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Floating Point Conversion Work:

For userid 'er6qt':

Your magic (32 bit) floating point number is -19.53125

This is the number that needs to be converted to (little endian) binary, and expressed in hexadecimal.

Your other magic floating-point number is, in hex, 0x00809f40

This is the number that needs to be converted to a (32 bit) floating point number.

Note that the hexadecimal printed above is in little-endian format!

Format taken from Bloomfield slide 9.17: Converting a Float from Decimal to Binary

-19.53125 (Floating point number \rightarrow little-endian binary (in hexadecimal))

- **Sign** is 1 (it's a negative number)
- **Exponent:**
 - $-19.53125/2^4 = -19.53125/16 = -1.220703125$ (exactly)
 - Exponent is $4 + 127 = 131$ (**1000 0011_b**)

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$$131/2 = 1$$

$$65/2 = 1$$

$$32/2 = 0$$

$$16/2 = 0$$

$$8/2 = 0$$

$$4/2 = 0$$

$$2/2 = 0$$

$$1/2 = 1$$

- **Mantissa:**
 - $-1.220703125 - 1 = -2.220703125$

- Getting the parts of the mantissa:

$$-19.53125 = 19 \frac{17}{32} = \frac{625}{32}$$

$$\frac{625}{512} - 1 = \frac{625}{512} - \frac{512}{512} = \frac{113}{512}$$

- From 113/512 we can subtract 1/8, yielding 49/512
- From 49/512 we can subtract 1/16, yielding 17/512
- From 17/512 we can subtract 1/32, yielding 1/512
- From 1/512 we can subtract 1/512, yielding zero

- Thus, the parts of the mantissa are $\frac{1}{8} + \frac{1}{16} + \frac{1}{32} + \frac{1}{512}$
- $-2.220703125 = \frac{1}{8} + \frac{1}{16} + \frac{1}{32} + \frac{1}{512}$
- = 0011 1000 1000 0000 0000 000 (Big-endian format)
- In binary, it's:
 - 1100 0001 1001 1100 0100 0000 0000 0000
- Switch to little-endian format:
 - 00000000 01000000 10011100 11000001
- Express in hexadecimal:
 - 0000 0000 0100 0000 1001 1100 1100 0001 (Little-endian format)
 - 0x00409cc1 or 0x409cc1 (ANSWER)

NEXT CONVERSION:

0x00809f40 (Binary (in hexadecimal) → floating point number)

- Convert back to little-endian binary representation:
 - 0x00809f40
 - 0000 0000 1000 0000 1001 1111 0100 0000
- Convert to big-endian binary:
 - 01000000 10011111 10000000 00000000
- Get value of exponent and subtract from 127:
 - 01000000 10011111 10000000 00000000
 - $2^7 + 2^0 = 128 + 1 = 129$
 - $129 - 127 = 2$ (exponent)
- Add mantissa fraction values together:
 - 01000000 10011111 10000000 00000000
 - $\frac{1}{8} + \frac{1}{16} + \frac{1}{32} + \frac{1}{64} + \frac{1}{128} + \frac{1}{256} = 0.125 + 0.0625 + 0.03125 + 0.015625 + 0.0078125 + 0.00390625 = 0.24609375$ (value that would be used when finding mantissa)
- Add 1 to get back to exponent value:
 - $0.24609375 + 1 = 1.24609375$ (exactly)
- Multiply by exponent to get floating point decimal:
 - $1.24609375 * 2^2 = 1.24609375 * 4 = 4.984375$ (ANSWER)