

QUESTION 4: UNIFICATION

1. $\text{unify}[t(s(s), G, s, p, t(K), s), t(s(G), G, s, p, t(K), U)]$

initially: $s = \{\}$, $A = t(s(s), G, s, p, t(K), s)$, $B = t(s(G), G, s, p, t(K), U)$.

- 1) $s = s \circ \{G=s\} = \{G=s\}$
 $A^\circ s = t(s(s), s, s, p, t(K), s)$
 $B^\circ s = t(s(s), s, s, p, t(K), U)$
- 2) $s = s \circ \{U=s\} = \{G=s, U=s\}$
 $A^\circ s = t(s(s), s, s, p, t(K), s)$
 $B^\circ s = t(s(s), s, s, p, t(K), s)$

Answer: $s = \{G=s, U=s\}$

2. $\text{unify}[g(l, M, g, G, U, g, v(M)), g(l, v(U), g, v(M), v(G), g, v(M))]$

initially: $s = \{\}$, $A = g(l, M, g, G, U, g, v(M))$, $B = g(l, v(U), g, v(M), v(G), g, v(M))$.

- 1) $s = s \circ \{M=v(U)\} = \{M=v(U)\}$
 $A^\circ s = g(l, v(U), g, G, U, g, v(v(U)))$.
 $B^\circ s = g(l, v(U), g, v(v(U)), v(G), g, v(v(U)))$.
- 2) $s = s \circ \{G=v(v(U))\} = \{M=v(U), G=v(v(U))\}$
 $A^\circ s = g(l, v(U), g, v(v(U)), U, g, v(v(U)))$.
 $B^\circ s = g(l, v(U), g, v(v(U)), v(v(v(U))), g, v(v(U)))$
- 3) $s = s \circ \{U = v(v(v(U)))\} \Rightarrow$ not possible, circular occurrence (occurs check will fail)

Answer: No MGU

3. $\text{unify}[m(M, N), n(M, N)]$

Answer: There isn't a unifier for 2 different predicates m and n.

4. $\text{unify}[p([v \mid [V \mid VV]]), p([v \mid V \mid VV])]$

Initially: $s = \{\}$, $A = p([v \mid [V \mid VV]])$, $B = p([v \mid V \mid VV])$.

- 1) $s = s \circ \{v = [v \mid V]\} \Rightarrow$ illegal substitution

Answer: No such substitution.

5. $\text{unify}[g([T]), g(T)]$

Initially: $s = \{\}$, $A = g([T])$, $B = g(T)$.

- 4) $s = s \circ \{T = [T]\} \Rightarrow$ not possible, circular occurrence (occurs check will fail on T)

Answer: No such substitution.