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# **AeroComBAT Documentation**

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## THE FEM INTERFACE MODULE

This module contains a basic environment for conducting finite element analysis.

The primary purpose of this library is to facilitate the creation of a FEM within the AeroComBAT package.

### SUMMARY OF THE CLASSES

- **Model:** The Model class has two main purposes. The first is that it is meant to serve as an organizational class. Once an aircraft part has been loaded into the model by using the `addAircraftPart()` method, the aircraft part can be loaded and constrained by the user. Once all parts have been loaded into the model and all loads and constraints have been applied, the user can choose to execute the `plotRigidModel()` method to visualize the model and make sure it accurately represents their problem. If the model appears as it should, the user can elect to run a static, buckling, normal mode, static aeroelastic, or dynamic flutter analysis.

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**Note:** Currently the only available part in the AeroComBAT package are wing parts, however this is likely to change as parts such as masses, fuselages and other types of aircraft parts are added.

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## 1.1 MODEL

`class AeroComBAT.FEM.Model`

Creates a Model which is used to organize and analyze FEM.

The primary use of Model objects are to organize FEM's and analyze them. The Model object doesn't create any finite elements. Instead, it loads aircraft parts which contain various types of finite element structural models as well as aerodynamic models. The type of model will depend on the type of aircraft part added. Once all of the models are created and added to the model object, the model object will serve as the analysis primary interface used to manipulate the generated model.

### Attributes

- **$K_g$  ( $DOF \times DOF$   $np.array[float]$ ):** This is the global stiffness matrix.
- **$K_{gr}$  ( $(DOF-CON) \times (DOF-CON)$   $np.array[float]$ ):** This is the global reduced stiffness matrix. In other words, the global stiffness matrix with the rows and columns corresponding to the constraints (CON) removed.
- **$F_g$  ( $DOF \times 1$   $np.array[float]$ ):** The global force vector.
- **$F_{gr}$  ( $(DOF-CON) \times 1$   $np.array[float]$ ):** The global reduced force vector. In other words, the global force vector with the rows corresponding to the constraints (CON) removed.
- **$M_g$  ( $DOF \times DOF$   $np.array[float]$ ):** The global mass matrix.
- **$M_{gr}$  ( $(DOF-CON) \times (DOF-CON)$   $np.array[float]$ ):** The global reduced mass matrix. In other words, the global mass matrix with the rows and columns corresponding to the constraints (CON) removed.

- Qg* (*DOFx1 np.array[float]*):** The global force boundary condition vector. This is where all of the nodal loads are stored before the system is assembled.
- nids* (*Array[int]*):** This array contains all of the node IDs used within the model.
- nodeDict* (*dict[NID,node]*):** This dictionary is a mapping of the node IDs used within the model to the corresponding node objects.
- elems* (*Array[obj]*):** This array contains all of the element objects used in the model.
- const* (*dict[NID,Array[DOF]]*):** This dictionary is a mapping of the node IDs constrained and the corresponding degrees of freedom that are constrained.
- parts* (*Array[int]*):** This array contains all of the part IDs corresponding to the parts that have been added to the model.

## Methods

- addElements*:** A method to add individual elements to the model.
- addAircraftParts*:** A method to add an Aircraft part to the model. This is a much more effective method than *addElements* as when a part is added, the model can utilize all of the organizational and post processing methods built into the part.
- resetPointLoads*:** A convenient way to reset all of the nodal loads in the model to zero.
- resetResults*:** A convenient way to clear the results in all of the elements from a previous analysis. This method is subject to change as the way in which results are stored is likely to change.
- applyLoads*:** A method to apply nodal loads as well as distributed loads to a range of elements, all of the elements in a part, or all of the elements in the model.
- applyConstraints*:** A method to apply nodal constraints to the model.
- staticAnalysis*:** A method which conducts a linear static analysis.
- normalModesAnalysis*:** A method which conducts a normal modes analysis on the model.
- plotRigidModel*:** A method to plot and visualize the model.
- plotDeformedModel*:** A method to plot and visualize the results from an analysis on the model.

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**Note:** When constraining nodes, only 0 displacement and rotation constraints are currently supported.

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### ***addAircraftParts* (*parts*)**

A method to add an array of aircraft parts to the model.

This method is a robust version of *addElements*. provided an array of part objects, this method will add the parts to the model. This includes adding all of the elements and nodes to the model, as well as a few other pieces of information.

#### **Args**

- parts* (*Array[obj]*):** An array of part objects.

#### **Returns**

- None



**addElement** (*elemarray*)

A method to add elements to the model.

Provided an array of elements, this method can add those elements to the model for analysis. This is a rather rudimentary method as the post processing methods utilized by the parts are not at the users disposal for the elements added to the model in this way.

**Args**

- elemarray (Array[obj]):** Adds all of the elements in the array to the model.

**Returns**

- None

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**Note:** Currently supported elements include: SuperBeam, Tbeam.

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**applyConstraints** (*NID, const*)

A method for applying nodal constraints to the model.

This method is the primary method for applying nodal constraints to the model.

**Args**

- NID (int):** The node ID of the node to be constrained.
- const (str, np.array[int]):** const can either take the form of a string in order to take advantage of the two most common constraints being 'pin' or 'fix'. If a different constraint needs to be applied, const could also be a numpy array listing the DOF (integers 1-6) to be constrained.

**Returns**

- None

**normalModesAnalysis** (*\*\*kwargs*)

Conducts normal mode analysis.

This method conducts normal mode analysis on the model. This will calculate all of the unknown frequency eigenvalues and eigenvectors for the model, which can be plotted later.

**Args**

- analysis\_name (str):** The string name to be associated with this analysis. By default, this is chosen to be 'analysis\_untitled'.

**Returns**

- None

---

**Note:** There are internal loads that are calculated and stored within the model elements, however be aware that these loads are meaningless and are only retained as a means to display cross section warping.

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**plotDeformedModel** (*\*\*kwargs*)

Plots the deformed model.

This method plots the deformed model results for a given analysis in the mayavi environment.

**Args**

- analysis\_name (str)*: The string identifier of the analysis.
- figName (str)*: The name of the figure. This is 'Rigid Model' by default.
- clr (1x3 tuple(int))*: The color tuple or RGB values to be used for plotting the reference axis for all beam elements. By default this color is black.
- numXSects (int)*: The number of cross-sections desired to be plotted for all wing sections. The default is 2.
- contour (str)*: A string keyword to determine what analysis should be plotted.
- contLim (1x2 Array[float])*: An array containing the lower and upper contour limits.
- warpScale (float)*: The scaling factor used to magnify the cross section warping displacement factor.
- displScale (float)*: The scaling factor used to magnify the beam element displacements and rotations.
- mode (int)*: If the analysis name refers to a modal analysis, mode refers to which mode from that analysis should be plotted.

**Returns**

- mayavi figure

**plotRigidModel** (*\*\*kwargs*)

Plots the rigid model.

This method plots the rigid model in the mayavi environment.

**Args**

- figName (str)*: The name of the figure. This is 'Rigid Model' by default.
- clr (1x3 tuple(int))*: The color tuple or RGB values to be used for plotting the reference axis for all beam elements. By default this color is black.
- numXSects (int)*: The number of cross-sections desired to be plotted for all wing sections. The default is 2.

**Returns**

- mayavi figure

**resetPointLoads** ()

A method to reset the point loads applied to the model.

This is a good method to reset the nodal loads applied to a model. This method will be useful when attempting to apply a series different analysis.

**Args**

- None

**Returns**

- None

**resetResults ()**

A method to reset the results in a model.

This is a good method to reset the results in the model from a given analysis. This method will be useful when attempting to apply a series different analysis.

**Args**

- None

**Returns**

- None

**staticAnalysis (\*\*kwargs)**

Linear static analysis.

This method conducts a linear static analysis on the model. This will calculate all of the unknown displacements in the model, and save not only displacements, but also internal forces and moments in all of the beam elements.

**Args**

- analysis\_name (str):** The string name to be associated with this analysis. By default, this is chosen to be 'analysisUntitled'.

**Returns**

- None



## THE STRUCTURES MODULE

This module contains a library of classes devoted to structural analysis.

The primary purpose of this library is to facilitate the ROM (reduced order modeling) of structures that can be simplified to beams. The real power of this library comes from its `XSect` class. This class can create and analyze a cross-section, allowing the user to accurately model a nonhomogeneous (made of multiple materials) anisotropic (materials that behave anisotropically such as composites) complex cross-sections.

It should be noted that classes are ordered by model complexity. The further down the `structures.py` library, the more complex the objects, often requiring multiple of their predecessors. For example, the `CQUAD4` class requires four node objects and a material object.

### SUMMARY OF THE CLASSES

- *Node*: Creates a node object with 3D position.
- *Material*: Creates a material object, generating the 3D constitutive relations.
- *MicroMechanics*: **Class to facilitate the calculation of composite stiffnesses** using micro-mechanical models where fibers are long and continuous.
- *CQUAD4*: **Creates a 2D linear quadrilateral element, mainly used to facilitate cross-sectional analysis, this class could be used** such that they could also be used to create plate or laminate element objects as well.
- *MaterialLib*: **Creates a material library object meant to hold many material** objects.
- *Ply*: Creates ply objects which are used in the building of a laminate object.
- *Laminate*: **Creates laminate objects which could be used for CLT (classical lamination theory) analysis as well as to be used in building a beam cross-section.**
- *XSect*: **Creates a cross-section object which can be used in the ROM of a beam** with a non-homogeneous anisotropic cross-section. Currently only supports simple box beam cross-section (i.e., four laminates joined together to form a box), however outer mold lines can take the shape of airfoil profiles. See the `Airfoil` class in `AircraftParts.py` for more info.
- *TBeam*: Creates a single Timoshenko beam object for FEA.
- *SuperBeam*: **Creates a super beam object. This class is mainly used to automate** the creation of many connected `TBeam` objects to be used later for FEA.
- *WingSection*: **A class which creates and holds many super beams, each of which** could have different cross-sections. It also helps to dimensionalize plates for simple closed-form composite buckling load approximations.

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**Note:** Currently the inclusion of thermal strains are not supported for any structural model.

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## 2.1 NODE

**class** AeroComBAT.Structures.**Node** (*nid*, *x*)

Creates a node object.

Node objects could be used in any finite element implementation.

### Attributes

- NID* (*int*): The integer identifier given to the object.
- x* (*Array[float]*): An array containing the 3 x-y-z coordinates of the node.
- summary* (*str*): A string which is a tabulated representation and summary of the important attributes of the object.

### Methods

- printSummary*: This method prints out basic information about the node object, such as it's node ID and it's x-y-z coordinates

**\_\_init\_\_** (*nid*, *x*)

Initializes the node object.

### Args

- nid* (*int*): The desired integer node ID
- x* (*Array[float]*): The position of the node in 3D space.

**printSummary** ()

Prints basic information about the node.

The printSummary method prints out basic node attributes in an organized fashion. This includes the node ID and x-y-z global coordinates.

### Args

- None

### Returns

- A printed table including the node ID and it's coordinates

## 2.2 MATERIAL

**class** AeroComBAT.Structures.**Material** (*MID*, *name*, *matType*, *mat\_constants*, *mat\_t*, *\*\*kwargs*)

creates a linear elastic material object.

This class creates a material object which can be stored within a material library object. The material can be in general orthotropic.

### Attributes

- name* (*str*): A name for the material.
- MID* (*int*): An integer identifier for the material.

- matType (str):** A string expressing what type of material it is. Currently, the supported materials are isotropic, transversely isotropic, and orthotropic.
- summary (str):** A string which is a tabulated representation and summary of the important attributes of the object.
- t (float):** A single float which represents the thickness of a ply if the material is to be used in a composite.
- rho (float):** A single float which represents the density of the material.
- Smat (6x6 numpy Array[float]):** A numpy array representing the compliance matrix in the fiber coordinate system.\*
- Cmat (6x6 numpy Array[float]):** A numpy array representing the stiffness matrix in the fiber coordinate system.\*

### Methods

- printSummary:** This method prints out basic information about the material, including the type, the material constants, material thickness, as well as the tabulated stiffness or compliance matrices if requested.

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**Note:** The CQUAD4 element assumes that the fibers are oriented along the (1,0,0) in the global coordinate system.

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\_\_init\_\_ (MID, name, matType, mat\_constants, mat\_t, \*\*kwargs)

Creates a material object

The main purpose of this class is assembling the constitutive relations. Regardless of the analysis

### Args

- MID (int):** Material ID.
- name (str):** Name of the material.
- matType (str):** The type of the material. Supported material types are “iso”, “trans\_iso”, and “ortho”.
- mat\_constants (1xN Array[Float]):** The requisite number of material constants required for any structural analysis. Note, this array includes the material density. For example, an isotropic material needs 2 elastic material constants, so the total length of mat\_constants would be 3, 2 elastic constants and the density.
- mat\_t (float):** The thickness of 1-ply of the material
- th (1x3 Array[float]):** The angles about which the material can be rotated when it is initialized. In degrees.

### Returns

- None

---

**Note:** While this class supports material direction rotations, it is more robust to simply let the CQUAD4 and Mesher class handle all material rotations.

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**printSummary** (*\*\*kwargs*)

Prints a tabulated summary of the material.

This method prints out basic information about the material, including the type, the material constants, material thickness, as well as the tabulated stiffness or compliance matrices if requested.

#### Args

- compliance** (*str*): A boolean input to signify if the **compliance** matrix should be printed.
- stiffness** (*str*): A boolean input to signify if the **stiffness matrix** should be printed.

#### Returns

- String print out containing the material name, as well as **material** constants and other defining material attributes. If requested this includes the material stiffness and compliance matrices.

## 2.3 CQUAD4

**class** AeroComBAT.Structures.**CQUAD4** (*EID, nodes, MID, matLib, \*\*kwargs*)

Creates a linear, 2D 4 node quadrilateral element object.

The main purpose of this class is to assist in the cross-sectional analysis of a beam, however it COULD be modified to serve as an element for 2D plate or laminate FE analysis.

#### Attributes

- type** (*str*): A string designating it a CQUAD4 element.
- xsect** (*bool*): States whether the element is to be used in cross- sectional analysis.
- th** (*1x3 Array[float]*): Array containing the Euler-angles expressing how the element constitutive relations should be rotated from the material fiber frame to the global CSYS. In degrees.
- EID** (*int*): An integer identifier for the CQUAD4 element.
- MID** (*int*): An integer referencing the material ID used for the constitutive relations.
- NIDs** (*1x4 Array[int]*): Contains the integer node identifiers for the node objects used to create the element.
- nodes** (*1x4 Array[obj]*): Contains the properly ordered nodes objects used to create the element.
- xs** (*1x4 np.array[float]*): Array containing the x-coordinates of the nodes used in the element
- ys** (*1x4 np.array[float]*): Array containing the y-coordinates of the nodes used in the element
- rho** (*float*): Density of the material used in the element.
- mass** (*float*): Mass per unit length (or thickness) of the element.
- U** (*12x1 np.array[float]*): This column vector contains the CQUAD4s 3 DOF (x-y-z) displacements in the local xsect CSYS due to cross- section warping effects.
- Eps** (*6x4 np.array[float]*): A matrix containing the 3D strain state within the CQUAD4 element.
- Sig** (*6x4 np.array[float]*): A matrix containing the 3D stress state within the CQUAD4 element.

#### Methods

- x**: Calculates the local xsect x-coordinate provided the desired master coordinates eta and xi.



- y**: Calculates the local xsect y-coordinate provided the desired master coordinates eta and xi.
- J**: Calculates the jacobian of the element provided the desired master coordinates eta and xi.
- resetResults**: Initializes the displacement (U), strain (Eps), and stress (Sig) attributes of the element.
- getDeformed**: Provided an analysis has been conducted, this method returns  $3 \times 2 \times 2$  np.array[float] containing the element warped displacements in the local xsect CSYS.
- getStressState**: Provided an analysis has been conducted, this method returns  $3 \times 2 \times 2$  np.array[float] containing the element stress at four points. The 3D stress state is processed to return the Von-Mises or Maximum Principal stress state.
- printSummary**: Prints out a tabulated form of the element ID, as well as the node ID's referenced by the element.

**J** (eta, xi)

Calculates the jacobian at a point in the element.

This method calculates the jacobian at a local point within the element provided the master coordinates eta and xi.

#### Args

- eta** (float): The eta coordinate in the master coordinate domain.\*
- xi** (float): The xi coordinate in the master coordinate domain.\*

#### Returns

- Jmat** ( $3 \times 3$  np.array[float]): The stress-resulant transformation array.

---

**Note:** Xi and eta can both vary between -1 and 1 respectively.

---

**\_\_init\_\_** (EID, nodes, MID, matLib, \*\*kwargs)

Initializes the element.

#### Args

- EID** (int): An integer identifier for the CQUAD4 element.
- nodes** ( $1 \times 4$  Array[obj]): Contains the properly ordered nodes objects used to create the element.
- MID** (int): An integer refrencing the material ID used for the constitutive relations.
- matLib** (obj): A material library object containing a dictionary with the material corresponding to the provided MID.
- xsect** (bool): A boolean to determine whether this quad element is to be usedfor cross-sectional analysis. Default value is True.
- th** ( $1 \times 3$  Array[float]): Array containing the Euler-angles expressing how the element constitutive relations should be rotated from the material fiber frame to the global CSYS. In degrees.

#### Returns

- None

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**Note:** The reference coordinate system for cross-sectional analysis is a

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local coordinate system in which the x and y axes are planer with the element, and the z-axis is perpendicular to the plane of the element.

**getDeformed** (*\*\*kwargs*)

Returns the warping displacement of the element.

Provided an analysis has been conducted, this method returns 3 2x2 np.array[float] containing the element warped displacements in the local xsect CSYS.

**Args**

- warpScale (float):** A multiplicative scaling factor intended to exaggerate the warping displacement within the cross-section.

**Returns**

- xdef (2x2 np.array[float]):** warped x-coordinates at the four corner points.
- ydef (2x2 np.array[float]):** warped y-coordinates at the four corner points.
- zdef (2x2 np.array[float]):** warped z-coordinates at the four corner points.

**getStressState** (*crit='VonMis'*)

Returns the stress state of the element.

Provided an analysis has been conducted, this method returns a 2x2 np.array[float] containing the element the 3D stress state at the four guass points by default.\*

**Args**

- crit (str):** Determines what criteria is used to evaluate the 3D stress state at the sample points within the element. By default the Von Mises stress is returned. Currently supported options include: Von Mises ('VonMis'), maximum principle stress ('MaxPrin'), and the minimum principle stress ('MinPrin').

**Returns**

- sigData (2x2 np.array[float]):** The stress state evaluated at four points within the CQUAD4 element.

---

**Note:** The Xsect method calcWarpEffects is what determines where strain

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and stresses are sampled. By default it samples this information at the Guass points where the stress/strain will be most accurate.

**printSummary** ()

A method for printing a summary of the CQUAD4 element.

Prints out a tabulated form of the element ID, as well as the node ID's referenced by the element.

**Args**

- None

**Returns**

- (str): Prints the tabulated EID, node IDs and material IDs associated** with the CQUAD4 element.

**resetResults ()**

Resets stress, strain and warping displacement results.

Method is mainly intended to prevent results for one analysis or sampling location in the matrix to effect the results in another.

**Args**

- None

**Returns**

- None

***x* (eta, xi)**

Calculate the x-coordinate within the element.

Calculates the local xsect x-coordinate provided the desired master coordinates eta and xi.

**Args**

- eta (float)*: The eta coordinate in the master coordinate domain.\*
- xi (float)*: The xi coordinate in the master coordinate domain.\*

**Returns**

- float*: The x-coordinate within the element.

---

**Note:** Xi and eta can both vary between -1 and 1 respectively.

---

***y* (eta, xi)**

Calculate the y-coordinate within the element.

Calculates the local xsect y-coordinate provided the desired master coordinates eta and xi.

**Args**

- eta (float)*: The eta coordinate in the master coordinate domain.\*
- xi (float)*: The xi coordinate in the master coordinate domain.\*

**Returns**

- (float)*: The y-coordinate within the element.

---

**Note:** Xi and eta can both vary between -1 and 1 respectively.

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## 2.4 MATERIAL LIBRARY

**class** AeroComBAT.Structures.**MaterialLib**

Creates a material library object.

This material library holds the materials to be used for any type of analysis. Furthermore, it can be used to generate new material objects to be automatically stored within it. See the Material class for supported material types.

### Attributes

- matDict (dict):** A dictionary which stores material objects as the values with the MIDs as the associated keys.

### Methods

- addMat:** Adds a material to the MaterialLib object dictionary.
- getMat:** Returns a material object provided an MID
- printSummary:** Prints a summary of all of the materials held within the matDict dictionary.

**\_\_init\_\_** ()

Initialize MaterialLib object.

The initialization method is mainly used to initialize a dictionary which houses material objects.

### Args

- None

### Returns

- None

**addMat** (MID, mat\_name, mat\_type, mat\_constants, mat\_t, *\*\*kwargs*)

Add a material to the MaterialLib object.

This is the primary method of the class, used to create new material objects and then add them to the library for later use.

### Args

- MID (int):** Material ID.
- name (str):** Name of the material.
- matType (str):** The type of the material. Supported material types are “iso”, “trans\_iso”, and “ortho”.
- mat\_constants (1xX Array[Float]):** The requisite number of material constants required for any structural analysis. Note, this array includes the material density. For example, an isotropic material needs 2 elastic material constants, so the total length of mat\_constants would be 3, 2 elastic constants and the density.
- mat\_t (float):** The thickness of 1-ply of the material
- th (1x3 Array[float]):** The angles about which the material can be rotated when it is initialized. In degrees.

- overwrite (bool):** Input used in order to define whether the material being added can overwrite another material already held by the material library with the same MID.

#### Returns

- None

#### **getMat** (MID)

Method that returns a material from the material library

#### Args

- MID (int):** The ID of the material which is desired

#### Returns

- (obj): A material object associated with the key MID

#### **printSummary** ()

Prints summary of all Materials in MaterialLib

A method used to print out tabulated summary of all of the materials held within the material library object.

Args: - None

Returns: - (str): A tabulated summary of the materials.

## 2.5 PLY

### **class** AeroComBAT.Structures.**Ply** (Material, th)

Creates a CLT ply object.

A class inspired by CLT, this class can be used to generate laminates to be used for CLT or cross-sectional analysis. It is likely that ply objects won't be created individually and then assembled into a laminate. More likely is that the plies will be generated within the laminate object. It should also be noted that it is assumed that the materials used are effectively at most transversely isotropic.

#### Attributes

- E1 (float):** Stiffness in the fiber direction.
- E2 (float):** Stiffness transverse to the fiber direction.
- nu\_12 (float):** In plane poisson ratio.
- G\_12 (float):** In plane shear modulus.
- t (float):** Thickness of the ply.
- Qbar (1x6 np.array[float]):** The terms in the rotated, reduced stiffness matrix. Ordering is as follows: [Q11,Q12,Q16,Q22,Q26,Q66]
- MID (int):** An integer referencing the material ID used for the constitutive relations.
- th (float):** The angle about which the fibers are rotated in the plane in degrees.

#### Methods

•**genQ**: Given the in-plane stiffnesses used by the material of the ply, the method calculates the terms of the reduced stiffness matrix.

•**printSummary**: This prints out a summary of the object, including thickness, referenced MID and in plane angle orientation theta in degrees.

`__init__(Material, th)`

Initializes the ply.

This method initializes information about the ply such as in-plane stiffness response.

#### Args

•**Material (obj)**: A material object, most likely coming from a material library.

•**th (float)**: The angle about which the fibers are rotated in the plane in degrees.

#### Returns

•None

`genQ(E1, E2, nu12, G12)`

A method for calculating the reduced compliance of the ply.

Intended primarily as a private method but left public, this method, for those unfamiliar with CLT, calculates the terms in the reduced stiffness matrix given the in plane ply stiffnesses. It can be thus inferred that this requires the assumption of plane stress. This method is primarily used during the ply instantiation.

#### Args

•**E1 (float)**: The fiber direction stiffness.

•**E2 (float)**: The stiffness transverse to the fibers.

•**nu12 (float)**: The in-plane poisson ratio.

•**G12 (float)**: The in-plane shear stiffness.

#### Returns

•**(1x4 np.array[float])**: The terms used in the reduced stiffness matrix. The ordering is: [Q11, Q12, Q22, Q66].

`printSummary()`

Prints a summary of the ply object.

A method for printing a summary of the ply properties, such as the material ID, fiber orientation and ply thickness.

#### Args

•None

#### Returns

•**(str)**: Printed tabulated summary of the ply.

## 2.6 LAMINATE

**class** AeroComBAT.Structures.**Laminate**(*n\_i\_tmp*, *m\_i\_tmp*, *matLib*, *\*\*kwargs*)

Creates a CLT laminate object.

This class has two main uses. It can either be used for CLT analysis, or it can be used to build up a 2D mesh for a discretized cross-section.

### Attributes

- **mesh** (*NxM np.array[int]*): This 2D array holds NIDs and is used to represent how nodes are organized in the 2D cross-section of the laminate.
- **xmesh** (*NxM np.array[int]*): This 2D array holds the rigid x-coordinates of the nodes within the 2D discretization of the laminate on the local xsect CSYS.
- **ymesh** (*NxM np.array[int]*): This 2D array holds the rigid y-coordinates of the nodes within the 2D discretization of the laminate on the local xsect CSYS.
- **zmesh** (*NxM np.array[int]*): This 2D array holds the rigid z-coordinates of the nodes within the 2D discretization of the laminate on the local xsect CSYS.
- **H** (*float*): The total laminate thickness.
- **rho\_A** (*float*): The laminate area density.
- **plies** (*1xN array[obj]*): Contains an array of ply objects used to construct the laminate.
- **t** (*1xN array[float]*): An array containing all of the ply thicknesses.
- **ABD** (*6x6 np.array[float]*): The CLT 6x6 matrix relating in-plane strains and curvatures to in-plane force and moment resultants.
- **abd** (*6x6 np.array[float]*): The CLT 6x6 matrix relating in-plane forces and moments resultants to in-plane strains and curvatures.
- **z** (*1xN array[float]*): The z locations of laminate starting and ending points. This system always starts at -H/2 and goes to H/2
- **equivMat** (*obj*): This is orthotropic material object which exhibits similar in-plane stiffnesses.
- **forceRes** (*1x6 np.array[float]*): The applied or resulting force and moment resultants generated during CLT analysis.
- **globalStrain** (*1x6 np.array[float]*): The applied or resulting strain and curvatures generated during CLT analysis.

### Methods

- **printSummary**: This method prints out defining attributes of the laminate, such as the ABD matrix and layup schedule.

**\_\_init\_\_**(*n\_i\_tmp*, *m\_i\_tmp*, *matLib*, *\*\*kwargs*)

Initializes the Laminate object

The way the laminate initialization works is you pass in two-three arrays and a material library. The first array contains information about how many plies you want to stack, the second array determines what material should be used for those plies, and the third array determines at what angle those plies lie. The class was developed this way as a means to facilitate laminate optimization by quickly changing the number of plies at a given orientation and using a given material.

### Args

- ***n\_i\_tmp* (1xN array[int]):** An array containing the number of plies using a material at a particular orientation such as: (theta=0,theta=45...)
- ***m\_i\_tmp* (1xN array[int]):** An array containing the material to be used for the corresponding number of plies in the *n\_i\_tmp* array
- ***matLib* (obj):** The material library holding different material objects.
- ***sym* (bool):** Whether the laminate is symmetric. (False by default)
- ***th* (1xN array[float]):** An array containing the orientation at which the fibers are positioned within the laminate.

#### Returns

- None

---

**Note:** If you wanted to create a [0\_2/45\_2/90\_2/-45\_2]\_s laminate of the same material, you could call laminate as:

```
lam = Laminate([2,2,2,2],[1,1,1,1],matLib,sym=True)
```

Or:

```
lam = Laminate([2,2,2,2],[1,1,1,1],matLib,sym=True,th=[0,45,90,-45])
```

Both of these statements are equivalent. If no theta array is provided and *n\_i\_tmp* is not equal to 4, then Laminate will default your fibers to all be running in the 0 degree orientation.

---

#### **printSummary** (*\*\*kwargs*)

Prints a summary of information about the laminate.

This method can print both the ABD matrix and ply information schedule of the laminate.

#### Args

- ***ABD* (bool):** This optional argument asks whether the ABD matrix should be printed.
- ***decimals* (int):** Should the ABD matrix be printed, python should print up to this many digits after the decimal point.
- ***plies* (bool):** This optional argument asks whether the ply schedule for the laminate should be printed.

#### Returns

- None

## 2.7 MESHER

**class** AeroComBAT.Structures.Mesher

Meshes cross-section objects

This class is used to discretize cross-sections provided laminate objects. Currently only two cross-sectional shapes are supported. The first is a box beam using an airfoil outer mold line, and the second is a hollow tube using as many laminates as desired. One of the main results is the population of the nodeDict and elemDict attributes for the cross-section.

#### Attributes



- None

### Methods

- boxBeam**: Taking several inputs including 4 laminate objects and meshes a 2D box beam cross-section.
- cylindricalTube**: Taking several inputs including n laminate objects and meshes a 2D cylindrical tube cross-section.

**boxBeam** (*xsect*, *meshSize*, *x0*, *xf*, *matlib*)

Meshes a box beam cross-section.

This method is currently the only supported and tested meshing method. The mesher assumes that the laminates in the box beam are oriented such that the top surfaces of the laminate are facing inwards. Therefore if you would like a particular fiber orientation on the outter or inner most surfaces, create your laminate layup schedules appropriately.

### Args

- xsect** (*obj*): The cross-section object to be meshed.
- meshSize** (*int*): The maximum aspect ratio an element can have
- x0** (*float*): The non-dimensional starting point of the cross-section on the airfoil.
- xf** (*float*): The non-dimesnional ending point of the cross-section on the airfoil.
- matlib** (*obj*): The material library object used to create CQUAD4 elements.

### Returns

- None

## 2.8 CROSS-SECTION

**class** AeroComBAT.Structures.XSect (*XID*, *Airfoil*, *xdim*, *laminates*, *matlib*, *\*\*kwargs*)

Creates a beam cross-section object,

This cross-section can be made of multiple materials which can be in general anisotropic. This is the main workhorse within the structures library.

### Attributes

- Color** (*touple*): A length 3 touple used to define the color of the cross-section.
- Airfoil** (*obj*): The airfoil object used to define the OML of the cross-section.
- typeXSect** (*str*): Defines what type of cross-section is to be used. Currently the only supported type is 'box'.
- normalVector** (*1x3 np.array[float]*): Expresses the normal vector of the cross-section.
- nodeDict** (*dict*): A dictionary of all nodes used to descretize the cross-section surface. The keys are the NIDs and the values stored are the Node objects.
- elemDict** (*dict*): A dictionary of all elements used to descretize the cross-section surface. the keys are the EIDs and the values stored are the element objects.

- **$X$  ( $ndx6$  *np.array[float]*):** A very large 2D array. This is one of the results of the cross-sectional analysis. This array relays the force and moment resultants applied to the cross-section to the nodal warping displacements exhibited by the cross-section.
- **$Y$  ( $6x6$  *np.array[float]*):** This array relays the force and moment resultants applied to the cross-section to the rigid section strains and curvatures exhibited by the cross-section.
- **$dXdz$  ( $ndx6$  *np.array[float]*):** A very large 2D array. This is one of the results of the cross-sectional analysis. This array relays the force and moment resultants applied to the cross-section to the gradient of the nodal warping displacements exhibited by the cross-section with respect to the beam axis.
- **$xt$  (*float*):** The x-coordinate of the tension center (point at which tension and bending are decoupled)
- **$yt$  (*float*):** The y-coordinate of the tension center (point at which tension and bending are decoupled)
- **$xs$  (*float*):** The x-coordinate of the shear center (point at which shear and torsion are decoupled)
- **$ys$  (*float*):** The y-coordinate of the shear center (point at which shear and torsion are decoupled)
- **$refAxis$  ( $3x1$  *np.array[float]*):** A column vector containing the reference axis for the beam.
- **$bendAxes$  ( $2x3$  *np.array[float]*):** Contains two row vectors about which bending from one axis is decoupled from bending about the other.
- **$F\_raw$  ( $6x6$  *np.array[float]*):** The 6x6 compliance matrix that results from cross-sectional analysis. This is the case where the reference axis is at the origin.
- **$K\_raw$  ( $6x6$  *np.array[float]*):** The 6x6 stiffness matrix that results from cross-sectional analysis. This is the case where the reference axis is at the origin.
- **$F$  ( $6x6$  *np.array[float]*):** The 6x6 compliance matrix for the cross-section about the reference axis. The reference axis is by default at the shear center.
- **$K$  ( $6x6$  *np.array[float]*):** The 6x6 stiffness matrix for the cross-section about the reference axis. The reference axis is by default at the shear center.
- **$T1$  ( $3x6$  *np.array[float]*):** The transformation matrix that converts strains and curvatures from the local xsect origin to the reference axis.
- **$T2$  ( $3x6$  *np.array[float]*):** The transformation matrix that converts forces and moments from the local xsect origin to the reference axis.
- **$x\_m$  ( $1x3$  *np.array[float]*):** Center of mass of the cross-section about in the local xsect CSYS
- **$M$  ( $6x6$  *np.array[float]*):** This mass matrix relays linear and angular velocities to linear and angular momentum of the cross-section.

## Methods

- **`resetResults`:** This method resets all results (displacements, strains and stresses) within the elements used by the cross-section object.
- **`calcWarpEffects`:** Given applied force and moment resultants, this method calculates the warping displacement, 3D strains and 3D stresses within the elements used by the cross-section.
- **`printSummary`:** This method is used to print characteristic attributes of the object. This includes the elastic, shear and mass centers, as well as the stiffness matrix and mass matrix.
- **`plotRigid`:** This method plots the rigid cross-section shape, typically in conjunction with a full beam model.
- **`plotWarped`:** This method plots the warped cross-section including a contour criteria, typically in conjunction with the results of the displacement of a full beam model.

`__init__` (*XID, Airfoil, xdim, laminates, matlib, \*\*kwargs*)

Instantiates a cross-section object.

The constructor for the class is effectively responsible for creating the 2D descretized mesh of the cross-section. It is important to note that while meshing technically occurs in the constructor, the work is handed by another class altogether. While not computationally heavily intensive in itself, it is responsible for creating all of the framework for the cross-sectional analysis.

#### Args

- *XID (int)*: The cross-section integer identifier.
- *Airfoil (obj)*: An airfoil object used to determine the OML shape of the cross-section.
- *xdim (1x2 array[float])*: The non-dimensional starting and stoping points of the cross-section. In other words, if you wanted to have your cross-section start at the 1/4 chord and run to the 3/4 chord of your airfoil, xdim would look like `xdim=[0.25,0.75]`
- *laminates (1xN array[obj])*: Laminate objects used to create the descretized mesh surface. Do not repeat a laminate within this array! It will reference this object multiple times and not mesh the cross-section properly then!
- *matlib (obj)*: A material library
- *typeXSect (str)*: The general shape the cross-section should take. Note that currently only a box beam profile is supported. More shapes and the ability to add stiffeners to the cross-section will come in later updates.
- *meshSize (int)*: The maximum aspect ratio you would like your 2D CQUAD4 elements to exhibit within the cross-section.

#### Returns

- None

`calcWarpEffects` (*\*\*kwargs*)

Calculates displacements, stresses, and strains for applied forces

The second most powerful method of the XSect class. After an analysis is run, the FEM class stores force and moment resultants within the beam element objects. From there, warping displacement, strain and stress can be determined within the cross-section at any given location within the beam using this method. This method will take a while though as it has to calculate 4 displacements and 24 stresses and strains for every element within the cross-section. Keep that in mind when you are surveying your beam or wing for displacements, stresses and strains.

#### Args

- *force (6x1 np.array[float])*: This is the internal force and moment resultant experienced by the cross-section.

#### Returns

- None

`plotRigid` (*\*\*kwargs*)

Plots the rigid cross-section along a beam.

This method is very useful for visually debugging a structural model. It will plot out the rigid cross-section in 3D space with regards to the reference axis.

### Args

- ***x* (*1x3 np.array[float]*)**: The rigid location on your beam you are trying to plot:
- ***beam\_axis* (*1x3 np.array[float]*)**: The vector pointing in the direction of your beam axis.
- ***figName* (*str*)**: The name of the figure.
- ***wireMesh* (*bool*)**: A boolean to determine if the wiremesh outline should be plotted.\*

### Returns

- (*fig*): Plots the cross-section in a mayavi figure.

---

**Note:** Because of how the mayavi wireframe keyword works, it will

---

appear as though the cross-section is made of triangles as opposed to quadrilaterals. Fear not! They are made of quads, the wireframe is just plotted as triangles.

### **plotWarped** (*\*\*kwargs*)

Plots the warped cross-section along a beam.

Once an analysis has been completed, this method can be utilized in order to plot the results anywhere along the beam.

### Args

- ***displScale* (*float*)**: The scale by which all rotations and displacements will be multiplied in order to make it visually easier to detect displacements.
- ***x* (*1x3 np.array[float]*)**: The rigid location on your beam you are trying to plot:
- ***U* (*1x6 np.array[float]*)**: The rigid body displacements and rotations experienced by the cross-section.
- ***beam\_axis* (*1x3 np.array[float]*)**: The vector pointing in the direction of your beam axis.
- ***contour* (*str*)**: Determines what value is to be plotted during as a contour in the cross-section.
- ***figName* (*str*)**: The name of the figure.
- ***wireMesh* (*bool*)**: A boolean to determine if the wiremesh outline should be plotted.\*
- ***contLim* (*1x2 array[float]*)**: Describes the upper and lower bounds of contour color scale.
- ***warpScale* (*float*)**: The scaling factor by which all warping displacements in the cross-section will be multiplied.

### Returns

- (*fig*): Plots the cross-section in a mayavi figure.

---

**Note:** Because of how the mayavi wireframe keyword works, it will

---

appear as though the cross-section is made of triangles as opposed to quadrilaterals. Fear not! They are made of quads, the wireframe is just plotted as triangles.

**printSummary** (*refAxis=True, decimals=8, \*\*kwargs*)

Print characteristic information about the cross-section.

This method prints out characteristic information about the cross-section objects. By default, the method will print out the location of the reference axis, the shear, tension, and mass center. This method if requested will also print the stiffness and mass matrices.

#### Args

- **refAxis (bool): Boolean to determine if the stiffness matrix** printed should be about the reference axis (True) or about the local xsect origin (False).
- **stiffMat (bool): Boolean to determine if the stiffness matrix** should be printed.
- **tensCntr (bool): Boolean to determine if the location of the tension** center should be printed.
- **shearCntr (bool): Boolean to determine if the location of the shear** center should be printed.
- **massCntr (bool): Boolean to determine if the location of the mass** center should be printed.
- **refAxisLoc (bool): Boolean to determine if the location of the** reference axis should be printed.

#### Returns

- (*str*): Prints out a string of information about the cross-section.

## 2.9 TIMOSHENKO BEAM

**class** AeroComBAT.Structures.**TBeam** (*x1, x2, xsect, EID=0, SBID=0, nid1=0, nid2=1*)

Creates a Timoshenko beam finite element object.

The primary beam finite element used by AeroComBAT, this beam element is similar to the Euler-Bernoulli beam finite element most are familiar with, with the exception that it has the ability to experience shear deformation in addition to just bending.

#### Attributes

- **type (str):**String describing the type of beam element being used.
- **U1 (dict): This dictionary contains the results of an analysis set.** The keys are the string names of the analysis and the values stored are 6x1 np.array[float] vectors containing the 3 displacements and 3 rotations at the first node.
- **U2 (dict): This dictionary contains the results of an analysis set.** The keys are the string names of the analysis and the values stored are 6x1 np.array[float] vectors containing the 3 displacements and 3 rotations at the second node.
- **Umode1 (dict): This dictionary contains the results of a modal analysis** set. The keys are the string names of the analysis and the values stored are 6xN np.array[float]. The columns of the array are the displacements and rotations at the first node associated with the particular mode.
- **Umode2 (dict): This dictionary contains the results of a modal analysis** set. The keys are the string names of the analysis and the values stored are 6xN np.array[float]. The columns of the array are the displacements and rotations at the second node associated with the particular mode.
- **F1 (dict): This dictionary contains the results of an analysis set.** The keys are the string names of the analysis and the values stored are 6x1 np.array[float] vectors containing the 3 internal forces and 3 moments at the first node.

- F2 (dict):** This dictionary contains the results of an analysis set. The keys are the string names of the analysis and the values stored are 6x1 np.array[float] vectors containing the 3 internal forces and 3 moments at the second node.
- Fmode1 (dict):** This dictionary contains the results of a modal analysis set. The keys are the string names of the analysis and the values stored are 6xN np.array[float]. The columns of the array are the forces and moments at the first node associated with the particular mode.\*
- Fmode2 (dict):** This dictionary contains the results of a modal analysis set. The keys are the string names of the analysis and the values stored are 6xN np.array[float]. The columns of the array are the forces and moments at the second node associated with the particular mode.\*
- xsect (obj):** The cross-section object used to determine the beams stiffnesses.
- EID (int):** The element ID of the beam.
- SBID (int):** The associated Superbeam ID the beam object belongs to.
- n1 (obj):** The first nodal object used by the beam.
- n2 (obj):** The second nodal object used by the beam.
- Fe (12x1 np.array[float]):** The distributed force vector of the element
- Ke (12x12 np.array[float]):** The stiffness matrix of the beam.
- Keg (12x12 np.array[float]):** The geometric stiffness matrix of the beam. Used for beam buckling calculations.
- Me (12x12 np.array[float]):** The mass matrix of the beam.
- h (float):** The magnitude length of the beam element.
- xbar (float):** The unit vector pointing in the direction of the rigid beam.

## Methods

- printSummary:** This method prints out characteristic attributes of the beam finite element.
- plotRigidBeam:** Plots the the shape of the rigid beam element.
- plotDisplBeam:** Plots the deformed shape of the beam element.
- printInternalForce:** Prints the internal forces of the beam element for a given analysis set

---

**Note:** The force and moments in the Fmode1 and Fmode2 could be completely

---

fictitious and be left as an artifact to fascilitate plotting of warped cross-sections. DO NOT rely on this information being meaningful.

\_\_\_**init**\_\_\_ (x1, x2, xsect, EID=0, SBID=0, nid1=0, nid2=1)  
Instantiates a timoshenko beam element.

This method instatiates a finite element timoshenko beam element. Currently the beam must be oriented along the global y-axis, however full 3D orientation support for frames is in progress.

## Args

- x1 (1x3 np.array[float]):** The 3D coordinates of the first beam element node.
- x2 (1x3 np.array[float]):** The 3D coordinates of the second beam element node.
- xsect (obj):** The cross-section object used to determine stiffnes and mass properties for the beam.

- EID (int)*: The integer identifier for the beam.
- SBID (int)*: The associated superbeam ID.
- nid1 (int)*: The first node ID
- nid2 (int)*: The second node ID

#### Returns

- None

#### `plotDisplBeam (**kwargs)`

Plots the displaced beam in 3D space.

This method plots the deformed beam finite element in 3D space. It is not typically called by the beam object but by a SuperBeam object or even a WingSection object.

#### Args

- environment (str)***: Determines what environment is to be used to plot the beam in 3D space. Currently only mayavi is supported.
- figName (str)***: The name of the figure in which the beam will appear.
- clr (1x3 tuple(float))***: This tuple contains three floats running from 0 to 1 in order to generate a color mayavi can plot.
- displScale (float)***: The scaling factor for the deformation experienced by the beam.
- mode (int)***: Determines what mode to plot. By default the mode is 0 implying a non-eigenvalue solution should be plotted.

#### Returns

- (*fig*): The mayavi figure of the beam.

#### `plotRigidBeam (**kwargs)`

Plots the rigid beam in 3D space.

This method plots the beam finite element in 3D space. It is not typically called by the beam object but by a SuperBeam object or even a WingSection object.

#### Args

- environment (str)***: Determines what environment is to be used to plot the beam in 3D space. Currently only mayavi is supported.
- figName (str)***: The name of the figure in which the beam will appear.
- clr (1x3 tuple(float))***: This tuple contains three floats running from 0 to 1 in order to generate a color mayavi can plot.

#### Returns

- (*fig*): The mayavi figure of the beam.

**printInternalForce** (*\*\*kwargs*)

Prints the internal forces and moments in the beam.

For a particular analysis set, this method prints out the force and moment resultants at both nodes of the beam.

#### Args

- analysis\_name (str):** The analysis name for which the forces are being surveyed.

#### Returns

- (str): This is a print out of the internal forces and moments within the beam element.

**printSummary** (*decimals=8, \*\*kwargs*)

Prints out characteristic information about the beam element.

This method by default prints out the EID, XID, SBID and the NIDs along with the nodes associated coordinates. Upon request, it can also print out the beam element stiffness, geometric stiffness, mass matrices and distributed force vector.

#### Args

- nodeCoord (bool):** A boolean to determine if the node coordinate information should also be printed.
- Ke (bool):** A boolean to determine if the element stiffness matrix should be printed.
- Keg (bool):** A boolean to determine if the element geometric stiffness matrix should be printed.
- Me (bool):** A boolean to determine if the element mass matrix should be printed.
- Fe (bool):** A boolean to determine if the element distributed force and moment vector should be printed.

#### Returns

- (str): Printed summary of the requested attributes.

## 2.10 SUPER-BEAM

**class** AeroComBAT.Structures.**SuperBeam** (*x1, x2, xsect, noe, SBID, btype='Tbeam', sNID=1, sEID=1*)

Create a superbeam object.

The superbeam object is mainly to facilitate creating a whole series of beam objects along the same line.

#### Attributes

- type (str):** The object type, a 'SuperBeam'.
- btype (str):** The beam element type of the elements in the superbeam.
- SBID (int):** The integer identifier for the superbeam.
- sNID (int):** The starting NID of the superbeam.
- enid (int):** The ending NID of the superbeam.
- xsect (obj):** The cross-section object referenced by the beam elements in the superbeam.



- noe (int)*: Number of elements in the beam.
- NIDs2EIDs (dict)*: Mapping of NIDs to beam EIDs within the superbeam
- x1 (1x3 np.array[float])*: The 3D coordinate of the first point on the superbeam.
- x2 (1x3 np.array[float])*: The 3D coordinate of the last point on the superbeam.
- sEID (int)*: The integer identifier for the first beam element in the superbeam.
- elems (dict)*: A dictionary of all beam elements within the superbeam. The keys are the EIDs and the values are the corresponding beam elements.
- xbar (1x3 np.array[float])*: The vector pointing along the axis of the superbeam.

### Methods

- getBeamCoord*: Returns the 3D coordinate of a point along the superbeam.
- printInternalForce*: Prints all internal forces and moments at every node in the superbeam.
- writeDisplacements*: Writes all displacements and rotations in the superbeam to a .csv
- getEIDatx*: Provided a non-dimensional point along the superbeam, this method returns the local element EID and the non-dimensional coordinate within that element.
- printSummary*: Prints all of the elements and node IDs within the beam as well as the coordinates of those nodes.

\_\_\_**init**\_\_\_ (*x1, x2, xsect, noe, SBID, btype='Tbeam', sNID=1, sEID=1*)  
Creates a superelement object.

This method instantiates a superelement. What it effectively does is mesh a line provided the starting and ending points along that line. Keep in mind that for now, only beams running parallel to the z-axis are supported.

### Args

- x1 (1x3 np.array[float])*: The starting coordinate of the beam.
- x2 (1x3 np.array[float])*: The ending coordinate of the beam.
- xsect (obj)*: The cross-section used through the superbeam.
- noe (int)*: The number of elements along the beam.
- SBID (int)*: The integer identifier for the superbeam.
- btype (str)*: The beam type to be meshed. Currently only Tbeam types are supported.
- sNID (int)*: The starting NID for the superbeam.
- sEID (int)*: The starting EID for the superbeam.

### Returns

- None

**getBeamCoord** (*x\_nd*)

Determine the global coordinate along superbeam.

Provided the non-dimensional coordinate along the beam, this method returns the global coordinate at that point.

**Args**

- ***x\_nd (float):*** The non-dimensional coordinate along the beam. Note that *x\_nd* must be between zero and one.

**Returns**

- *(1x3 np.array[float]):* The global coordinate corresponding to *x\_nd*

**getEIDatx (x)**

Returns the beam EID at a non-dimensional x-location in the superbeam.

Provided the non-dimensional coordinate along the beam, this method returns the global beam element EID, as well as the local non-dimensional coordinate within the specific beam element.

**Args**

- *x (float):* The non-dimensional coordinate within the super-beam

**Returns**

- ***EID (int):*** The EID of the element containing the non-dimensional coordinate provided.
- ***local\_x\_nd (float):*** The non-dimensional coordinate within the beam element associated with the provided non-dimensional coordinate within the beam.

**printInternalForce (\*\*kwargs)**

Prints the internal forces and moments in the superbeam.

For every node within the superbeam, this method will print out the internal forces and moments at those nodes.

**Args**

- ***analysis\_name (str):*** The name of the analysis for which the forces and moments are being surveyed.

**Returns**

- *(str):* Printed output expressing all forces and moments.

**printSummary (decimals=8, \*\*kwargs)**

Prints out characteristic information about the super beam.

This method by default prints out the EID, XID, SBID and the NIDs along with the nodes associated coordinates. Upon request, it can also print out the beam element stiffness, geometric stiffness, mass matrices and distributed force vector.

**Args**

- ***nodeCoord (bool):*** A boolean to determine if the node coordinate information should also be printed.
- ***Ke (bool):*** A boolean to determine if the element stiffness matrix should be printed.
- ***Keg (bool):*** A boolean to determine if the element geometric stiffness matrix should be printed.
- ***Me (bool):*** A boolean to determine if the element mass matrix should be printed.

- Fe (bool):** A boolean to determine if the element distributed force and moment vector should be printed.

#### Returns

- (*str*): Printed summary of the requested attributes.

#### **writeDisplacements** (*\*\*kwargs*)

Write internal displacements and rotations to file.

For every node within the superbeam, this method will tabulate all of the displacements and rotations and then write them to a file.

#### Args

- fileName (str)*: The name of the file where the data will be written.
- analysis\_name (str):** The name of the analysis for which the displacements and rotations are being surveyed.

#### Returns

- fileName (file):** This method doesn't actually return a file, rather it writes the data to a file named "fileName" and saves it to the working directory.

#### **writeForcesMoments** (*\*\*kwargs*)

Write internal force and moments to file.

For every node within the superbeam, this method will tabulate all of the forces and moments and then write them to a file.

#### Args

- fileName (str)*: The name of the file where the data will be written.
- analysis\_name (str):** The name of the analysis for which the forces and moments are being surveyed.

#### Returns

- fileName (file):** This method doesn't actually return a file, rather it writes the data to a file named "fileName" and saves it to the working directory.

## 2.11 WING SECTION

**class** AeroComBAT.Structures.**WingSection** (*x1, x2, chord, name, x0\_spar, xf\_spar, laminates, matLib, noe, SSBID=0, SNID=0, SEID=0, \*\*kwargs*)

Creates a wing section object.

This class instantiates a wing section object which is intended to represent the section of a wing enclosed by two ribs. This allows primarily for two different things: it allows the user to vary the cross-section design of the wing by enabling different designs in each wing section, as well as enabling the user to estimate the static stability of the laminates that make up the wing-section design.

#### Attributes

- Airfoils (*Array[obj]*):** This array contains all of the airfoils used over the wing section. This attribute exists primarily to facilitate the meshing process and is subject to change.
- XSects (*Array[obj]*):** This array contains all of the cross-section objects used in the wing section. If the cross-section is constant along the length of the wing section, this array length is 1.
- SuperBeams (*Array[obj]*):** This array contains all of the superbeam objects used in the wing section. If the cross-section is constant along the length of the wing section, this array length is 1.
- xdim (*1x2 Array[float]*):** This array contains the non-dimensional starting and ending points of the wing section spar. They are non-dimensionalized by the chord length.
- Laminates (*Array[obj]*):** This array contains the laminate objects used by the cross-sections in the wing section.
- x1 (*1x3 np.array[float]*):** The starting coordinate of the wing section.
- x2 (*1x3 np.array[float]*):** The ending coordinate of the wing section.
- XIDs (*Array[int]*):** This array contains the integer cross-section IDs

### Methods

- plotRigid:** This method plots the rigid wing section in 3D space.
- plotDispl:** Provided an analysis name, this method will deformed state of the wing section. It is also capable of plotting cross-section criteria, such as displacement, stress, strain, or failure criteria.

**Warning:** While it is possible to use multiple cross-section within the wing section, this capability is only to be utilized for tapering cross sections, not changing the cross-section type or design (such as by changing the laminates used to make the cross-sections). Doing so would invalidate the ritz method buckling solutions applied to the laminate objects.

`__init__` (*x1, x2, chord, name, x0\_spar, xf\_spar, laminates, matLib, noe, SSBID=0, SNID=0, SEID=0, \*\*kwargs*)

Creates a wing section object

This wing section object is in some way an organizational object. It holds a collection of superbeam objects which in general could all use different cross-sections. One could for example use several super-beams in order to simulate a taper within a wing section discretely. These objects will also be used in order to determine the buckling span of the laminate objects held within the cross-section.

### Args

- x1 (*1x3 np.array[float]*):** The starting coordinate of the wing section.
- x2 (*1x3 np.array[float]*):** The ending coordinate of the wing section.
- chord (*func*):** A function that returns the chord length along a wing provided the scalar length from the wing origin to the desired point.
- name (*str*):** The name of the airfoil to be used to mesh the cross-section. This is subject to change since the meshing process is only a placeholder.
- x0\_spar (*float*):** The non-dimensional starting location of the cross section. This value is non-dimensionalized by the local chord length.
- xf\_spar (*float*):** The non-dimensional ending location of the cross section. This value is non-dimensionalized by the local chord length.

- laminates (Array[obj])***: This array contains the laminate objects to be used in order to mesh the cross-section.
- matLib (obj)***: This material library object contains all of the materials to be used in meshing the cross-sections used by the wing section.
- noe (float)***: The number of beam elements to be used in the wing per unit length.
- SSBID (int)***: The starting superbeam ID in the wing section.
- SNID (int)***: The starting node ID in the wing section.
- SEID (int)***: The starting element ID in the wing section.
- SXID (int)***: The starting cross-section ID in the wing section.
- numSupBeams (int)***: The number of different superbeams to be used in the wing section.
- typeXSect (str)***: The type of cross-section used by the wing section.
- meshSize (int)***: The maximum aspect ratio an element can have within the cross-sections used by the wing sections.
- ref\_ax (str)***: The reference axis used by the cross-section. This is axis about which the loads will be applied on the wing section.

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**Note:** The chord function could take the shape of:  $\text{chord} = \text{lambda } y: (\text{ctip}-\text{croot}) * y / \text{b}_s + \text{croot}$

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#### **plotDispl** (*\*\*kwargs*)

Plots the deformed wing section object in 3D space.

Provided an analysis name, this method will plot the results from the corresponding analysis including beam/cross-section deformation, and stress, strain, or failure criteria within the sampled cross-sections.

#### **Args**

- figName (str)***: The name of the plot to be generated. If one is not provided a semi-random name will be generated.
- environment (str)***: The name of the environment to be used when plotting. Currently only the 'mayavi' environment is supported.
- clr (1x3 tuple(int))***: This tuple represents the RGB values that the beam reference axis will be colored with.
- numXSects (int)***: This is the number of cross-sections that will be plotted and evenly distributed throughout the beam.
- contour (str)***: The contour to be plotted on the sampled cross sections.
- contLim (1x2 Array[float])***: The lower and upper limits for the contour color plot.
- warpScale (float)***: The visual multiplication factor to be applied to the cross-sectional warping displacement.
- displScale (float)***: The visual multiplication factor to be applied to the beam displacements and rotations.
- analysis\_name (str)***: The analysis name corresponding to the results to be visualized.
- mode (int)***: For modal analysis, this corresponds to the mode-shape which is desired to be plotted.

#### **Returns**

- (*figure*): This method returns a 3D plot of the rigid wing section.

**Warning:** In order to limit the size of data stored in memory, the local cross-sectional data is not stored. As a result, for every additional cross-section that is plotted, the time required to plot will increase substantially.

**plotRigid** (*\*\*kwargs*)

Plots the rigid wing section object in 3D space.

This method is exceptionally helpful when building up a model and debugging it.

#### Args

- figName (str):*** The name of the plot to be generated. If one is not provided a semi-random name will be generated.
- environment (str):*** The name of the environment to be used when plotting. Currently only the 'mayavi' environment is supported.
- clr (1x3 tuple(int)):*** This tuple represents the RGB values that the beam reference axis will be colored with.
- numXSects (int):*** This is the number of cross-sections that will be plotted and evenly distributed throughout the beam.

#### Returns

- (*figure*): This method returns a 3D plot of the rigid wing section.

**Warning:** In order to limit the size of data stored in memory, the local cross-sectional data is not stored. As a result, for every additional cross-section that is plotted, the time required to plot will increase substantially.

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