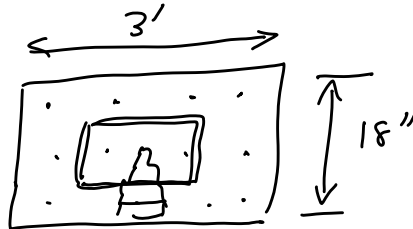


10/20/2010

# THIS LECTURE

- FINISH THEORY OF EVAP. MODELLING
- EXAMPLES

- expts
- simulations



WINDOW OR  
GLASS BREAK  
CRITERION.

open  
for next  
2 semesters

⇒ Review



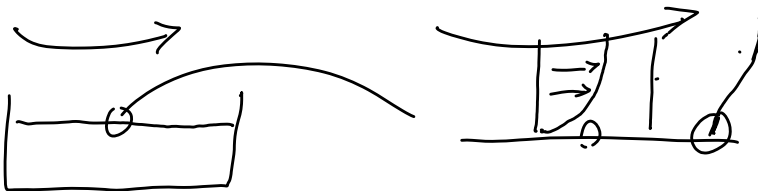
LIQUIDS CLASSIFIED BY FLASH POINT  
TEMPERATURE & FIREPOINT TEMP.

$0 < T_{FLASH} < 37^{\circ}C$	CLASS I
$37 < \quad < 60^{\circ}C$	II
$60^{\circ}C < \quad$	III

FOR IGNITION OF A FLAMMABLE POOL, THE

$$X_L < \frac{P_i}{P_{atm}} < X_u$$

$$X_F \equiv \frac{P_F}{P_{atm}}$$



neglect radiation

$$q''(y=0) = -K \frac{\partial T}{\partial y} \Big|_{y=0}$$

gas conductivity  
@ interface.

we would need  $\frac{\partial T}{\partial y}$  from flow solution.

$$q''|_{wall} = -K \frac{\partial T}{\partial z} \Big|_{wall} \stackrel{\text{Fourier's law}}{=} h(T_w - T_{\infty}) \quad \text{Newton's Law of cooling}$$

$h \equiv$  heat transfer coefficient. We find  $h$  using correlations such as  $Nu_L \equiv \frac{hL}{K} = C Re^m Pr^n$

$L \equiv$  charact length

$K \equiv$  thermal cond. gas mix

$m, n, C \equiv$  correlation specific coeff.

$Re \equiv$  Reynolds #  $\equiv \frac{U_\infty L}{\nu}$

$U_\infty \equiv$  flow speed

$\nu \equiv$  kinematic visc.

$Pr \equiv$  Prandtl #  $\equiv \frac{\nu}{\alpha}$

$\alpha \equiv$  thermal diffusivity

mass transfer problems  $\dot{m}_i'' \equiv \frac{kg \cdot i}{s \cdot m^2}$   
 $\uparrow$  mass flux.

$$\dot{m}_i'' = -\rho D \left. \frac{\partial Y_i}{\partial z} \right|_0 = h_m (Y_{i,w} - Y_{i,\infty})$$

$\uparrow$  diffusive flux       $\underbrace{\quad}_{\text{Fick's law}}$        $\underbrace{\quad}_{\text{mass flux}}$

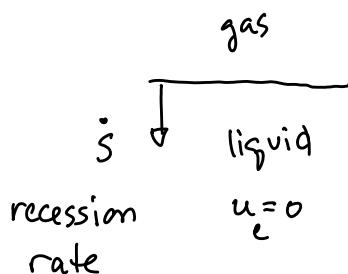
$$* \left[ h_m = \frac{h}{c_p} \right]$$

$$\text{Lewis \#} \equiv \frac{\alpha}{D}$$

$$\text{Stanton \#} = \frac{h}{\rho U_\infty c_p} = \frac{h_m}{\rho U_\infty}$$

low mass transfer limit.

$\swarrow$  Clarification



in lab frame the problem is unsteady.

moving w/ the interface

$$\begin{array}{c} \uparrow \rho_v u_v \\ \hline \uparrow \rho_e \dot{s} \end{array} \quad \rho_v u_v = \rho_e \dot{s} \quad \text{mass conservation}$$

We discussed that the species velocity can be decomposed into the mass averaged velocity & a species velocity.

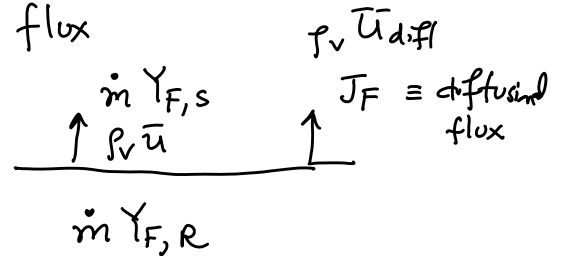
$$u_v = \bar{u} + \bar{u}_{diff}$$

$$\rho_v u_v = \rho_v \bar{u} + \rho_v \bar{u}_{diff}$$

diffusional flux



Just focusing on  $H_2O$



for most of this chapter, we will neglect  $m Y_{F,s}$

we will use  $J_F \approx h_m \Delta Y_F$

surface energy balance

$$\begin{array}{c} \downarrow q'' \\ \downarrow q''_{cond} \end{array} \quad \begin{array}{c} \uparrow \dot{m}'' h_g \\ \uparrow \dot{m} h_{eig} \end{array} \quad 0$$

steady ...

$$q'' + \dot{m}'' h_{eig} = q''_{cond} + \dot{m}'' h_g$$

$$q''_{incident} = \dot{m}'' (h_g - h_{eig}) + q''_{cond}$$

The incident heat flux causes phase change & contributes to the in-depth heating of the pool.

$$q''_{inc} = \underbrace{\dot{m}'' h_{fg}}_{\text{Latent heat of vaporization}} + \cancel{q''_{cond}}_{\text{sensible}}$$



shallow, insulated pool, well mixed  
then  $q''_{\text{cond}} = 0$ .

then  $q''_{\text{in}} = \dot{m}'' h_{fg}$

$$\left. \begin{aligned} q''_{\text{in}} &= h(T_{\infty} - T_{\text{surf}}) \\ \dot{m}''_{\text{out}} &= h_m(Y_{\text{surf}} - Y_{\infty}) \end{aligned} \right\} \begin{aligned} h(T_{\infty} - T_{\text{surf}}) &= h_m h_{fg} \\ &\quad (Y_{\text{surf}} - Y_{\infty}) \end{aligned}$$

$T_{\infty} = 30^\circ\text{C}$ ,  $Y_{\infty, \text{H}_2\text{O}} = 0$ ,  $h = 20 \frac{\text{W}}{\text{m}^2\text{K}}$ ,  $h_{fg} = \dots$

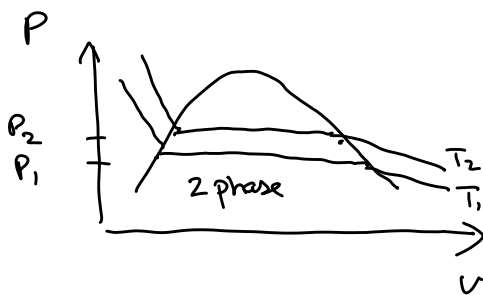


Do we have all info required to find  $\dot{m}$ ?

No! It would be great to have  $T_{\text{surf}}$ !

$$Y_{\text{surf}} = f(P_{\text{surf}})$$

$$T_{\text{surf}} = f(P_{\text{surf}})$$



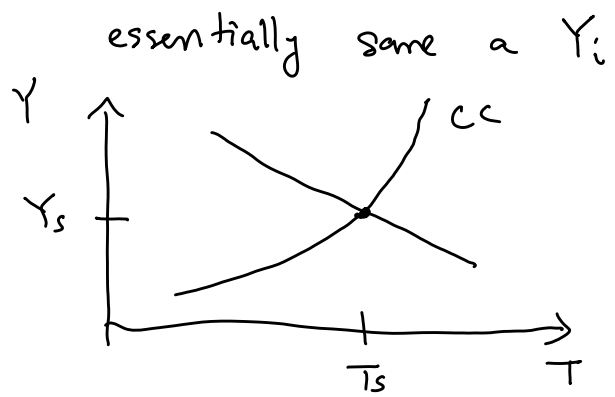
The surface is assumed to be a saturated mixture.

Thermodynamic relationships  
Clausius - Clapyron

derived from Gibbs eqn. Equilibrium relationships.

near. endpoint  $\frac{d \ln P}{dT} = \frac{h_{fg}}{RT^2}$  integrate this.

$$\left( \frac{P_{\text{surf}, i}}{P_0} \right) = \exp \left[ - \frac{h_{fg} M_i}{R} \left( \frac{1}{T_s} - \frac{1}{T_{\text{boil}}} \right) \right]$$



2 eqns in 2 unknowns.