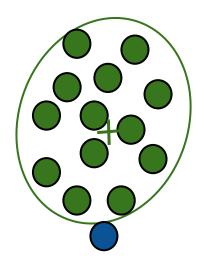


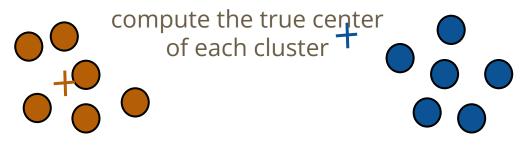


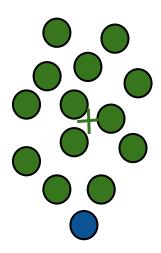


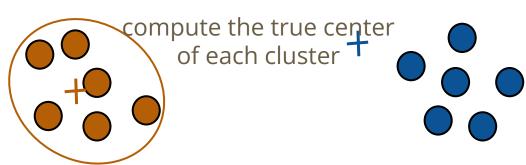


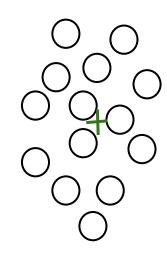


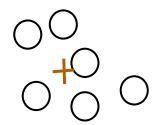


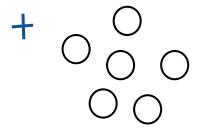


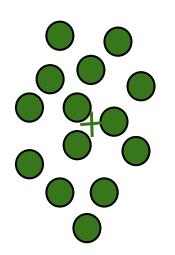


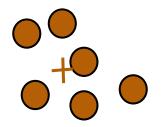


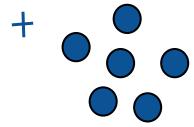


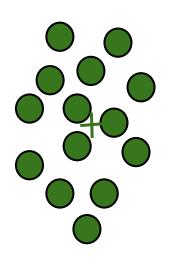


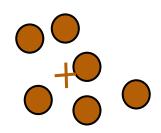


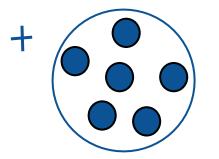


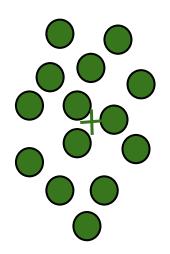


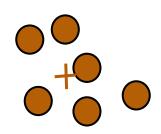


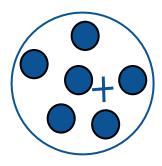


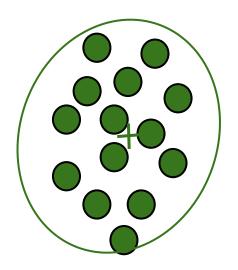


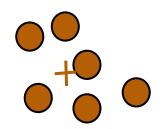


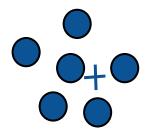


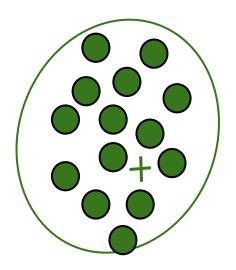


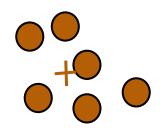


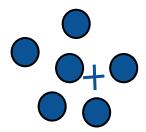


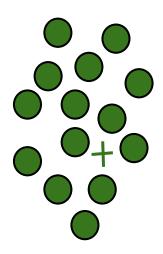


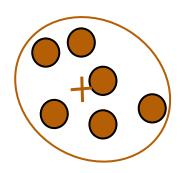


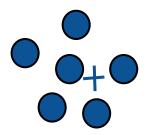


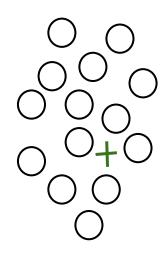


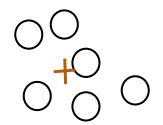


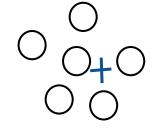


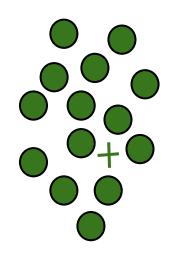


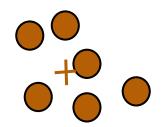


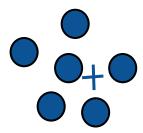


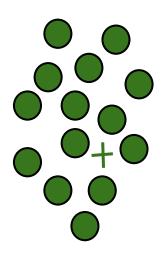


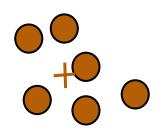


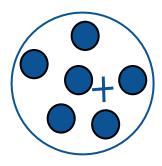


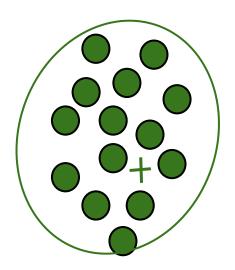


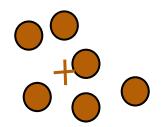


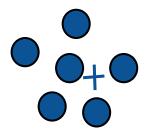


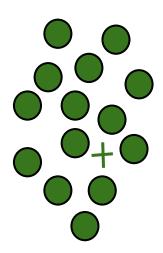


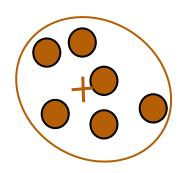


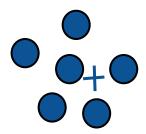


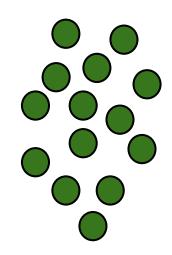


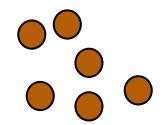


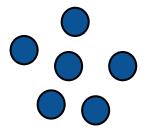












Questions

