

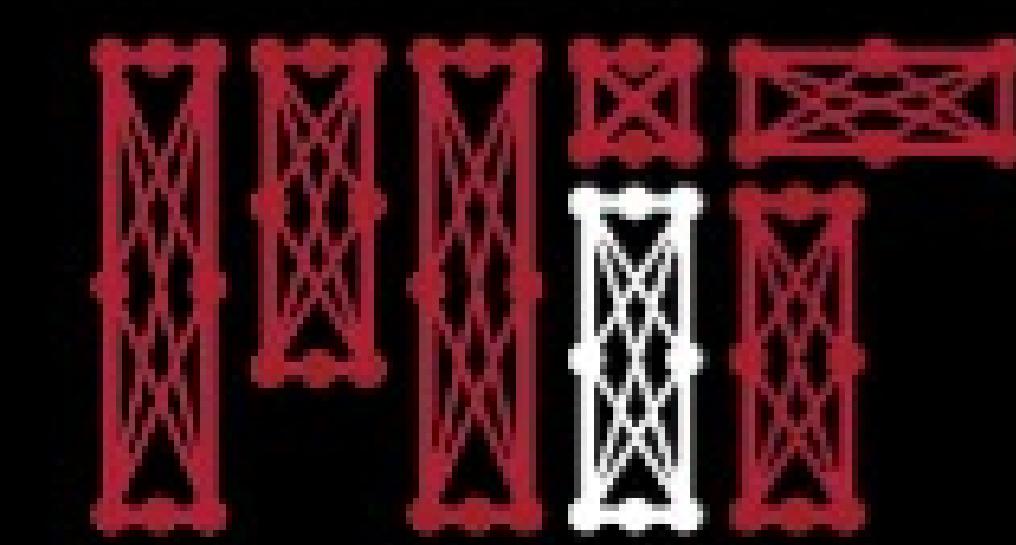


Deep Computer Vision

Alexander Amini

MIT 6.S191

January 20, 2021




6.S191 Introduction to Deep Learning
introtodeeplearning.com @MITDeepLearning





**“To know what is
where by looking.”**

To discover from images what is present in the world, where things are, what actions are taking place, to predict and anticipate events in the world

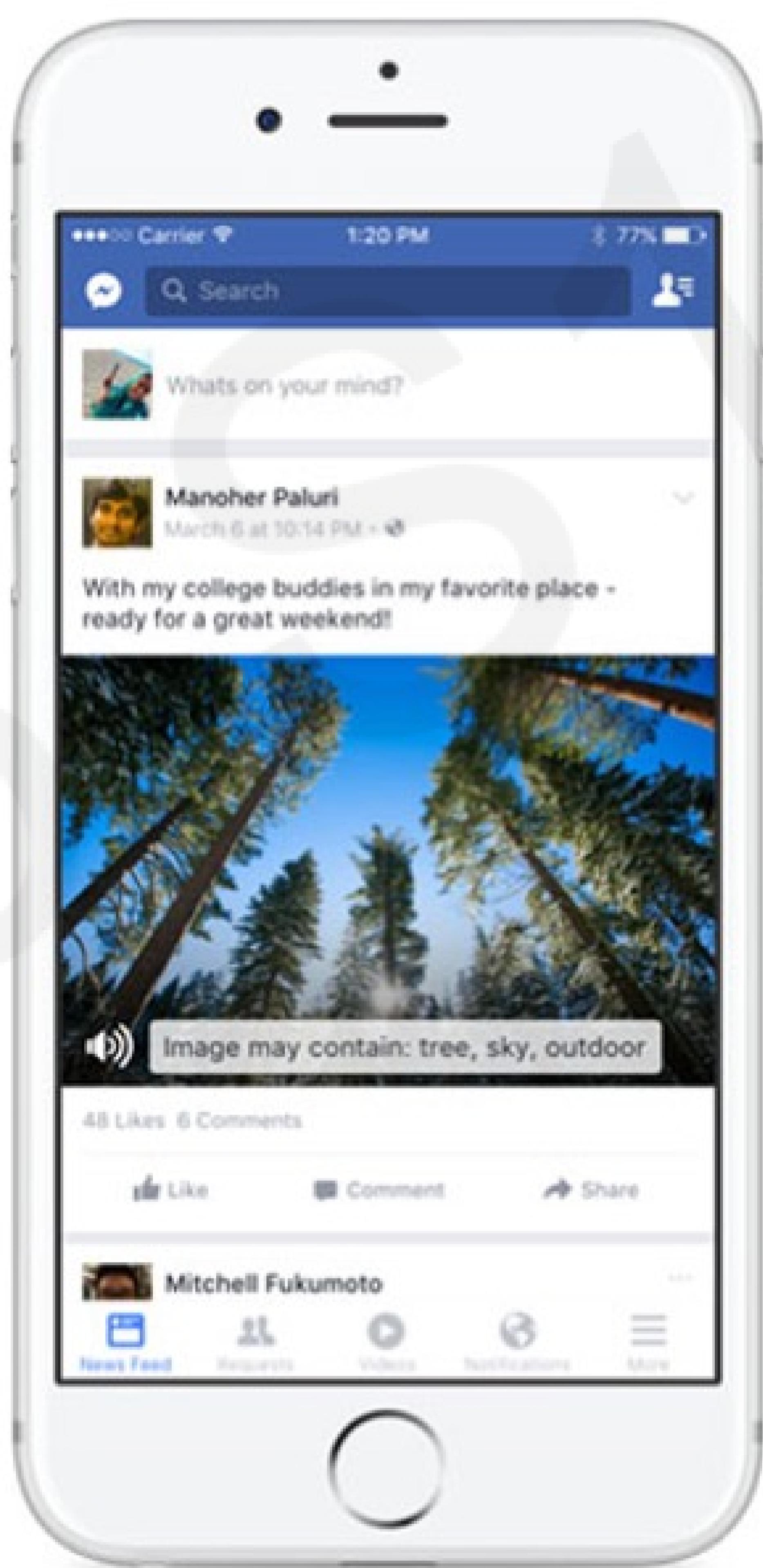


The rise and impact of computer vision

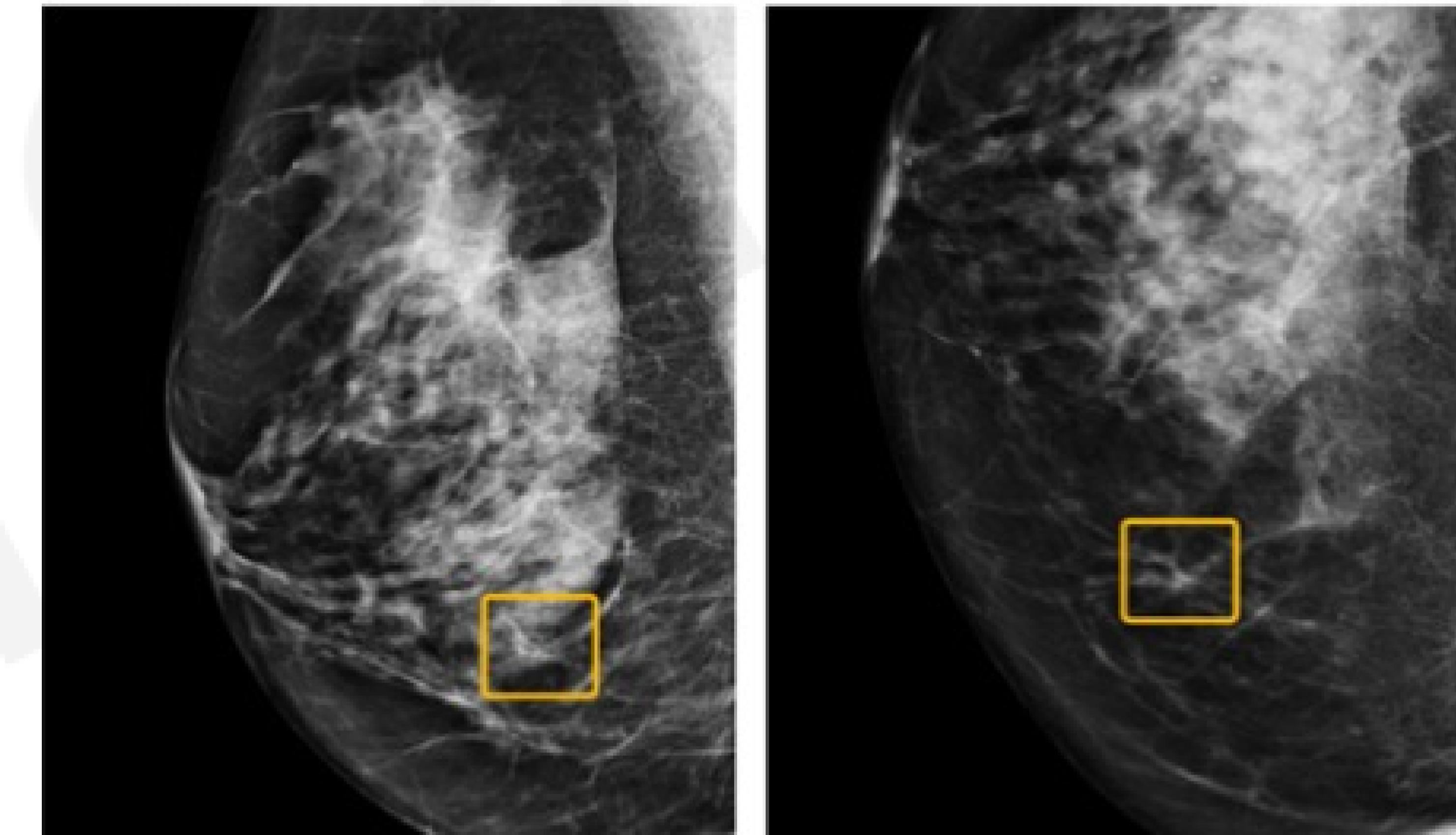
Robotics



Accessibility



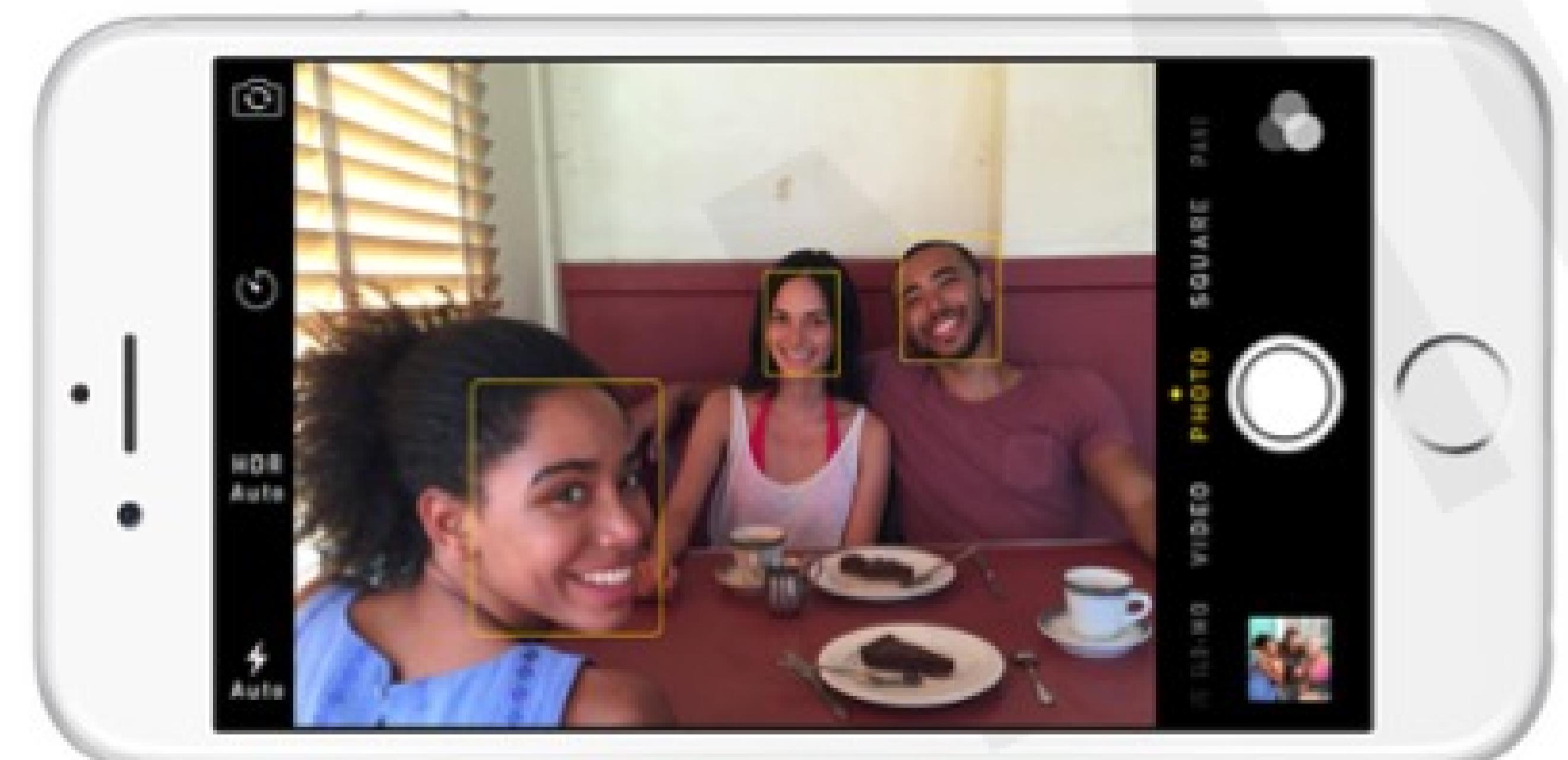
Biology & Medicine



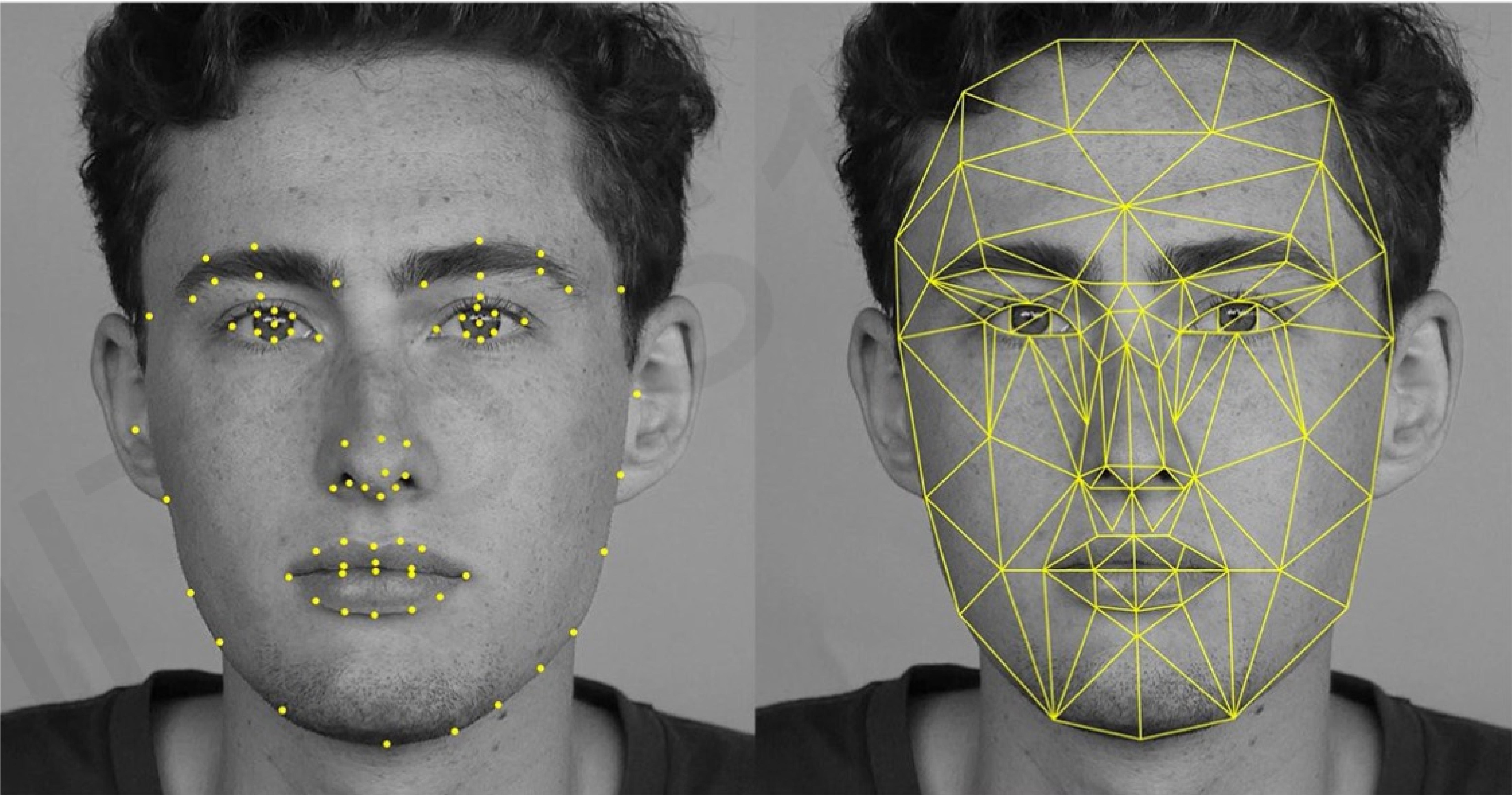
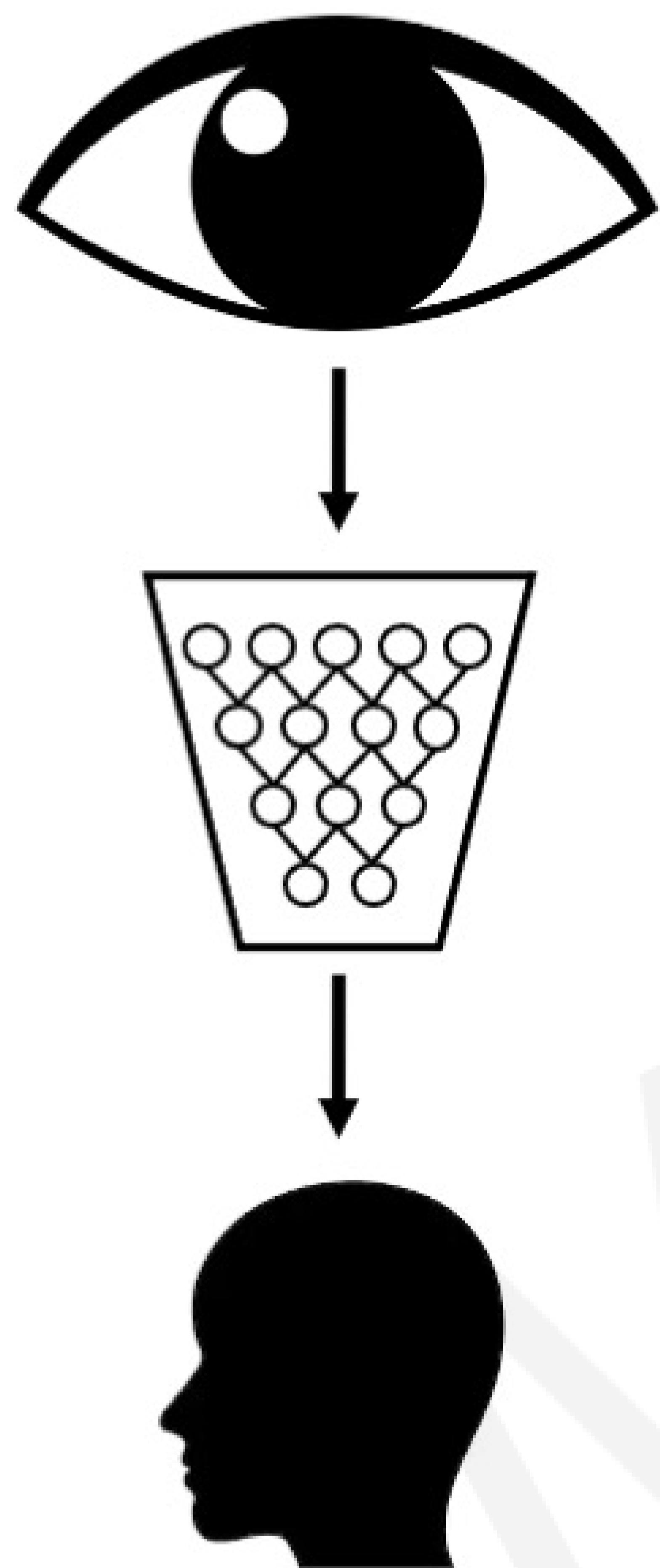
Autonomous driving



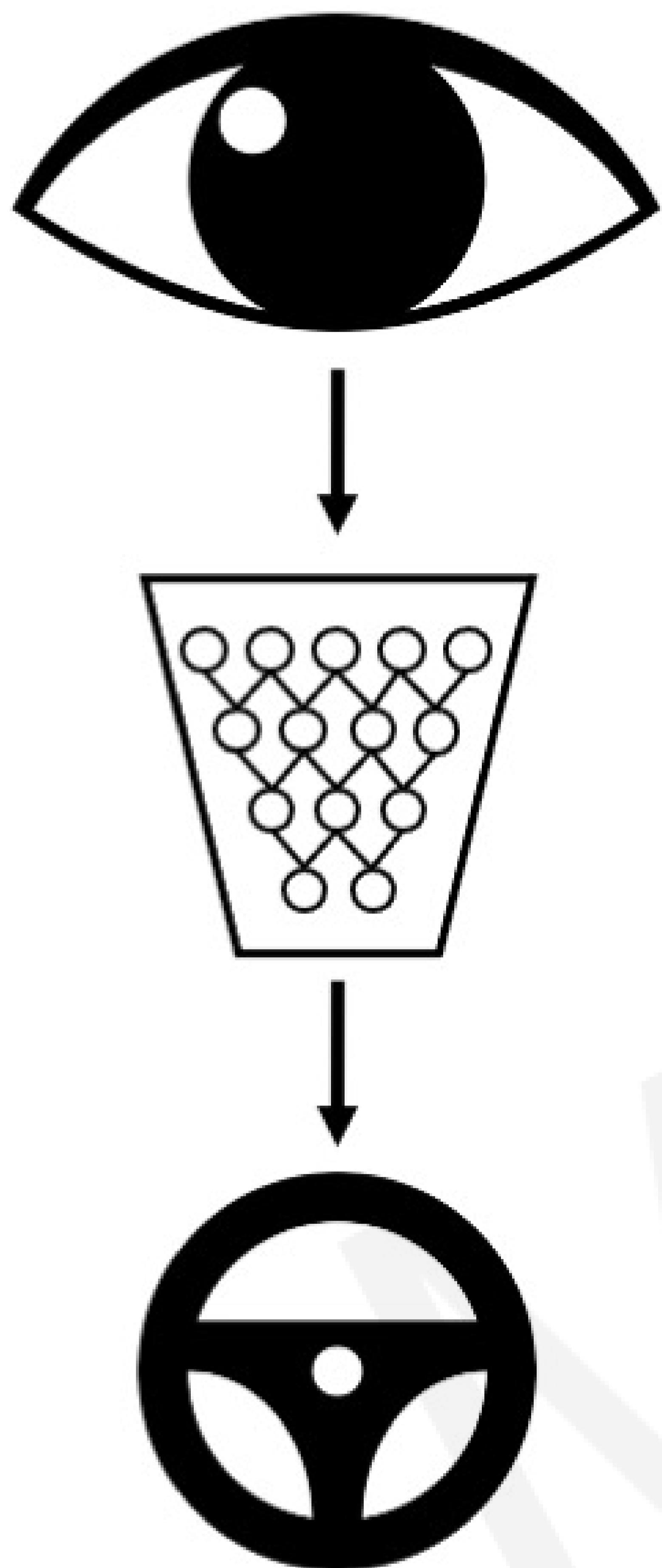
Mobile computing



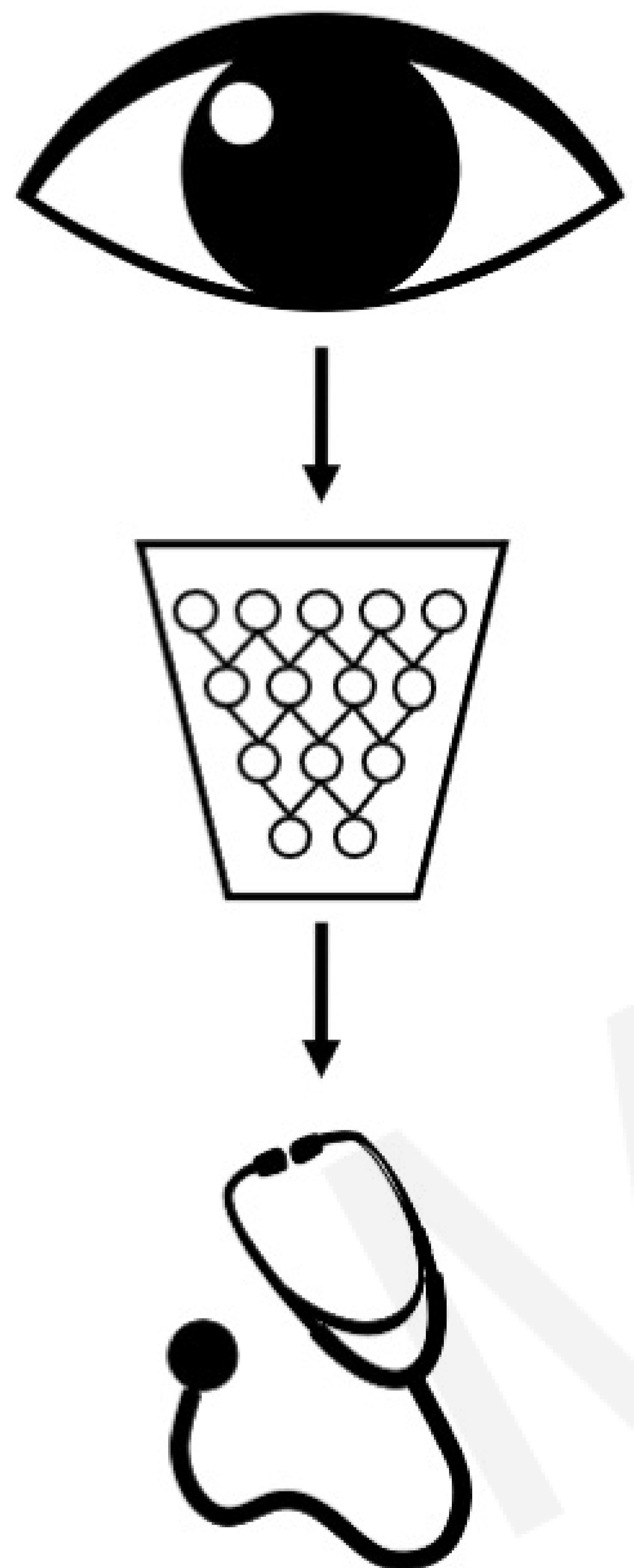
Impact: Facial Detection & Recognition



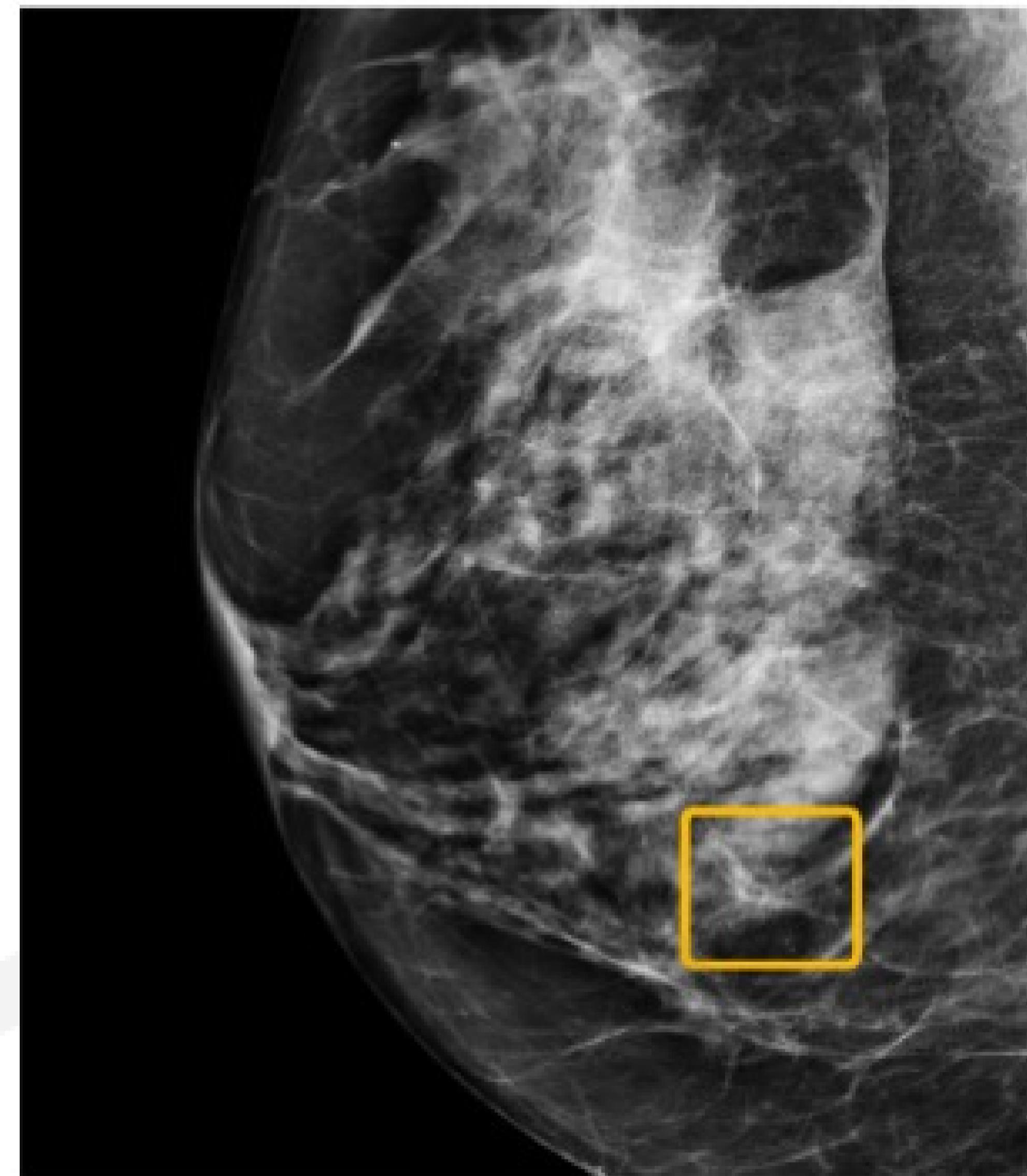
Impact: Self-Driving Cars



Impact: Medicine, Biology, Healthcare



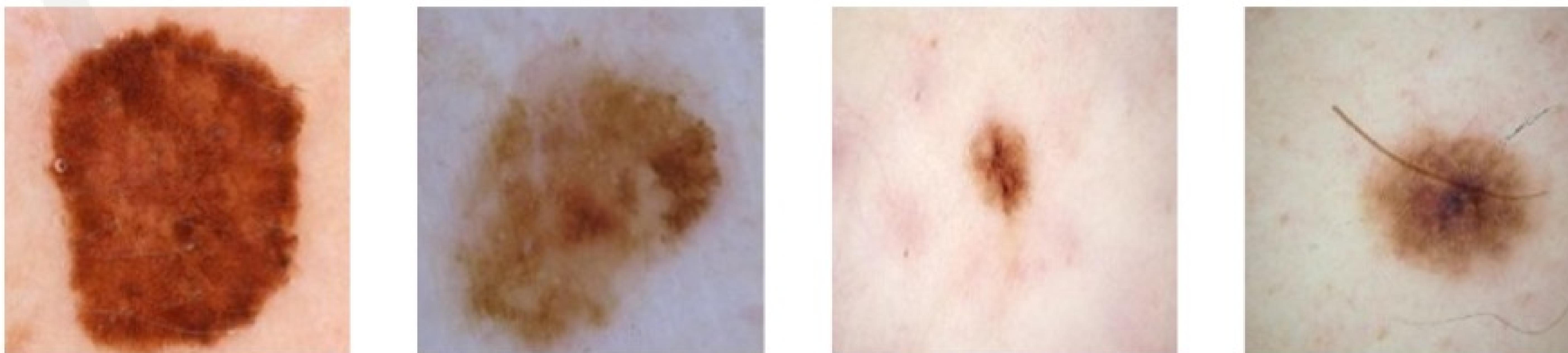
Breast cancer



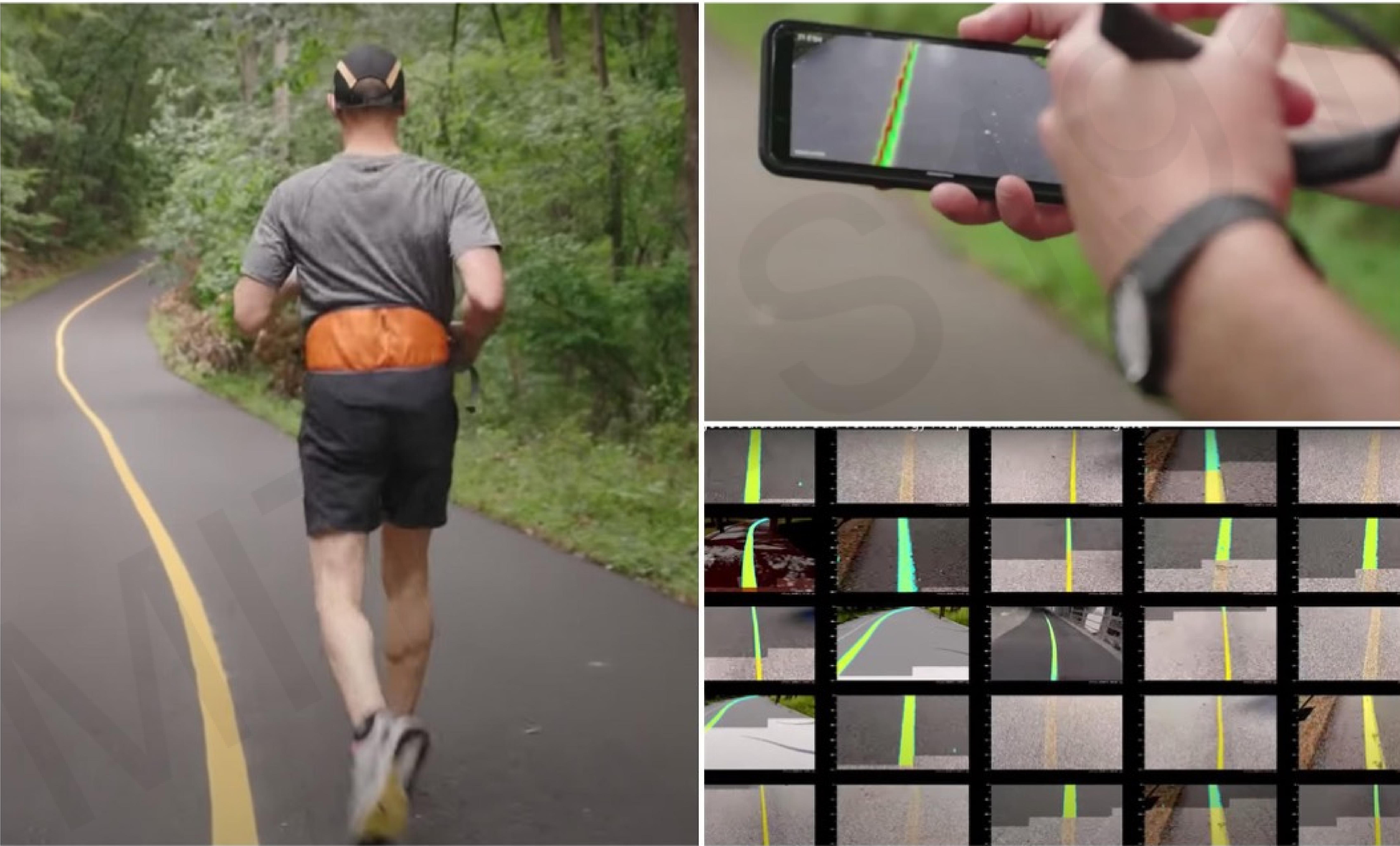
COVID-19



Skin cancer



Impact: Accessibility

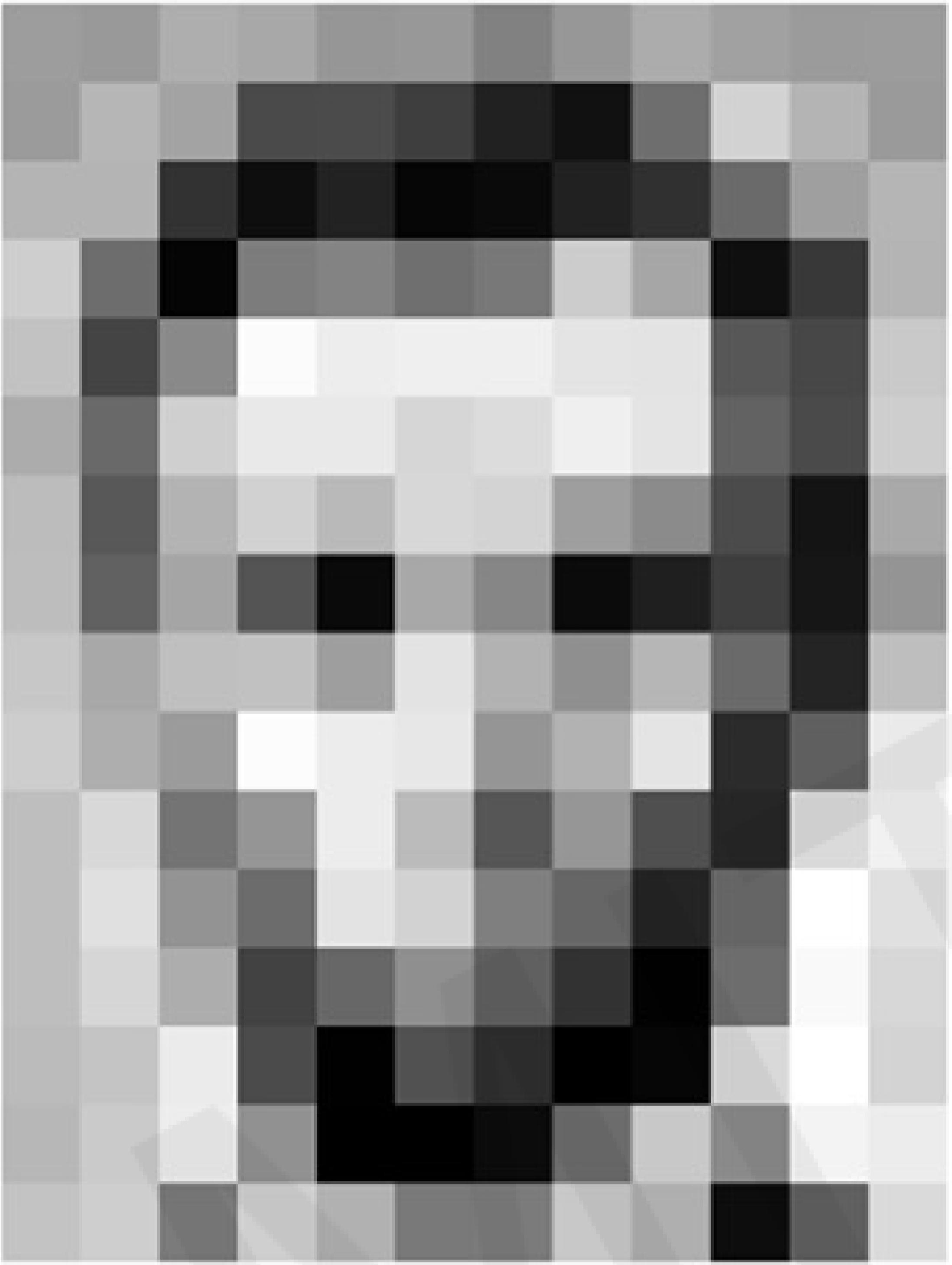




John Watkinson
ANDROID ENGINEER

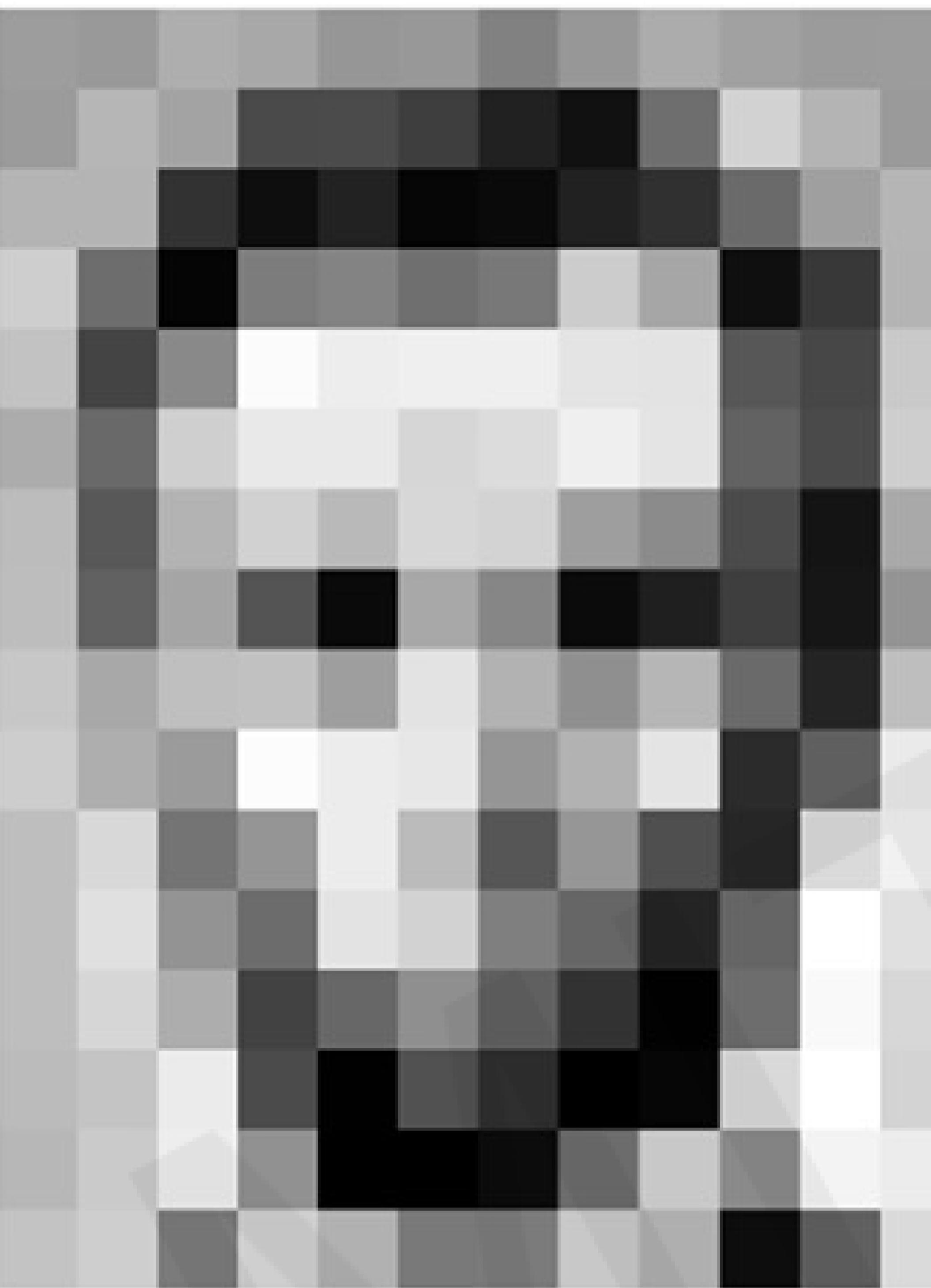
What Computers “See”

Images are Numbers



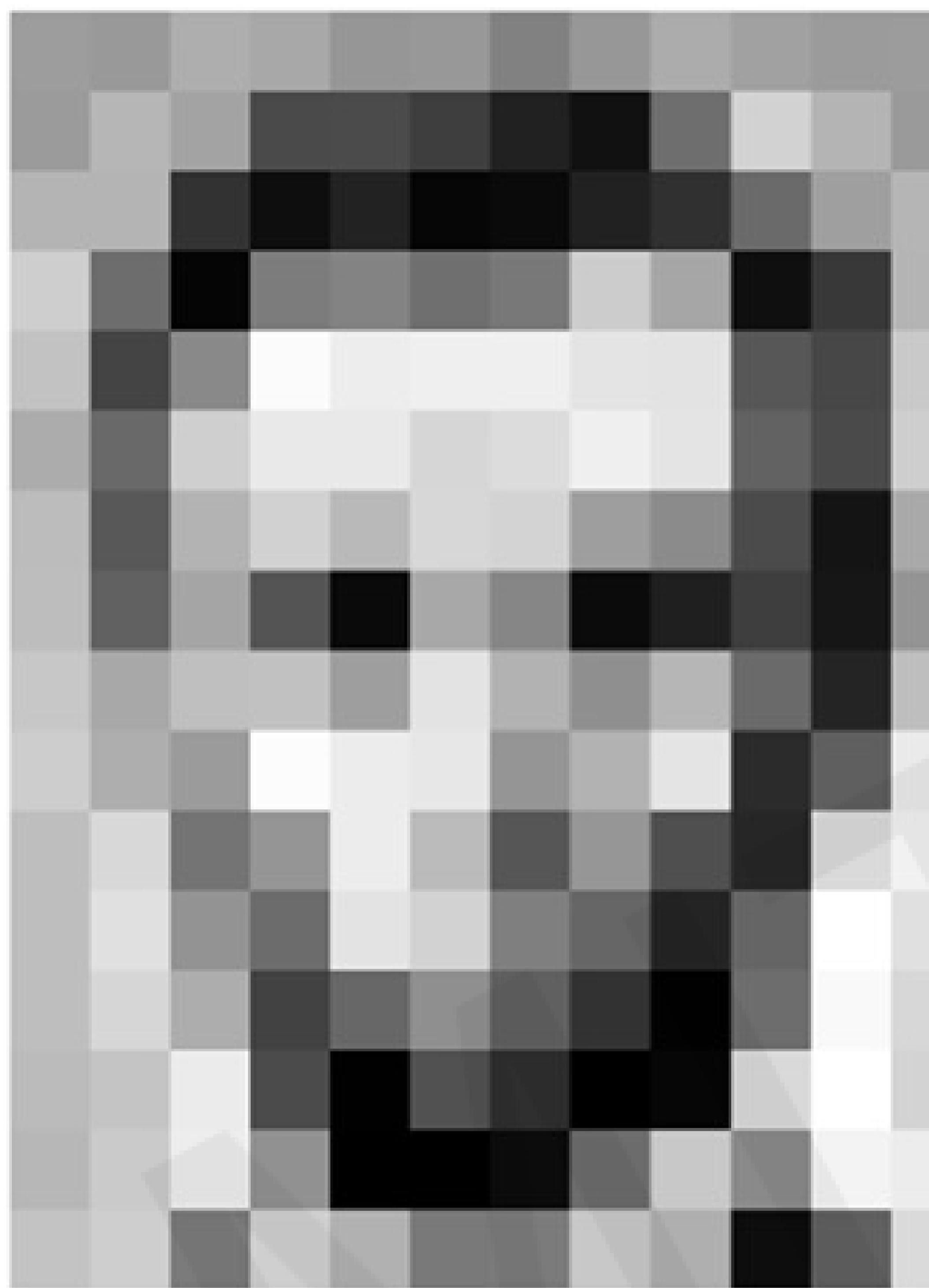
6.S191

Images are Numbers



| | | | | | | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 157 | 153 | 174 | 168 | 150 | 152 | 129 | 151 | 172 | 161 | 155 | 156 |
| 155 | 182 | 169 | 74 | 76 | 62 | 93 | 17 | 110 | 210 | 180 | 154 |
| 180 | 180 | 50 | 14 | 94 | 6 | 10 | 33 | 45 | 106 | 159 | 181 |
| 206 | 109 | 5 | 124 | 191 | 111 | 120 | 204 | 166 | 15 | 56 | 180 |
| 194 | 63 | 157 | 251 | 237 | 299 | 239 | 228 | 227 | 87 | 71 | 201 |
| 172 | 105 | 207 | 233 | 233 | 214 | 220 | 239 | 228 | 98 | 74 | 206 |
| 188 | 68 | 179 | 209 | 185 | 215 | 211 | 158 | 139 | 75 | 20 | 169 |
| 189 | 97 | 165 | 84 | 10 | 168 | 134 | 11 | 31 | 62 | 22 | 148 |
| 199 | 168 | 191 | 193 | 158 | 227 | 178 | 143 | 182 | 106 | 36 | 190 |
| 206 | 174 | 155 | 252 | 236 | 231 | 149 | 178 | 228 | 43 | 95 | 234 |
| 190 | 216 | 116 | 149 | 236 | 187 | 85 | 150 | 79 | 38 | 218 | 241 |
| 190 | 224 | 147 | 108 | 227 | 210 | 127 | 102 | 35 | 101 | 255 | 224 |
| 190 | 214 | 173 | 66 | 103 | 143 | 95 | 50 | 2 | 109 | 249 | 215 |
| 187 | 196 | 235 | 75 | 1 | 81 | 47 | 0 | 6 | 217 | 255 | 211 |
| 183 | 202 | 237 | 145 | 0 | 0 | 12 | 108 | 200 | 138 | 243 | 236 |
| 196 | 206 | 123 | 207 | 177 | 121 | 123 | 200 | 175 | 13 | 96 | 218 |

Images are Numbers



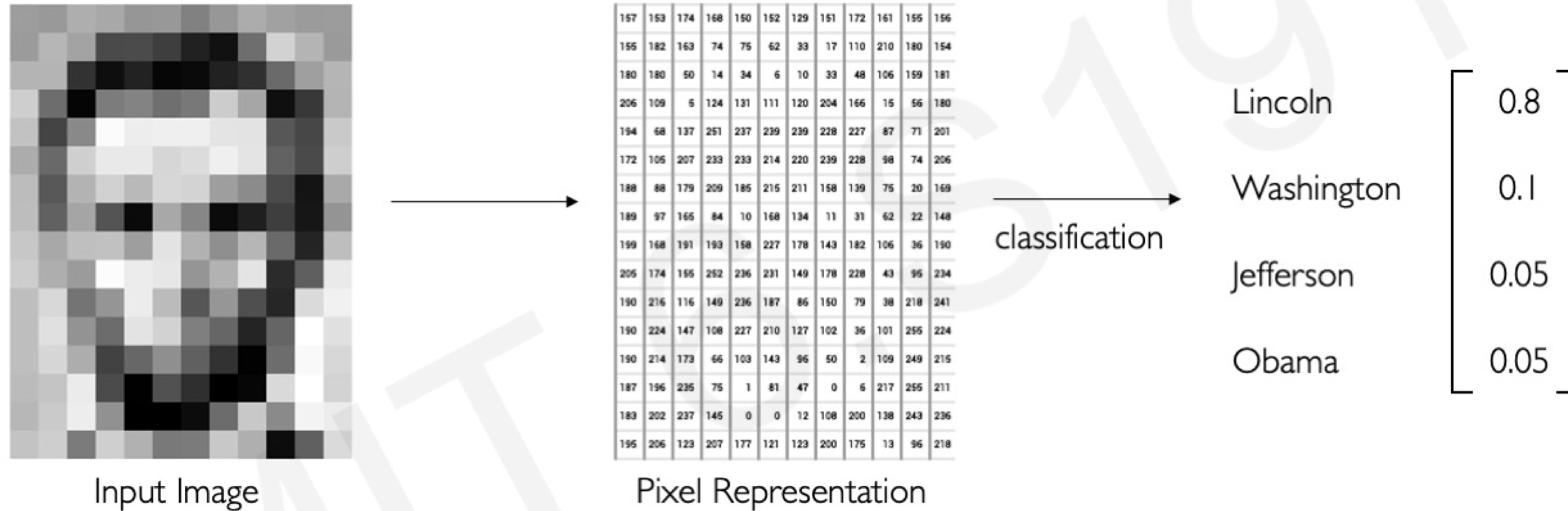
| | | | | | | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 157 | 153 | 174 | 168 | 150 | 152 | 129 | 151 | 172 | 161 | 155 | 156 |
| 155 | 182 | 163 | 74 | 76 | 62 | 93 | 17 | 110 | 210 | 180 | 154 |
| 180 | 180 | 50 | 14 | 34 | 6 | 10 | 33 | 43 | 106 | 159 | 181 |
| 206 | 109 | 5 | 124 | 131 | 111 | 120 | 204 | 166 | 15 | 56 | 180 |
| 194 | 68 | 137 | 251 | 237 | 299 | 239 | 228 | 227 | 87 | 71 | 201 |
| 172 | 105 | 207 | 233 | 233 | 214 | 220 | 239 | 228 | 98 | 74 | 206 |
| 188 | 88 | 179 | 209 | 185 | 215 | 211 | 158 | 139 | 75 | 20 | 169 |
| 189 | 97 | 165 | 84 | 10 | 168 | 134 | 11 | 31 | 62 | 22 | 148 |
| 199 | 168 | 191 | 193 | 158 | 227 | 178 | 143 | 182 | 106 | 36 | 190 |
| 206 | 174 | 155 | 252 | 236 | 231 | 149 | 178 | 228 | 43 | 95 | 234 |
| 190 | 216 | 116 | 149 | 236 | 187 | 85 | 150 | 79 | 38 | 218 | 241 |
| 190 | 224 | 147 | 108 | 227 | 210 | 127 | 102 | 35 | 101 | 255 | 224 |
| 190 | 214 | 173 | 66 | 103 | 143 | 95 | 50 | 2 | 109 | 249 | 215 |
| 187 | 196 | 235 | 75 | 1 | 81 | 47 | 0 | 6 | 217 | 255 | 211 |
| 183 | 202 | 237 | 145 | 0 | 0 | 12 | 108 | 200 | 138 | 243 | 236 |
| 195 | 206 | 123 | 207 | 177 | 121 | 123 | 200 | 175 | 13 | 96 | 218 |

What the computer sees

| | | | | | | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 157 | 153 | 174 | 168 | 150 | 152 | 129 | 151 | 172 | 161 | 155 | 156 |
| 155 | 182 | 163 | 74 | 76 | 62 | 93 | 17 | 110 | 210 | 180 | 154 |
| 180 | 180 | 50 | 14 | 34 | 6 | 10 | 33 | 48 | 106 | 159 | 181 |
| 206 | 109 | 5 | 124 | 131 | 111 | 120 | 204 | 166 | 16 | 56 | 180 |
| 194 | 68 | 137 | 251 | 237 | 239 | 239 | 228 | 227 | 87 | 71 | 201 |
| 172 | 105 | 207 | 233 | 233 | 214 | 220 | 239 | 228 | 98 | 74 | 206 |
| 188 | 88 | 179 | 209 | 185 | 215 | 211 | 158 | 139 | 75 | 20 | 169 |
| 189 | 97 | 165 | 84 | 10 | 168 | 134 | 11 | 31 | 62 | 22 | 148 |
| 199 | 168 | 191 | 193 | 158 | 227 | 178 | 143 | 182 | 143 | 182 | 106 |
| 206 | 174 | 155 | 252 | 236 | 231 | 149 | 178 | 228 | 43 | 95 | 234 |
| 190 | 216 | 116 | 149 | 236 | 187 | 85 | 150 | 79 | 38 | 218 | 241 |
| 190 | 224 | 147 | 108 | 227 | 210 | 127 | 102 | 35 | 101 | 255 | 224 |
| 190 | 214 | 173 | 66 | 103 | 143 | 95 | 50 | 2 | 109 | 249 | 215 |
| 187 | 196 | 235 | 75 | 1 | 81 | 47 | 0 | 6 | 217 | 255 | 211 |
| 183 | 202 | 237 | 145 | 0 | 0 | 12 | 108 | 200 | 138 | 243 | 236 |
| 195 | 206 | 123 | 207 | 177 | 121 | 123 | 200 | 175 | 13 | 96 | 218 |

An image is just a matrix of numbers [0,255]!
i.e., 1080x1080x3 for an RGB image

Tasks in Computer Vision



- **Regression:** output variable takes continuous value
- **Classification:** output variable takes class label. Can produce probability of belonging to a particular class

High Level Feature Detection

Let's identify key features in each image category



Nose,
Eyes,
Mouth



Wheels,
License Plate,
Headlights



Door,
Windows,
Steps

Manual Feature Extraction

Domain knowledge

Define features

Detect features
to classify

Problems?

Manual Feature Extraction

Domain knowledge

Define features

Detect features
to classify

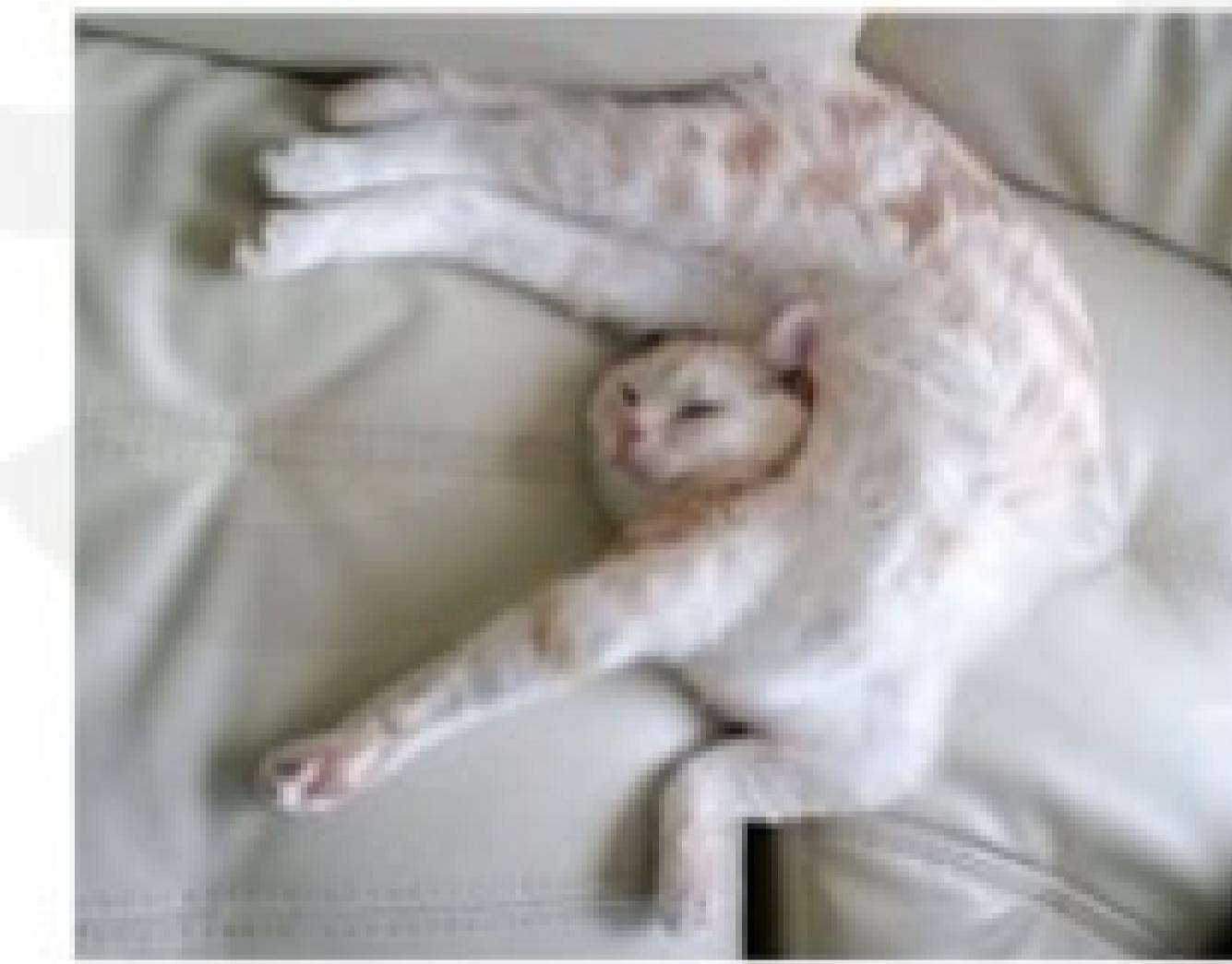
Viewpoint variation



Scale variation



Deformation



Occlusion



Illumination conditions



Background clutter



Intra-class variation



Manual Feature Extraction

Domain knowledge

Define features

Detect features
to classify

Viewpoint variation



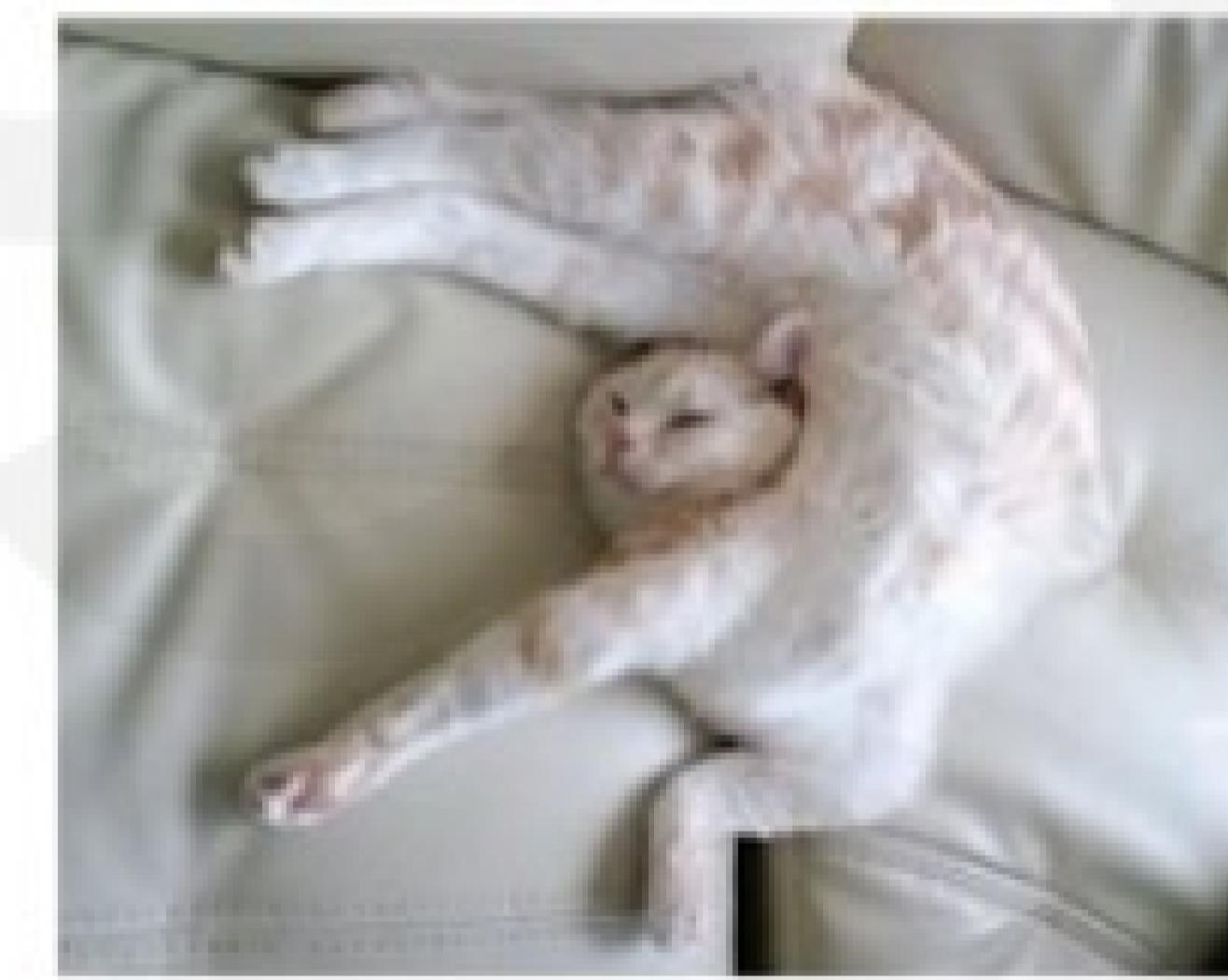
Illumination conditions



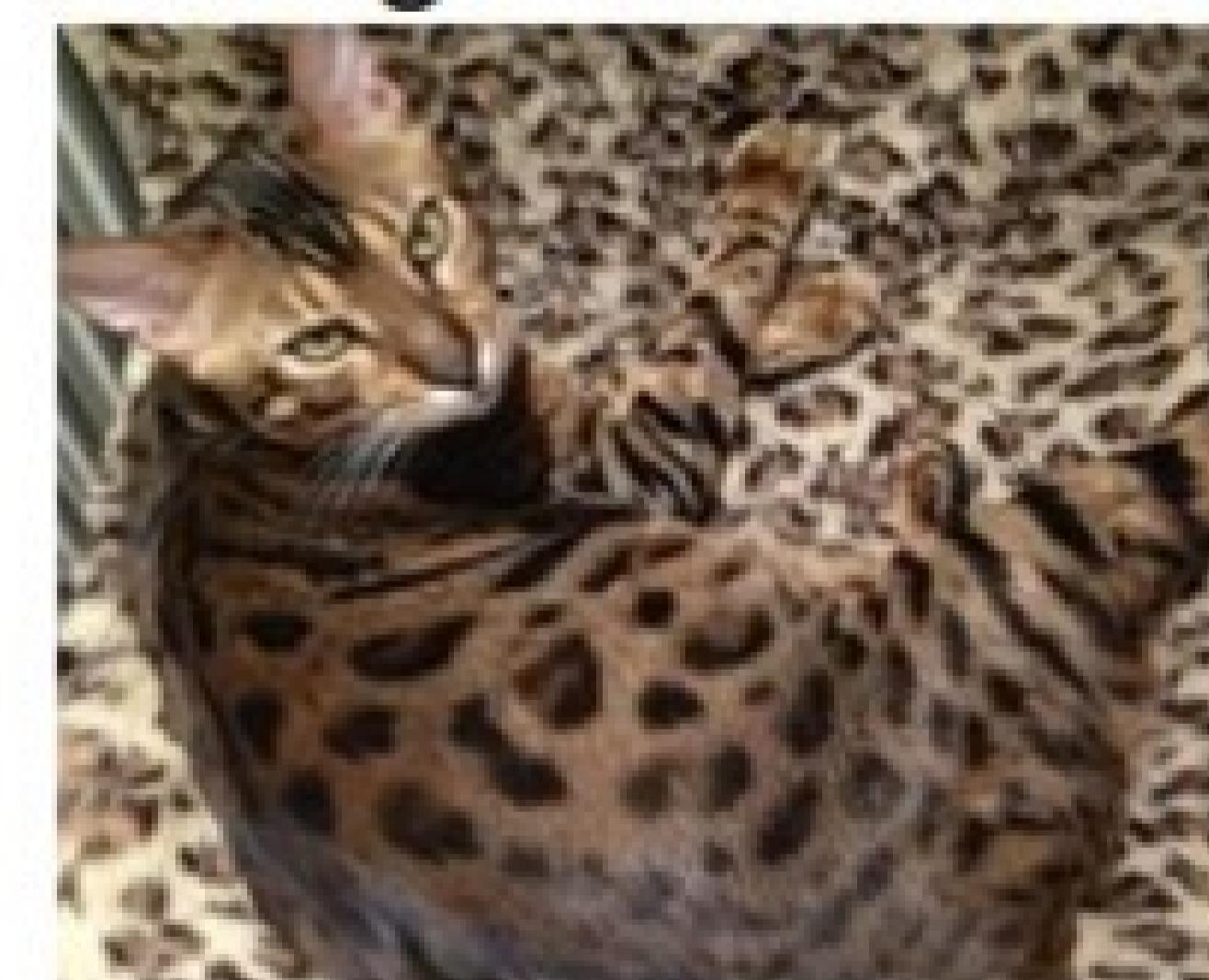
Scale variation



Deformation



Background clutter



Occlusion



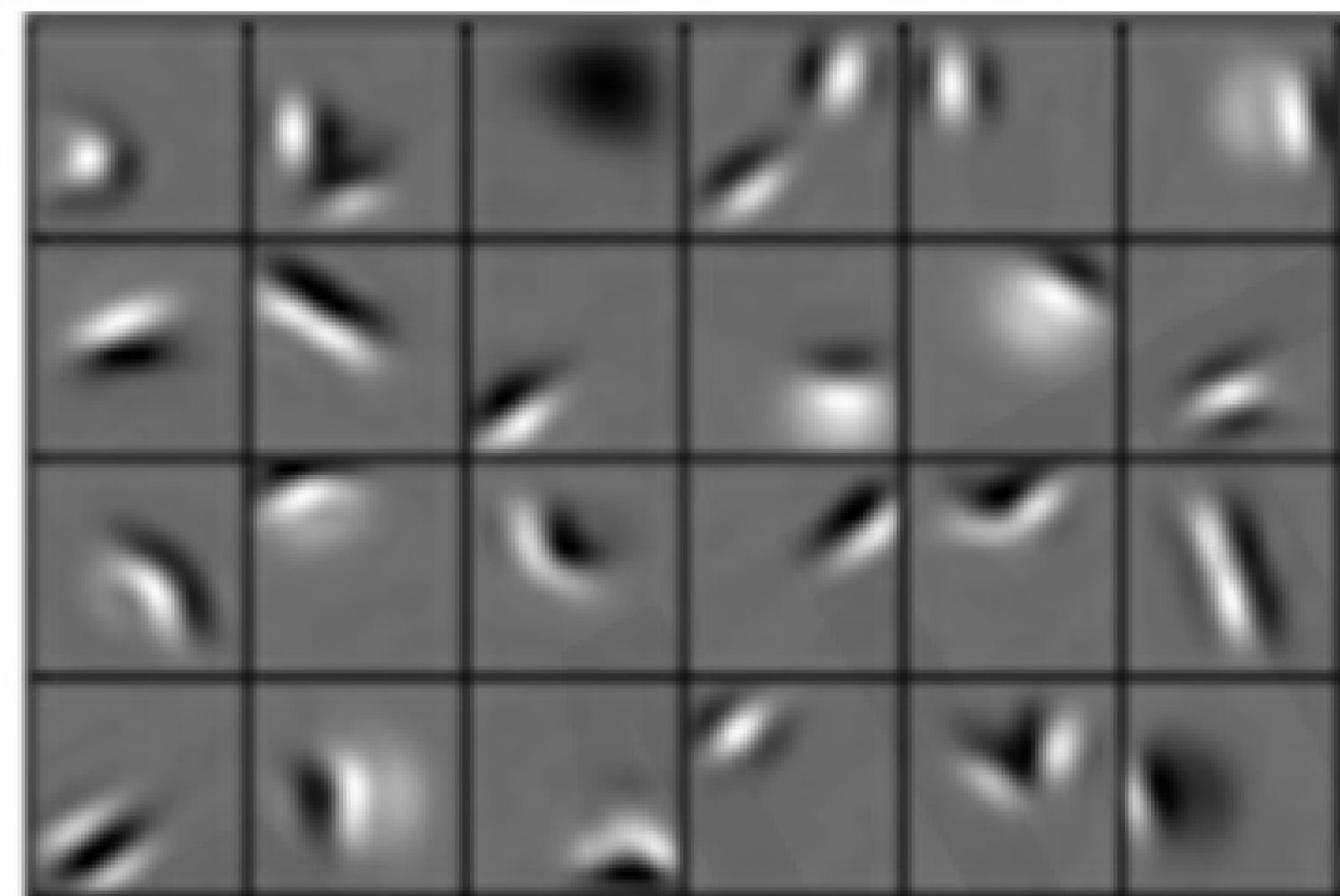
Intra-class variation



Learning Feature Representations

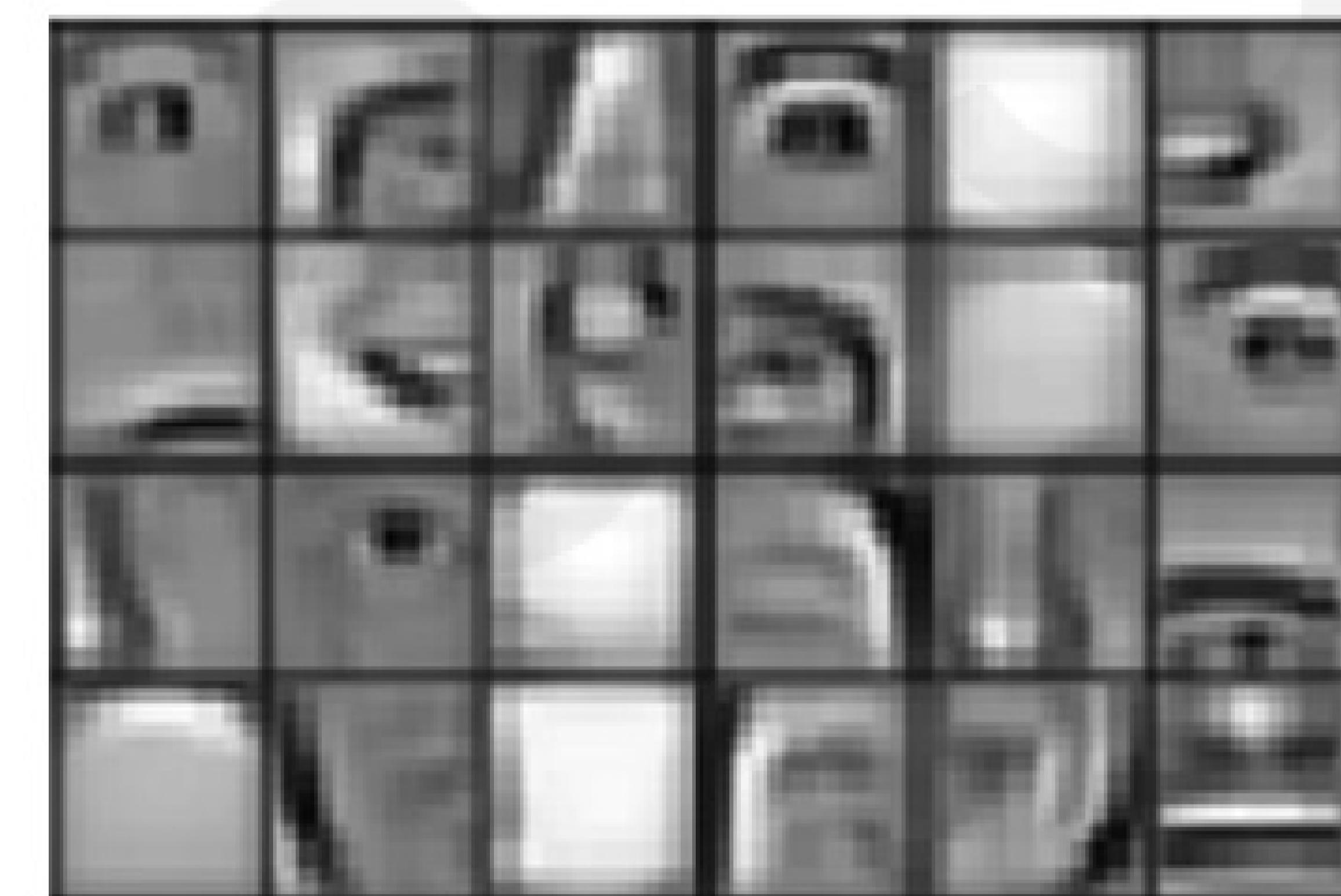
Can we learn a **hierarchy of features** directly from the data instead of hand engineering?

Low level features



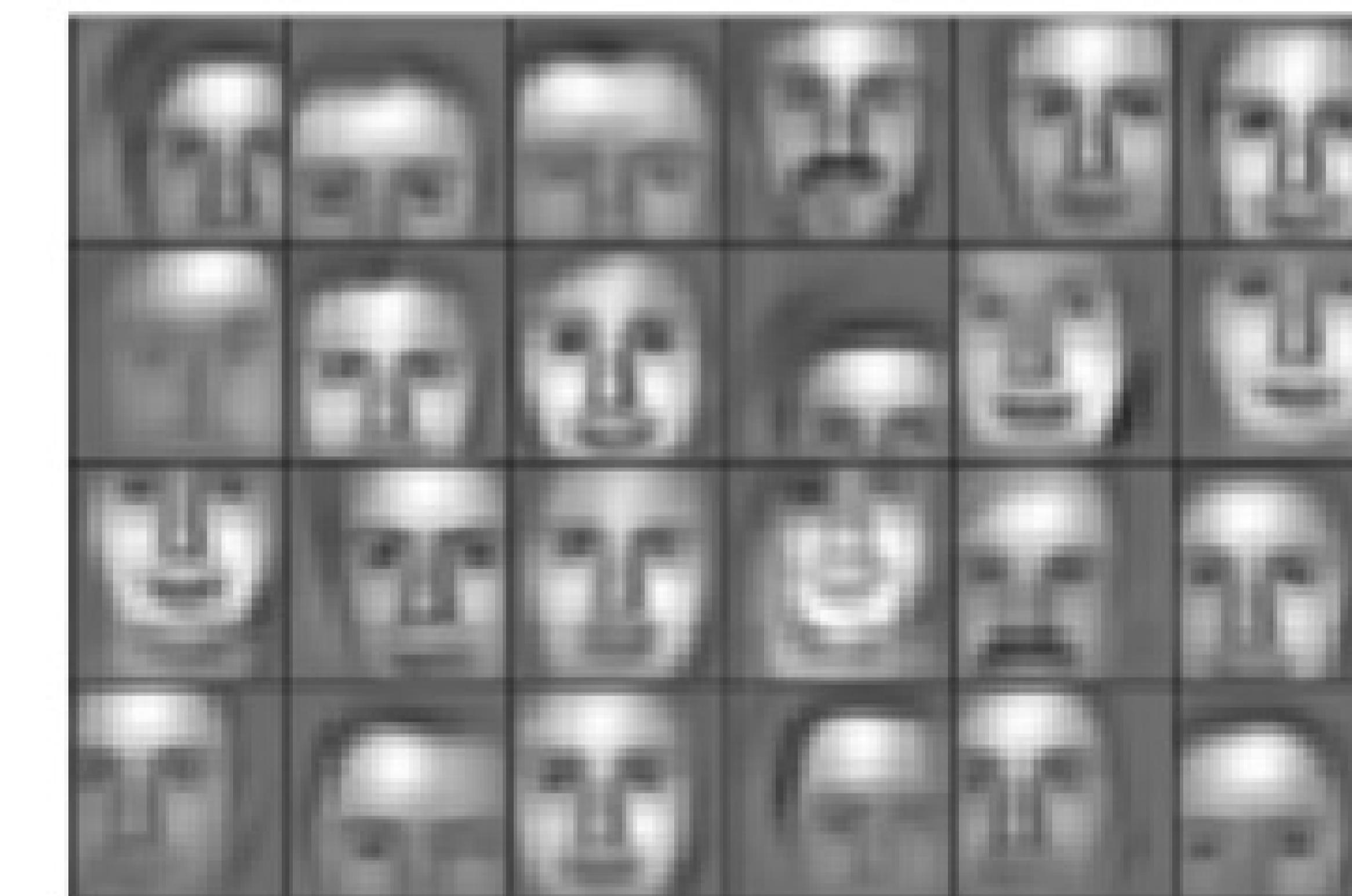
Edges, dark spots

Mid level features



Eyes, ears, nose

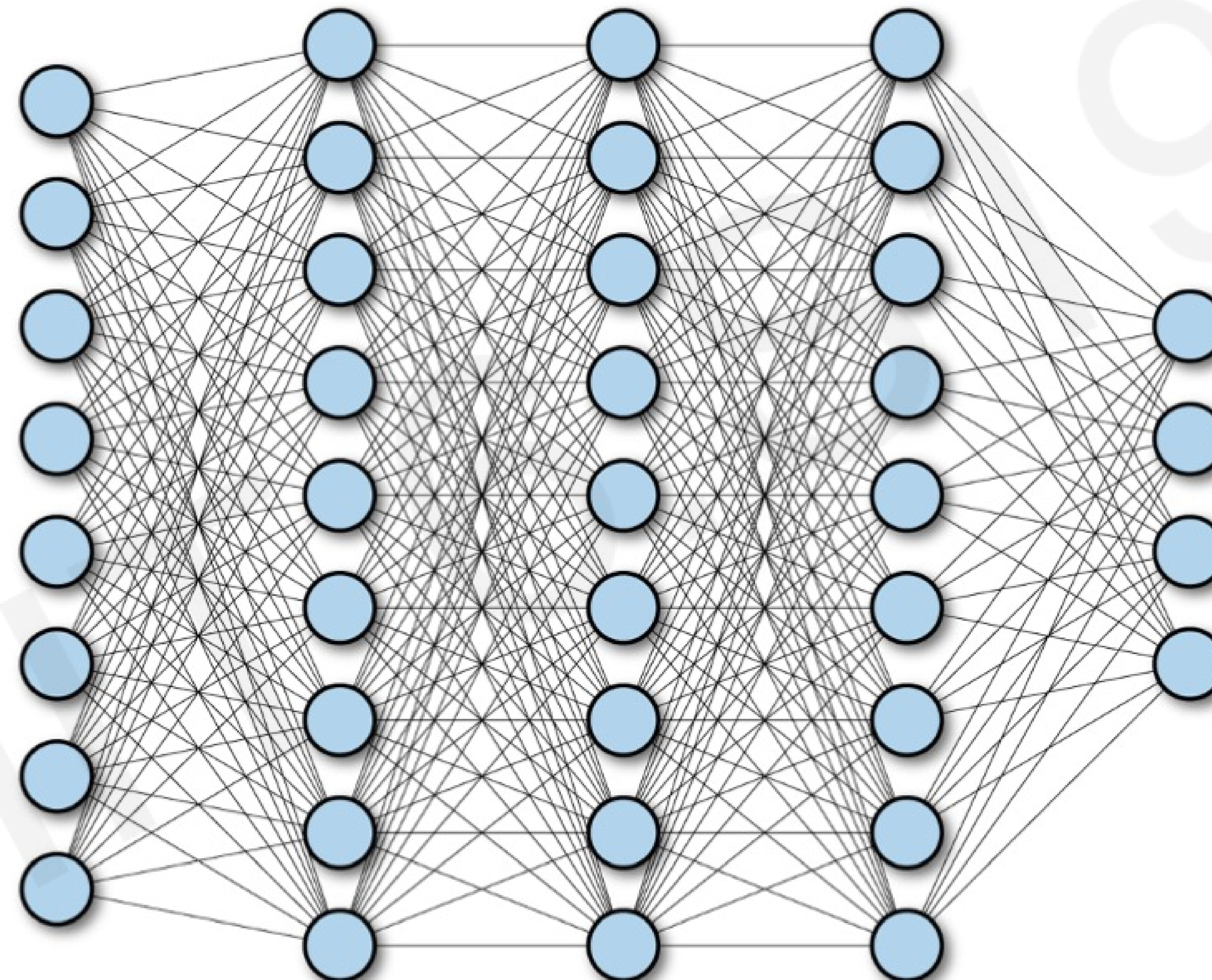
High level features



Facial structure

Learning Visual Features

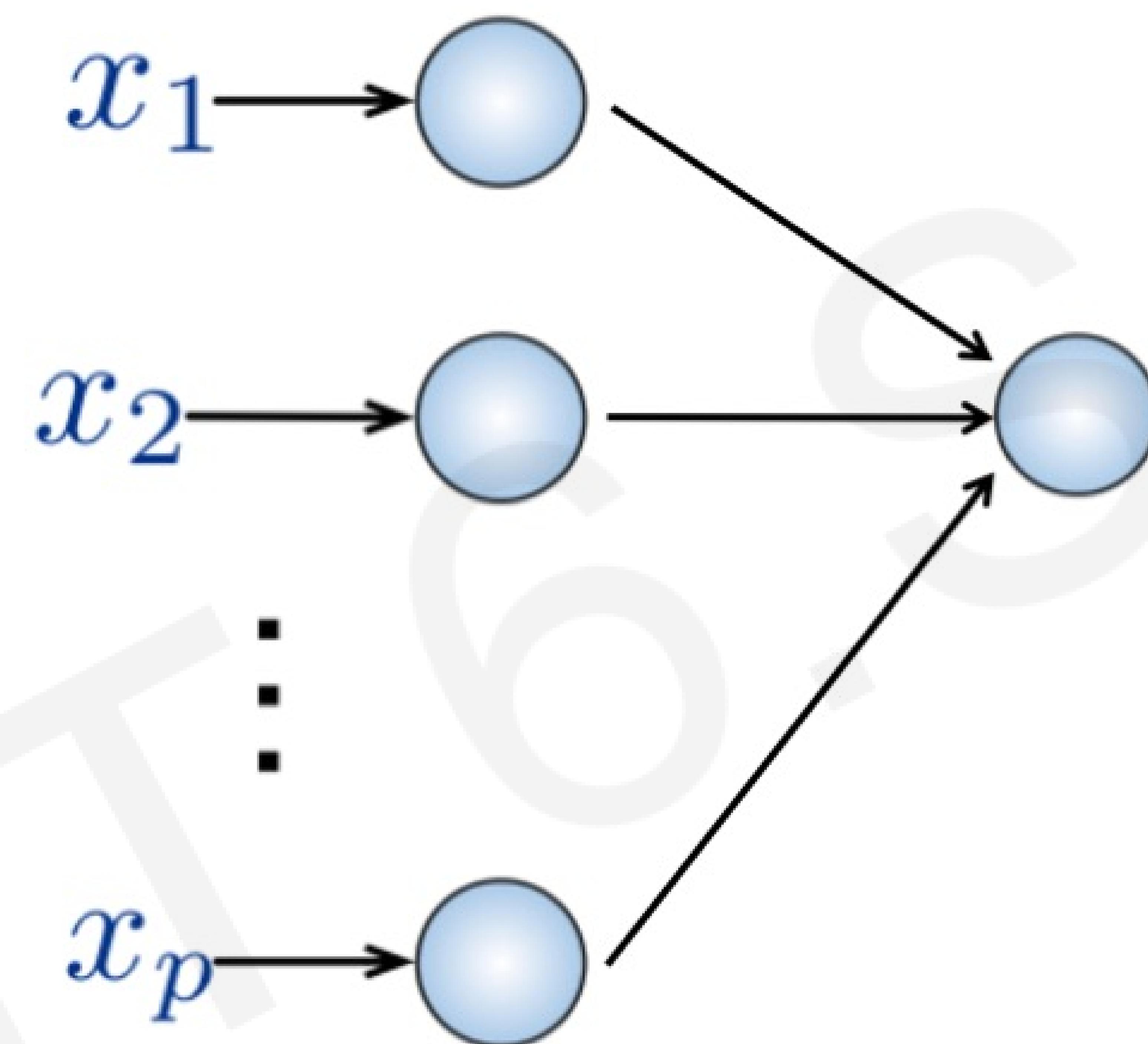
Fully Connected Neural Network



Fully Connected Neural Network

Input:

- 2D image
- Vector of pixel values



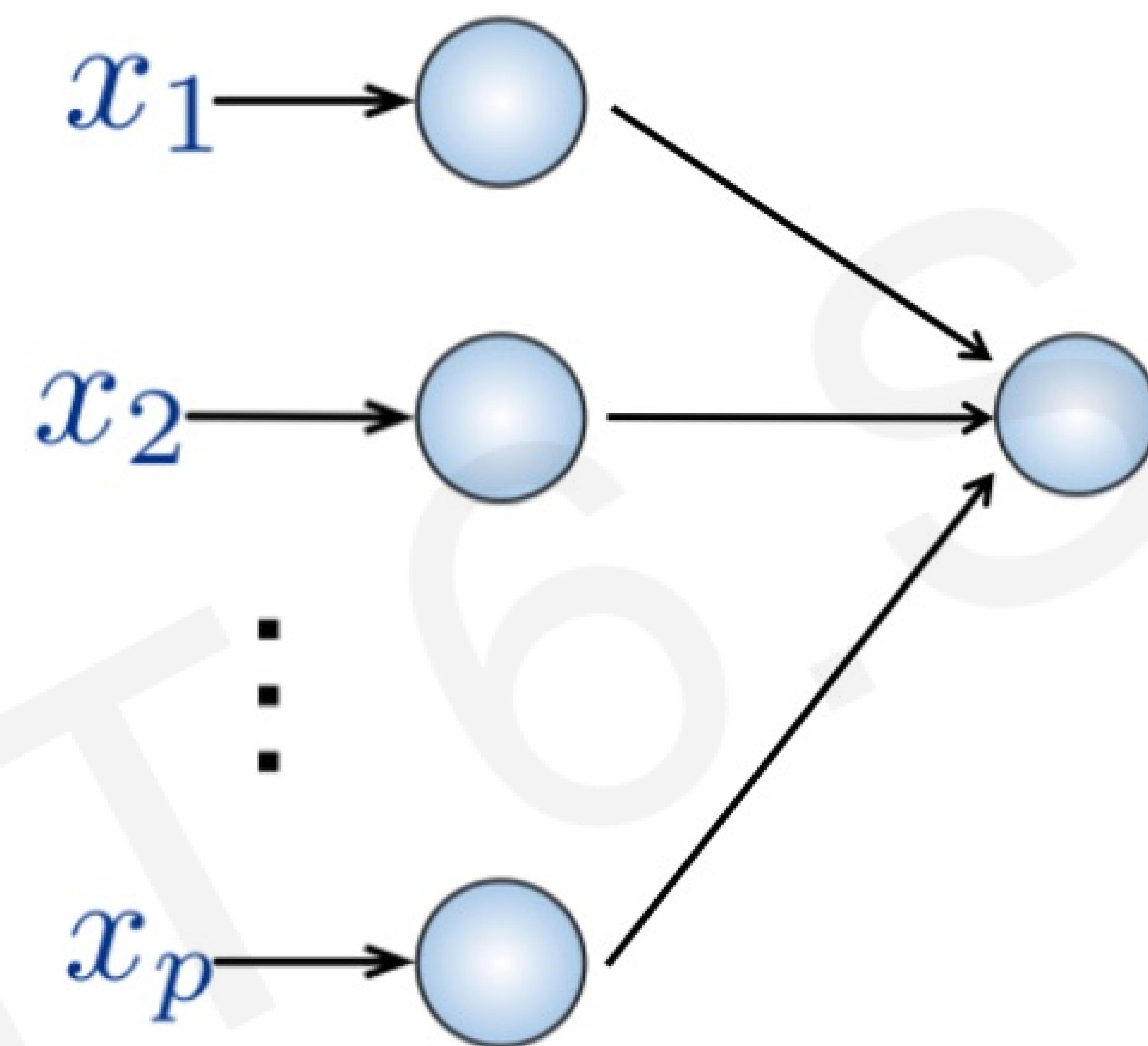
Fully Connected:

- Connect neuron in hidden layer to all neurons in input layer
- No spatial information!
- And many, many parameters!

Fully Connected Neural Network

Input:

- 2D image
- Vector of pixel values



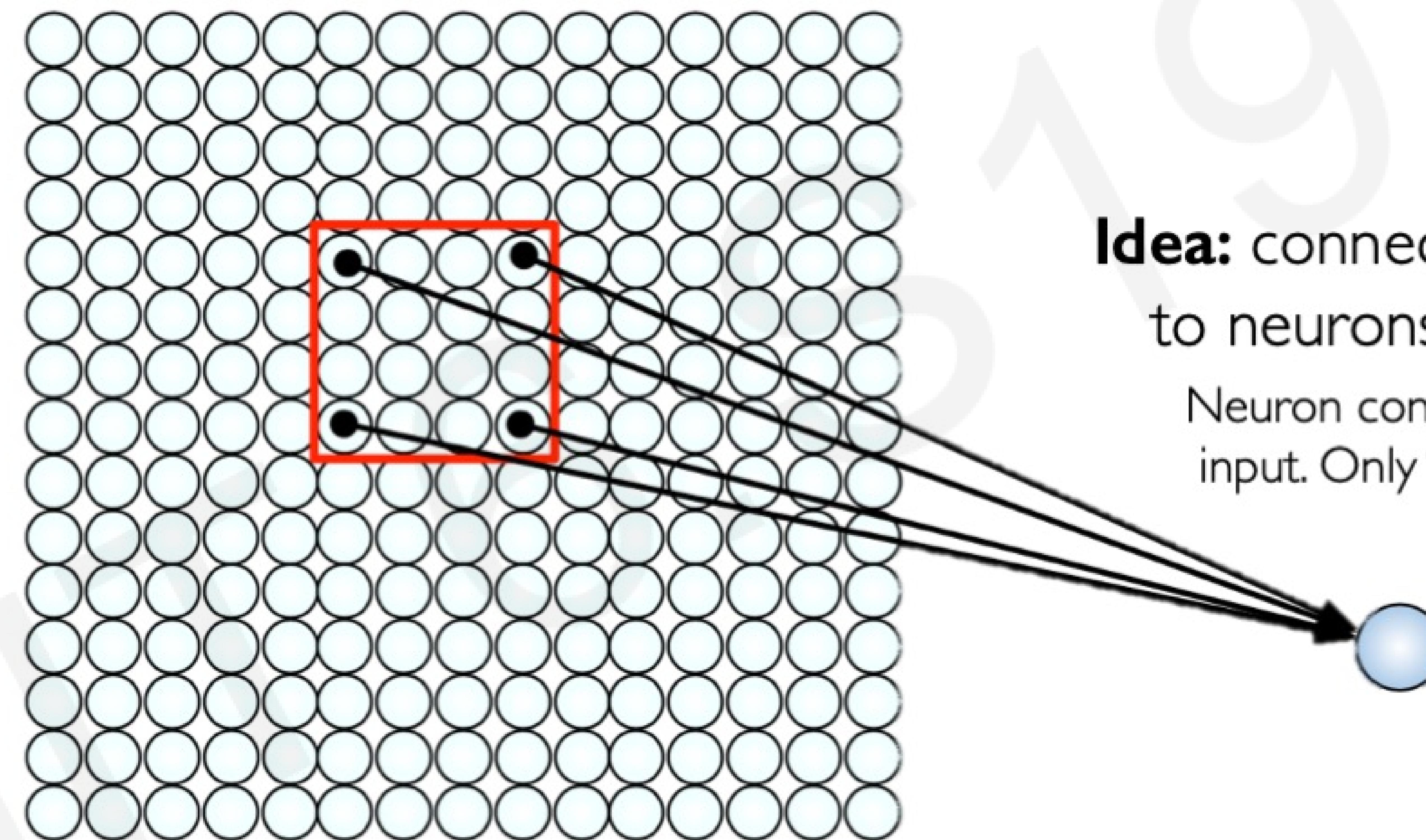
Fully Connected:

- Connect neuron in hidden layer to all neurons in input layer
- No spatial information!
- And many, many parameters!

How can we use **spatial structure** in the input to inform the architecture of the network?

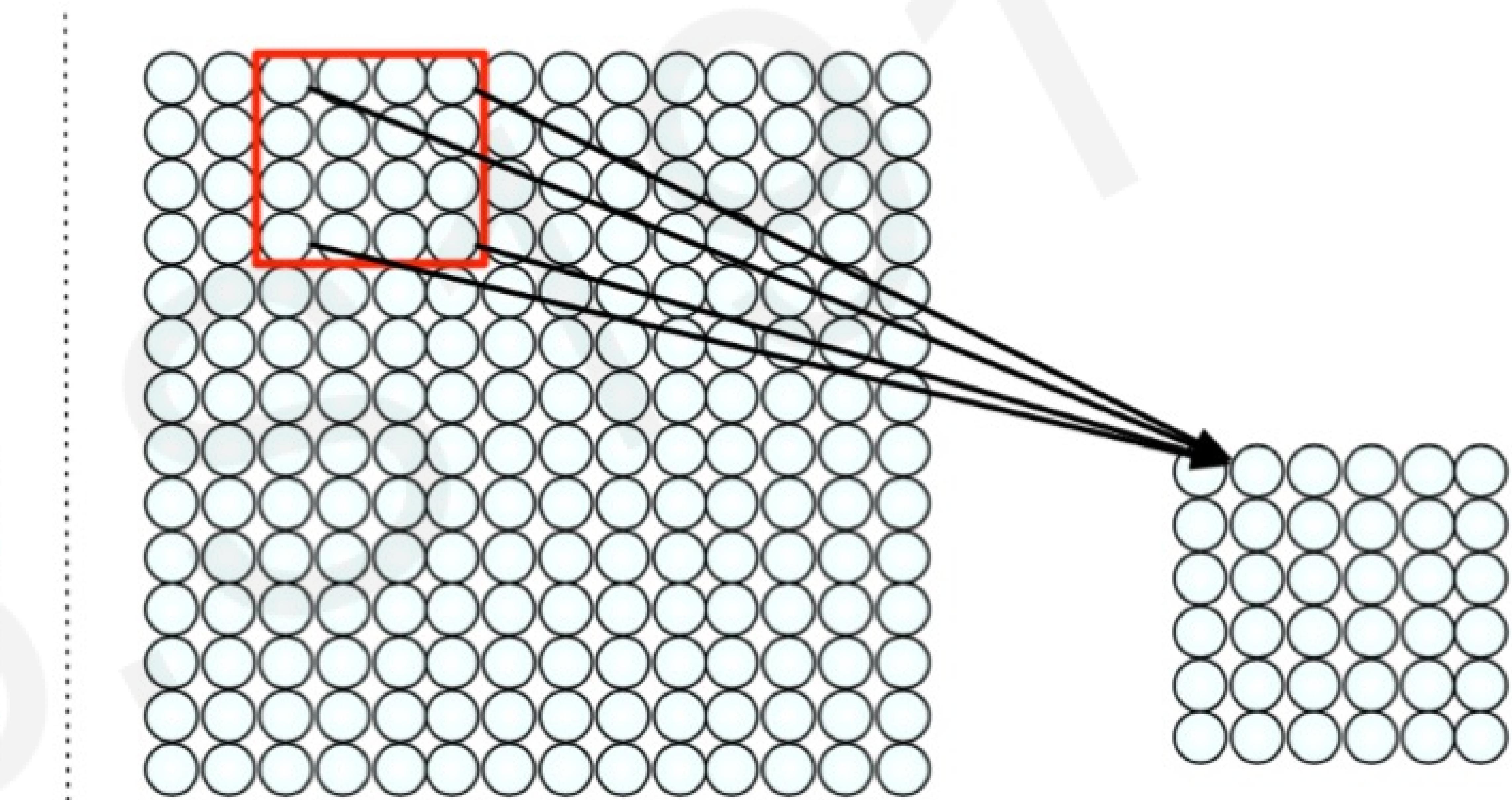
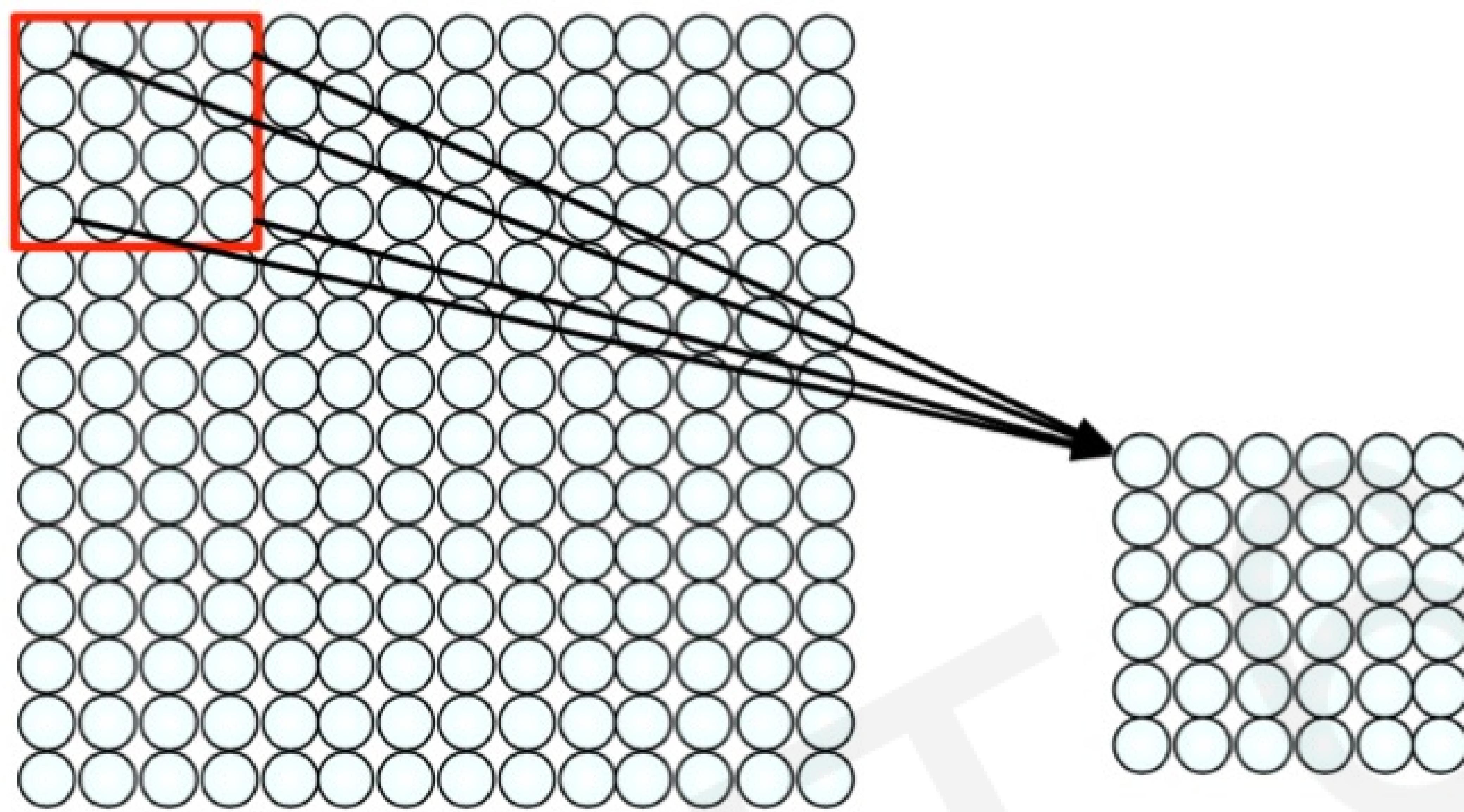
Using Spatial Structure

Input: 2D image.
Array of pixel values



Idea: connect patches of input
to neurons in hidden layer.
Neuron connected to region of
input. Only “sees” these values.

Using Spatial Structure



Connect patch in input layer to a single neuron in subsequent layer.

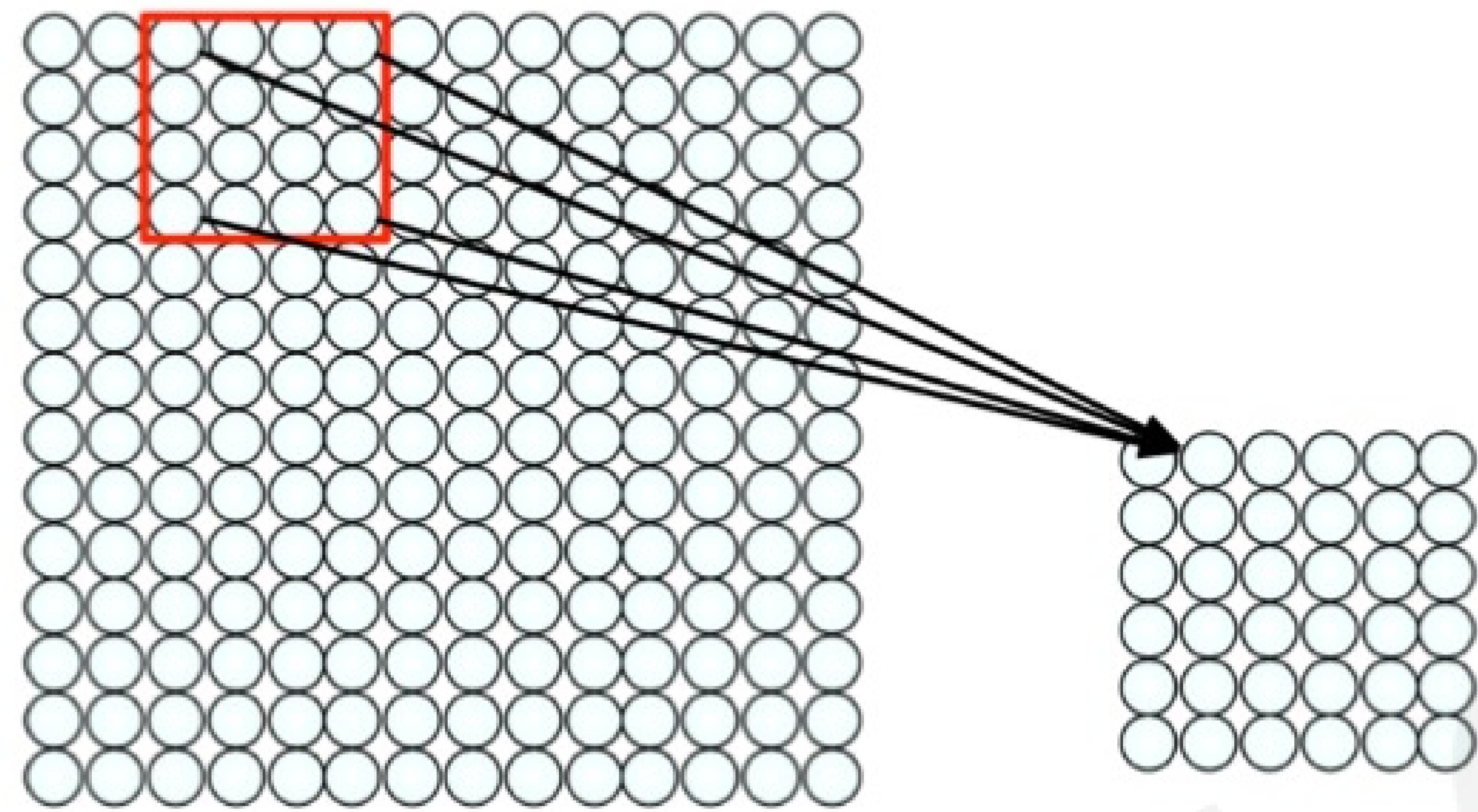
Use a sliding window to define connections.

*How can we **weight** the patch to detect particular features?*

Applying Filters to Extract Features

- 1) Apply a set of weights – a filter – to extract **local features**
- 2) Use **multiple filters** to extract different features
- 3) Spatially **share** parameters of each filter
(features that matter in one part of the input should matter elsewhere)

Feature Extraction with Convolution



- Filter of size 4×4 : 16 different weights
- Apply this same filter to 4×4 patches in input
- Shift by 2 pixels for next patch

This “patchy” operation is **convolution**

- 1) Apply a set of weights – a filter – to extract **local features**
- 2) Use **multiple filters** to extract different features
- 3) **Spatially share** parameters of each filter

Feature Extraction and Convolution

A Case Study

X or X?

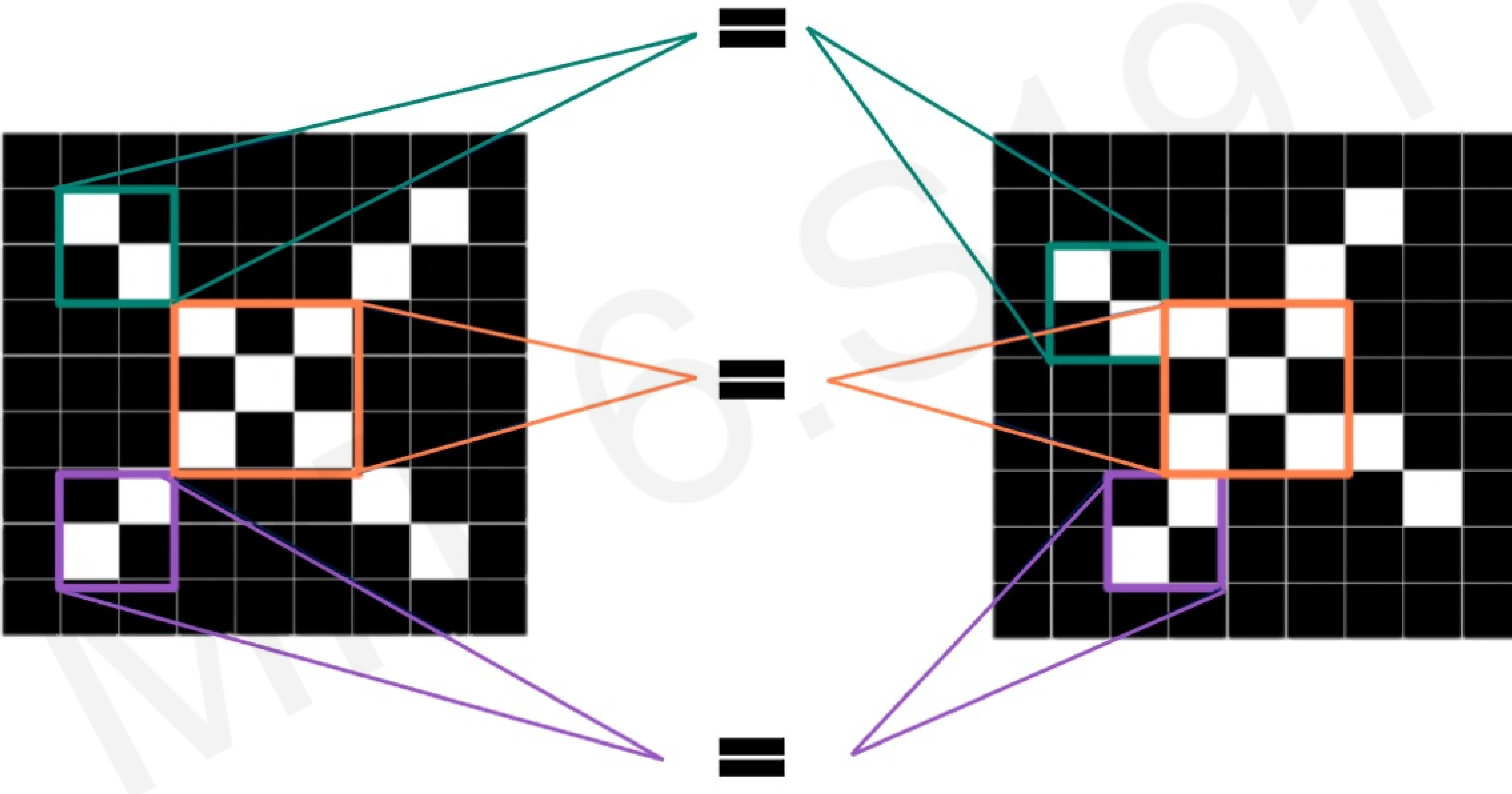


| | | | | | | | | |
|----|----|----|----|----|----|----|----|----|
| -1 | -1 | -1 | -1 | -1 | -1 | -1 | -1 | -1 |
| -1 | 1 | -1 | -1 | -1 | -1 | -1 | 1 | -1 |
| -1 | -1 | 1 | -1 | -1 | -1 | 1 | -1 | -1 |
| -1 | -1 | -1 | 1 | -1 | 1 | -1 | -1 | -1 |
| -1 | -1 | -1 | -1 | 1 | -1 | -1 | -1 | -1 |
| -1 | -1 | -1 | -1 | 1 | -1 | -1 | -1 | -1 |
| -1 | -1 | -1 | 1 | -1 | 1 | -1 | -1 | -1 |
| -1 | -1 | 1 | -1 | -1 | -1 | 1 | -1 | -1 |
| -1 | 1 | -1 | -1 | -1 | -1 | 1 | -1 | -1 |
| -1 | -1 | -1 | -1 | -1 | -1 | -1 | -1 | -1 |

| | | | | | | | | |
|----|----|----|----|----|----|----|----|----|
| -1 | -1 | -1 | -1 | -1 | -1 | -1 | -1 | -1 |
| -1 | -1 | -1 | -1 | -1 | -1 | -1 | 1 | -1 |
| -1 | 1 | -1 | -1 | -1 | -1 | 1 | -1 | -1 |
| -1 | -1 | 1 | 1 | -1 | -1 | 1 | -1 | -1 |
| -1 | -1 | -1 | -1 | 1 | -1 | -1 | -1 | -1 |
| -1 | -1 | -1 | -1 | 1 | -1 | -1 | -1 | -1 |
| -1 | -1 | -1 | 1 | -1 | 1 | -1 | -1 | -1 |
| -1 | -1 | 1 | -1 | -1 | -1 | 1 | -1 | -1 |
| -1 | -1 | -1 | -1 | -1 | -1 | -1 | 1 | -1 |
| -1 | -1 | -1 | -1 | -1 | -1 | -1 | -1 | -1 |

Image is represented as matrix of pixel values... and computers are literal!
We want to be able to classify an X as an X even if it's shifted, shrunk, rotated, deformed.

Features of X



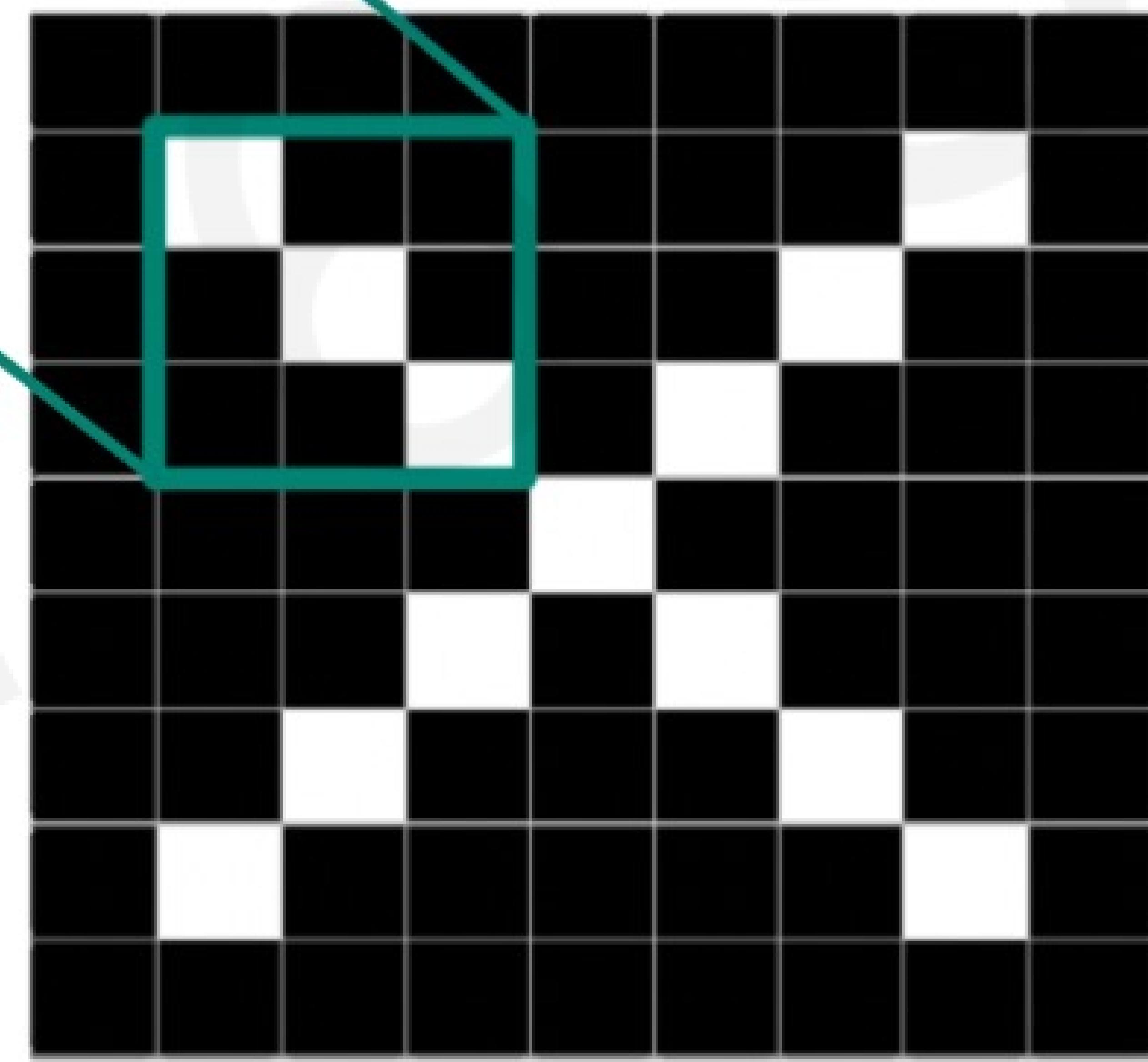
Filters to Detect X Features

filters

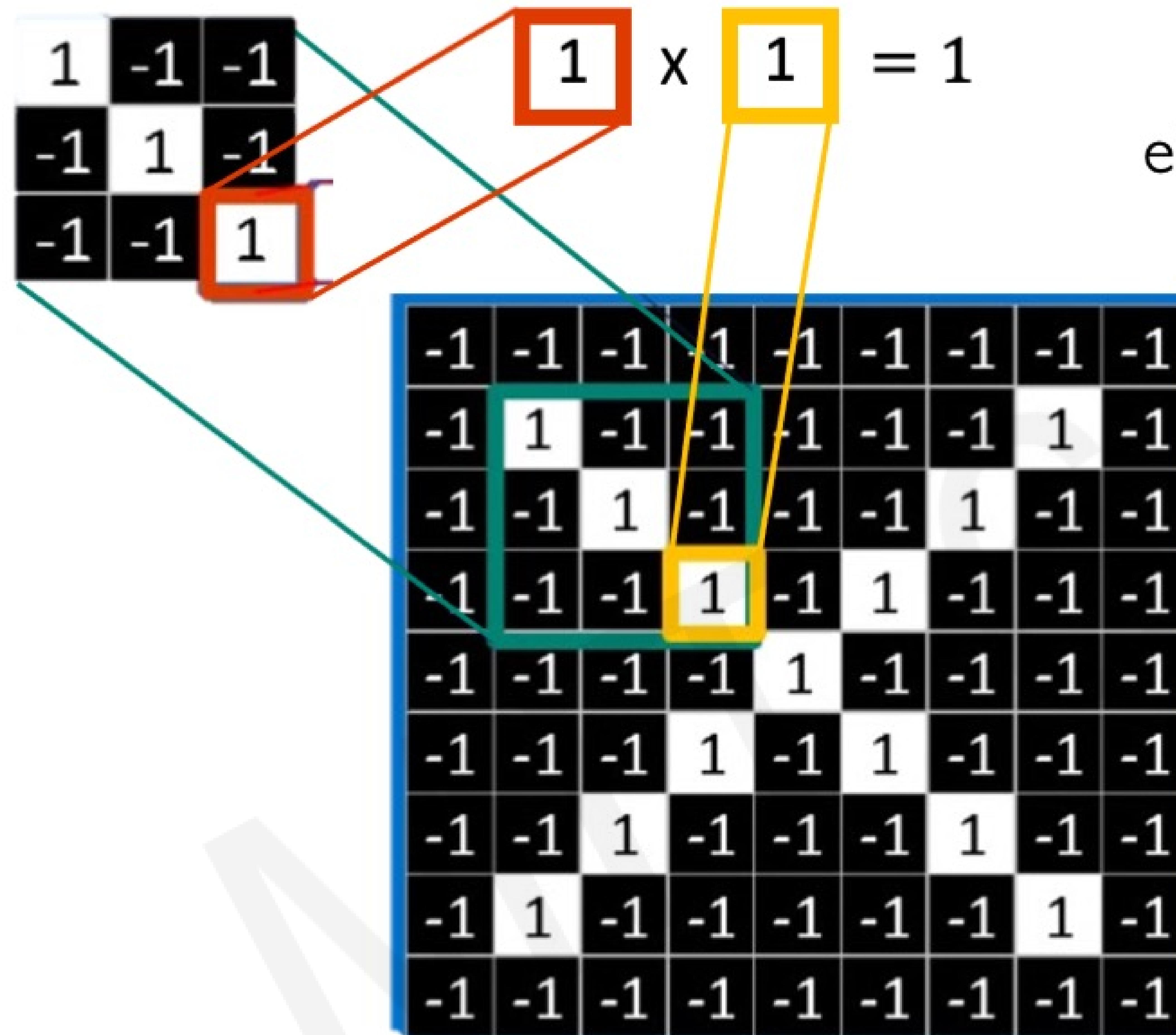
$$\begin{bmatrix} 1 & -1 & -1 \\ -1 & 1 & -1 \\ -1 & -1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & -1 & 1 \\ -1 & 1 & -1 \\ 1 & -1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -1 & -1 & 1 \\ -1 & 1 & -1 \\ 1 & -1 & -1 \end{bmatrix}$$

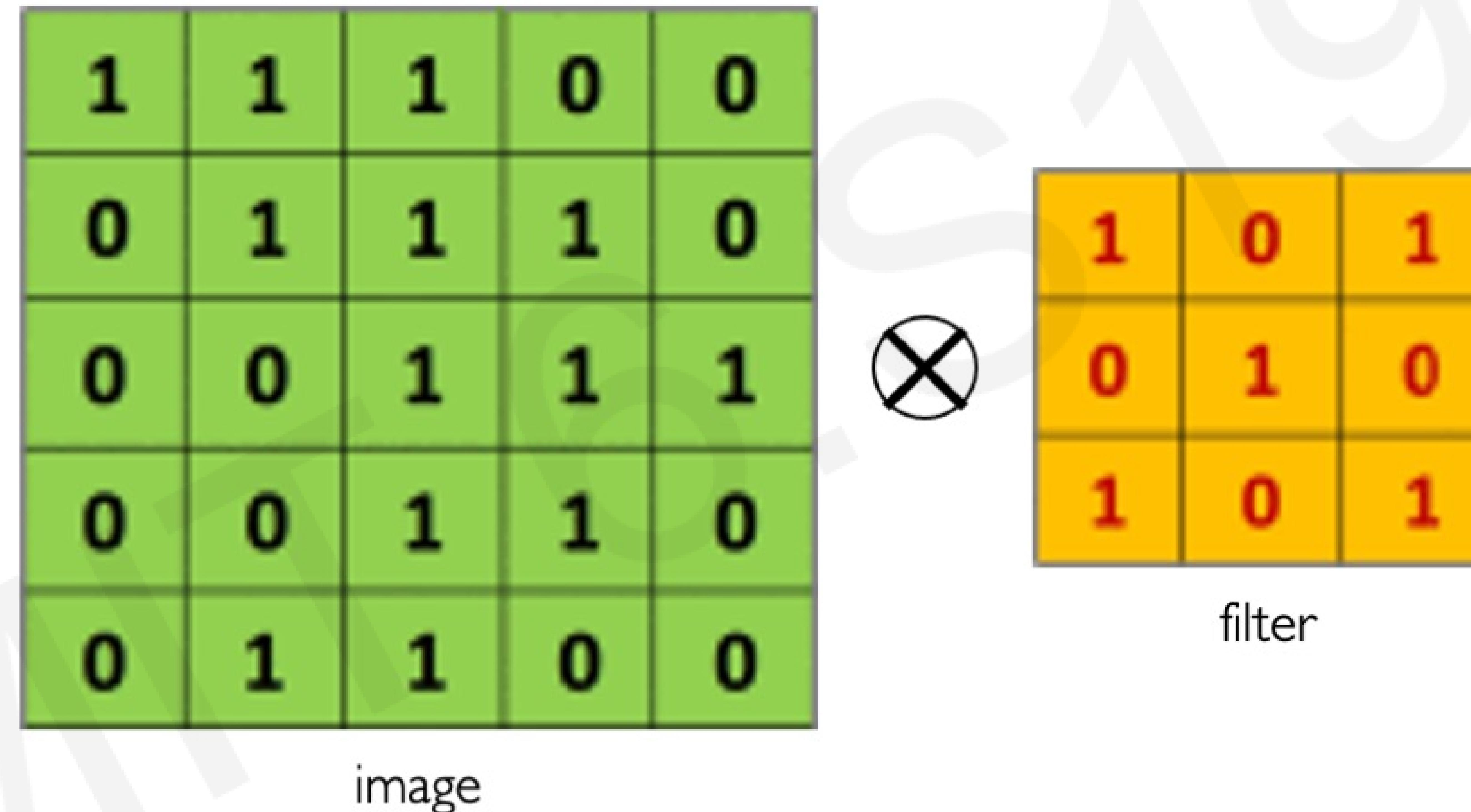


The Convolution Operation



The Convolution Operation

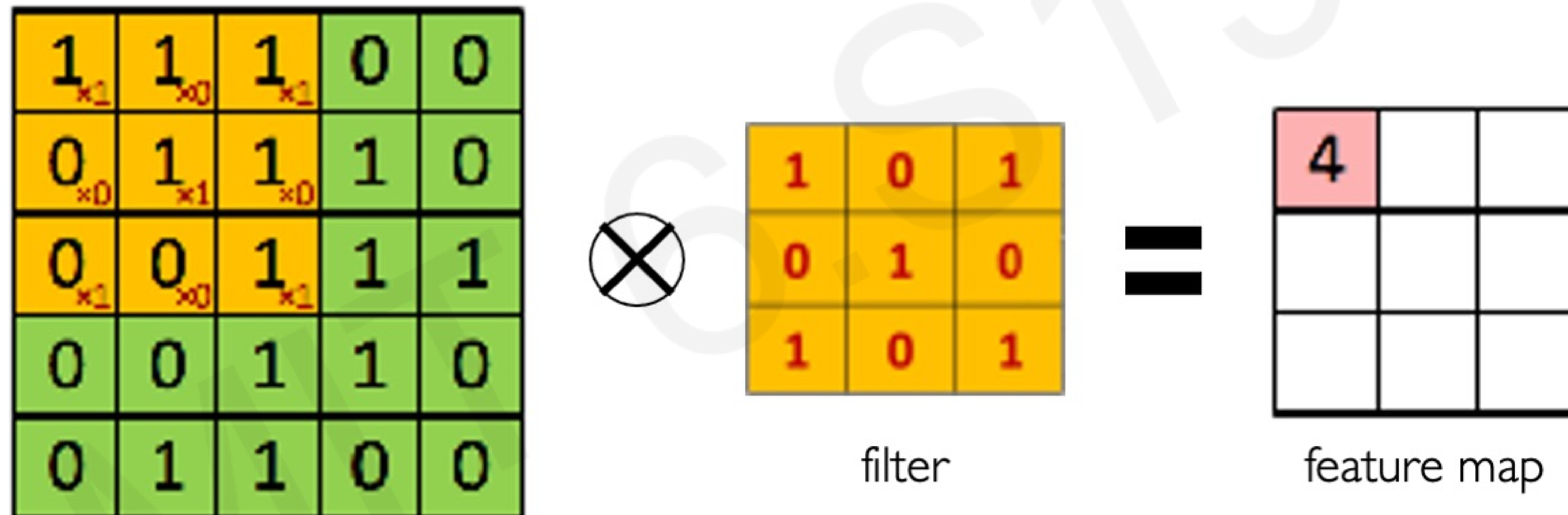
Suppose we want to compute the convolution of a 5x5 image and a 3x3 filter:



We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs...

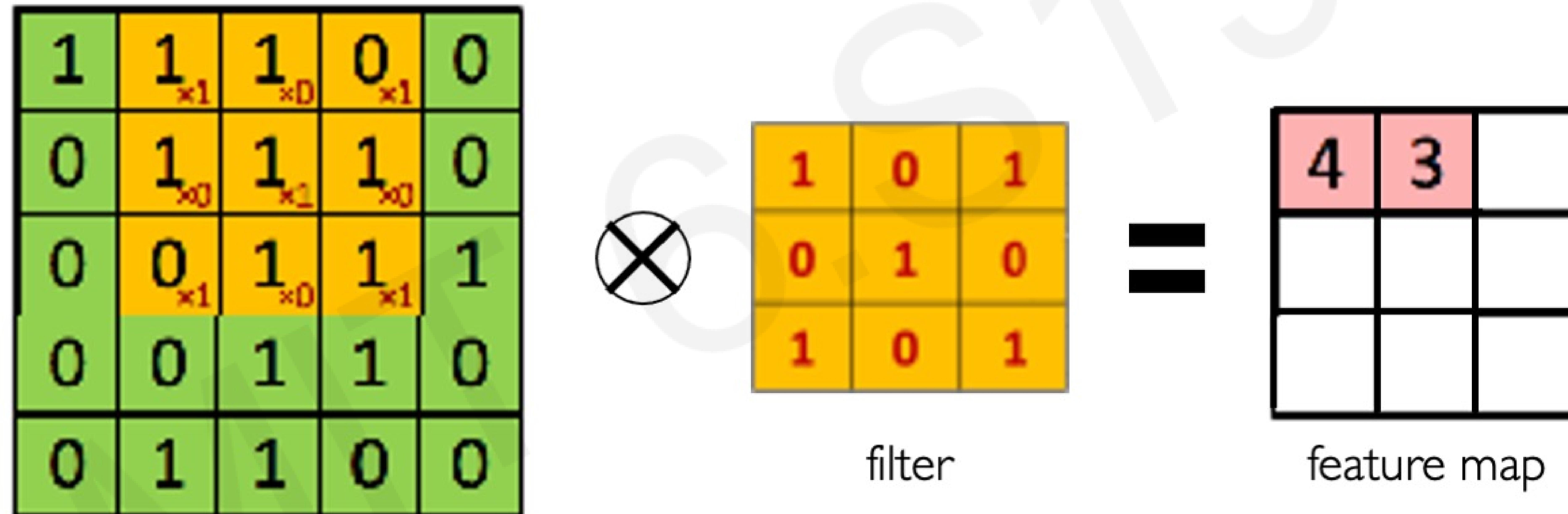
The Convolution Operation

We slide the 3×3 filter over the input image, element-wise multiply, and add the outputs:



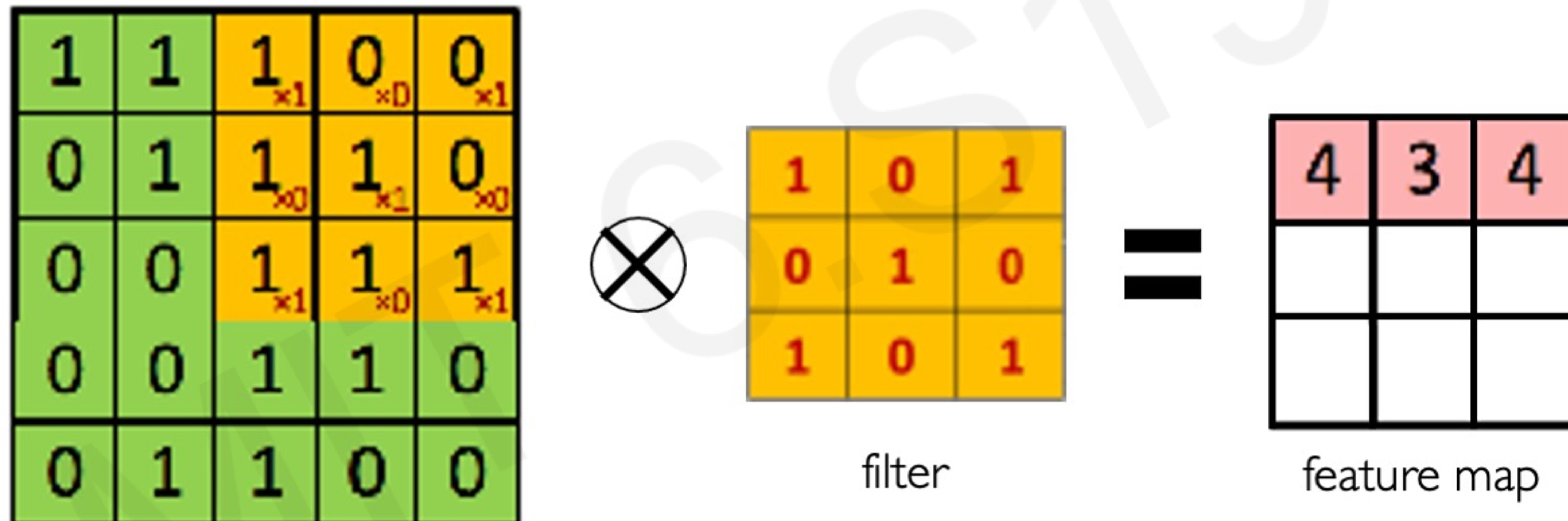
The Convolution Operation

We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs:



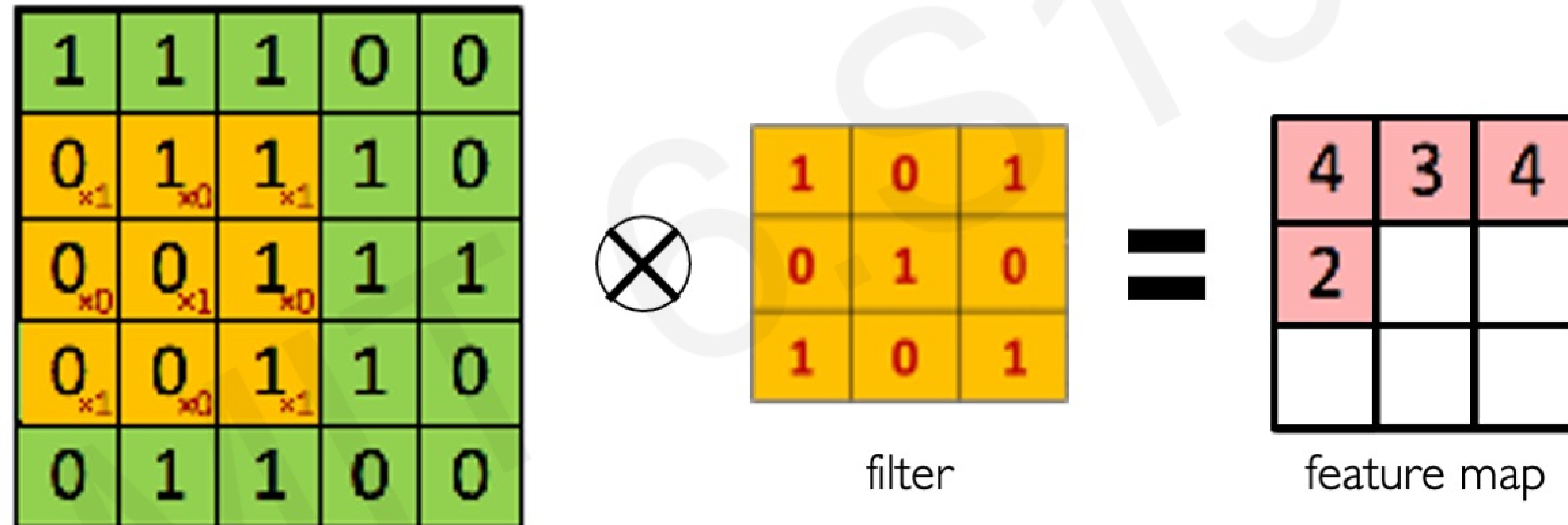
The Convolution Operation

We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs:



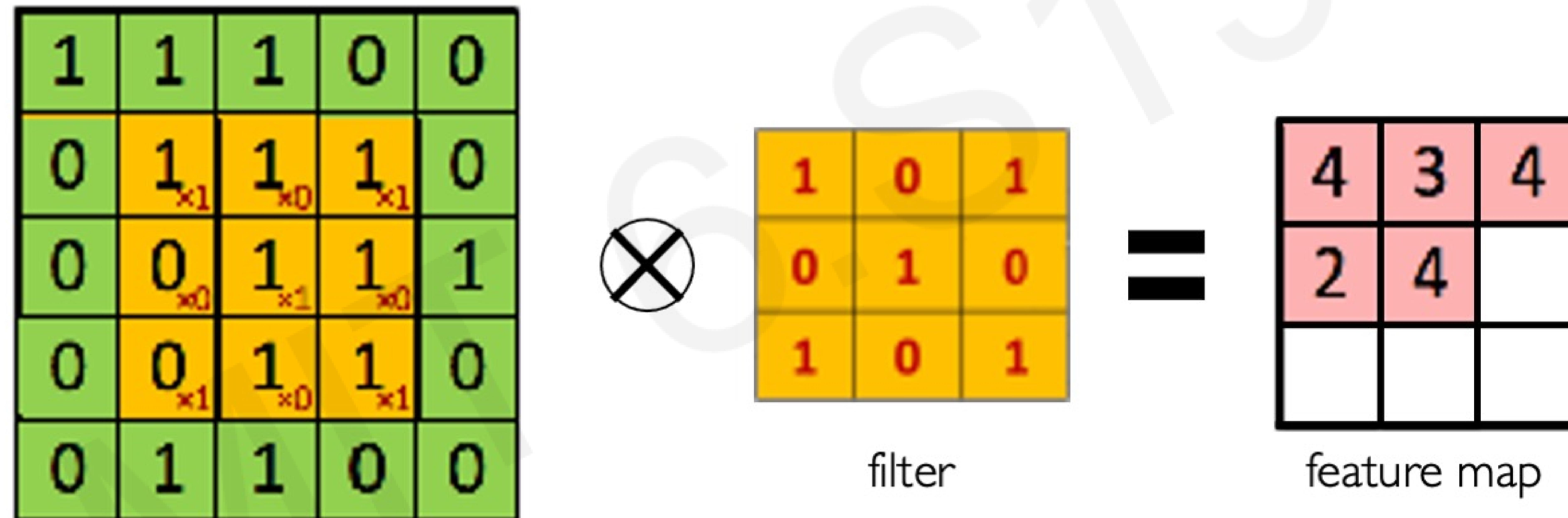
The Convolution Operation

We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs:



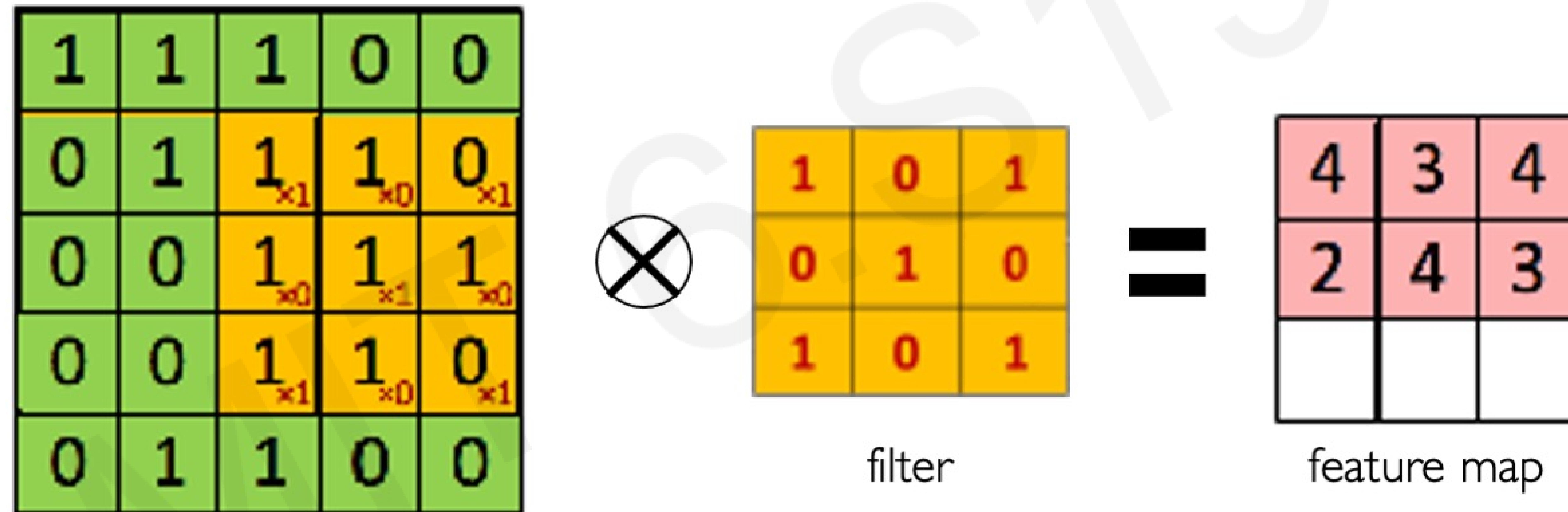
The Convolution Operation

We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs:



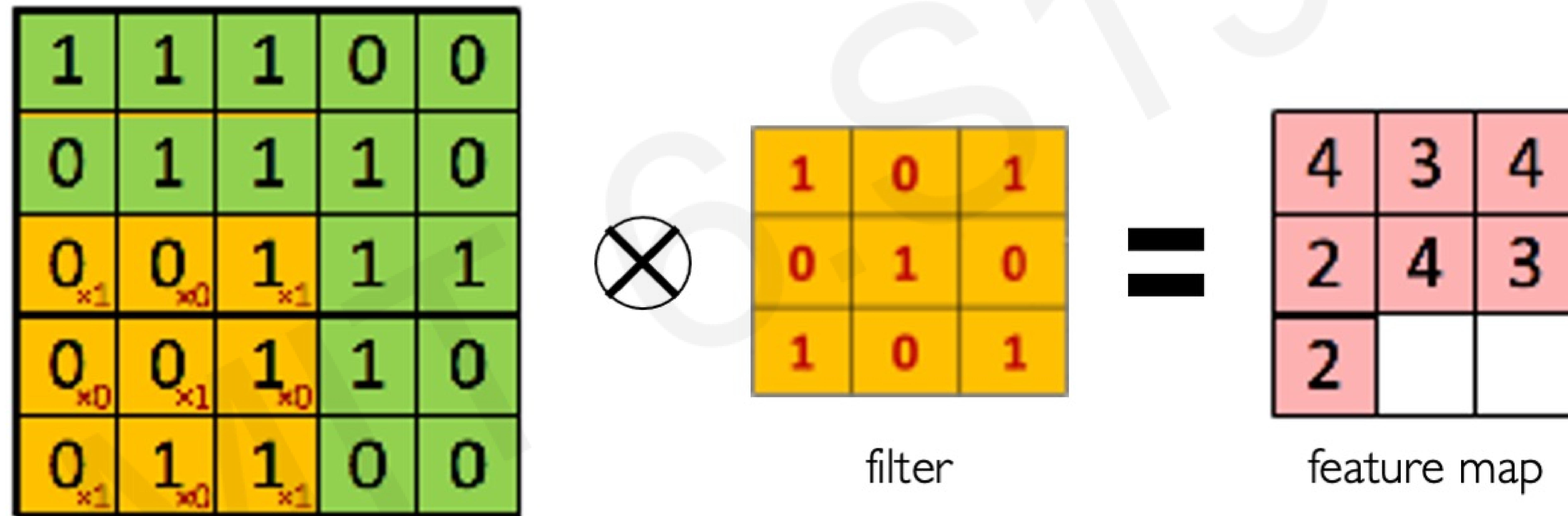
The Convolution Operation

We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs:



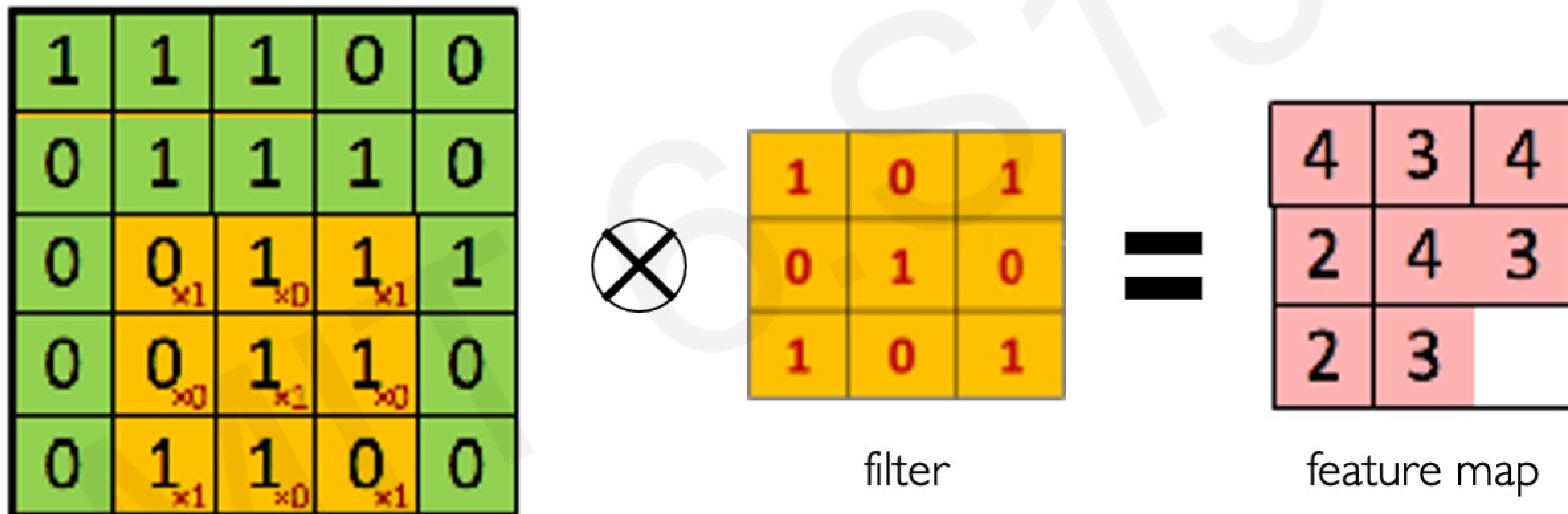
The Convolution Operation

We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs:



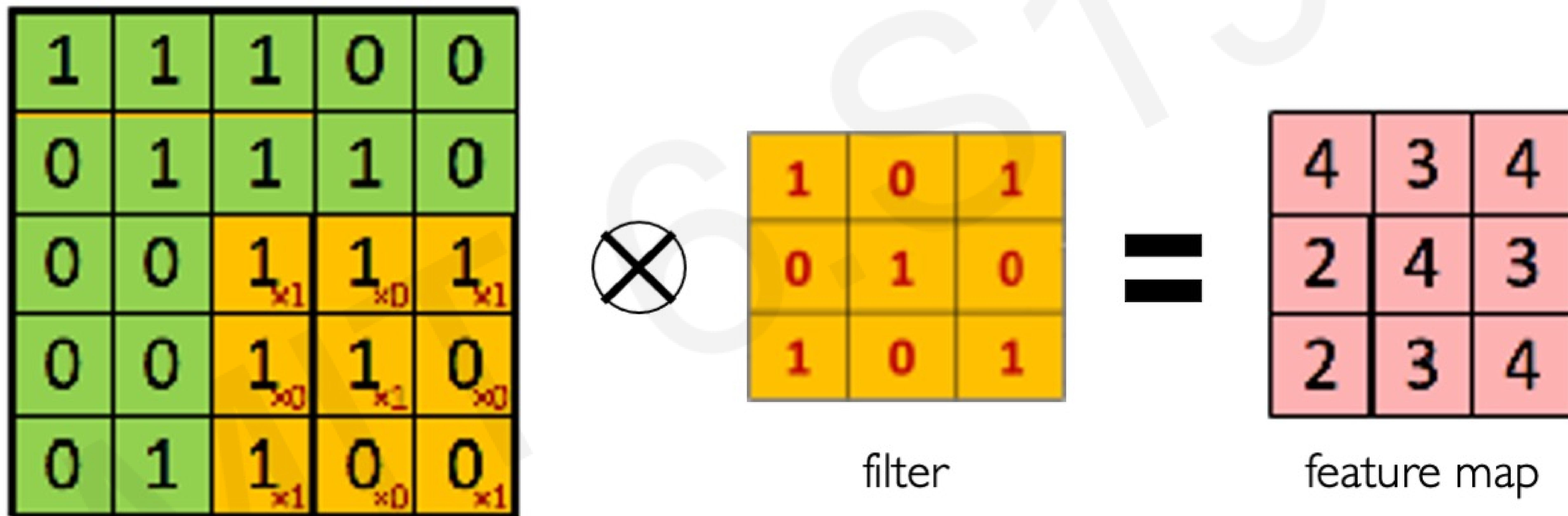
The Convolution Operation

We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs:



The Convolution Operation

We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs:



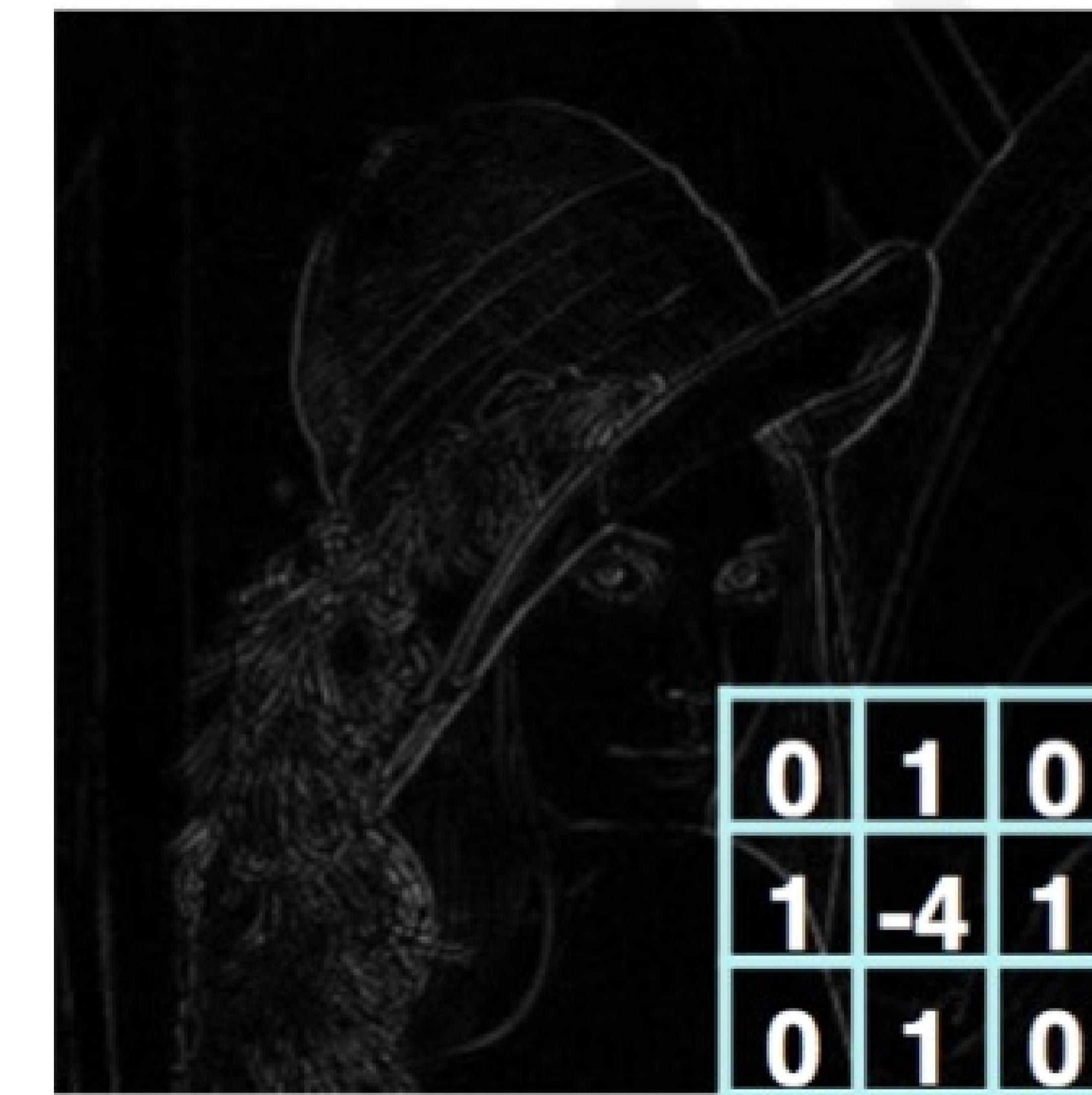
Producing Feature Maps



Original



Sharpen

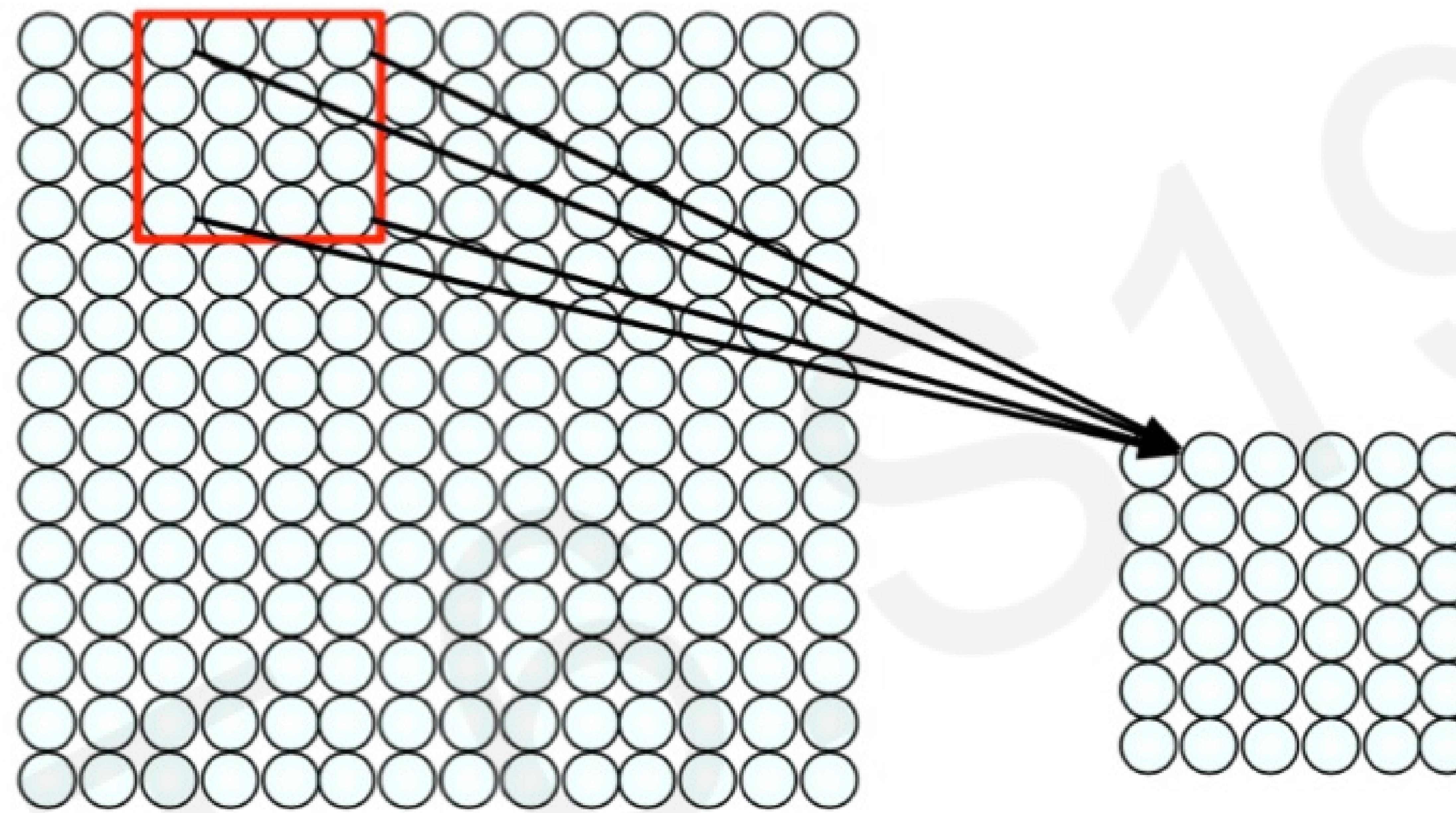


Edge Detect



“Strong” Edge
Detect

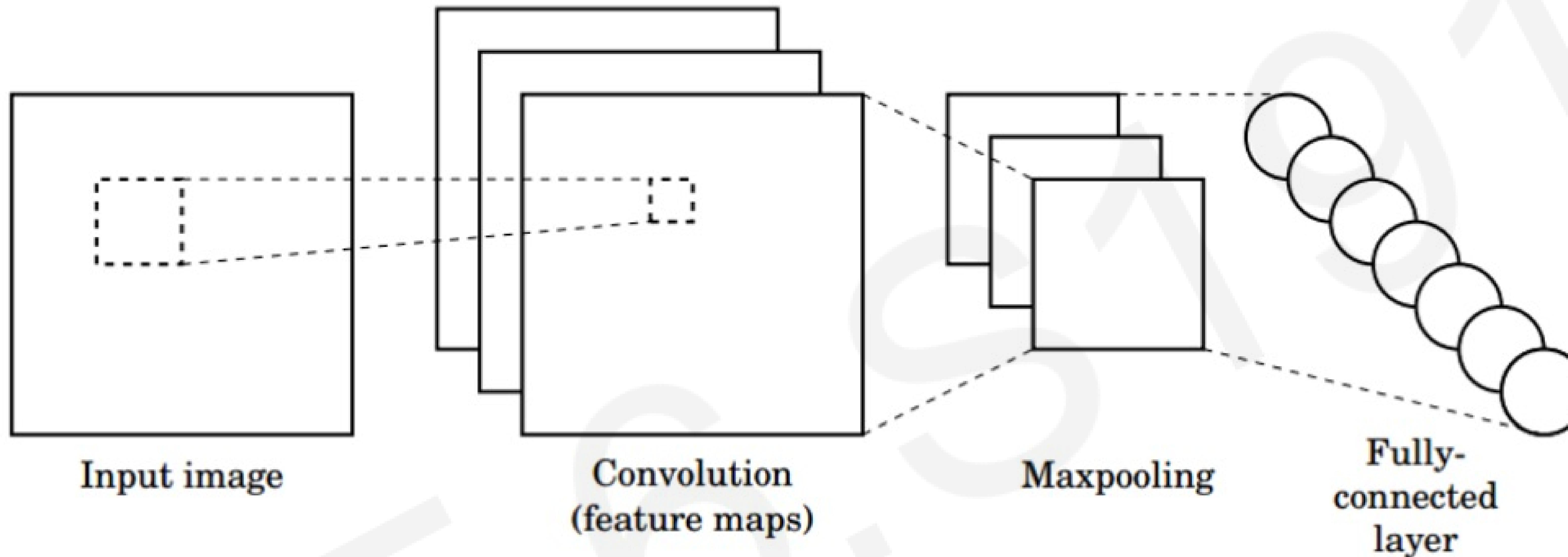
Feature Extraction with Convolution



- 1) Apply a set of weights – a filter – to extract **local features**
- 2) Use **multiple filters** to extract different features
- 3) **Spatially share** parameters of each filter

Convolutional Neural Networks (CNNs)

CNNs for Classification



1. Convolution: Apply filters to generate feature maps.

 `tf.keras.layers.Conv2D`

2. Non-linearity: Often ReLU.

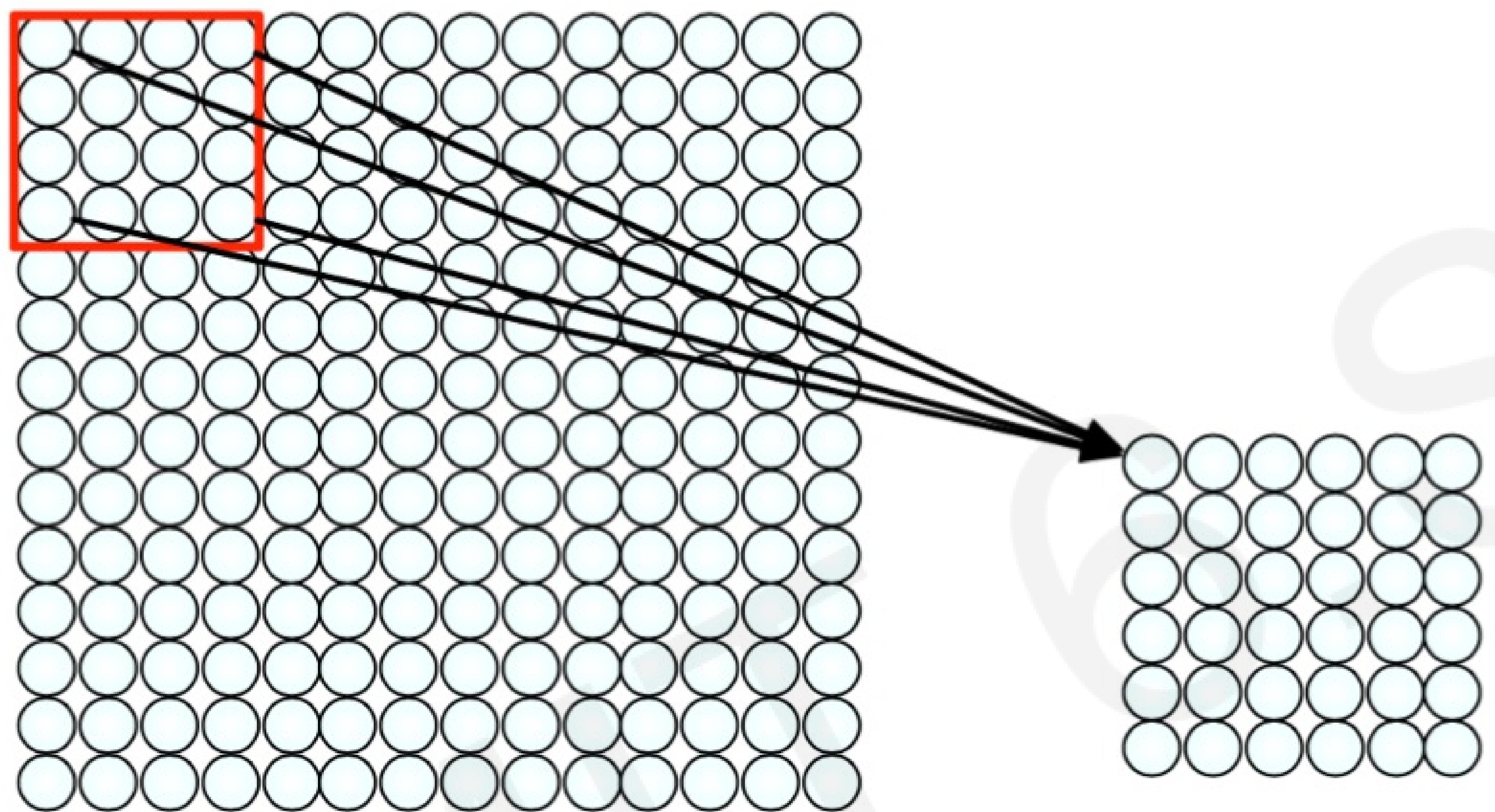
 `tf.keras.activations.*`

3. Pooling: Downsampling operation on each feature map.

 `tf.keras.layers.MaxPool2D`

Train model with image data.
Learn weights of filters in convolutional layers.

Convolutional Layers: Local Connectivity

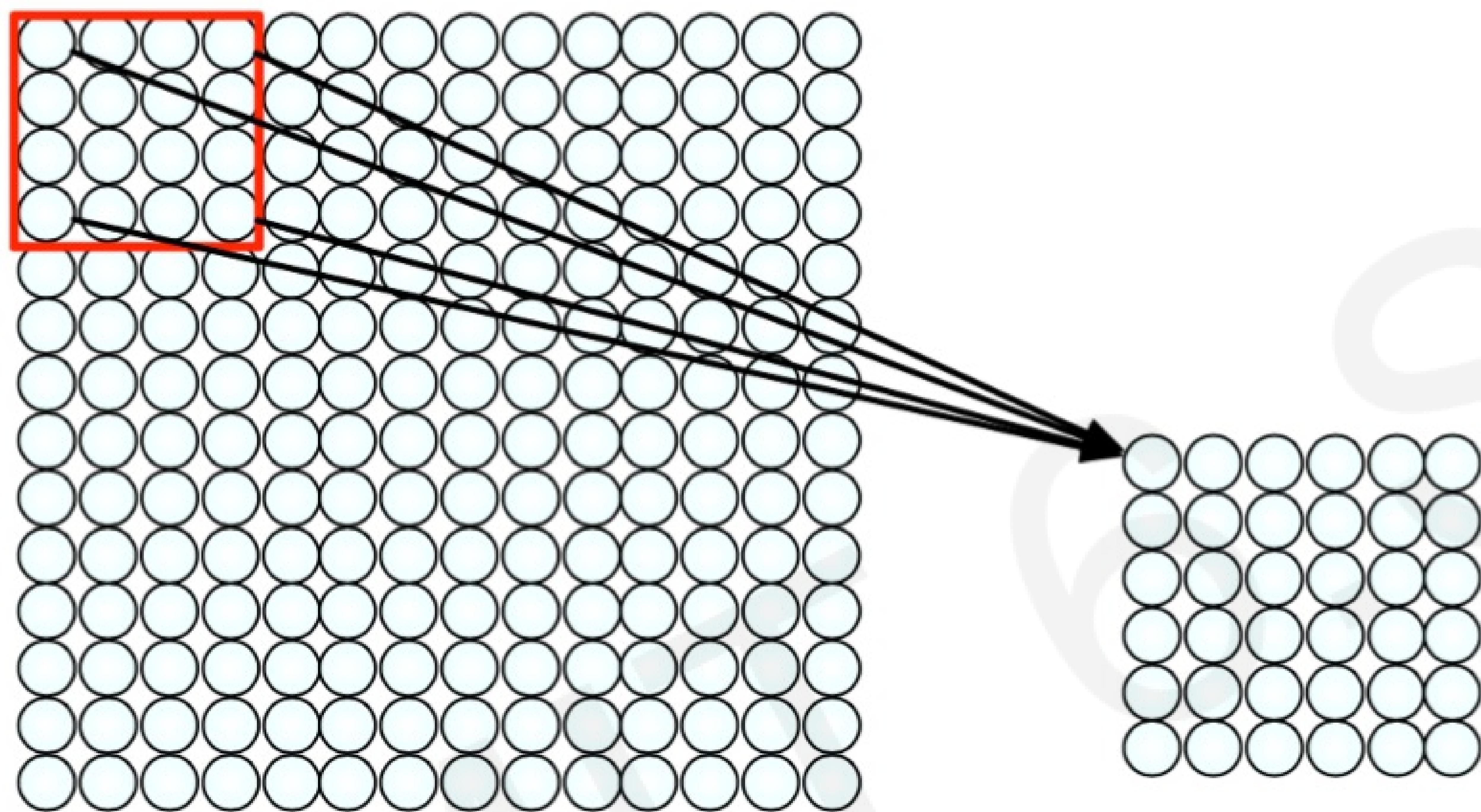


 `tf.keras.layers.Conv2D`

For a neuron in hidden layer:

- Take inputs from patch
- Compute weighted sum
- Apply bias

Convolutional Layers: Local Connectivity



4x4 filter: matrix
of weights w_{ij}

$$\sum_{i=1}^4 \sum_{j=1}^4 w_{ij} x_{i+p,j+q} + b$$

for neuron (p,q) in hidden layer



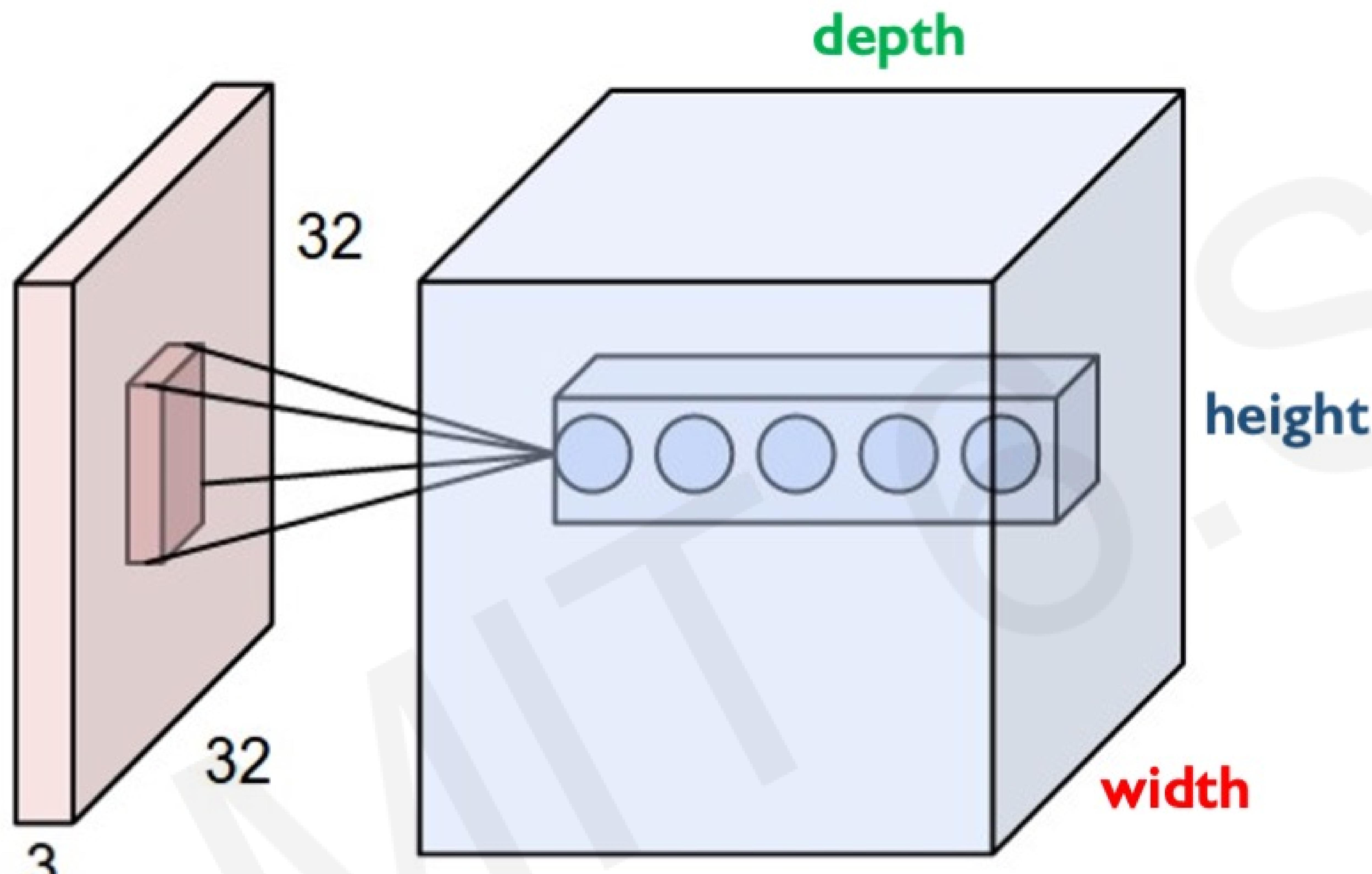
`tf.keras.layers.Conv2D`

For a neuron in hidden layer:

- Take inputs from patch
- Compute weighted sum
- Apply bias

- 1) applying a window of weights
- 2) computing linear combinations
- 3) activating with non-linear function

CNNs: Spatial Arrangement of Output Volume



Layer Dimensions:

$h \times w \times d$

where h and w are spatial dimensions
 d (depth) = number of filters

Stride:

Filter step size

Receptive Field:

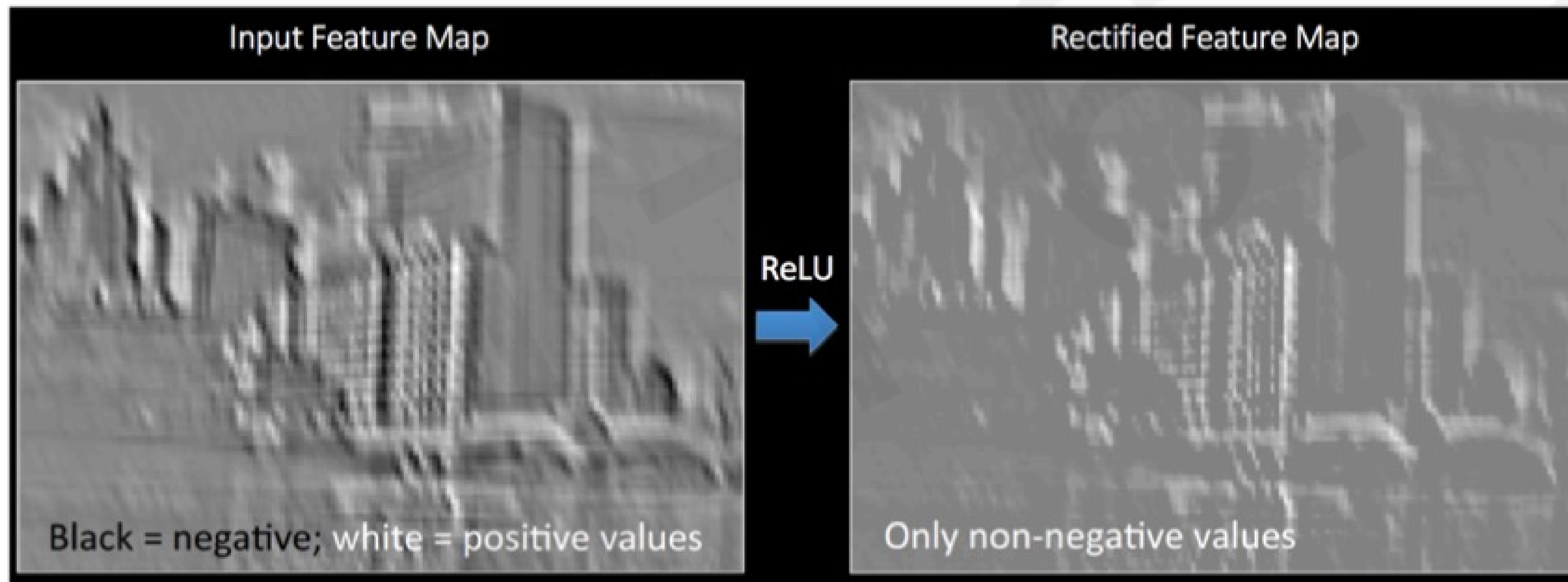
Locations in input image that
a node is path connected to



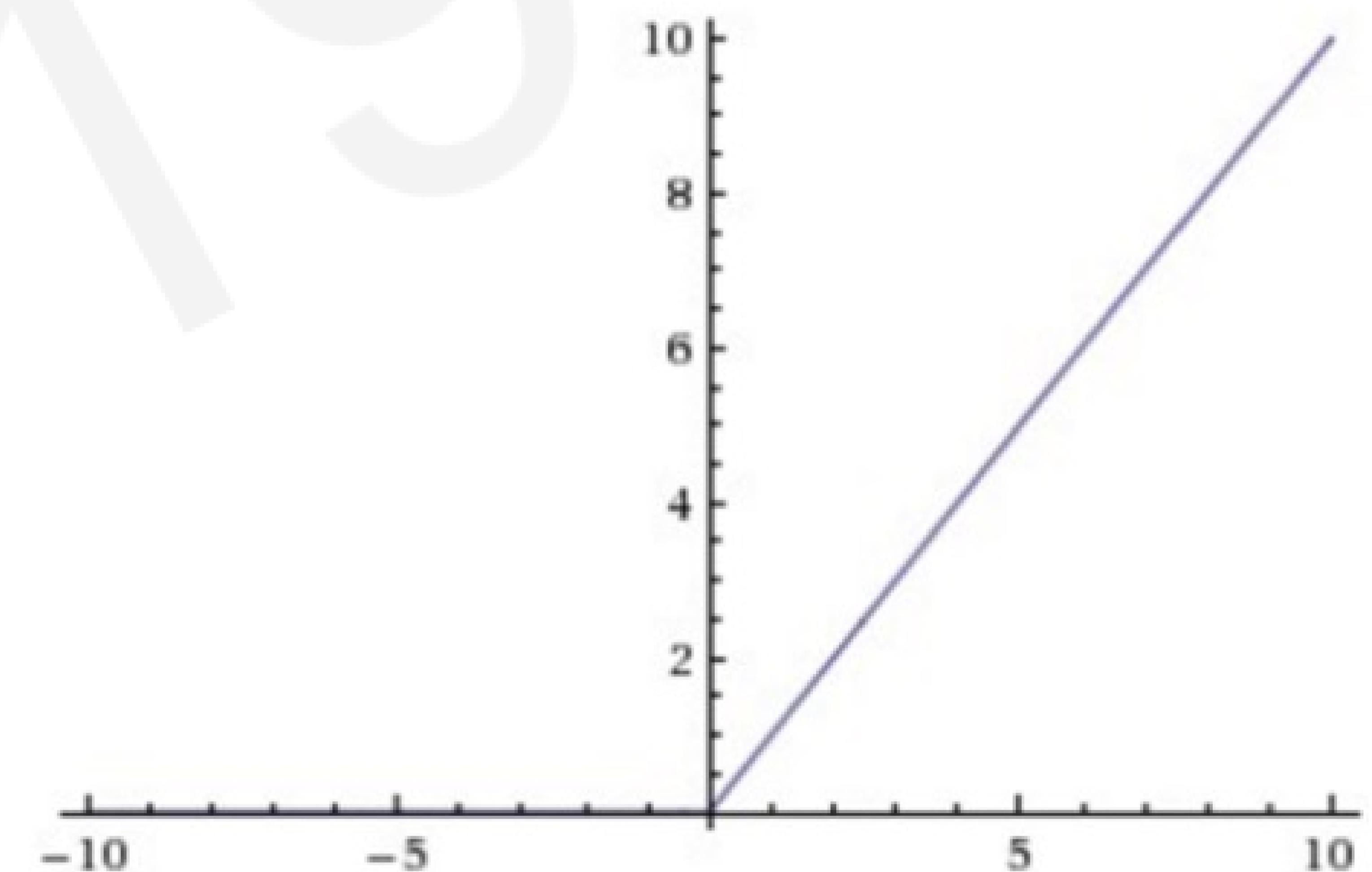
```
tf.keras.layers.Conv2D( filters=d, kernel_size=(h,w), strides=s )
```

Introducing Non-Linearity

- Apply after every convolution operation (i.e., after convolutional layers)
- ReLU: pixel-by-pixel operation that replaces all negative values by zero. **Non-linear operation!**

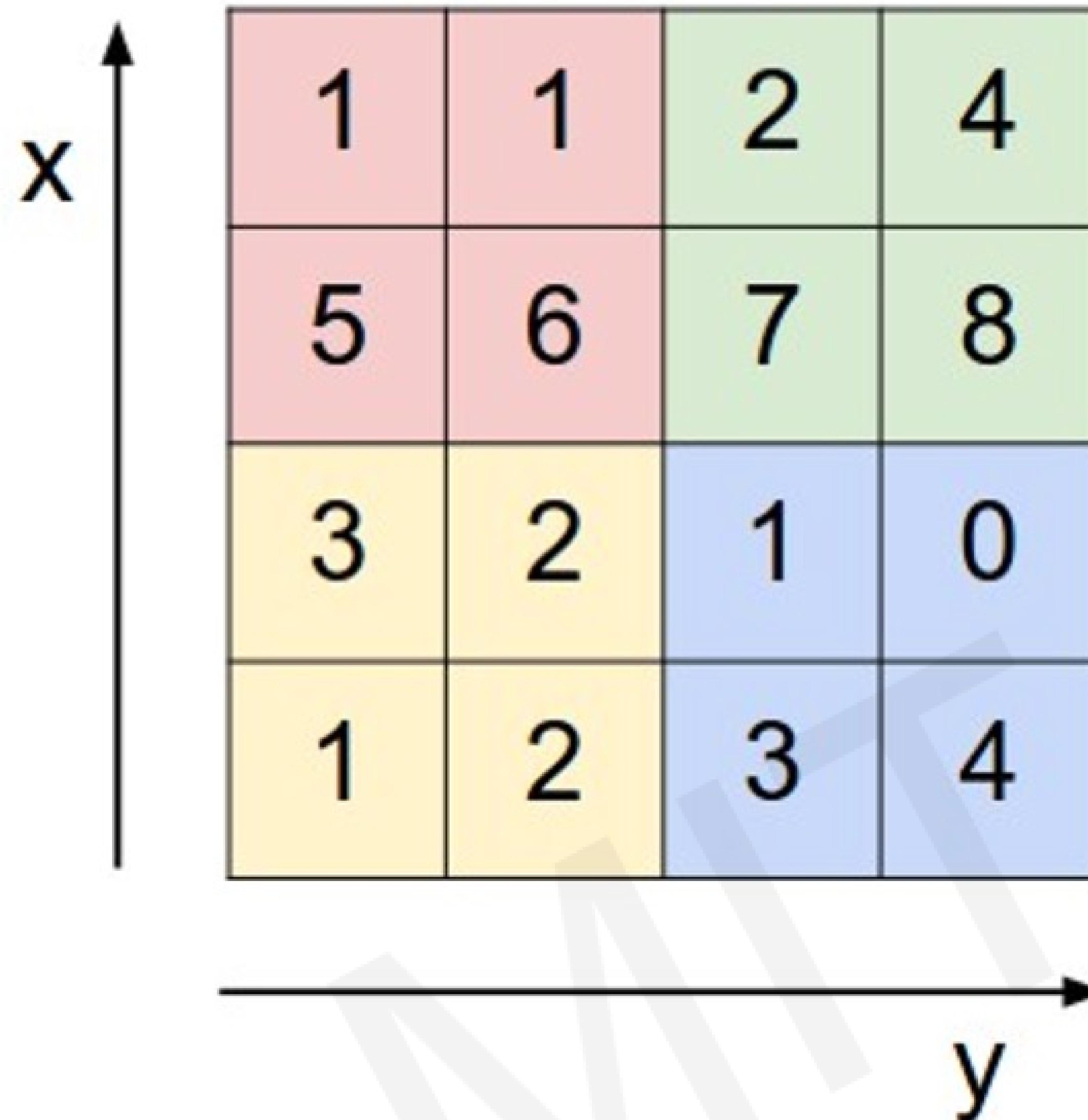


Rectified Linear Unit (ReLU)



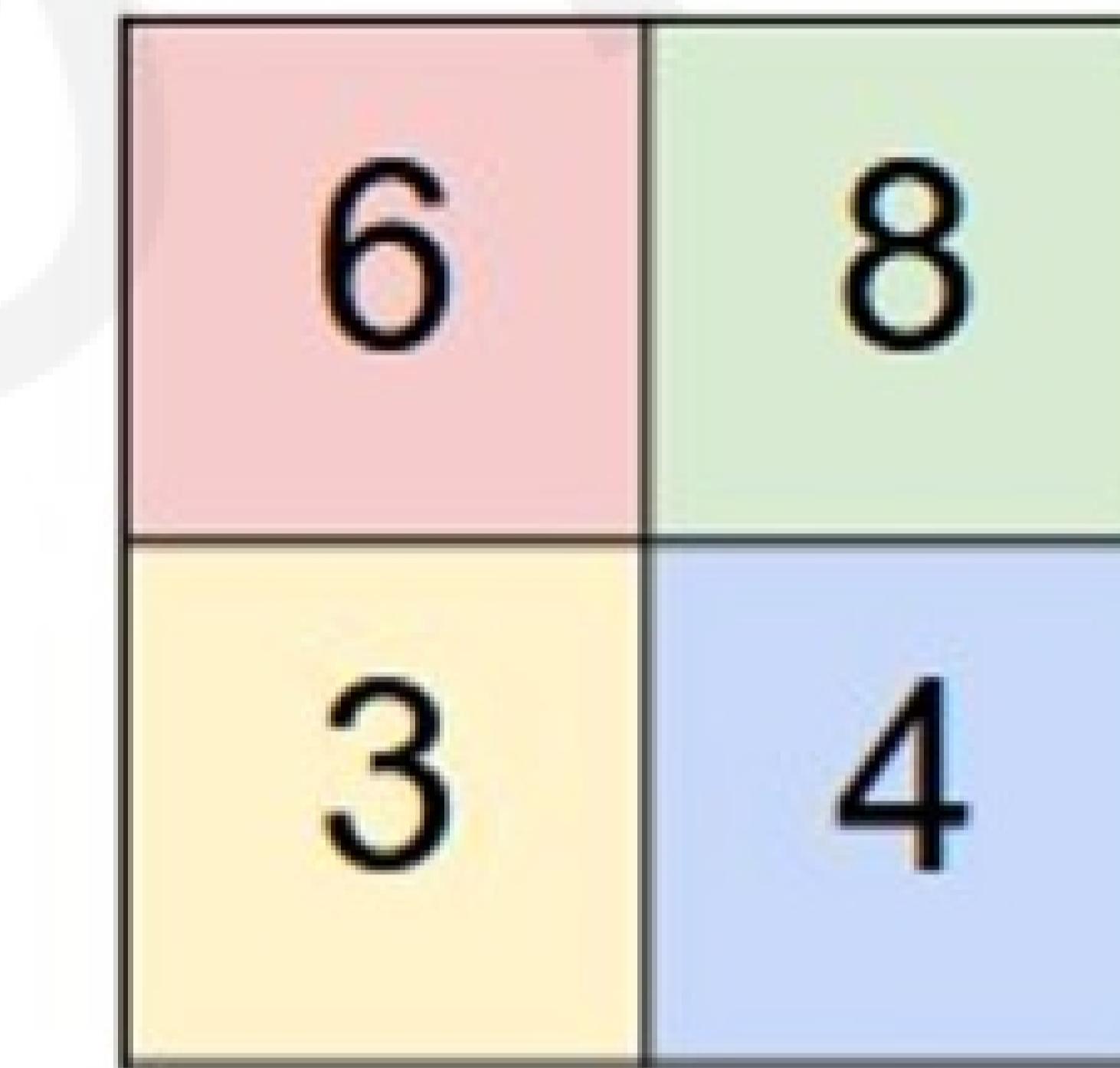
 `tf.keras.layers.ReLU`

Pooling



max pool with 2x2 filters
and stride 2

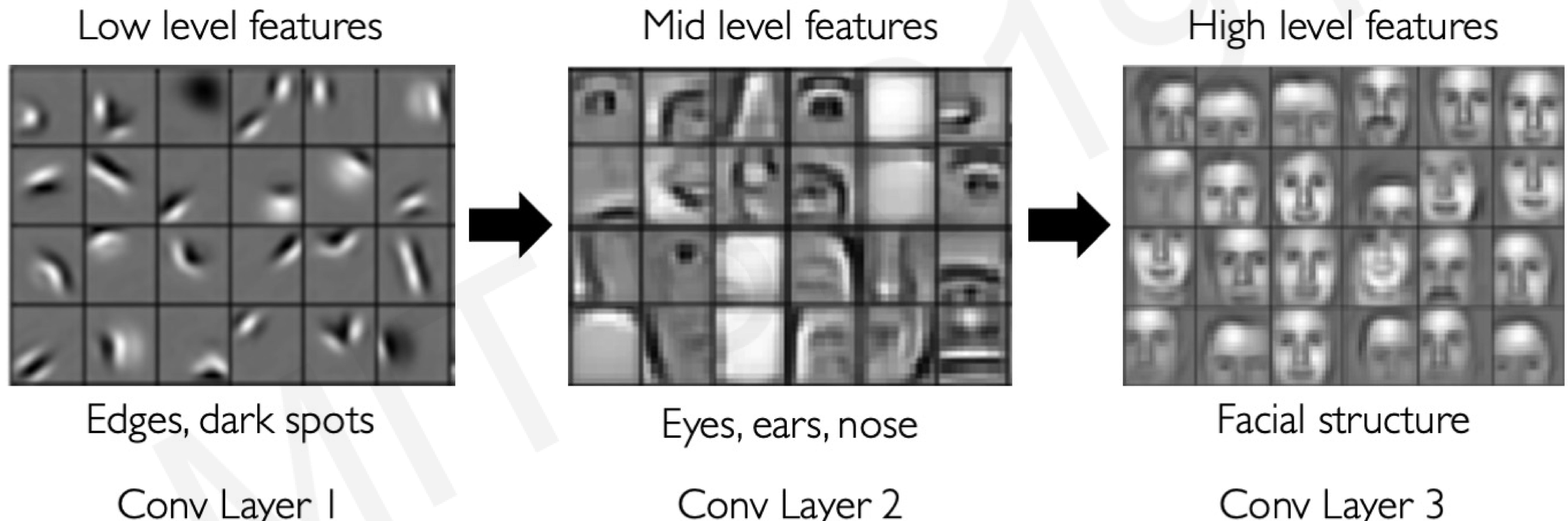
```
tf.keras.layers.MaxPool2D(  
    pool_size=(2,2),  
    strides=2  
)
```



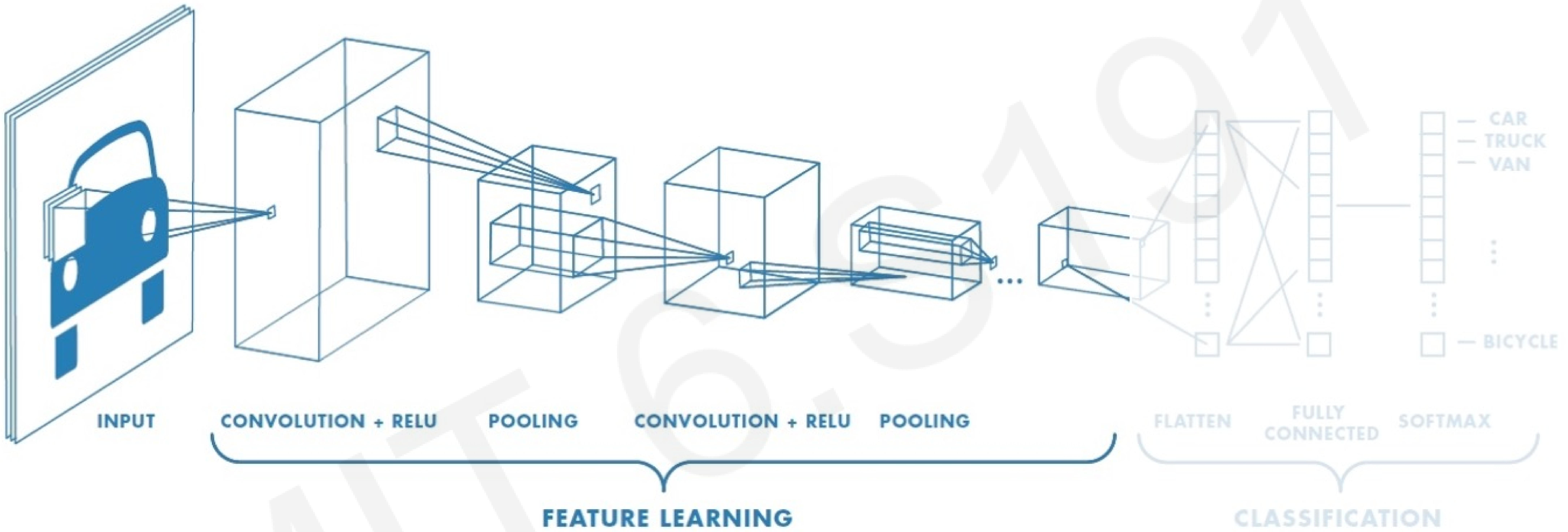
- 1) Reduced dimensionality
- 2) Spatial invariance

How else can we downsample and preserve spatial invariance?

Representation Learning in Deep CNNs

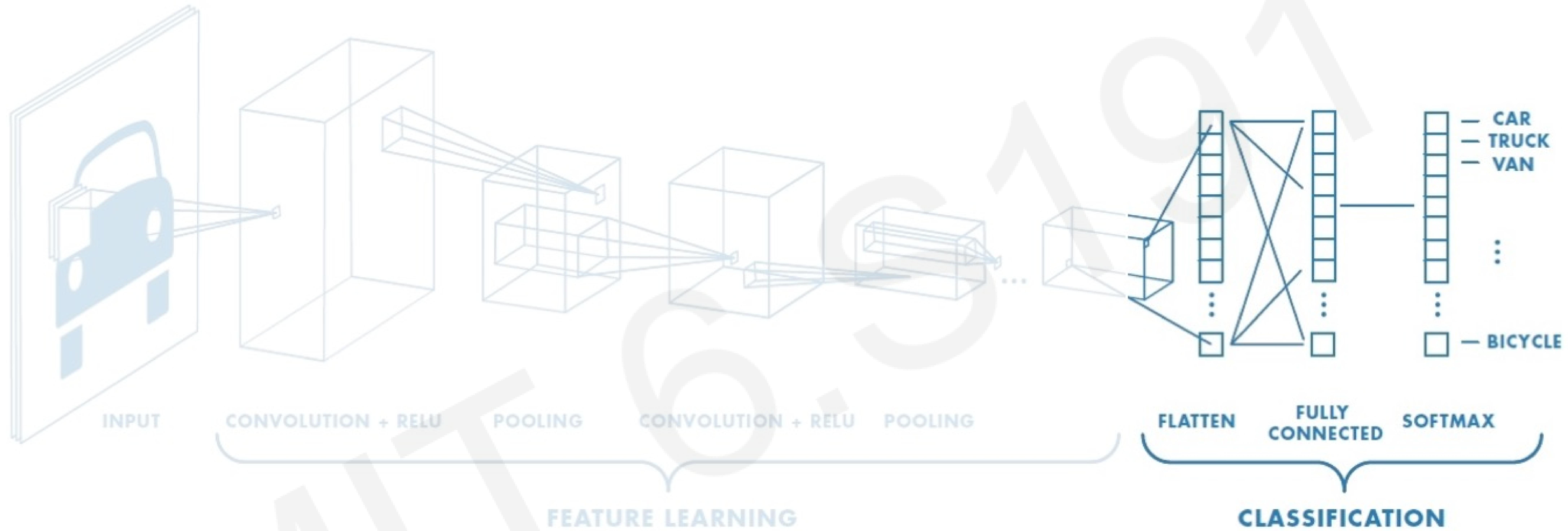


CNNs for Classification: Feature Learning



1. Learn features in input image through **convolution**
2. Introduce **non-linearity** through activation function (real-world data is non-linear!)
3. Reduce dimensionality and preserve spatial invariance with **pooling**

CNNs for Classification: Class Probabilities



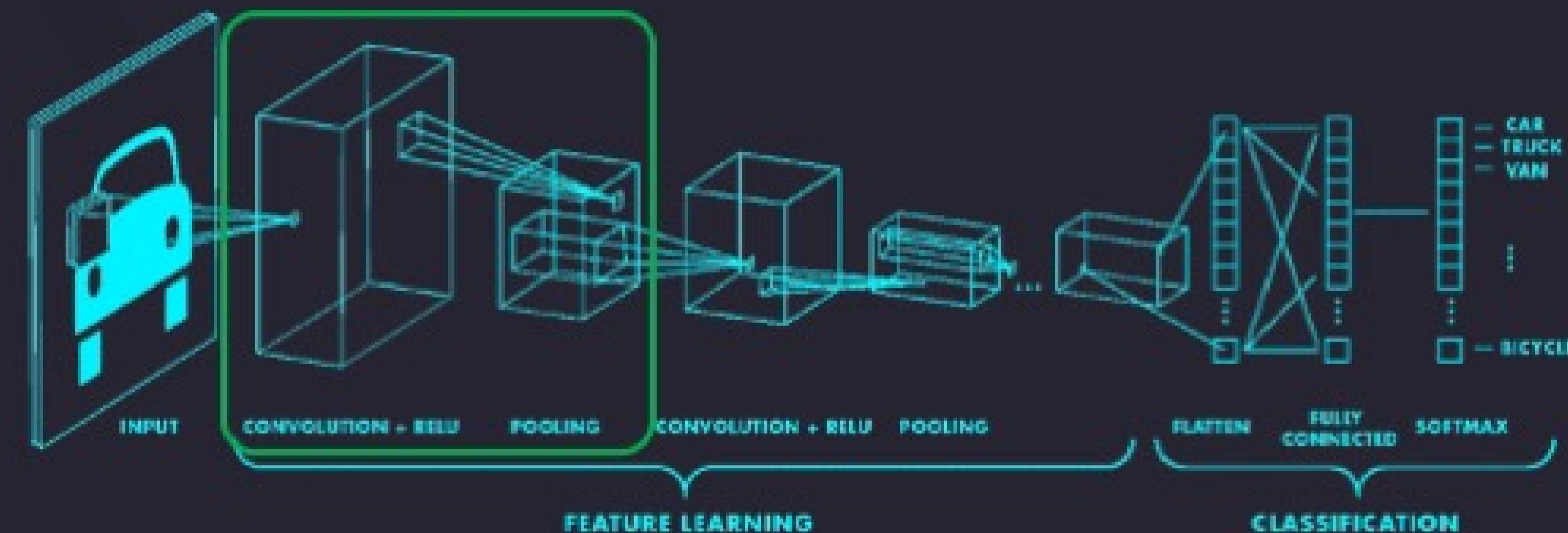
- CONV and POOL layers output high-level features of input
- Fully connected layer uses these features for classifying input image
- Express output as **probability** of image belonging to a particular class

$$\text{softmax}(y_i) = \frac{e^{y_i}}{\sum_j e^{y_j}}$$

Putting it all together

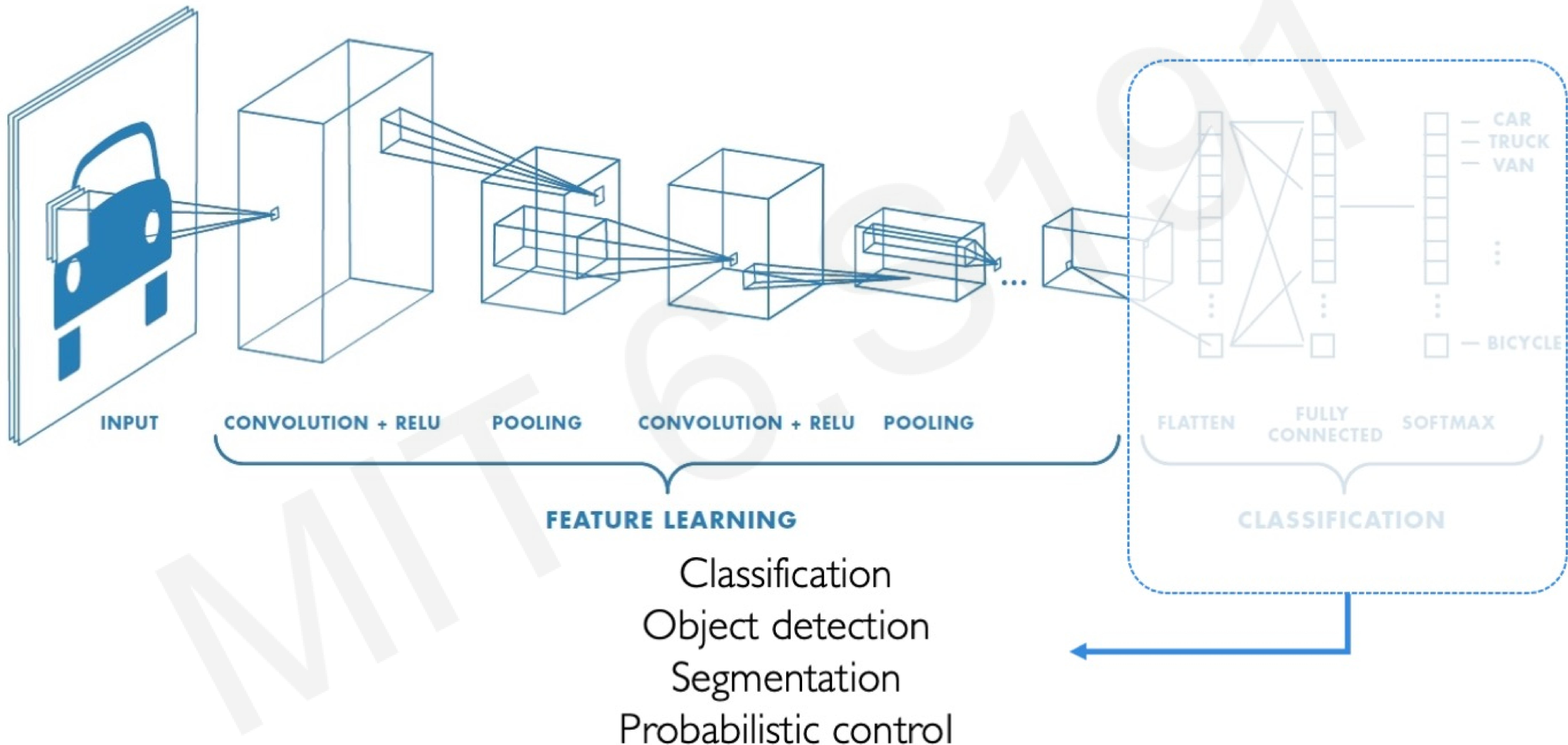
```
import tensorflow as tf

def generate_model():
    model = tf.keras.Sequential([
        # first convolutional layer
        tf.keras.layers.Conv2D(32, filter_size=3, activation='relu'),
        tf.keras.layers.MaxPool2D(pool_size=2, strides=2),
        # second convolutional layer
        tf.keras.layers.Conv2D(64, filter_size=3, activation='relu'),
        tf.keras.layers.MaxPool2D(pool_size=2, strides=2),
        # fully connected classifier
        tf.keras.layers.Flatten(),
        tf.keras.layers.Dense(1024, activation='relu'),
        tf.keras.layers.Dense(10, activation='softmax') # 10 outputs
    ])
    return model
```



An Architecture for Many Applications

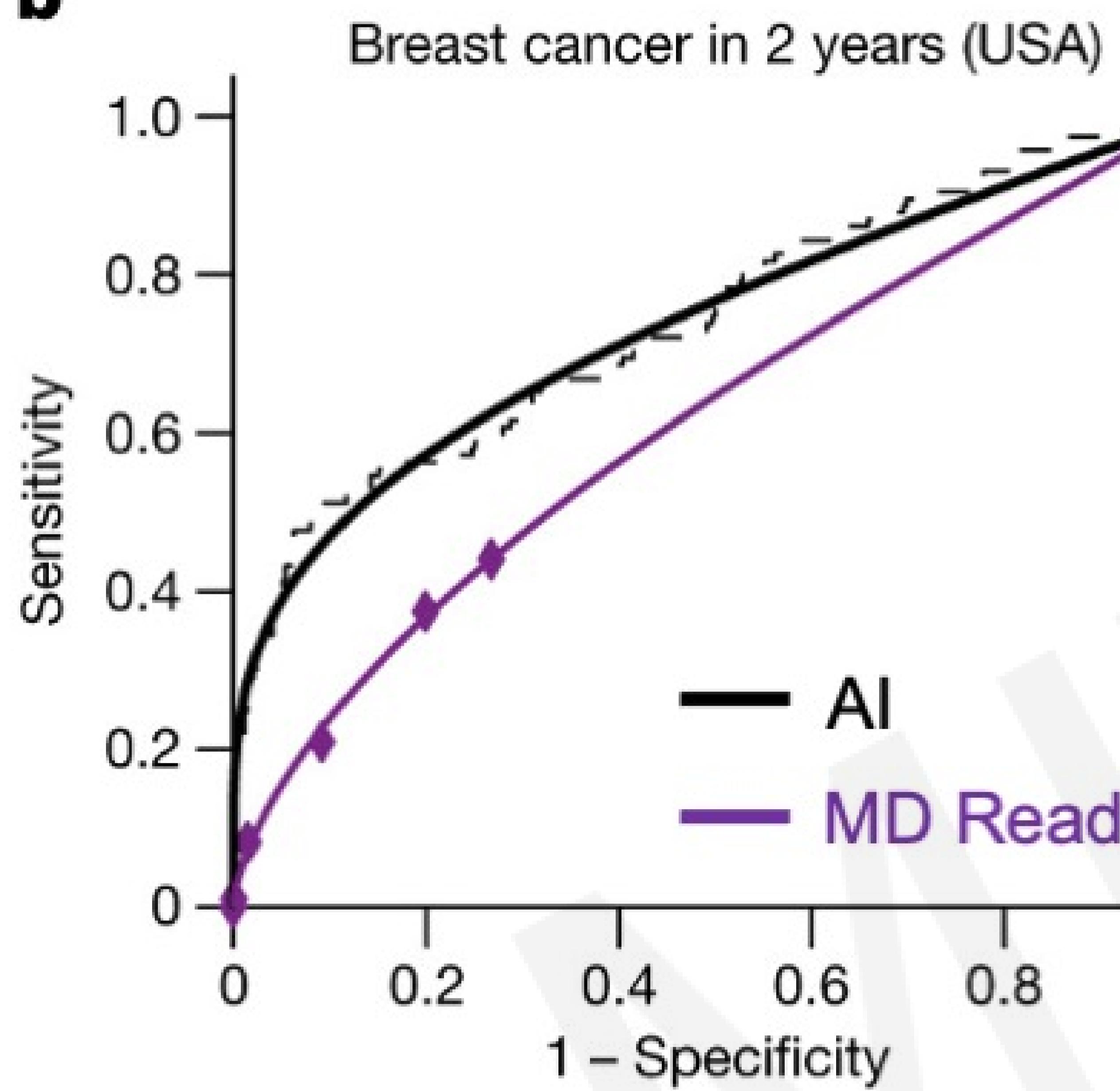
An Architecture for Many Applications



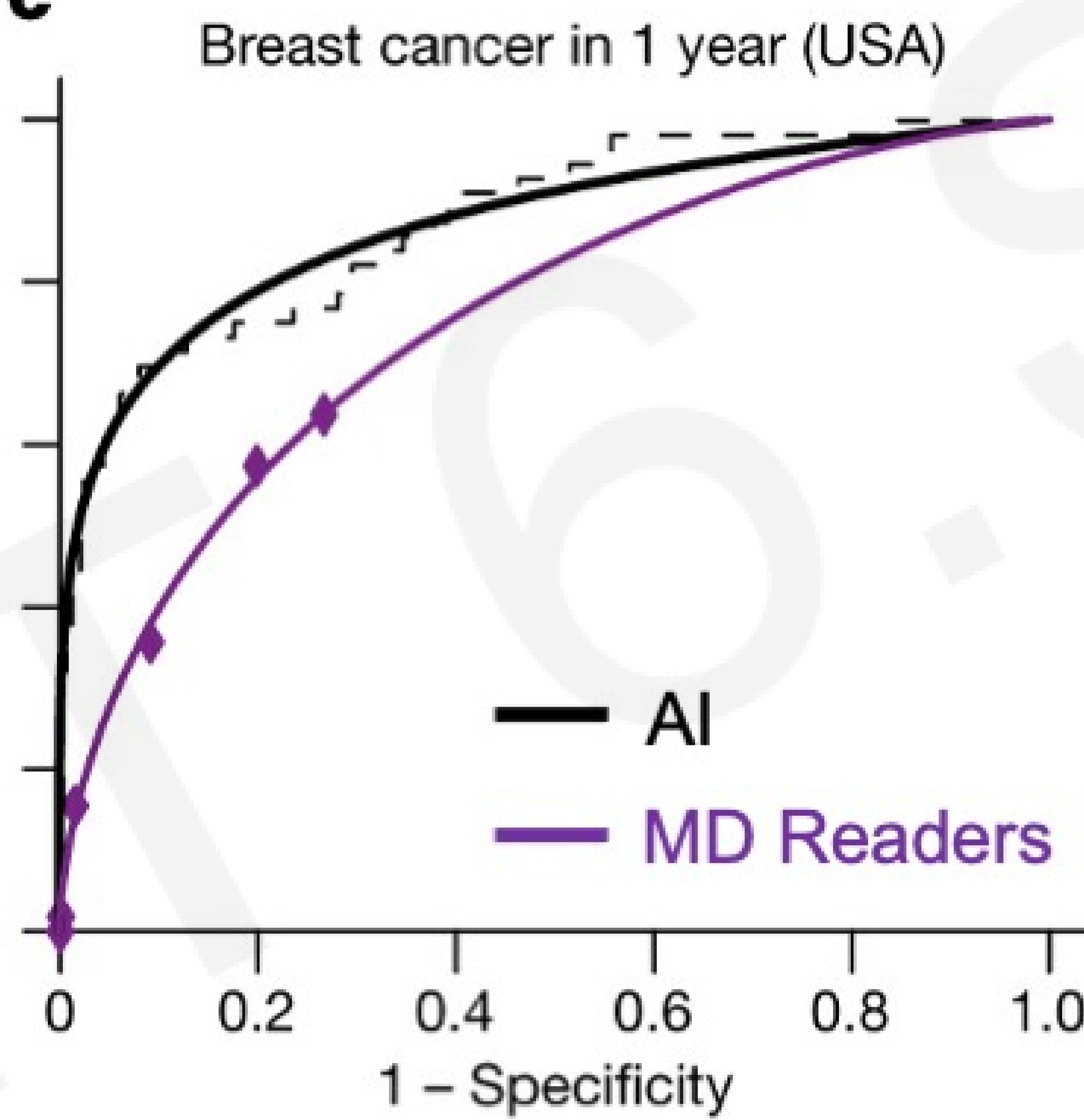
Classification: Breast Cancer Screening

International evaluation of an AI system for breast cancer screening

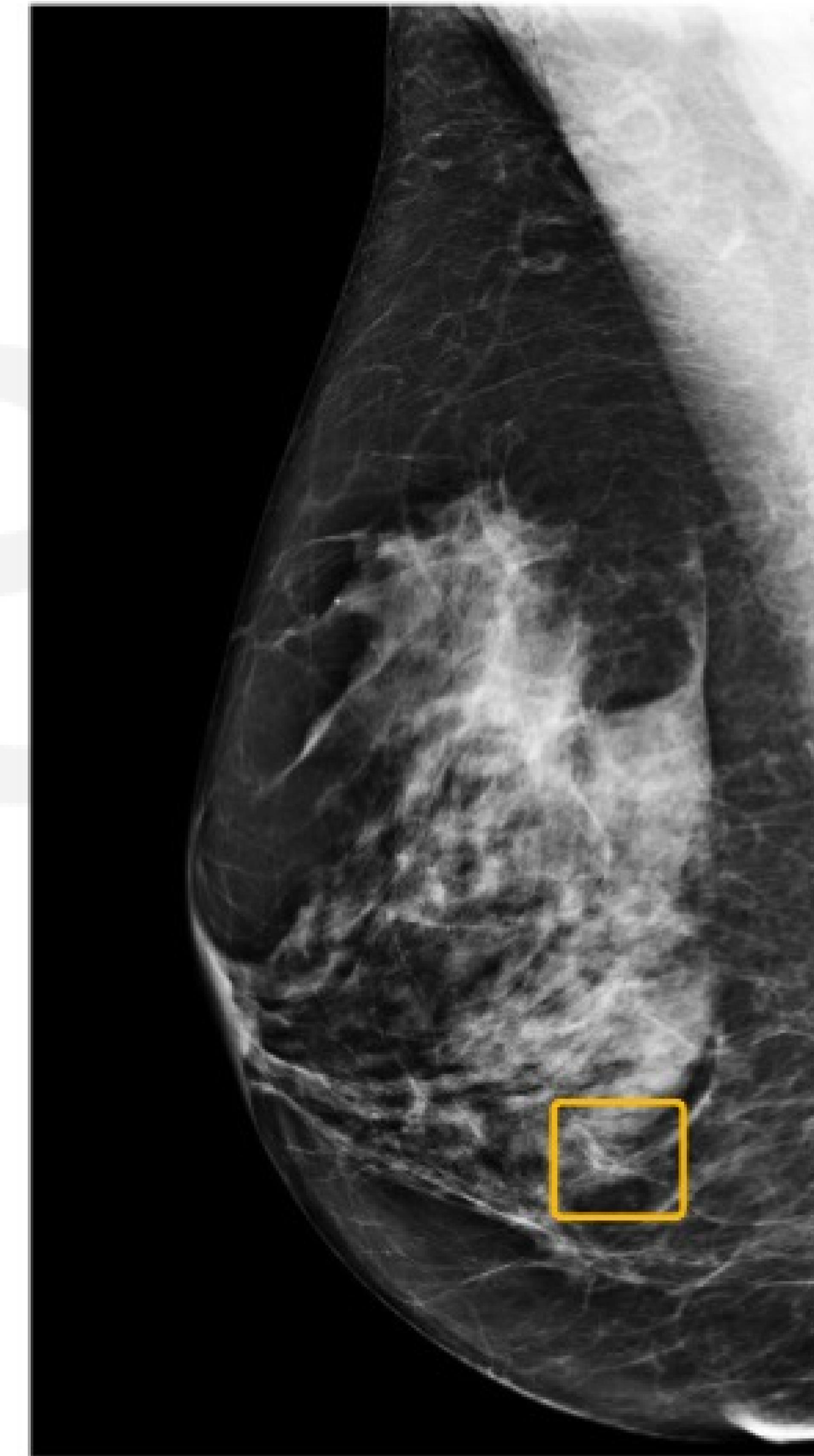
b



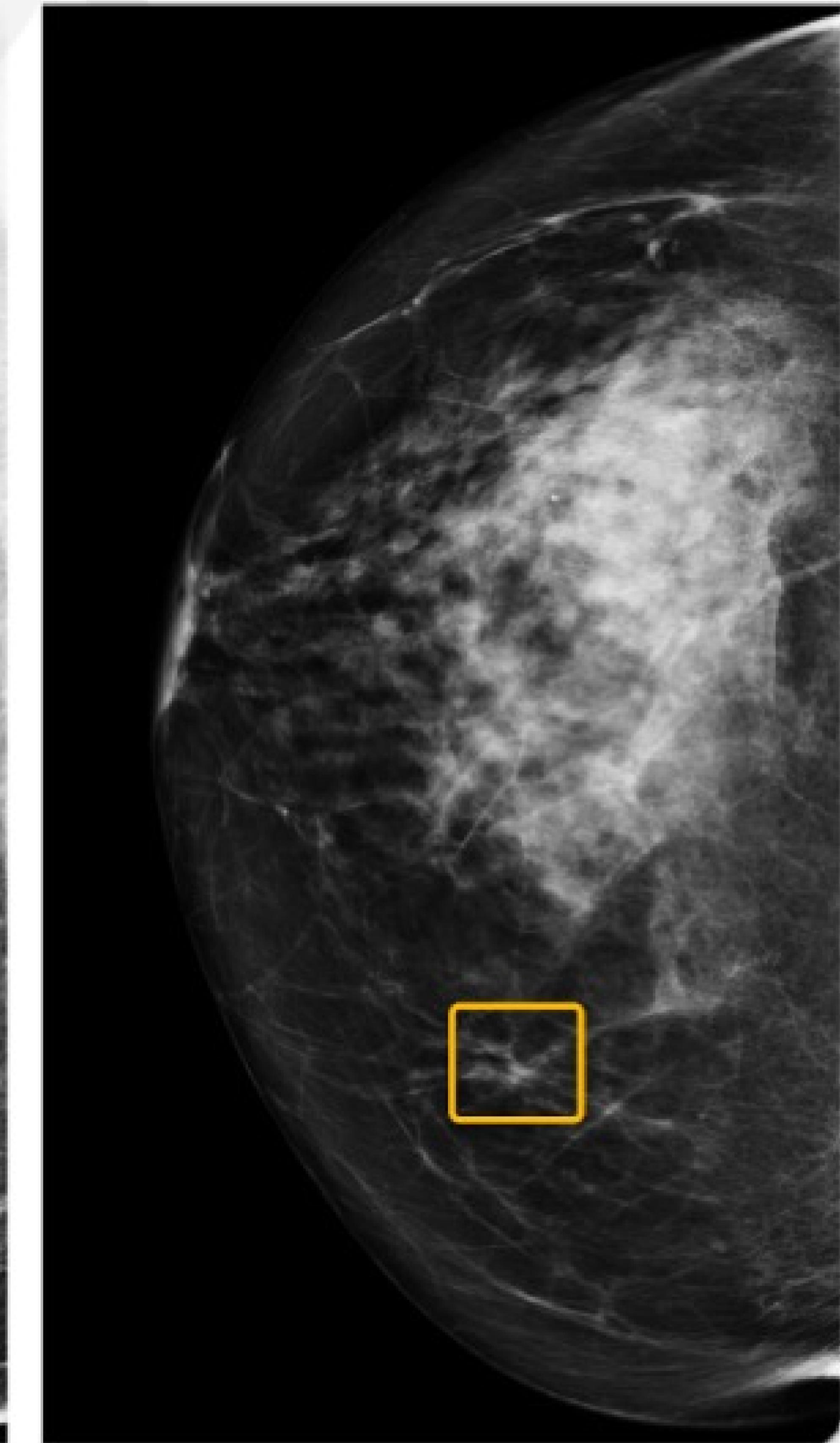
c



CNN-based system outperformed expert radiologists at detecting breast cancer from mammograms



Breast cancer case missed by radiologist but detected by AI



Object Detection

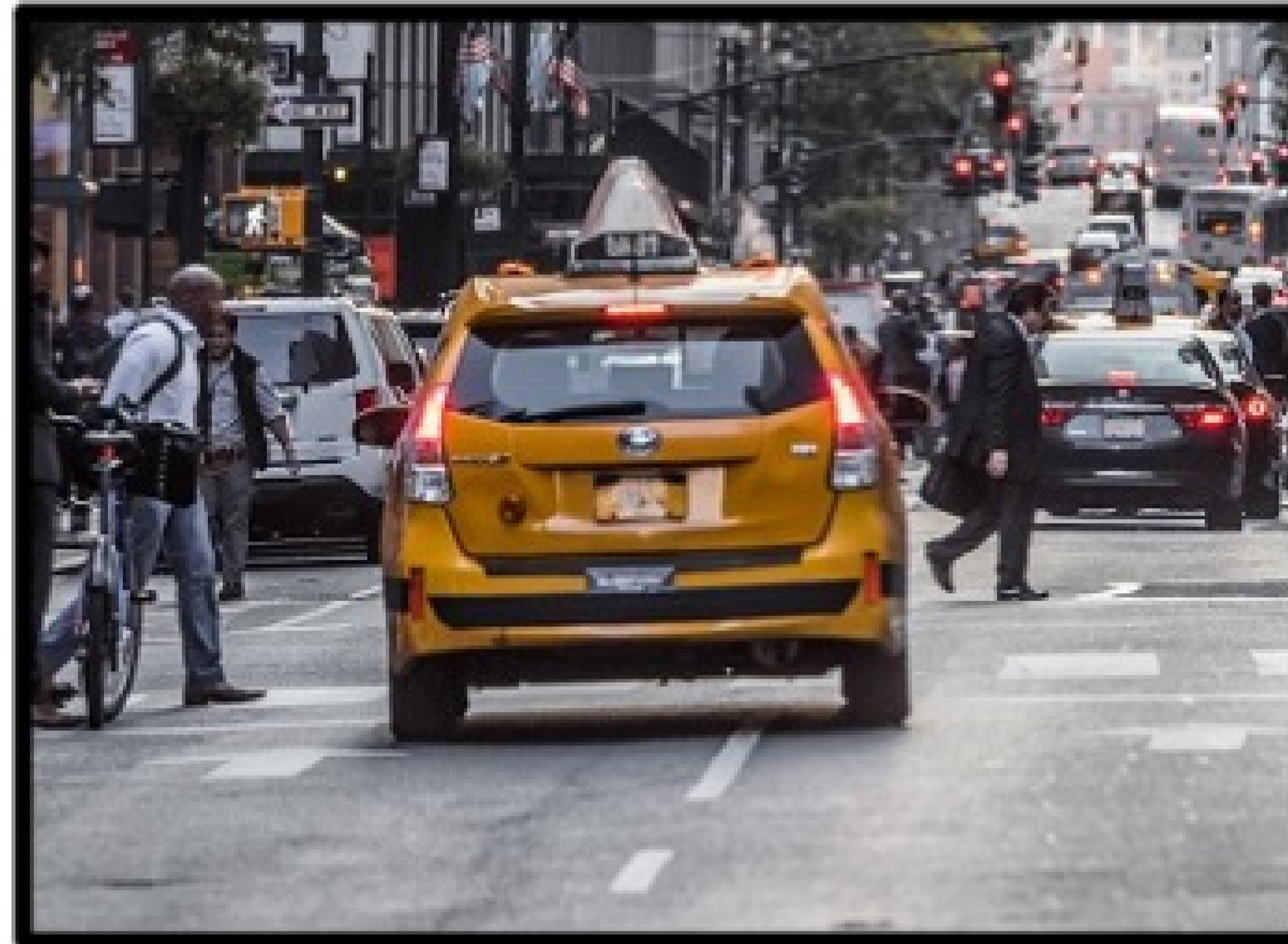


Image X

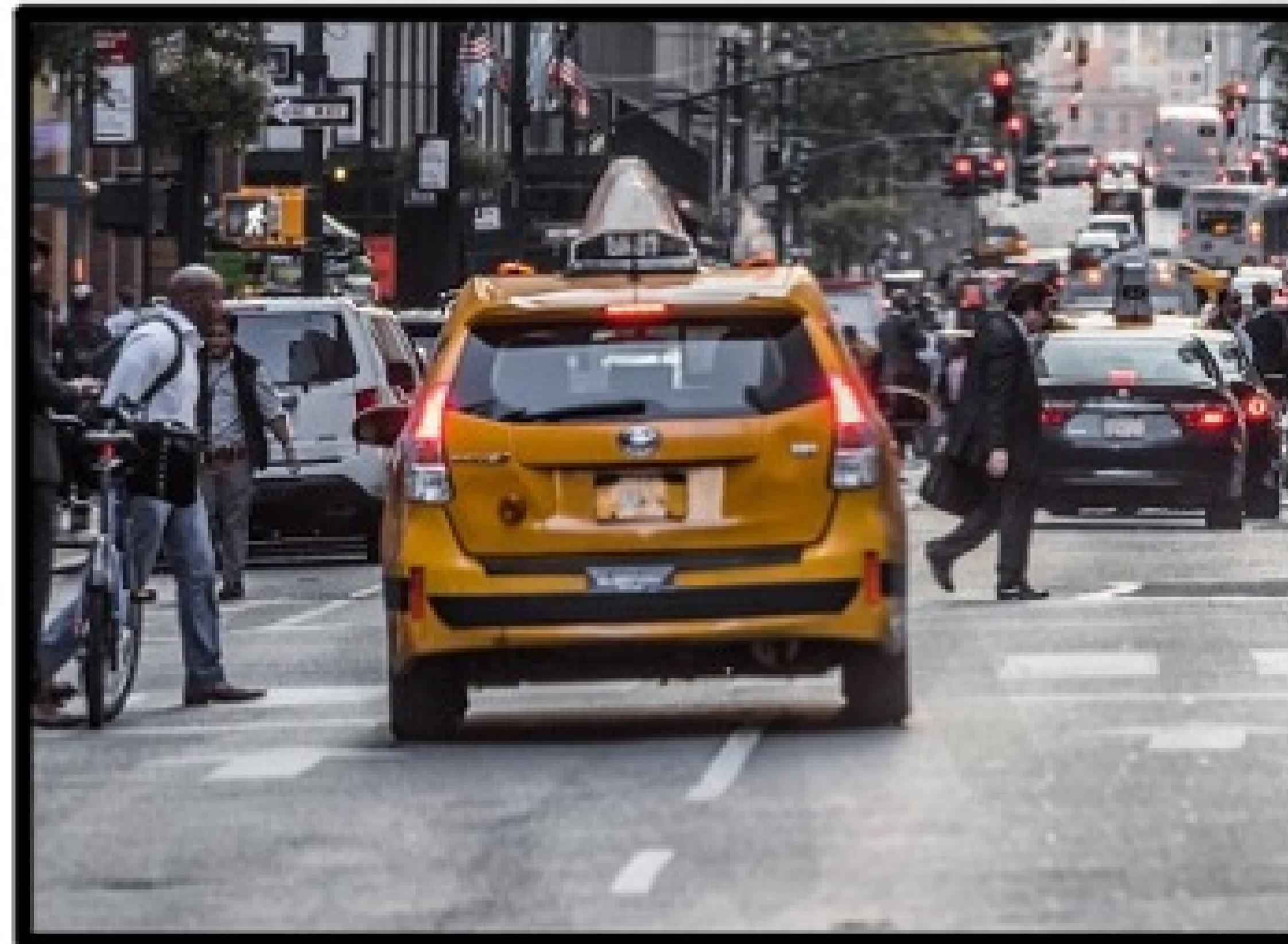
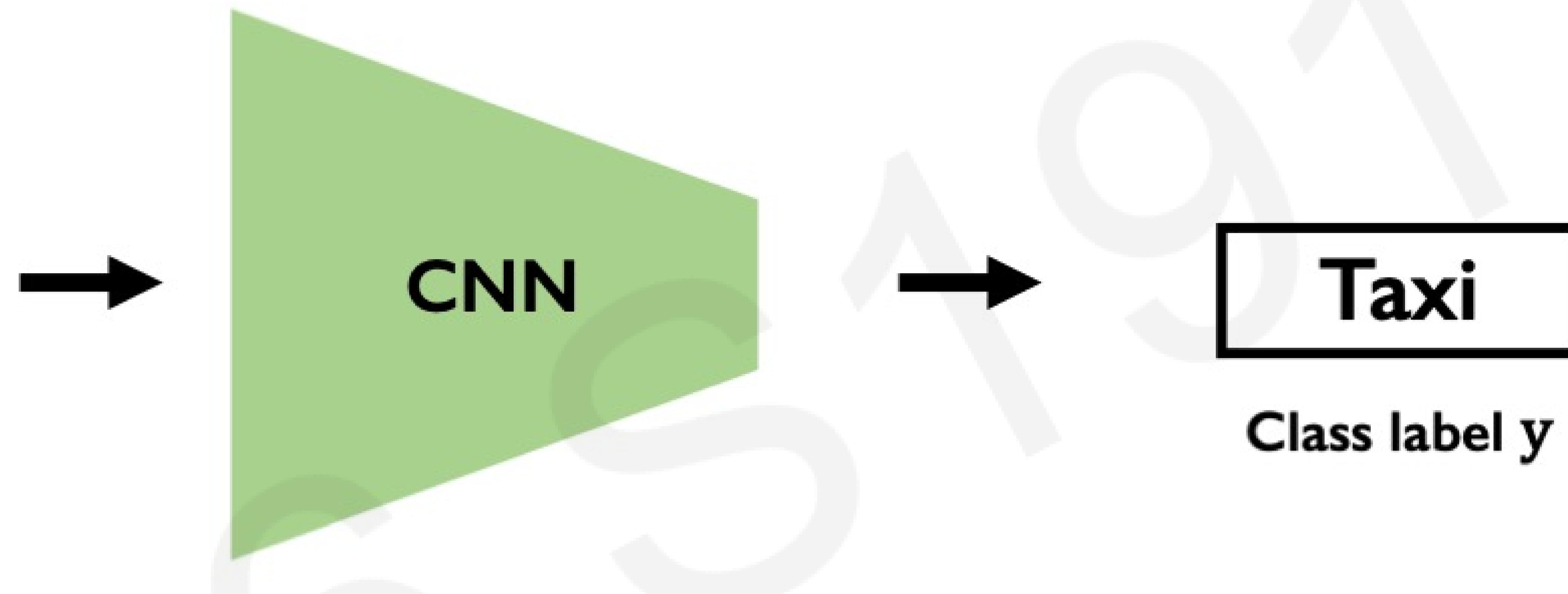
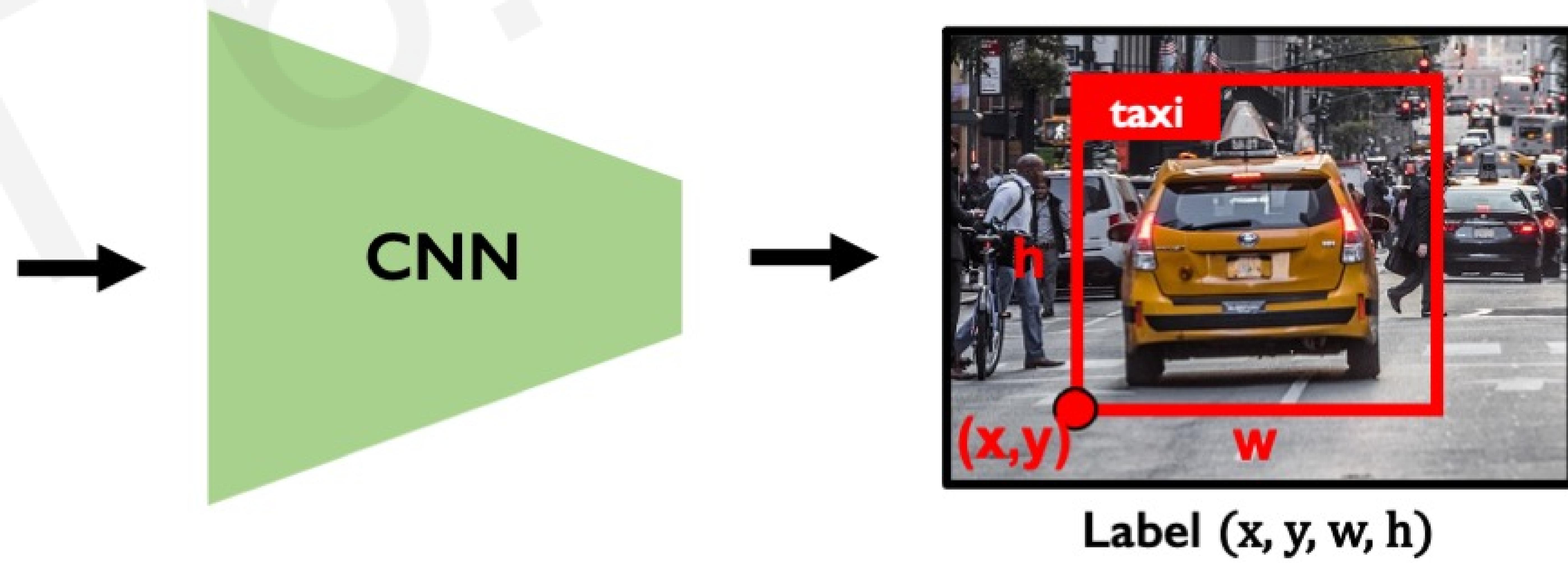


Image X



Object Detection

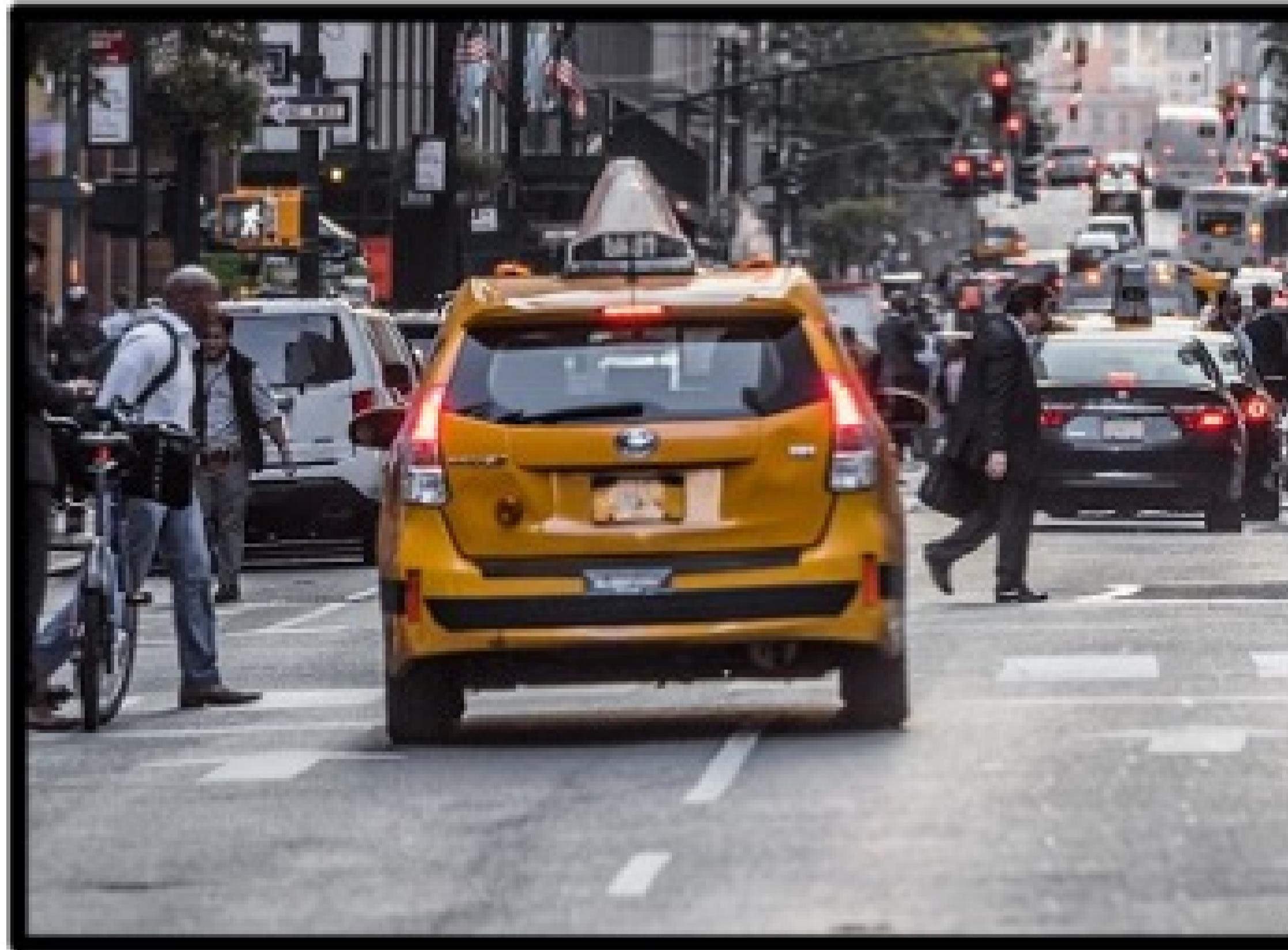
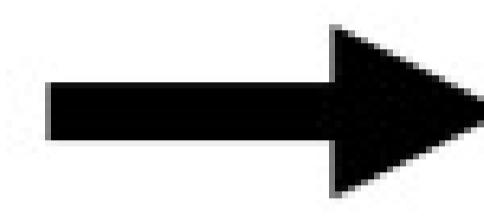


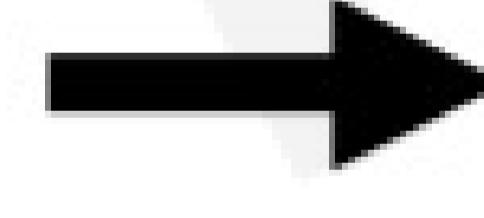
Image X



Output:
taxi: (x_l, y_l, w_l, h_l)

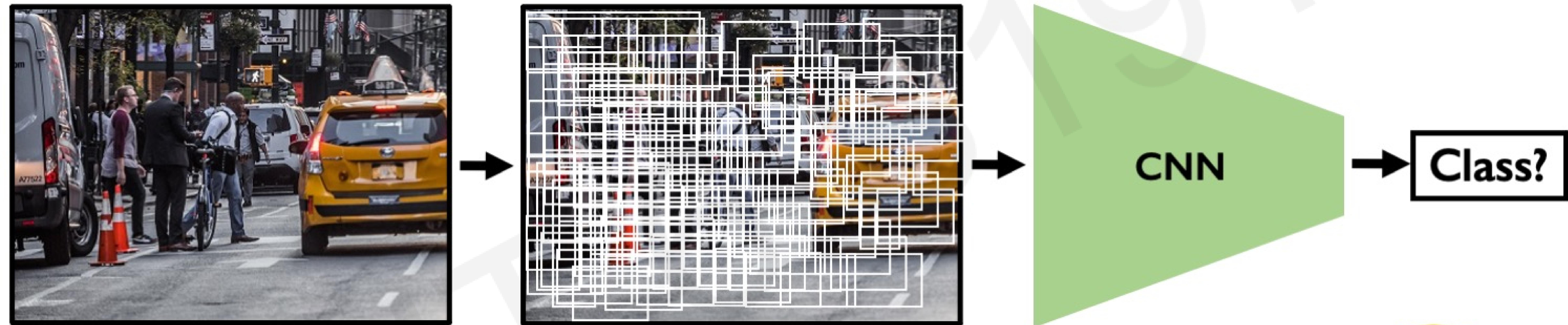


Image X



Output:
taxi: (x_l, y_l, w_l, h_l)
person: (x_2, y_2, w_2, h_2)
person: (x_3, y_3, w_3, h_3)
...

Naïve Solution to Object Detection



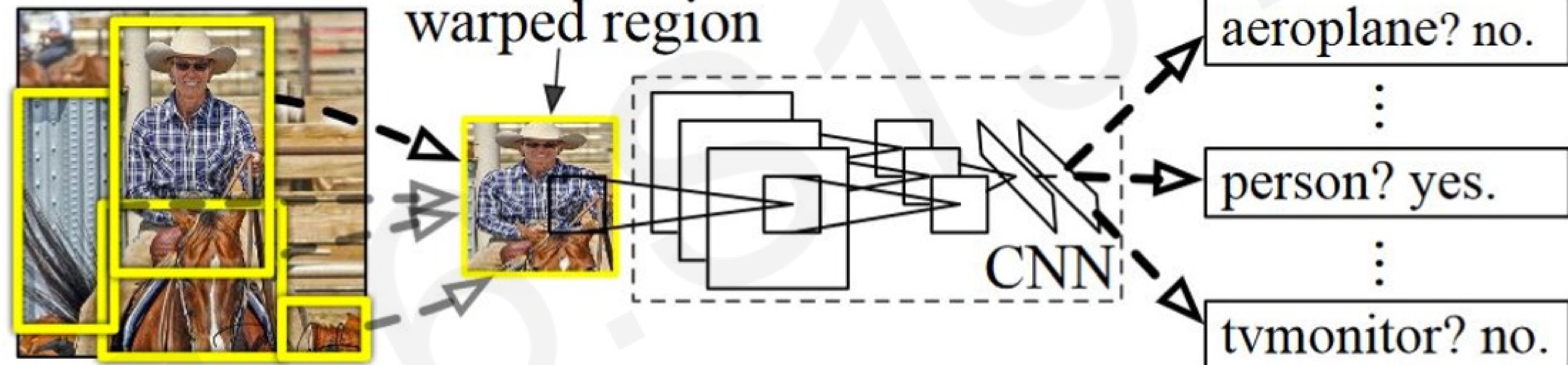
Problem: Way too many inputs! This results in too many scales, positions, sizes!

Object Detection with R-CNNs

R-CNN algorithm: Find regions that we think have objects. Use CNN to classify.



1. Input image



2. Extract region proposals (~2k)

3. Compute CNN features

4. Classify regions

Problems: 1) Slow! Many regions; time intensive inference.
2) Brittle! Manually defined region proposals.

Faster R-CNN Learns Region Proposals

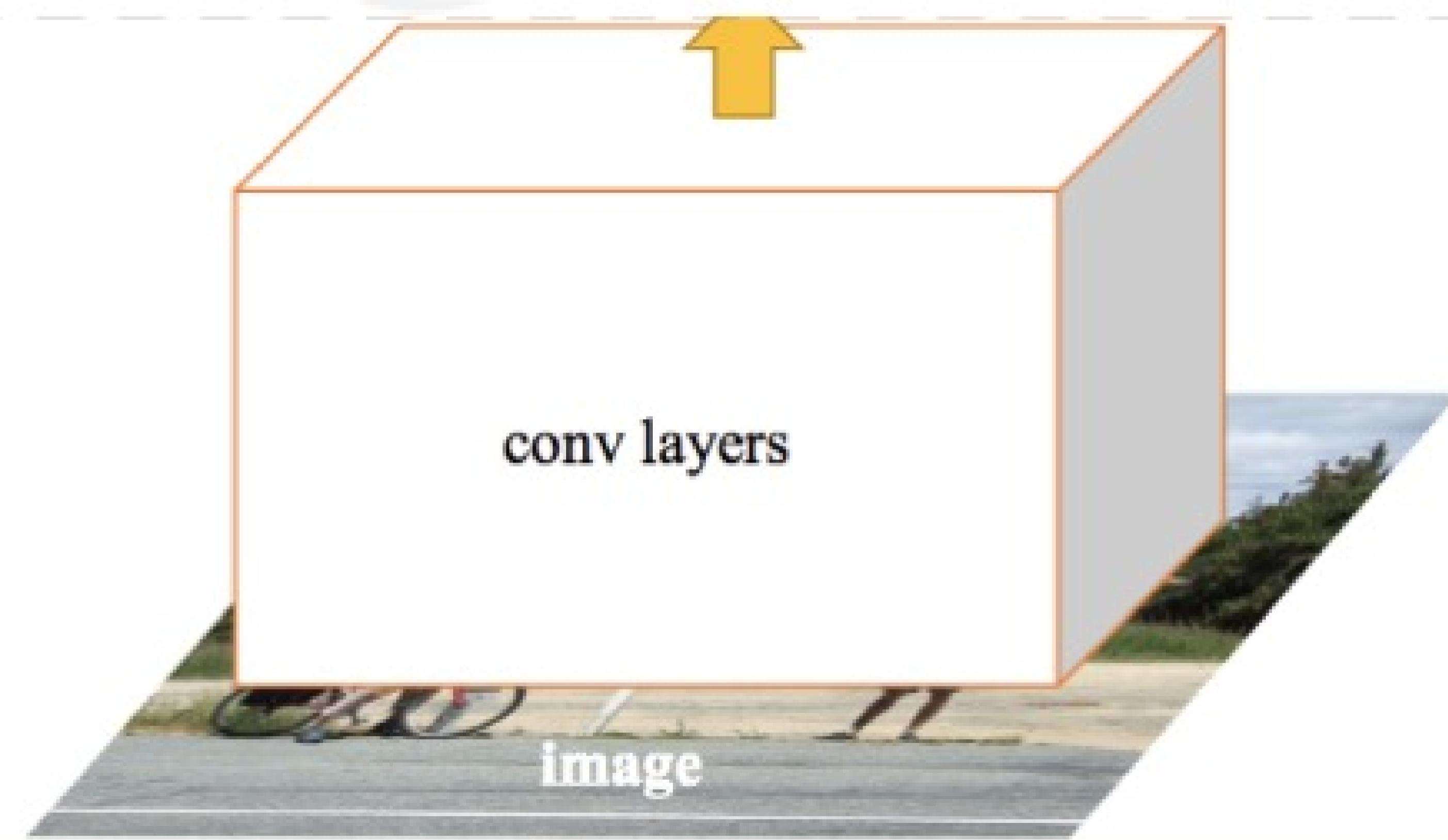
Classification of regions →
object detection

Feature extraction over
proposed regions

Region proposal network
to learn candidate regions

Learned, data-driven

Image input directly into
convolutional feature extractor
Fast! Only input image once!



Semantic Segmentation: Fully Convolutional Networks

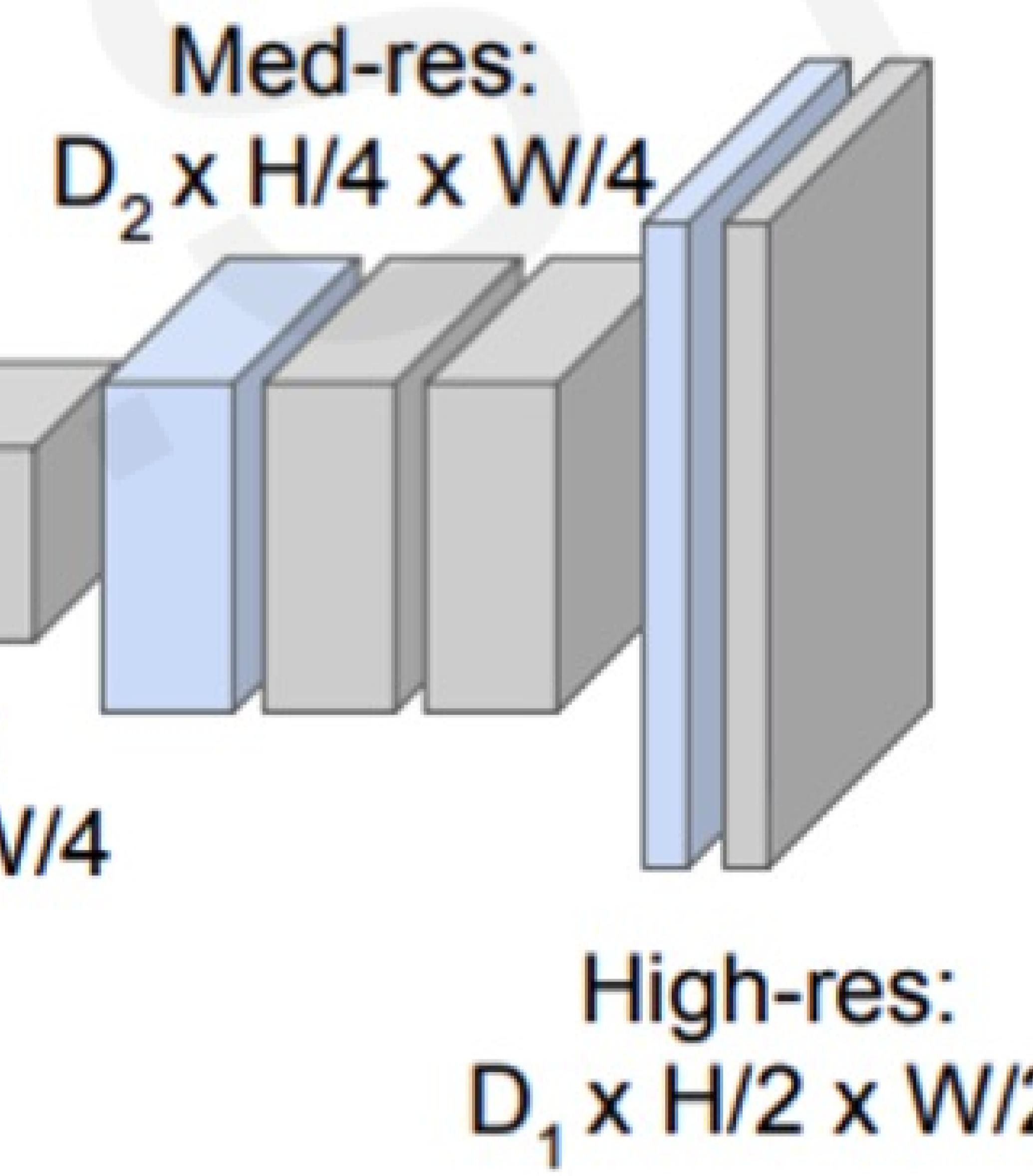
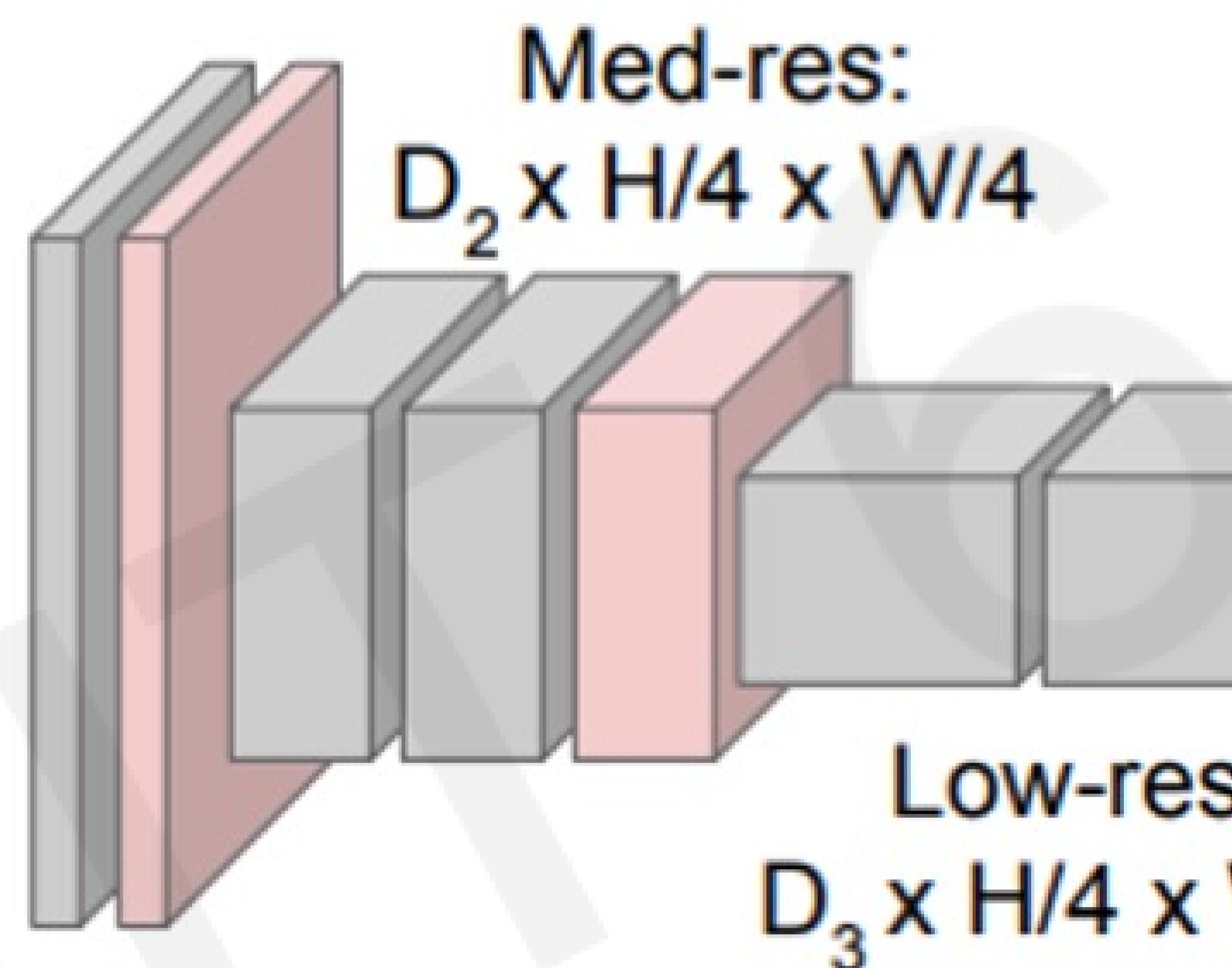
FCN: Fully Convolutional Network.

Network designed with all convolutional layers,
with **downsampling** and **upsampling** operations



Input:
 $3 \times H \times W$

High-res:
 $D_1 \times H/2 \times W/2$

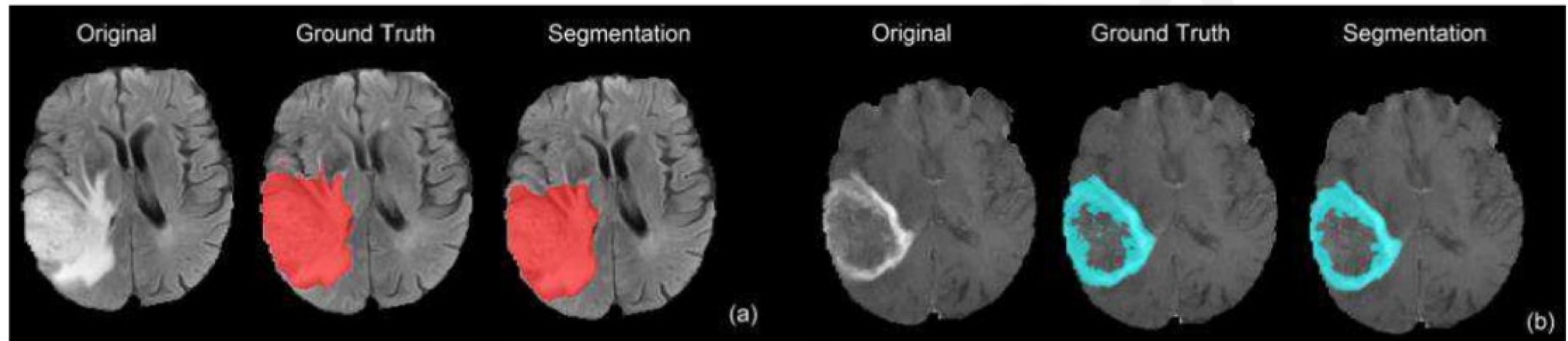


Predictions:
 $H \times W$

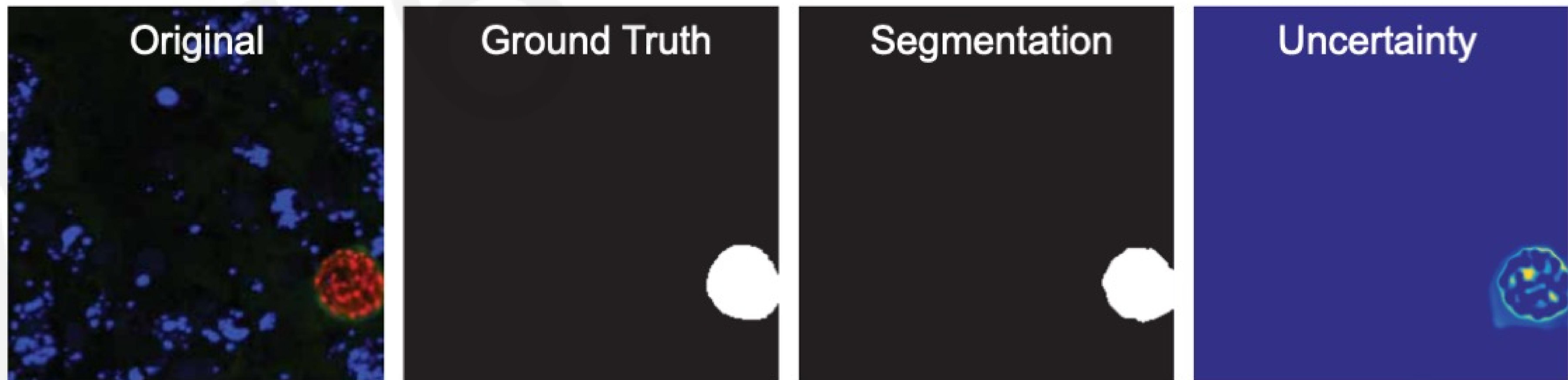
 `tf.keras.layers.Conv2DTranspose`

Semantic Segmentation: Biomedical Image Analysis

Brain Tumors
Dong+ MIUA 2017.



Malaria Infection
Soleimany+ arXiv 2019.



Continuous Control: Navigation from Vision

Raw Perception

I

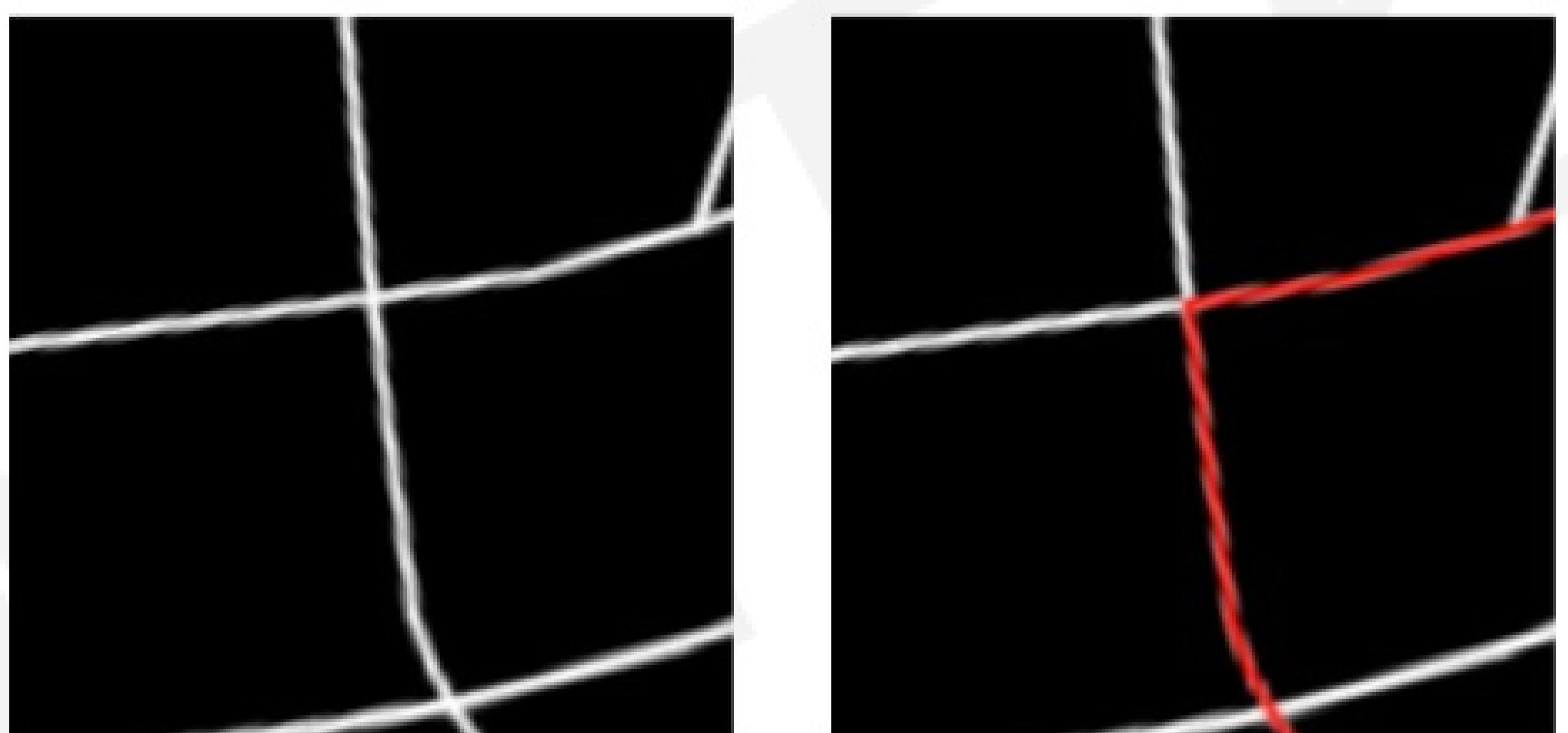
(ex. camera)



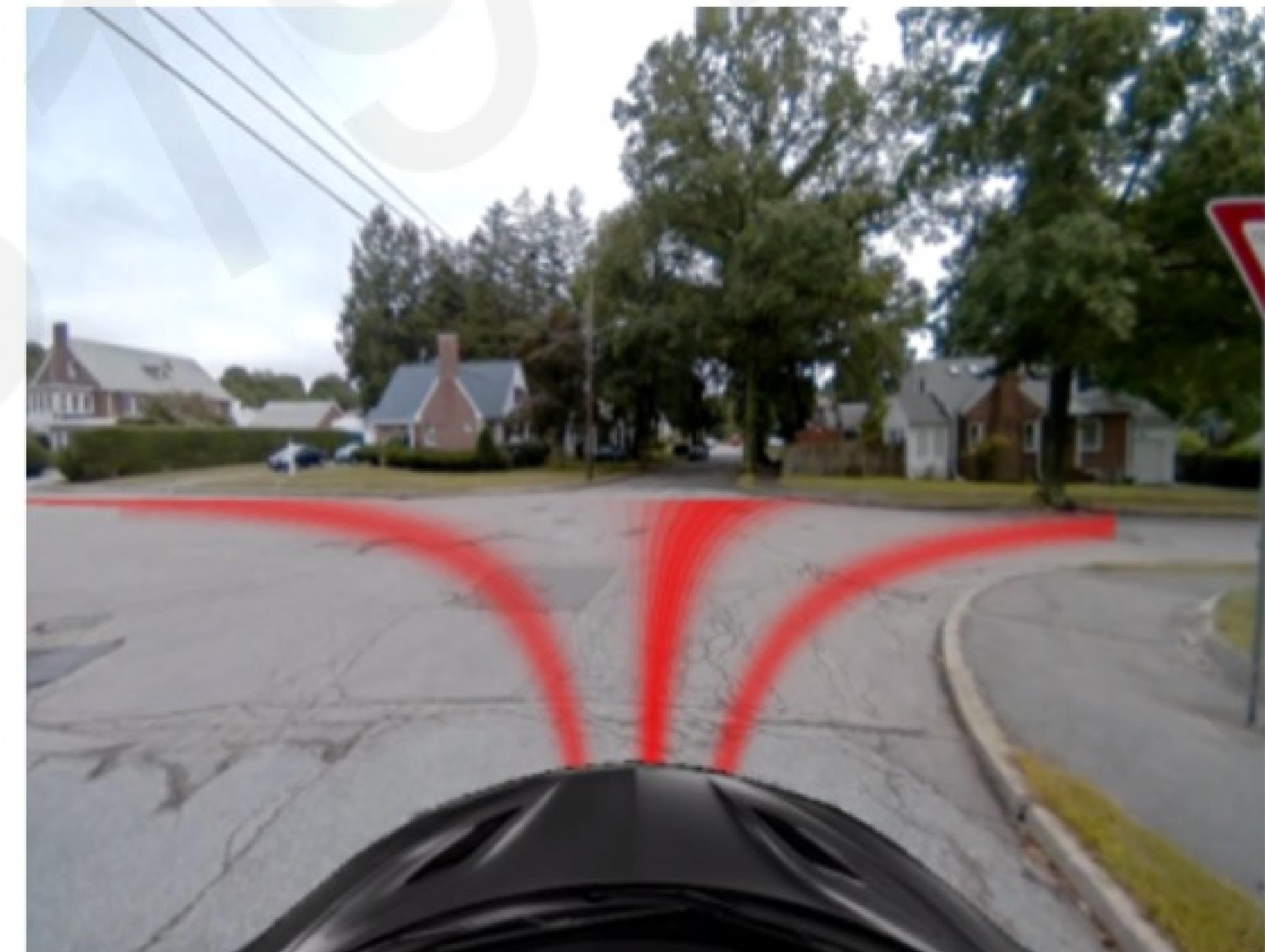
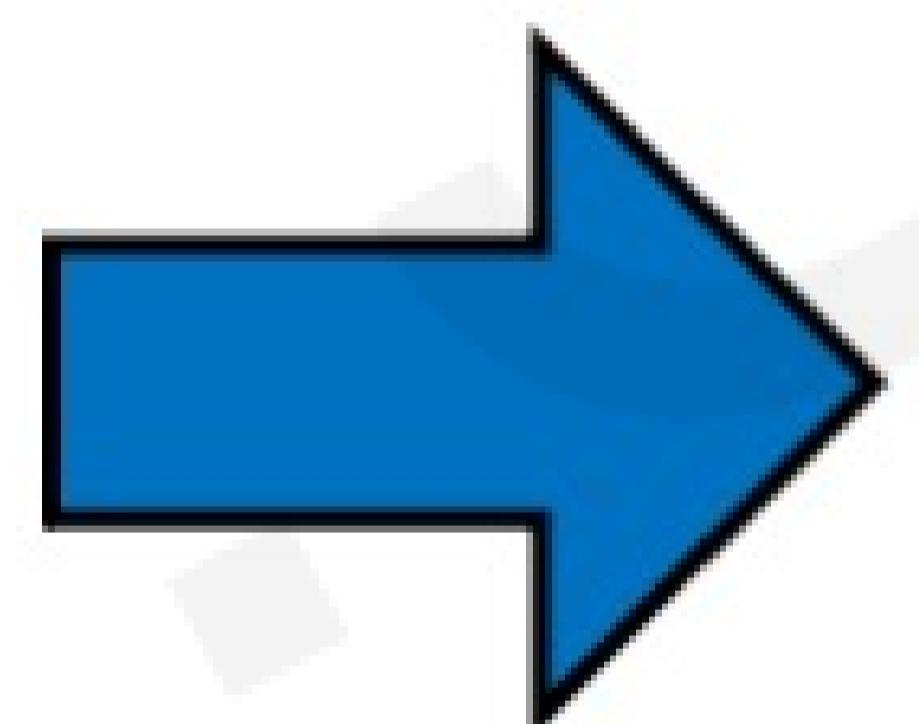
Coarse Maps

M

(ex. GPS)

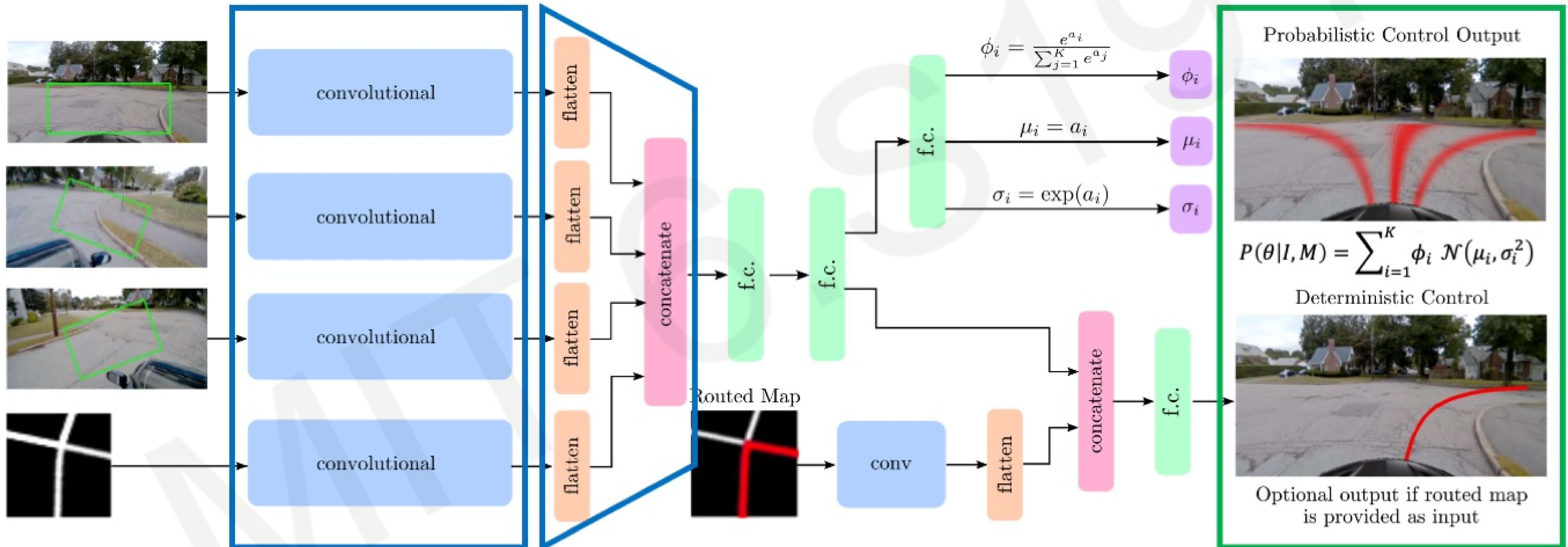


Possible Control Commands



End-to-End Framework for Autonomous Navigation

Entire model is trained end-to-end **without any human labelling or annotations**



$$L = -\log(P(\theta|I, M))$$

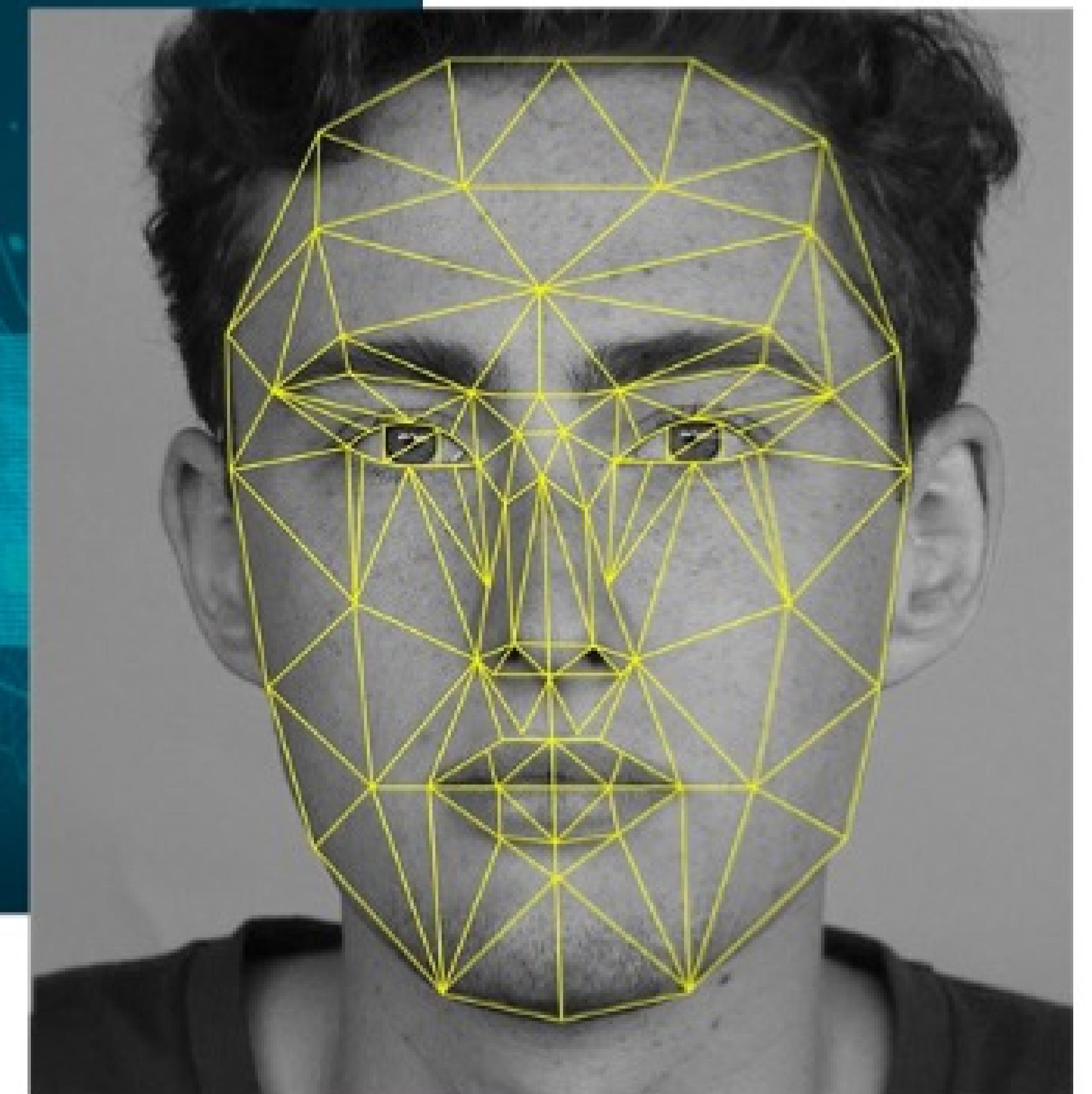
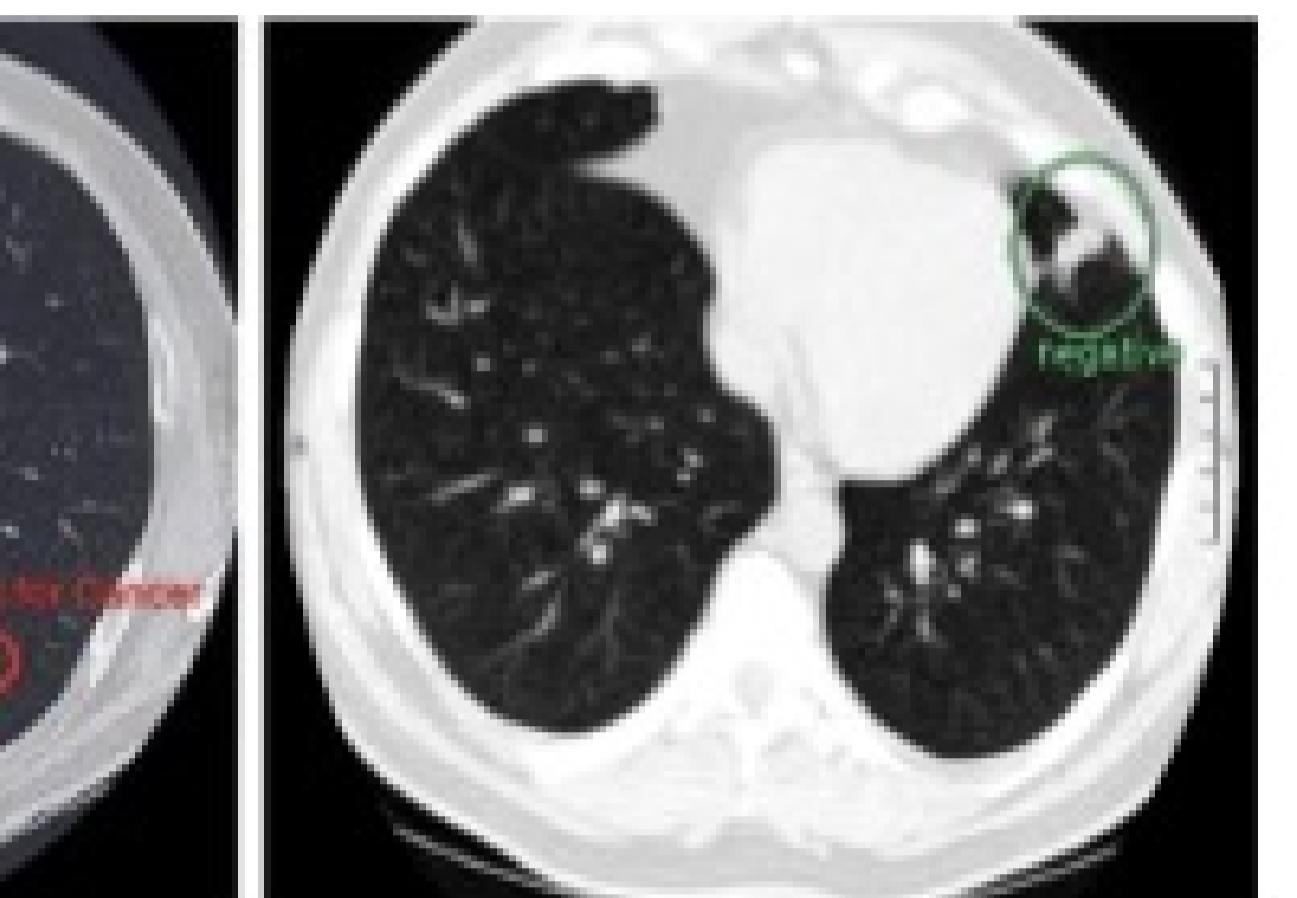
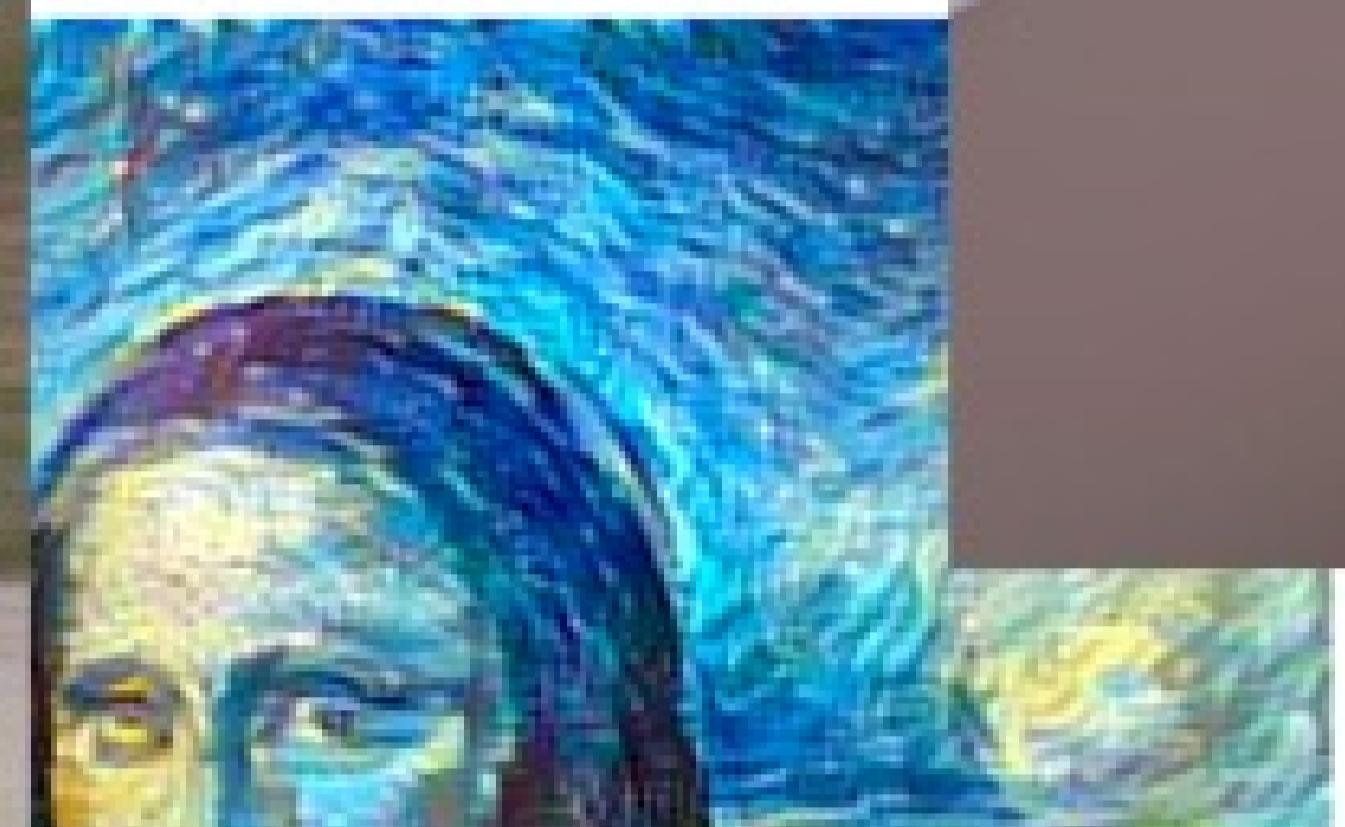


Auto ON

Navigation and Localization



Deep Learning for Computer Vision: Impact



Deep Learning for Computer Vision: Summary

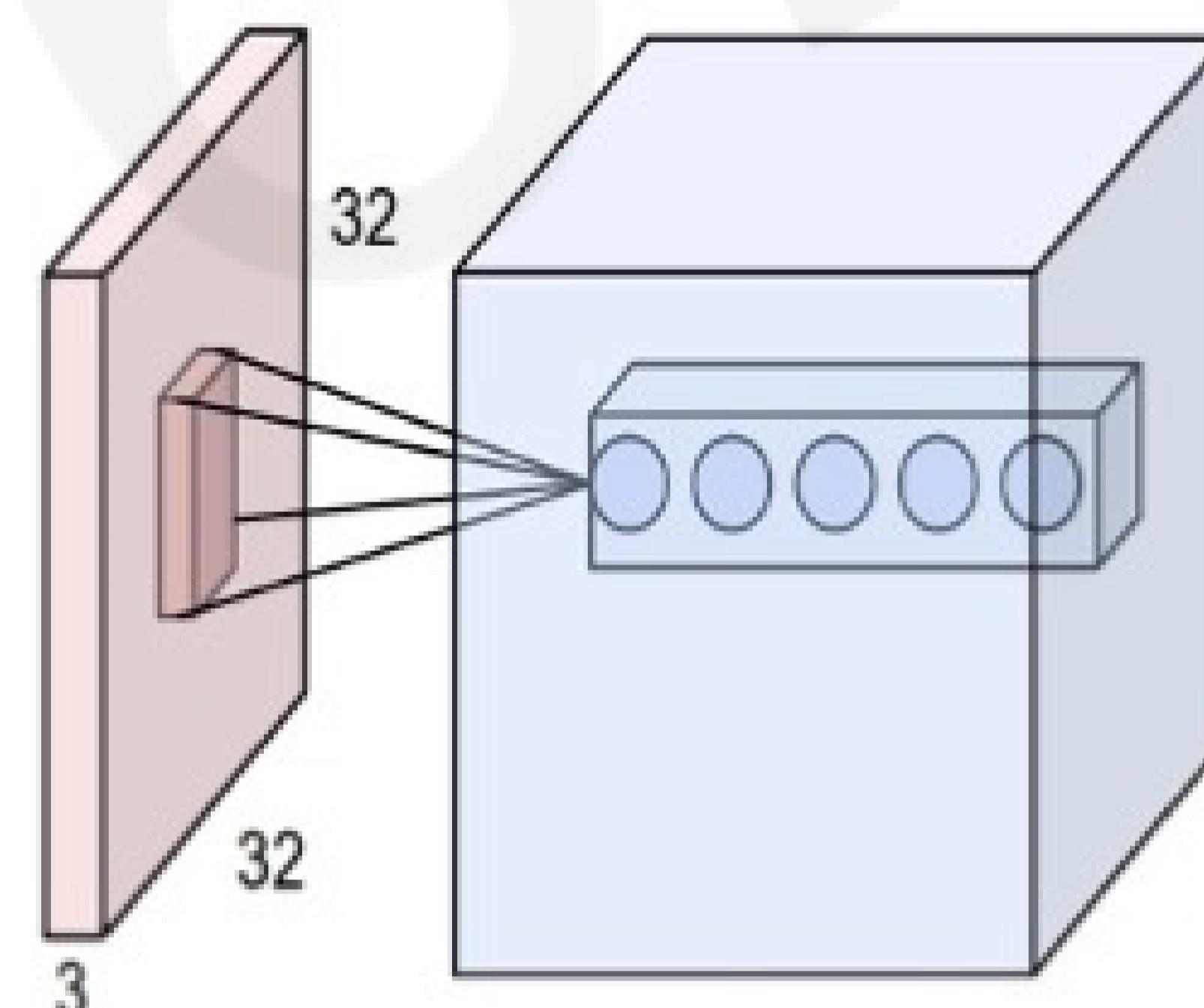
Foundations

- Why computer vision?
- Representing images
- Convolutions for feature extraction



CNNs

- CNN architecture
- Application to classification
- ImageNet



Applications

- Segmentation, image captioning, control
- Security, medicine, robotics





6.S191:

Introduction to Deep Learning

Lab 2: Computer Vision

Link to download labs:
<http://introtodeeplearning.com#schedule>

1. Open the lab in Google Colab
2. Start executing code blocks and filling in the #TODOs
3. Need help? Come to the class Gather.Town!