

7.7

A flame radiates 40% of its energy. The fuel supply is 100 g/s and its heat of combustion is 30 kJ/g.

A thin drapery is 3 m from the flame. Assume piloted ignition. When will the drapery ignite? The ambient temperature is 20 C and the heat transfer coefficient of the drapery is 10 W/(m²K). The drapery properties are:

$$\rho := 40 \quad c_p := 1400 \quad T_{ig} := 350 + 273 \quad d_d := 0.002 \quad h_e := 10 \quad T_e := 20 + 273$$

invert eqn 7.27 in terms of t_{ig}

If we use spherical approximation of heat flux

$$X_r := 0.4 \quad HRR := 30 \cdot 100 \cdot 1000 \quad Rad := 3 \quad q_{rad} := \frac{X_r \cdot HRR}{4 \cdot \pi \cdot Rad^2}$$

$$q_{rad} = 1.061 \times 10^4 \quad \frac{W}{m^2}$$

$$t_{ig} := \frac{(-\rho \cdot c_p \cdot d_d) \cdot \ln \left[1 - \frac{h_e \cdot (T_{ig} - T_e)}{q_{rad}} \right]}{h_e} \quad t_{ig} = 4.172 \quad \text{seconds}$$

if we use cylindrical approximation

$$H := Rad$$

$$q_{rad_cyl} := \frac{X_r \cdot HRR}{2 \cdot \pi \cdot Rad \cdot H} \quad q_{rad_cyl} = 2.122 \times 10^4 \quad \frac{W}{m^2}$$

$$t_{ig_cyl} := \frac{(-\rho \cdot c_p \cdot d_d) \cdot \ln \left[1 - \frac{h_e \cdot (T_{ig} - T_e)}{q_{rad_cyl}} \right]}{h_e} \quad t_{ig_cyl} = 1.893 \quad \text{seconds}$$