

Lab Assignment-6

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Ans:

(1) Name of the Experiment:
Implementation of 4-bit Magnitude Comparator.

(2) Objective:

- i) To investigate the rules of comparing two 4-bit numbers.
- ii) To familiarize with the boolean functions of a magnitude comparator
- iii) To implement the circuit for two 4-bit numbers.

(3) Required Components and Equipments:

↳ Logic Gates (XNOR, AND-4, AND, NOR, AND-3).

↳ Inputs (using logicstate)

↳ LEDs (Blue or any other colors)

↳ Power Source / Ground.

(2)

④ Experimental Setup : (No need to draw IC configurations)

$$A = B$$

A₃ A₂ A₁ A₀

1 0 1 1

B₃ B₂ B₁ B₀

1 0 1 1

A	B	A xnor B
0	0	1
0	1	0
1	0	0
1	1	1

$$A_0 \text{ equal } B_0 = A_0 \text{ xnor } B_0$$

$$A_1 B_1 = A_1 \text{ xnor } B_1$$

$$A_2 B_2 = A_2 \text{ xnor } B_2$$

$$A_3 B_3 = A_3 \text{ xnor } B_3$$

$$A \text{ equal } B = A_0 \text{ xnor } B_0 \cdot A_1 \text{ xnor } B_1 \cdot$$

$$A_2 \text{ xnor } B_2 \cdot A_3 \text{ xnor } B_3$$

$$A_3 \text{ xor } B_3 = X_3$$

(3)

$A > B$

$A_3 A_2 A_1 A_0$
1 0 1 1

$B_3 B_2 B_1 B_0$
0 0 1 1

$A_3 A_2 A_1 A_0$
1 1 0 1
 $B_3 B_2 B_1 B_0$
1 0 1 1

$A_3 A_2 A_1 A_0$
1 1 1 1
 $A_3 A_2 A_1 A_0$
1 1 1 0

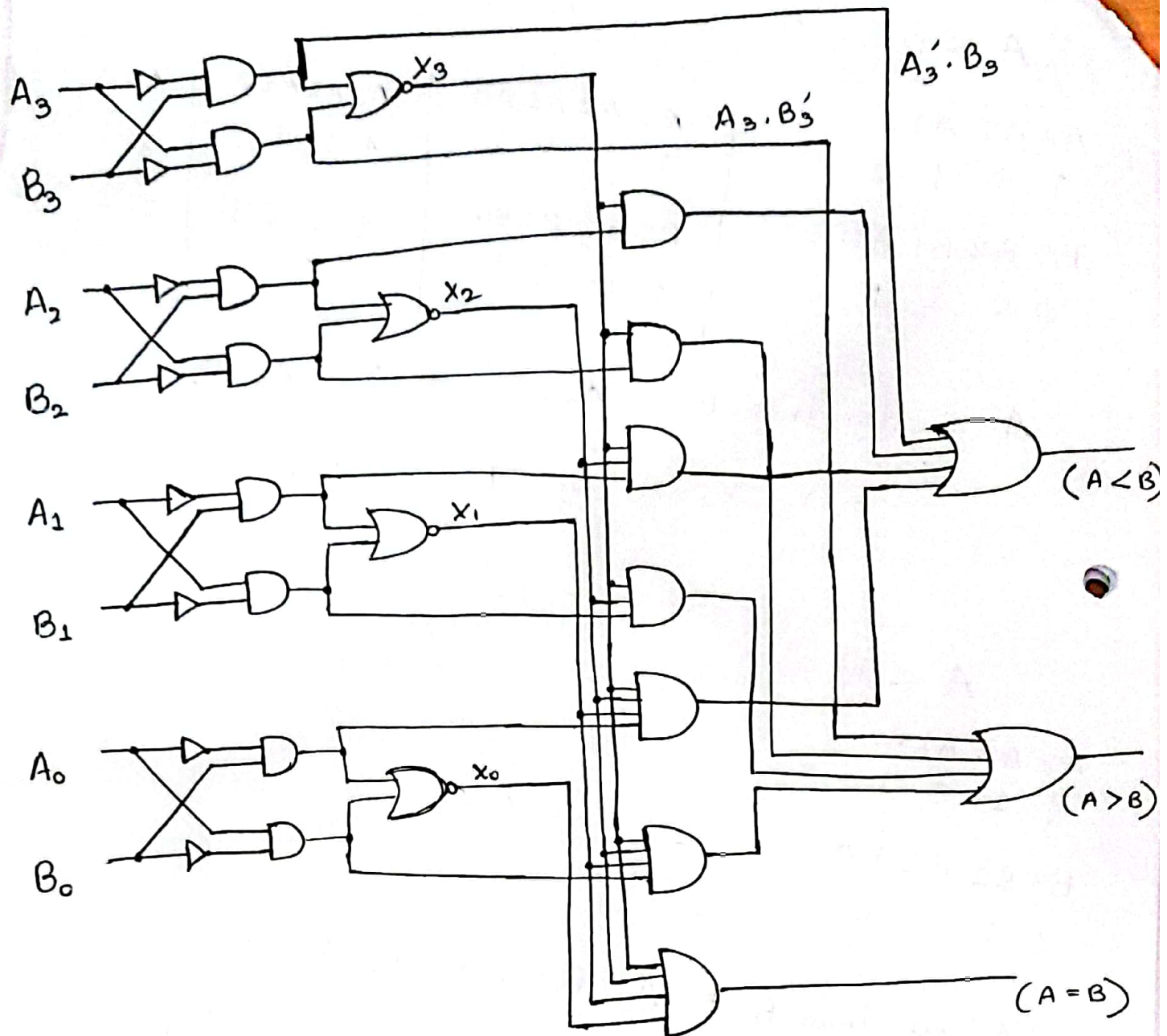
$$A \text{ greater than } B = A_3 \cdot B_3' + X_3 \cdot A_2 \cdot B_2' + X_3 \cdot X_2 \cdot A_1 \cdot B_1' + X_3 \cdot X_2 \cdot X_1 \cdot A_0 \cdot B_0'$$

$A < B$

$A_3 A_2 A_1 A_0$
1 1 0 1

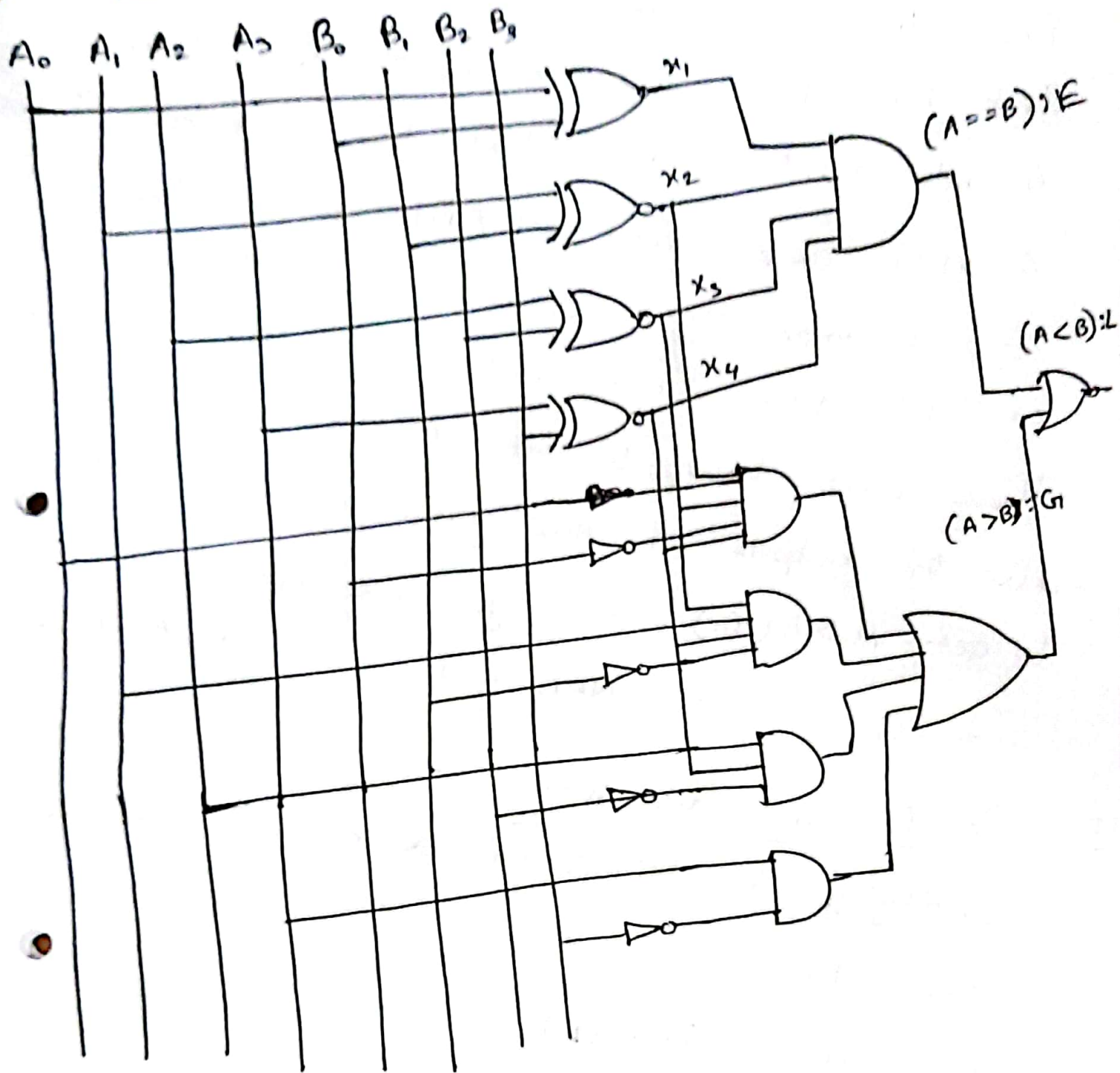
$B_3 B_2 B_1 B_0$
1 1 1 0

$$A \text{ less than } B = A_3' \cdot B_3 + X_3 \cdot A_2' \cdot B_2 + X_3 \cdot X_2 \cdot A_1' \cdot B_1 + X_3 \cdot X_2 \cdot X_1 \cdot A_0' \cdot B_0$$



OR

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⑥

From the diagram we can see that, there have been taken all the inputs from two, 4-bits number. After that, there was also taken 4 XNOR Gates and 4 AND Gates. Then, all of ~~them~~ these outputs we connected which we got from XNOR Gates with an AND Gate. These were taken to get $A = B (E)$. After that all the outputs of AND gates with an OR gate to get $A > B (G)$. Finally, we connected E and G with a NOR gate to get $A < B (L)$.

⑤ Results and discussion:
Justifying the design of a 4-bit magnitude Comparator.

i) For $A = B$, if: (E)

$$A_1 = B_1$$

$$A_2 = B_2$$

$$A_3 = B_3$$

$$A_4 = B_4$$

(7)

$$(A_1 = B_1) : x_1 = A_1' B_1' + A_1 B_1 = A_1 \cdot B_1 \quad \text{OR} \quad (A_2 = B_2)$$

$$\text{OR } (A_2 = B_2) : x_2 = A_2' B_2' + A_2 B_2 = A_2 \cdot B_2$$

$$\text{OR } (A_3 = B_3) : x_3 = A_3' B_3' + A_3 B_3 = A_3 \cdot B_3$$

$$\text{OR } (A_4 = B_4) : x_4 = A_4' B_4' + A_4 B_4 = A_4 \cdot B_4$$

$$\therefore (A = B) = x_1 \cdot x_2 \cdot x_3 \cdot x_4$$

ii) For $(A > B)$, if: (G)

$$(A_4 = 1, B_4 = 0) : A_4 \cdot B_4' \quad \text{OR} \quad (A_4 = B_4) \text{ and } (A_3 = 1, B_3 = 0)$$

$$\therefore x_4 \cdot A_3 \cdot B_3' \quad \text{OR} \quad (A_4 = B_4) \text{ and } (A_2 = 1, B_2 = 0) :$$

$$x_4 \cdot x_3 \cdot A_2 \cdot B_2' \quad \text{OR} \quad (A_4 = B_4) \text{ and } (A_3 = B_3)$$

and $(A_2 = B_2)$ and

$$(A_1 = 1 \text{ and } B_1 = 0) : x_4 \cdot x_3 \cdot x_2 \cdot A_1 \cdot B_1'$$

$$\therefore (A > B) = A_4 \cdot B_4' + x_4 \cdot A_3 \cdot B_3' + x_4 \cdot x_3 \cdot A_2 \cdot B_2' + x_4 \cdot x_3 \cdot x_2 \cdot A_1 \cdot B_1'$$

ii) For $(A < B)$ if : (L) .

$(A_4 = 0, B_4 = 1) : A'_4 \cdot B_4$ OR $(A_4 = B_4)$ and

$(A_3 = 0, B_3 = 1) : x_4 \cdot A_3 \cdot B_3$ OR $(A_4 = B_4)$ and

$(A_3 = B_3)$ and $(A_2 = 0, B_2 = 1) : x_4 \cdot x_3 \cdot A'_2 \cdot B_2$

OR $(A_4 = B_4)$ and $(A_3 = B_3)$ and $(A_2 = B_2)$

and $(A_1 = 0, B_1 = 1) : x_4 \cdot x_3 \cdot x_2 \cdot A'_1 \cdot B_1$

$$(A < B) = A'_4 \cdot B_4 + x_4 \cdot A'_3 \cdot B_3 + x_4 \cdot x_3 \cdot A'_2 \cdot B_2 + x_4 \cdot x_3 \cdot x_2 \cdot A'_1 \cdot B_1$$

The changes have to be made to find the 3rd result in the circuit design .

$$(A = B) : E = x_1 \cdot x_2 \cdot x_3 \cdot x_4$$

$$(A > B) : G = A_4 \cdot B'_4 + x_4 \cdot A_3 \cdot B'_3 + x_4 \cdot x_3 \cdot A_2 \cdot B'_2 + x_4 \cdot x_3 \cdot x_2 \cdot A_1 \cdot B'_1$$

$$(A < B) : L = A'_4 \cdot B_4 + x_4 \cdot A'_3 \cdot B_3 + x_4 \cdot x_3 \cdot A'_2 \cdot B_2 + x_4 \cdot x_3 \cdot x_2 \cdot A'_1 \cdot B_1$$

$$\therefore (A < B) = E'.G \Rightarrow L = (E + G)'$$

Implement Using NOR Gates:

$A > B$	$A == B$	$A < B$
0	0	1
0	1	0
1	0	0
1	1	Undefined